

# **Compressed Sensing: Single Pixel Imaging in Short-Wave Infrared Spectrum**

**Examensarbete**

TQET33

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# 1 Introduction

The development and research of compressed sensing applied to a single pixel camera (SPC) is a relative new area in signal processing with the first functioning camera architecture in 2006. Since then numerous improvements and methods have been proposed how to capture images. In this section a introduction to the SPC architecture and a brief introduction of compressed imaging is presented followed by the aim, research questions and thesis outline.

## 1.1 Background

Compressed sensing (CS) allows reconstruction of a sparse signal being sampled with far fewer samples required to fulfill the sampling theorem. Swedish Defence Research Agency (FOI) became interested in the subject some years ago and tests potential applications. One of the potential applications are a camera with a single pixel which can reconstruct a scene, therefore FOI built a SPC platform in the short-wave infrared (SWIR) spectrum for the purpose to study and evaluate this kind of system.

The SWIR spectrum is electromagnetic radiation with wavelengths between 700 - 2500 nm and SWIR cameras can therefore capture images illuminated by the sun, moon, star light and airglow thus works both by day and night. SWIR light can to some extent pass through smoke and fog which makes it robust camera for day and night applications. Some camouflage that is hard to spot in visual spectrum is visible in the SWIR spectrum. The system used in this master's thesis uses a digital micromirror array (DMD) to sample the light from the scene. The system will sample less single pixel measurements than the number of pixels in the reconstructed image with the drawback that it has to capture each measurement in consecutive order instead of all at the same time.

## 1.2 Compressive sensing & imaging

Compressive sensing is a new sampling strategy which reconstructs a compressible or sparse signal by finding solution to undetermined linear system where the number of measurements  $M$  is less than the number of data points  $N$  in signal. Two constraints need to be fulfilled to apply compressed sensing sampling: the sampled signal needs to be spares in some basis e.g. Fourier or gradient, the second condition is that the measurement matrix must be incoherent with the sparse transform. The characteristic undetermined linear system in CS is defined as  $\mathbf{y} = \Phi\mathbf{x}$  where  $\mathbf{y}$  contains the measurements from the measurement matrix  $\Phi$  sensing the signal  $\mathbf{x}$ . In figure 1 such linear equation system is shown.

$$\begin{matrix} \mathbf{y} \\ \begin{matrix} y_1 \\ y_2 \\ y_3 \\ \vdots \\ y_M \end{matrix} \end{matrix} = \boxed{\Phi} \quad \begin{matrix} \mathbf{x} \\ \begin{matrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ \vdots \\ x_N \end{matrix} \end{matrix}$$

The diagram illustrates the linear equation system  $\mathbf{y} = \Phi\mathbf{x}$ . On the left, the vector  $\mathbf{y}$  is shown as a column of measurements  $y_1, y_2, y_3, \dots, y_M$ . An equals sign follows. To the right of the equals sign is a large rectangular box labeled  $\Phi$ , which represents the measurement matrix. This matrix is filled with entries  $\Phi_1, \Phi_2, \Phi_3, \dots, \Phi_M$ , corresponding to the measurements  $y_1, y_2, y_3, \dots, y_M$  respectively. To the right of the matrix  $\Phi$  is another column vector labeled  $\mathbf{x}$ , representing the signal, with entries  $x_1, x_2, x_3, x_4, \dots, x_N$ .

Figure 1: CS undetermined linear system

Scientists at Rice university in Texas, USA realized that the new method could be used to create a new camera architecture with a single photo diode in the sensor, the single pixel camera was born and thus a new sub field of compressed sensing was created called compressive imaging.

To be able to apply CS to imaging in the first place the constraints in CS needs to hold for images as well. The first requirement is that the signal needs to be compressible or sparse in some basis which natural images is known to be because they can be compressed using for example JPEG (Discrete cosine transform), JPEG2000 (Wavelet). The second constraint is that the measurement matrix must be incoherent with the sparse transform which for example i.i.d random distribution or some structure with the same property as i.i.d random distribution.

### 1.3 System architecture

The SPC in this master's thesis was designed with reflecting telescope optics to act as a lens to focus the scene. As seen in figure 2 light from the scene enters through the aperture in the camera where the primary mirror focus the light the via the secondary mirror onto the DMD. To this point, the SPC works like a conventional camera with a DMD where the image sensor would be placed in the convectional camera. The SPC has an DMD in the focal point which resemble an image sensor but instead of photo diodes for each pixel there is a tiny mirror which individually can either reflect light 12 degrees to the right or left as seen in figure 2. The incoming focused light can ether be dumped or it can be reflected into the single pixel SWIR detector through an lens.

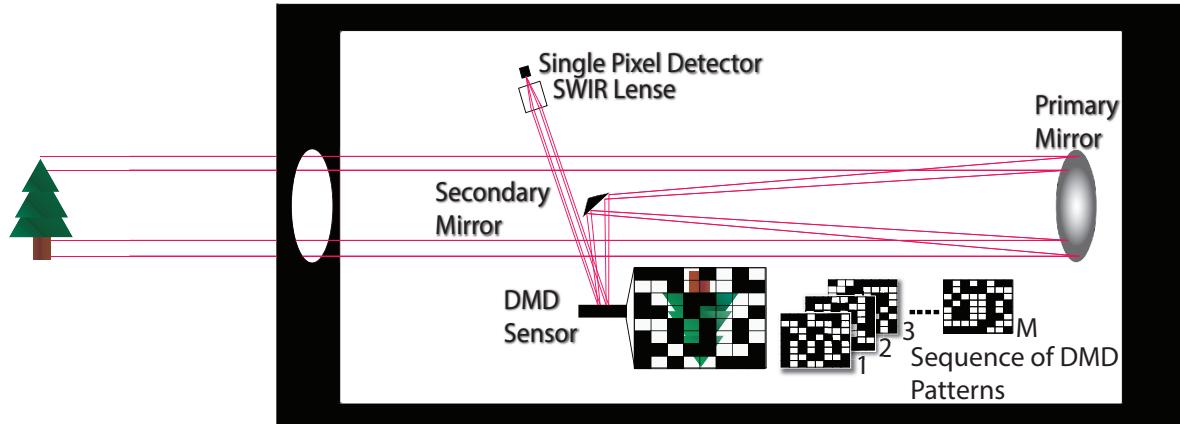


Figure 2: System overview

To connect the architecture with the math from CS it can be interpreted as, the light from the scene which is focused on the DMD is the desired signal  $\mathbf{x}$ , the image. The DMD can individually set each mirror the ether direct the light from each 'pixel' to the single pixel sensor or dump the light i.e a spatial light modulator (SLM). The DMD sets a pattern of pixel of intress which is a measurement matrix  $\Phi_m$  to be summarized in the single pixel sensor  $y_m$  as a measurement. One measurement is the inner product of a measurement matrix and the signal,  $\Phi_m \times x = y_m$ . To complete a full measurement the process is repeated with different measurement matrices set on the DMD to the full undetermined linear system  $\mathbf{y} = \Phi\mathbf{x}$ .

### 1.4 Measurement matrix & reconstruction

How is the measurement matrix chosen? As told before the measurement matrix needs to be incoherent with the sparse transform and the DMD can only direct the light or not which mathematically is ether a zero or a one. The research tells that for example a i.i.d. Gaussian distribution with equal probability of a zero or one will with high probability be incoherent with a natural image scene. But how about the first constraint that the signal  $\mathbf{x}$  needs to be sparse or compressible in some basis? Often natural images is not sparse in the spatial domain unless the scene

is for example the night sky, well a good property of CS that the scene can be transformed to an other basis like this,

$$\mathbf{y} = \Phi \mathbf{x} \Leftrightarrow \mathbf{y} = \Phi \Psi \Theta, \quad (1)$$

where  $\Psi$  is a sparsifying basis for example to the DCT or Wavelet basis. And  $\Theta$  is the coefficients vector which is more sparse then the spatial coefficient vector  $\mathbf{x}$ . And the transformation will not compromise the incoherence between the reconstruction matrix  $A = \Psi \Phi$  and the coefficients  $\Theta$  in the new basis. This means that the signal  $\mathbf{x}$  will be reconstructed with optimization in a more sparse basis  $\Theta$  and then transformed back to the spatial domain.

What is special about CS is not just how the problem is presented but also how to solve it. It is known that an undetermined linear system has infinite many solution so how does the signal get recovered? CS exploit the characteristics of the signal  $x$  which is known to be sparse in some basis. With for example  $\ell_1$  optimization,

$$\hat{\Theta} = \arg \min \|\Theta\|_{\ell_1} \text{ subject to } \Phi \Psi \Theta = y, \quad (2)$$

which means that  $\ell_1$  optimization minimizes the non zero elements of  $\Theta$  and can exactly reconstruct a K-spares vector or approximate a compressible vector. The exact recovery can be accomplished with high probability using  $M \geq \mathcal{O}(K \log(N/K))$  measurements. This is why CS is powerful, it enables sub-Nyquist measurements with exact recovery in the noiseless case which can be approximated in real applications.

In the compressed imaging case where noise is present an other optimization algorithm has shown to be more successful at recovering images: total variation. Total variation regularization minimizes the magnitude of the gradient in the image and doing so it preserve edges and piece-wise constant structure in the image which is desired.

## 1.5 Motivation

Why would a SPC be beneficial to a conventional camera? The SPC has more components and several measurements have to be made over time while a regular camera measures all pixels on the sensor at the same time, and the reconstruction shifts burden to the processor. There are two major reasons why a SPC is of interest, it is not to compete with the conventional cameras in the visual spectrum where cameras in all price ranges and quality already exist and are relative cheap to build. The focus lies in more exotic spectrum of light like SWIR or Terahertz (X-ray) wavelengths where the image sensors are hard to build which brings up cost and the ability to create high resolution sensors. With CS and the SPC architecture manufacturing cost can be significantly reduced while the image resolution increases. For example a state of the art SWIR camera cost about half a million SEK which can be reduced by a factor of 100 with a SPC with the same resolution.

## 1.6 Aim

What image quality can be achieved in natural images captured with a single pixel camera in daylight using state of the art methods?

## 1.7 Research questions

- How can the quality of images reconstructed by CS or a SPC be evaluated?
- What is the state of the art method to capture and reconstruct images using a SPC architecture?
- What image quality is achieved using state of the art methods applied to the SPC?

## **1.8 Limitations**

- The hardware rig provided by FOI
- 

## **1.9 Thesis outline**

## 2 Related work

In this section important, relevant and fundamental articles to this master's thesis is presented each with a summary. The articles covers compressed sensing theory applied to compressed imaging, SPC architecture and how to evaluate the images i.e. the fundamental source of information on how to build a state of the art SPC system and how to evaluate its performance.

### 2.1 Compressive sensing

- [1], [2] "Sparse Modeling" by G. Y. Grabarnik and I. Rish and "Sparse and redundant representation" by M Elad is two books which thoroughly presents the topic of sparse and redundant representation and modeling. The fundamental principles and constraints that needs to be fulfilled in CS. The books presents different minimization algorithms and how to implement them.
- In [3] "Compressed sensing" David L. Donoho proposed the framework of compressed sensing and the application of images capturing.
- [4] "Compressive Sensing: From Theory to Applications, A survey" by S. Qaisar et al. 2013, reviews CS background, theory and mathematics and has a extensive survey of reconstruction algorithm and potential CS applications.

### 2.2 Compressive imaging

- [5], [6] "An architechture for compressive imaging" and "A New compressive imaging camera architecture using Optical-Domain Compression" by M. B. Wakin, D Takhar, et al. 2006, presents the first single pixel camera architecture using CS to reconstruct the images.
- [7] "Single-Pixel Imaging via Compressive Sampling" by M. F. Duarte et al. 2008, is an introduction and summary to CS and CI including the SPC architecture. This article also compares different scanning methodologies and their conditions.
- [8] "Single Pixel SWIR Imaging using Compressed Sensing" by C. Brännlund and D. Gustafsson. 2016, was written to show the initial results and proof of concept of the SPC architecture at FOI.
- [9] "A high resolution SWIR camera via compressed sensing" is a paper from L. McMackin et al. 2012 at Inveiw Technology which develop and produces compressive sensing cameras. The paper contains a brief review of CS and CI followed by a presentation of their camera architecture.
- [10] "Compressed Sensing for 3D Laser Radar" by E. Fall. 2014, is a master's thesis where CS/CI is evaluated for a potential depth camera architecture using a one pixel sensor.
- [11] "Multi image super resolution using compressed sensing" by T. Edler et al. 2011, presents the results from using a small detector array instead of just one single sensor, but still using CS to reconstruct the images. With this technique the subsampling ratio and the exposure time is reduced.

#### 2.2.1 Measurement matrix & reconstruction

- [12] Chengbo Li:s master's thesis "An Efficient Algorithm For Total Variation Regularization with Applications to the Single Pixel Camera and Compressive Sensing" describes a total variation algorithm Li constructed which solve the CS problem. The algorithm is faster and produces better results for images than previous popular algorithms.

- [13]–[15] Fast and Efficient Compressive Sensing Using Structurally Random Matrices (SRM). The articles describes why and how to implement SRM, in these articles the Hadamard or DCT matrices is proposed to replace the i.i.d random matrix. With SRM the reconstruction time is reduced by replacing matrix multiplication with fast transforms. In addition to improved reconstruction time the new method does not need to store the measurement matrix in memory which enables reconstruction of high resolution images.
- [16] "An Improved Hadamard Measurement Matrix Based on Walsh Code For Compressive Sensing" Shows that sequency-ordered Walsh Hadamard matrix gives better reconstruction than the Hadamard matrix with the same benefits of using the Hadamard matrix. The resulting reconstructed image has near optimal reconstruction performance.

### 2.3 Evaluation

- [17] "The essential guide to image processing" by Al Boviks contains the majority of fundamental image processing techniques and measurements. Two image quality metrics of interest is PSNR and SSIM which can be used when a reference image is available.
- [18] "No-Reference Image Quality Assessment in the Spatial Domain" is the article describing the blind/referenceless image spatial quality evaluator (BRISQUE). The BRISQUE algorithm evaluates image quality and "naturalness" based on statistics in the image. BRISQUE is used when there is no reference image available and therefore can be used to evaluate images produced by the SPC.
- [19] "Prestandamått för sensorsystem" by F Näsström et al. 2016, describes methods and tools to evaluate sensor systems at FOI.

### 2.4 Analysis

### 3 Method

New method introduction depending on how the disposition will be in the final form

In order to answer the research questions stated in section 1.7 a state of the art SPC, experiments and evaluation methods needs to be set up. In this section the SPC hardware and image sensing and reconstruction scheme is described.

#### 3.1 Single pixel camera architecture & hardware

FOI designed the SWIR SPC platform using a DMD, a Newtonian telescope and a single pixel SWIR detector. The system also has a reference camera in the visual spectrum which can capture images if all micro mirrors in the DMD are turned away from the single pixel sensor and towards the reference camera, it can also be used to check that the patterns are displayed correct on the DMD.

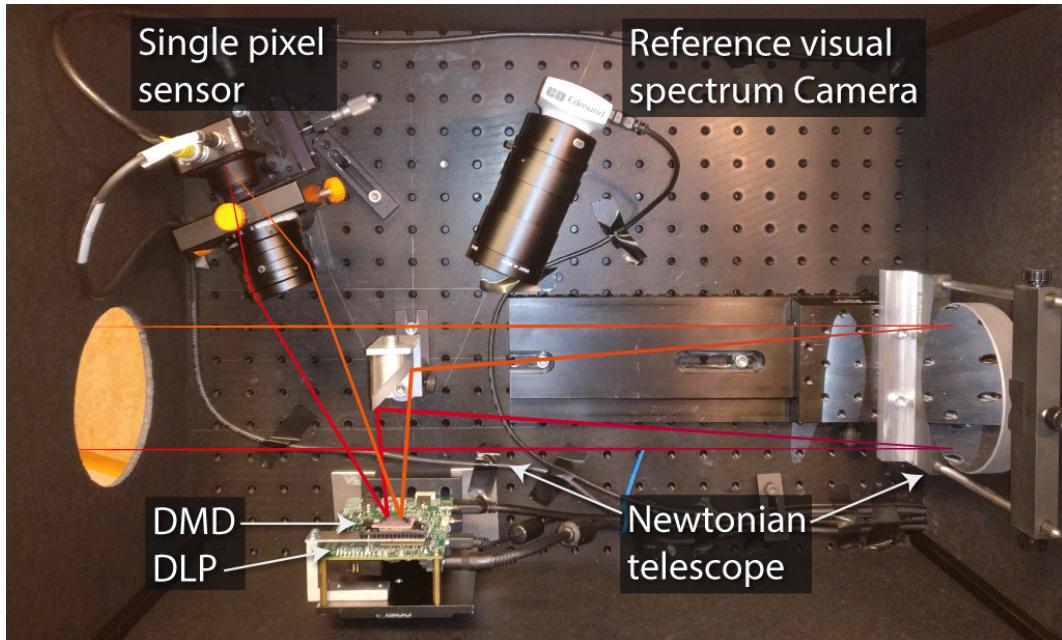


Figure 3: Single pixel imaging system (SPIS), adopted from [8].

As seen in figure 3 light from the scene is focused by the Newtonian telescope and reflected onto the DMD. The mirrors on the DMD can turned individually either into the single pixel sensor or the reference camera. The DMD acts as a Spatial Light Modulator (SLM) and reflects different patterns which is 'summed up' in the single pixel sensor as an intensity. The reconstructed image from the system will have the same resolution as the DMD patterns. The DLP is the DMD control unit which controls which patterns are displayed on the DMD either by reading images from memory or the video port.

##### 3.1.1 Newtonian telescope

A Newtonian telescope is a reflecting telescope, using a concave primary mirror and a flat diagonal secondary mirror, see figure 3. In this set-up the telescope act as a lens focusing the scene onto the DMD. The motivation to use a Newtonian telescope instead of a lens system is partly that chromatic aberration is eliminated and partly that a reflective optical system works over a greater range of wavelengths that includes SWIR, near infrared (NIR) and the visible spectrum.

### 3.1.2 DLP and DMD

The DMD (Texas Instruments DLP4500NIR) is a matrix of micro mirrors that can be individually tilted  $\pm 12^\circ$  and reflects wavelengths in the range 700-2500 nm. The DMD is controlled by the DLP (DLP LightCrafter 4500) which can be controlled either by video port (HDMI) or by the internal flash memory. The internal memory can theoretically be faster than the video port but due to constraints in both memory and memory bandwidth the fastest measurement matrix rate gets stuck at 270 – 300 Hz. The video port can be operated at 120 Hz and display one bit plane at the time from a 24 bit signal, which gives a maximum measurement matrix rate at  $120 \times 24 = 2880$  Hz, but in the current configuration only 60 Hz frame rate was achieved giving a measurement matrix rate at 1440 Hz. At this rate with the number of measurements relative to number of pixels in reconstructed image between 20% – 30% a  $256 \times 256$  pixel images data would be acquired in 9 – 13 seconds and for a  $512 \times 512$  pixel image 36 – 53 seconds. To control the DMD the software 'DLP LightCrafter 4500 Control Software' is used.

The DMD in the setup is constructed with a diamond shaped pattern instead of a regular square grid which is used in regular camera image sensors. The diamond shape causes the index of each mirror to be skewed against what a normal grid would look like. As seen in figure 4 the indexes of the mirrors column is two mirror column arrays wide while a row is a single row.

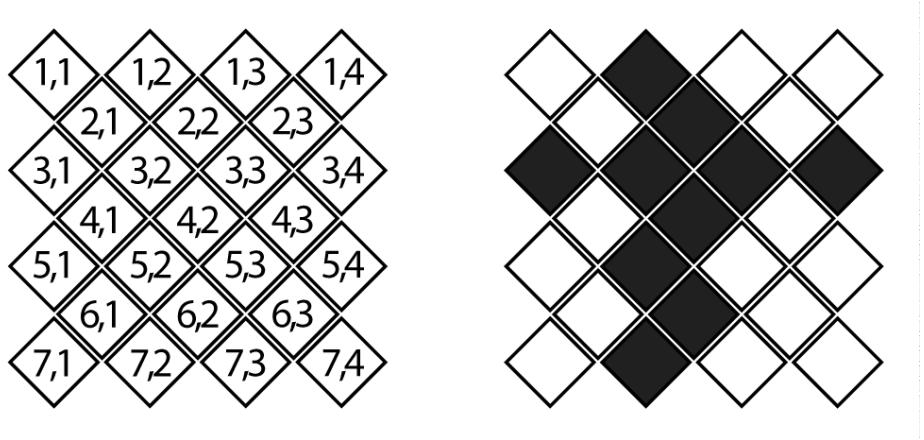


Figure 4: DMD matrix, left shows each tiles index and right shows second row and second column in black.

Because the reconstruction algorithm and measurement matrix needs to be a square matrix with the side length with a power of 2 the resulting images ratio would be 2 to 1 while the image should have the ratio 1 to 1. The resulting image would need to be transformed into the real ratio where information potentially gets lost. Therefore the index of mirrors was changed so that each 'pixel' gets two mirrors as seen in figure 5. This will result in rows and columns gets equal amount of space and the aspect ratio will be preserved to 1 to 1.

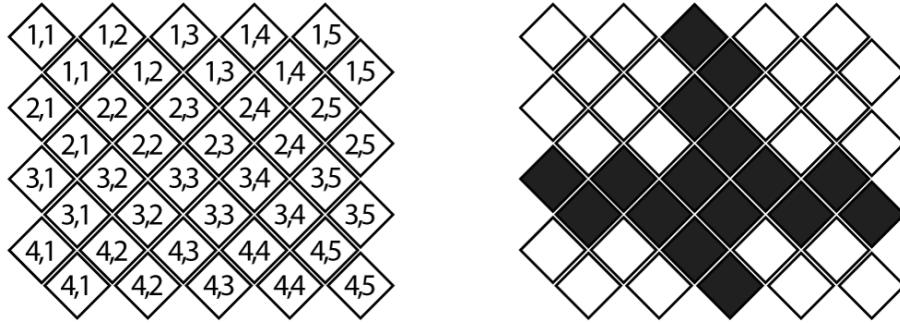


Figure 5: DMD matrix, left shows each tiles index and right shows third row and third column in black.

Connect the DMD to CS and the physical aspect (every mirror is a pixel). I:I:D gaussian with DMD only can take values 1,0 gives 50% evenly distributed pixels measurements for every measurement matrix which looks something like figure 6.

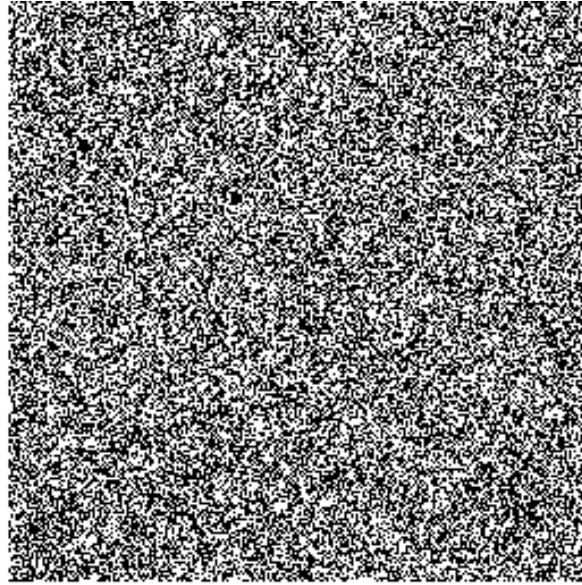


Figure 6: A typical measurement matrix presented on the DMD with the resolution  $256 \times 256$  pixels.

### 3.1.3 Lens

The lens mounted on the single pixel sensor is an 50mm SWIR Fixed Focal Length Lens with an variable appature from f1.4 designed for wavelengths ranging from the 800 nm in the visual spectrum to 2000 nm in the SWIR spectrum. [20]

### 3.1.4 Single pixel sensor

The single pixel sensor is a Thorlabs PDA20C/M and is sensitive in wavelength range 800-1700 nm which is beyond the visual spectrum (390-700 nm). The sensor outputs an analog signal in volt which the sampler converts to a discret value. [21]

### 3.1.5 Signal spectrum

All components characteristics assembled the wavelengths that pass through the system and measured in the single pixel sensor is between 800-1700 nm.

## 3.2 Compressive imaging

Write introduction to CS, create some intuition

The single pixel sensor captures a scene by measuring the light intensity focused into the detector reflected from the DMD matrix. The DMD sensing matrix changes to obtain new measurements,  $M$  unique sensing matrix measurements is captured to reconstruct an image with  $N$  pixels. Each sensing matrix index is encoded either by a one or a zero (turning the mirror onto or away from the sensor). The compressive imaging sampling model is defined as

$$\mathbf{y} = \Phi \mathbf{x} + \epsilon, \quad (3)$$

,  $\mathbf{x}_{N \times 1}$  is the signal (image) with  $N$  samples (pixels),  $\mathbf{y}_{M \times 1}$  is the vector with  $M$  measurements,  $\Phi_{M \times N}$  is the measurements matrix (each unique sensing matrix  $\Phi_{1 \times N}$  as a row vector) and  $\epsilon$  is the noise. In conventional sampling the number of measurements  $M$  needs to be at least equal to the number of samples  $N$  to recover the signal but CS states that  $M$  can be relatively small compared to  $N$  given how compressible the signal is. The signal  $\mathbf{x}$  can be represented as

$$\Psi \theta = \mathbf{x}, \quad (4)$$

where,  $\Psi_{N \times N}$  is some basis matrix and  $\theta_{N \times 1}$  is the coefficients where  $\theta$  is  $K$ -sparse.  $K$ -sparse means that the signal  $\mathbf{x}$  has  $K$  non zero elements in basis  $\Psi$ ,  $\|\theta\|_0 = K$ . Given equation 4, equation 3 can be expand to

$$\mathbf{y} = \Phi \mathbf{x} + \epsilon = \Phi \Psi \theta + \epsilon = \mathbf{A} \theta + \epsilon, \quad (5)$$

where,  $\mathbf{A}_{M \times N} = \Phi \Psi$  is the reconstruction matrix. The last statement is what makes CS powerful, a signal which is not sparse can be sampled with measurement matrix  $\Phi$  and then reconstructed with reconstruction matrix  $\mathbf{A}$  in a basis where  $\mathbf{x}$  is sparse or compressible. [1]

Noise does not effect the measurement very much because half the intensity from the image is measured in one pixel sensor bumping the signal to noise ratio from a conv camera where each pixel has some noise half the pixels share that noise making SPC very robust to noise even in low light situations.

## 3.3 Measurement matrix & Restricted isometry property (RIP)

Introduce the topic.

In the noiseless case exact recovery of the image  $\mathbf{x}$  is achievable if RIP holds for the reconstruction matrix  $\Phi \Rightarrow \Phi \Psi = \mathbf{A}$ , the constraint is defined as,

$$(1 - \delta_K) \|\mathbf{x}\|_{\ell_2}^2 \leq \|\mathbf{A} \mathbf{x}\|_{\ell_2}^2 \leq (1 + \delta_K) \|\mathbf{x}\|_{\ell_2}^2, \quad (6)$$

where  $\delta_K \in [0, 1)$  is the smallest constant to satisfy RIP for a  $K$ -sparse signal  $\mathbf{x}$ . To determine a sampling matrix is a NP-hard problem (which means that there are no feasible way of creating a optimal reconstruction matrix) and generally  $\mathbf{x}$  is not known and varies which means that there are no general optimal reconstruction matrices for natural images. The solution is to find a general

reconstruction matrix that satisfies RIP with high probability. The solution which also should be incoherent with the base matrix  $\Psi$  is to construct the measurement matrix using a i.i.d random distribution which gives  $\delta_K \ll 1$  with high probability. Using random measurement matrices the number of measurements needed to satisfy RIP with high probability is  $M \geq O(K \log(N/K)) \ll N$ . [2], [3]

The problem using random matrices is that they need to be stored in memory for the reconstruction algorithm, when the image resolution is increased the measurement matrix increases exponentially. For images with resolution of  $512 \times 512$  and larger the data gets infeasible for a normal computer to handle. Fortunately using fast transforms in the reconstruction algorithm can exclude using vector multiplication resulting in faster reconstruction and the need to store the measurement matrix in memory. But in order to do so special measurement matrices are used, in this master's thesis the sequency ordered Walsh Hadamard measurement matrix will be used with the TVAL3 reconstruction algorithm described in section 3.4.1.

### 3.3.1 Sequency Ordered Walsh Hadamard measurement matrix

Besides from eliminating the need to store the measuring matrix for reconstruction the sequency ordered Walsh Hadamard (SOWH) matrix can be generated when sent to the DMD eliminating the need to store the matrix at all. SOWH has the same characteristics and properties of an i.i.d random matrix and therefore also fulfills the RIP condition with high probability and research has shown that there is no significant loss in recovery of the signal relative i.i.d random measurement matrix [16]. An other property of SOHW is that it only contains -1 and 1 which easily be converted to 0 and 1 when sent to the DMD.

The naturally ordered Hadamard matrix of dimension  $2^k$ ,  $k \in \mathbb{N}$  are constructed by the recursive formula

$$H_0 = 1, \quad (7)$$

$$H_1 = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}, \quad (8)$$

and in general,

$$H_k = \begin{bmatrix} H_{k-1} & H_{k-1} \\ H_{k-1} & -H_{k-1} \end{bmatrix} = H_1 \oplus H_{k-1} \quad (9)$$

where  $\oplus$  denotes the Kronecker product. To construct the sequency ordered Walsh Hadamard matrix from the naturally ordered Hadamard matrix three steps is required:

- Convert row index to binary.
- Convert the binary row index to gray code.
- Apply bit reverse on the gray code index.

then order the rows after the bit reverse to obtain the sequency ordered Walsh Hadamard matrix.

$n_H$	0	1	2	3
Binary	00	01	10	11
Gray code	00	01	11	10
Bit-reverse	00	10	11	01
$n_W$	0	2	3	1

Table 1: How to convert a naturally ordered Hadamard matrix to a sequency ordered Walsh Hadamard matrix by shifting row with index  $n_W$  to  $n_H$

for example

$$H_2 = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix} \Rightarrow W_2 = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{bmatrix}. \quad (10)$$

To use the sequency ordered Walsh Hadamard matrix as an measurement matrix the fist row is omitted, permutations to the columns is performed,  $M$  rows are choosen at random and the indices with a  $-1$  is shifted to 0. This last step is required to convert the measurement matrix so it gets the characteristics of an i.i.d random matrix and thus fulfill the RIP condition [14], [22], [23]. How the matrix was permuted and which rows was choosen i which order is stored so the reconstruction algorithm can use that information. [12], [14], [16].

### 3.4 Reconstruction method

To reconstruct the image  $\mathbf{x}$  the sparest set of coefficients in  $\theta$  is desired. The optimal approach to find these coefficients would be to use  $\ell_0$  minimization

$$\hat{\theta} = \arg \min \|\theta\|_0 \text{ subject to } \mathbf{y} = \mathbf{A}\theta. \quad (11)$$

Simply minimizing nonzero indices  $\theta$  in the sparsifying basis  $\Psi$ , but this problem is known to be NP-hard. A better approach is the  $\ell_1$  minimization, for example Basis Pursuit denoise (BPDN),

$$\hat{\theta} = \arg \min \|\theta\|_1 \text{ subject to } \|\mathbf{y} - \mathbf{A}\theta\|_2 < \epsilon. \quad (12)$$

In 2006 Donoho [3] for the fist time guarantied theoretical  $\ell_0/\ell_1$  equivalence which holds in the CS case, which means using a  $\ell_1$  minimizer is guaranteed to find the sparsest solution in polynomial time in the noiseless case which can be approximated in the noisy and compressible signal case. The drawback with the  $\ell_1$  minimizer is that it require more measurements than the optimal case with  $\ell_0$  but it is still  $M \ll N$ . Since 2006 many more types of optimization algorithms has evolved which solves the problem with different methods but with the same goal: finding the largest most significant coefficients of  $\theta$ . [3], [6], [7]

#### 3.4.1 Total variation: TVAL3

The reconstruction algorithm that was chosen in this Master's thesis was a total variation regularization algorithm. Natural images often contains sharp edges and piecewise smooth areas which the TV regularization algorithm is good at preserving. The main difference between TV an other reconstruction algorithms is that TV considers the gradient of signal sparse instead of the signal, thus finding the sparsest gradient. The TV optimization problem in TVAL3 is defined as

$$\min_{\mathbf{x}} \sum_i \|D_i \mathbf{x}\|, \text{ subject to } \Phi \mathbf{x} = \mathbf{y}, \mathbf{x} \geq 0, \quad (13)$$

where  $D_i \mathbf{x}$  is the discrete gradient of  $\mathbf{x}$  at position  $i$ .

TVAL3 stands for "Total Variation Augmented Lagrangian Alternating Direction Algorithm", accordingly is a TV regularization algorithm which uses augmented Lagrangian and alternating direction methods, where augmented Lagrangian is a method in optimization for solving constrained problems by substitute the original constrained problem with a series unconstrained subproblems and introduce a penalty term. To solve the new subproblems the alterning direction method is used [12].

As mentioned earlier in section 3.3.1 the main reason why the sequency ordered Walsh Hadamard matrix is used is to eliminate the need to store the matrix in memory during reconstruction and a

promise to speed up the reconstruction. In TVAL3 there are two multiplications between matrix and a vector that dominates the computation time,

$$\Phi \mathbf{x}^k \text{ and } \Phi^\top (\Phi \mathbf{x}^k - \mathbf{y}). \quad (14)$$

The idea is to replace the multiplication with fast transforms. To explain the concept some observations and new functions need to be defined. The first observation is that the sequency ordered Walsh Hadamard matrix is a transform matrix which also can be computed with the fast Walsh Hadamard transform (fwht),

$$\mathbf{W}\mathbf{x} = \text{fwht}(\mathbf{x}), \quad (15)$$

where  $\mathbf{W}$  is a sequency ordered Walsh Hadamard matrix and  $\mathbf{x}$  is the signal vector. The wht is a generalized class of Fourier transforms which decomposes input vector into superposition of Walsh functions.

From section 3.3.1 it was briefly mention in the last paragraph that in order for the measurement matrix to fulfill RIP the columns is permuted and rows are chosen in random to create the measurement matrix from the sequency ordered Walsh Hadamard matrix, two functions is created to carry out does operations. First the permutation function  $\pi(\cdot)$ , which from a random seed permute the order of the columns in a matrix or the order of a vector. The second function  $\Pi_M(\cdot)$  chooses  $M$  row in a matrix at random and stacks them in a new matrix. Then the definition of the measurement matrix  $\Phi$  constructed from the sequency ordered Walsh Hadamard matrix  $\mathbf{W}$  leads to observation 2

$$\Phi = \pi(\Pi_M(\mathbf{W})) = \Pi_M(\pi(\mathbf{W})). \quad (16)$$

It does not matter in which order the functions i applied, it gives the same result. With matrix  $\mathbf{A}$  and vector  $\mathbf{u}$  observation 3 is formulated as,

$$\pi(\mathbf{A})\mathbf{u} = \mathbf{A}\pi(\mathbf{u}), \quad (17)$$

which shows that there is no difference between multiply a column-permuted matrix with a vector and multiply the same matrix with the vector permuted.

With all observations combined the matrix multiplication is replaced with the fwht in observation 4

$$\mathbf{y} = \Phi \mathbf{x} = \pi(\Pi_M(\mathbf{W}))\mathbf{x} = \Pi_M(\mathbf{W})\pi(\mathbf{x}) = \Pi_M(\mathbf{W}\pi(\mathbf{x})) = \Pi_M(\text{fwht}(\pi(\mathbf{x}))), \quad (18)$$

with the conclusion that the multiplication between the measurement matrix constructed using the permuted sequency ordered Walsh Hadamard matrix and the signal can be performed with the signal permuted, fast transformed using fwht and choosing rows, both permutations using the same functions  $\pi(\cdot)$  and  $\Pi_M(\cdot)$  and random seed as when the measurement matrix was created.

Using this method will reduce the overall computational complexity considerably and it will make the measurement matrix redundant in the reconstruction, only the two permutation functions  $\pi(\cdot)$  and  $\Pi_M(\cdot)$  needs to be stored. Excluding the measurement matrix in the reconstruction results in larger resolution images ( $512 \times 512$  pixels and larger) can be reconstructed. [12], [14]

### 3.5 Image Capturing and processing chain

To capture an image the SPC setup is only a subsystem in the whole process from acquiring the signal to reconstructing the image. In figure 7 the whole process of capturing an image is presented with all subsystems and signal/image processing steps included.

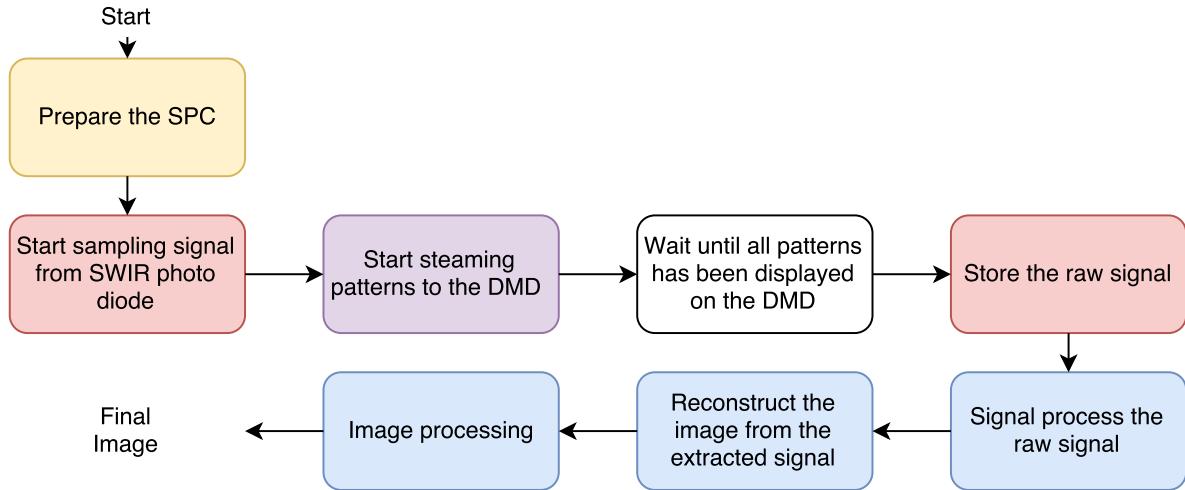


Figure 7: Block diagram of image capturing and processing chain, from signal acquisition to final image. Each color represents different subsystems in hardware or software.

This experimental setup has no full automatic system where a button can be pressed and the system produces an image. In the setup the subsystems works completely independently and needs to be operated manually in the right order at the right time. Each color in figure 7 represents a subsystem in hardware or software. Each subsystem is described in the following subsection.

### 3.5.1 Prepare the SPC

The first step in the yellow block "Prepare the SPC" is making sure the SPC is up and running but also to point the camera at the scene and set the correct focus. The scene is located with the aid of the reference visual camera (see figure 3) with all the mirrors in the DMD directed to that camera. The focus is adjusted manually by moving the primary mirror back or forth, this procedure may introduce some error to the focus.

### 3.5.2 Sampling

The red blocks subsystem "Start sampling signal from SWIR photo diode" and "Store the raw signal" is conducted in a separate software which controls the A/D converter and thus the sampling. When the SPC is prepared the sampling of the signal is started with sampling rate such that every measurement has several sampling points thus oversampling the signal. The oversampling is needed because when the mirrors move from one pattern (measurement matrix) to the next the signal is uncertain for some time, the oversampling is also used to suppress noise from the photo diode, more on that in section 3.5.4. After the signal is sampled the obtained signal needs to be stored on the computer manually.

### 3.5.3 Streaming patterns to the DMD

The subsystem "Streaming patterns to the DMD" represented in purple in the block diagram is controlled by two different softwares, one which manipulates the pattern-signal received by the DMD and one which sends the patterns to the DMD. The patterns are sent to the DMD through a HDMI cable where the DMD is set up such that the DMD acts as a second screen to the computer. This enables to show anything on the DMD that a screen can show. The patterns are stored as a video and played back on the DMD "screen" with a media player which shows each pattern in consecutive order. This is the major bottleneck of the system where each measurement matrix needs to be

displayed one after the other depending on how fast frame rate can be achieved. The naive approach would be to display one pattern per frame which is linked to the frame rate of the DMD, lets say for example 60 frames per second (fps) then for a  $512 \times 512$  pixel large image sampled with  $M/N = 20\%$  measurement matrices gives 52428 patterns which would take

$$52428/60 = 874 \text{ seconds} = 14.5 \text{ minutes to sample which is a long exposure time for a still image with the constraint that the scene should be stationary to obtain a stationary signal.}$$

Fortunately with the software "DLP LightCrafter 4500 EVM GUI" controlling the DMD the received video signal can be manipulated before displayed onto the DMD. The software includes a function which can break down the received 24-bit color image into 1 bit planes which can be displayed in consecutive order, so for each frame received 24 patterns is encoded on that frame then the DMD software isolates each bit plane and displays them in consecutive order. This function improves the naive implementation by a factor of 24, which reduces the time to sample the image from the last example from 874 seconds to  $874/24 = 36$  seconds. This exposure time is of course not optimal for natural images outdoors but acceptably for the experimental setup.

To create the video that feeds the patterns to the DMD each pattern i.e. measurement matrix is created as presented in section 3.3.1. Then for each group of 8 unique patterns drawn from the rows of the measurement matrix are stacked in each bit plane of a 8 bit image as seen in figure 8.

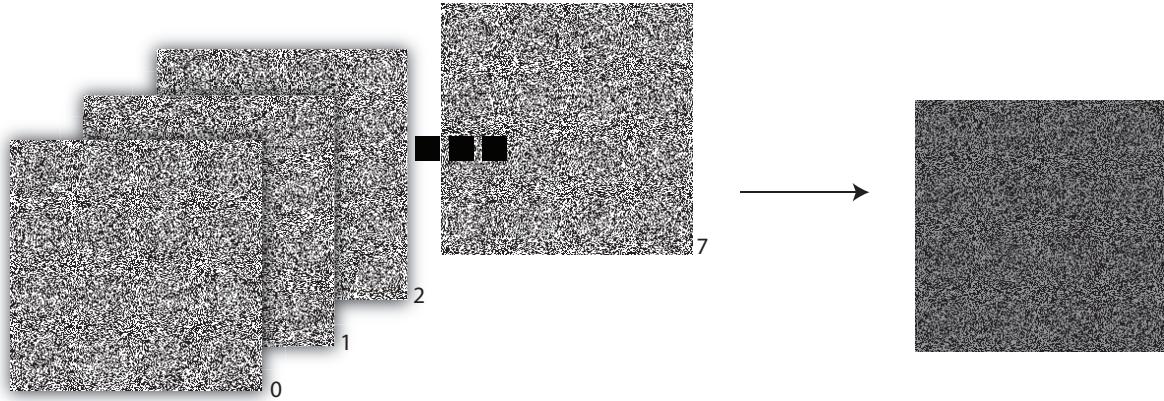


Figure 8: Stack each group of 8 measurement matrices in separate bit planes creating one 8 bit image with each matrix in one bit plane.

Then for each group of three 8 bit images a 24 bit color image is constructed as seen in figure 9.

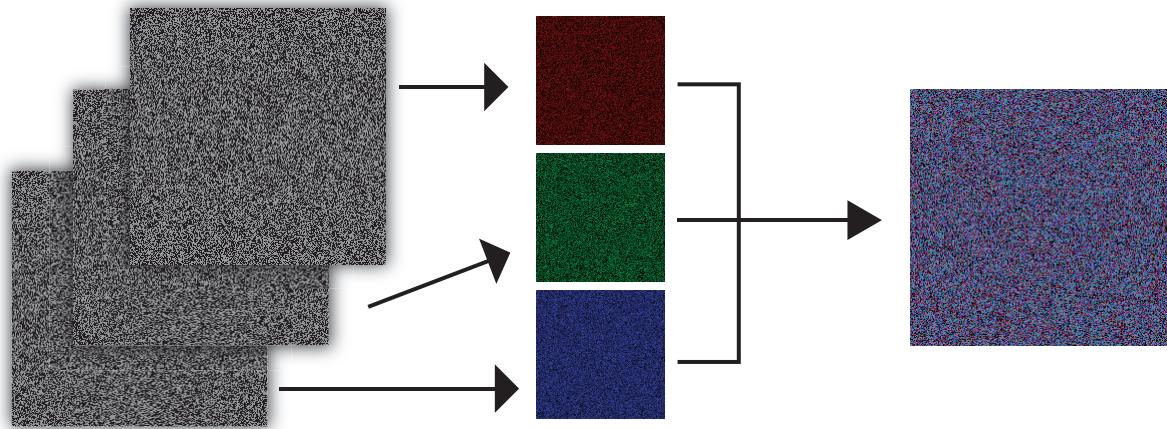


Figure 9: Stack each group of three 8 bit plane images into one 24 bit color image. This is one frame in the video sent to the DMD.

This 24 bit color image corresponds to one frame in the video, to create the video this is done so each pattern is represented in the video.

### 3.5.4 Signal processing

When the sampled signal is stored on the computer the remaining signal/image processing and reconstruction represented by blue blocks in figure 7 is conducted in MATLAB. In this section the signal processing of the sampled signal is described.

The first step is to refine the raw over sampled signal so that each measurement matrix correspond to one measurement in signal  $\mathbf{y}$ . This is done by first find every set of indices corresponds to every measurement matrix, as seen in figure 10 where the signal indices which corresponds to one measurement matrix is isolated by the purple lines.

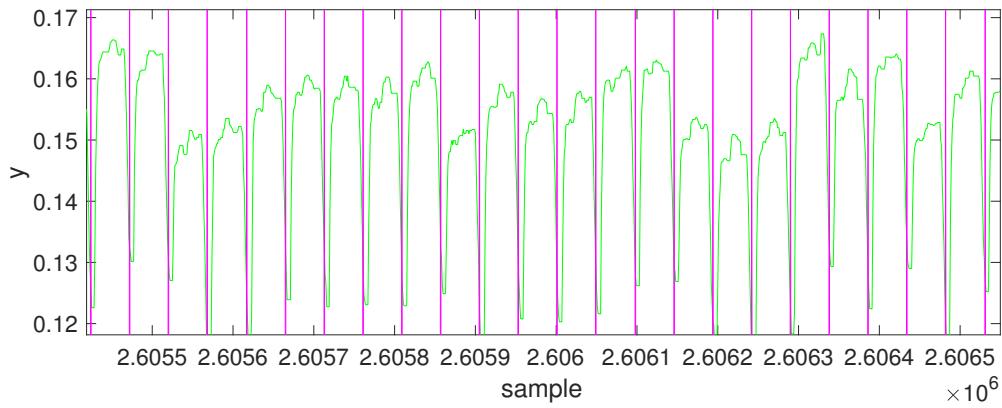


Figure 10: —

The next step is to determine one value for each measurement. This is done in two steps the first is to omit values which corresponds to the DMD changing pattern seen in figure 10 where the purple line divides the measurements the DMD is changing pattern which gives an uncertain signal. With

the omitted parts of the signal corresponding to one measurement the mean is calculated and set to the value for each measurement, as seen in figure 11.

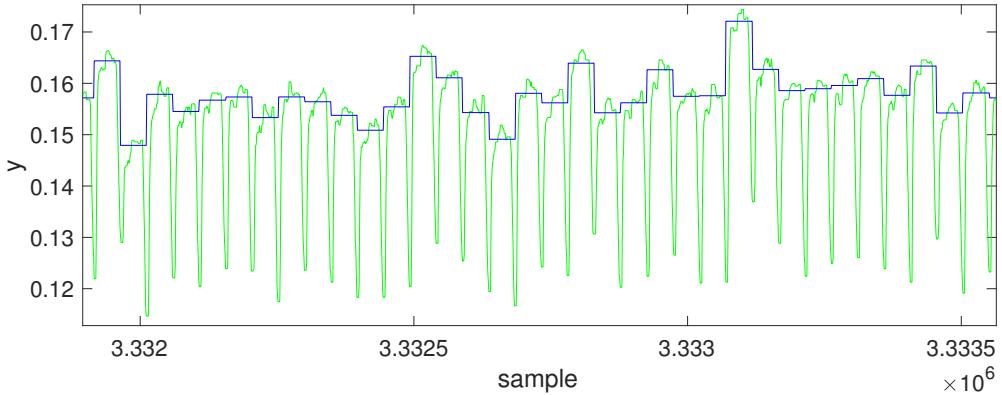


Figure 11: —

### 3.5.5 Dynamics in scene

So far the measurement vector  $\mathbf{y}$  has been determined, in the ideal case even with added noise the measured signal should be stationary because the image is assumed to be constant with half the pixels measured at random uniformed spread across the image. Each pixel in the image has the same value in each measurement with some noise added which is divided by all pixels being measured i.e. half the pixels which does not have a significant impact of the reconstructed image. But when capturing images outdoors with natural light in addition with long exposure time as described in section 3.5.3 it is not certain that the image (or every pixel) is constant over the exposure time which will reduce reconstruction performance because of the ambiguity of each pixel. The potential dynamics in a scene can be divided into two categories: luminance change and object movement. In this subsection the luminance change problem is modeled with corresponding algorithm to suppress the impact on the reconstructed image. The object movement problem will not be modeled, instead be avoided when capturing the signal by making sure the scene is as static as possible.

In natural outdoor images it can be assumed the the primary source of light comes from the sun, but even on a clear day the light intensity from the sun is not constant. If the scene is assumed to be completely stationary even the slightest intensity change will be added for all pixels being measured changing the mean intensity of the measured signal  $\mathbf{y}$  which should be stationary. With the assumption that the image is constant and the luminance change uniformly adds the same intensity to each pixel per measurement the problem can be modeled.

Start of with the original theorem and disregard the noise,

$$\mathbf{y} = \Phi\mathbf{x}, \quad (19)$$

the image  $\mathbf{x}$  can not longer be considered constant for all measurements, the luminance change will change image  $\mathbf{x}$  for every measurement matrix  $\Phi_i$  depending on the uniform luminance change. This can be described for one measurement as,

$$y_i = \Phi_i \mathbf{x}_i = \Phi_i(\mathbf{x} + \mathbf{l}_i) = \Phi_i \mathbf{x} + \Phi_i \mathbf{l}_i, \quad (20)$$

where  $\mathbf{l}_i$  uniform adds the same intensity over the whole image  $\mathbf{x}$  for measurement  $i$ . It is known from before that the measurement matrix  $\Phi_i$  contains 50% zeros and ones which gives,

$$y_i = \Phi_i \mathbf{x} + \Phi_i \mathbf{l}_i = \Phi_i \mathbf{x} + \frac{N}{2} c_i, \quad (21)$$

where  $c_i$  is the uniform intensity change coefficient for measurement  $i$ . This function can be generalized for all measurements,

$$\mathbf{y} = \Phi \mathbf{x} + \frac{N}{2} \mathbf{c} = \Phi \mathbf{x} + \mathbf{c}, \quad (22)$$

where  $\mathbf{c}$  is the intensity change vector.

The goal is now to remove the intensity change vector from signal  $\mathbf{y}$ . Using the knowledge that the signal  $\mathbf{y}$  should be stationary and assumes that the rate of change in intensity has a much lower frequency than the intensity change between individual measurement matrices, then  $\mathbf{c}$  can be approximated by the moving average and simply removed from signal  $\mathbf{y}$ . The moving average is calculated at each data point in the signal vector  $\mathbf{y}$  by calculating the average of  $k$  points centered around the data point.

### 3.5.6 Reconstruction

Reconstruction is performed using the TVAL3 algorithm described in section 3.4.1. The algorithm takes in measurement matrix  $\Phi$ , signal  $\mathbf{y}$  and algorithm settings as arguments and outputs the reconstructed image. The setting used throughout all experiments is:

- $opts.mu = 2024$
- $opts.beta = 64$
- $opts.maxcnt = 10$
- $opts.maxit = 1000$
- $opts.tol\_inn = 10^{-5}$
- $opts.tol = 10^{-10}$
- $opts.mu0 = 2^4$
- $opts.beta0 = 2^0$
- $opts.nonneg = \text{true}$
- $opts.isreal = \text{true}$

Which solves for a real non negative solution described in section 3.4.1.

### 3.5.7 Image processing

From the reconstructed image some light image processing is done. There are only two operations applied to the reconstructed image and the reason why is that the images presented in the evaluation should represent what can be expected from the system. Furthermore often image processing is applied on special problems or artifacts in the images and it is not desired to cover up if there exist such problems. Therefore the two operations used is median filter and adjusting the intensity for higher contrast.

The reconstructed image has a high dynamic range and if only a small set of neighboring pixels is reconstructed with a high intensity peak which not correlates to the rest of the image these pixels will drop the contrast in the rest of the image, to remove these peaks the median filter is used. The

median filter will also remove "salt and pepper" noise while edges are preserved. The built in MATLAB function *medfilt2* will be used.

The second operation is an intensity transform to maximize the contrast in the image, the built in MATLAB function *imadjust* will be used.

### 3.6 Evaluation: Image quality assessment

The evaluation will be divided in to two categories: reconstructed images from synthetic data and images reconstructed from data acquired by the SPC.

All results is produced with subsampling ratios ranging from 5-30% and evaluated. The upper limit was set to 30% partly because of the hardware limitations with long exposure time and partly because the main advantage of CS/CI is to minimize the required subsampling ratio.

The evaluation on synthetic data is focused on evaluating the performance of the measurement matrix and reconstruction algorithm. Evaluating synthetic data gives two possibilities that can not be achieved with images reconstructed using the SPC which is that there is a reference image which the resulting image can be compared to.

Reconstructed image from synthetic data is acquired by creating a signal  $\mathbf{y}_{M \times 1}$  taking the inner product of  $\mathbf{y} = \Phi\mathbf{x} + \epsilon$  where,  $\mathbf{x}$  is the synthetic image reshaped to a vector,  $\Phi$  is the measurement matrix with the desired amount of measurements  $M$  and synthetic noise  $\epsilon$  which can be regulated to simulate different conditions, then using the reconstruction algorithm on the signal  $\mathbf{y}$  to obtain the reconstructed image  $\hat{\mathbf{x}}$ . Because the measurement matrix and reconstruction algorithm is independent of the SPC hardware the subsystem can be evaluated independently. Two advantages of evaluation the sensing and reconstruction independently of the SPC is that parameters such as number of measurements and noise can be regulated easy and the second advantage is that a reference image is available for comparison.

#### 3.6.1 Evaluation Using reference image

With a reference image available two image quality assessments are performed on the result from the simulation: Peak signal-to-noise ratio (PSNR) and SSIM. PSNR is defined as

$$\text{PSNR}[f(x, y), g(x, y)] = 10 \log_{10} \frac{E^2}{\text{MSE}[f(x, y), g(x, y)]} \quad (23)$$

where,  $f(x, y)$  and  $g(x, y)$  is intensity in pixel  $(x, y)$  and MSE is the mean square error between the images defined as

$$\text{MSE}[f(x, y), g(x, y)] = \frac{1}{mn} \sum_{x=0}^{m-1} \sum_{y=0}^{n-1} [f(x, y) - g(x, y)]^2. \quad (24)$$

The SSIM algorithm is not focused on pixel to pixel differences like PSNR but instead of the structure of the image in small windows. SSIM separates luminance, contrast and structure and calculates the difference in each category in a small window to calculate the similarity of the images. SSIM index is defined as

$$\text{SSIM}[f(x, y), g(x, y)] = \sum_n l[f(n), g(n)]^\alpha c[f(n), g(n)]^\beta s[f(n), g(n)]^\gamma, \quad (25)$$

where  $n$  is the window,  $\alpha = \beta = \gamma = 1$  and

$$\text{luminance: } l = \frac{2\mu_{f(n)}\mu_{g(n)} + C_1}{\mu_{f(n)}^2 + \mu_{g(n)}^2 + C_1}, \quad (26)$$

$$\text{contrast: } c = \frac{2\sigma_{f(n)}\sigma_{g(n)} + C_2}{\sigma_{f(n)}^2 + \sigma_{g(n)}^2 + C_2}, \quad (27)$$

$$\text{structure: } s = \frac{\sigma_{f(n)g(n)} + C_3}{\sigma_{f(n)}\sigma_{g(n)} + C_3}, \quad (28)$$

where,

- $\mu_{f(n)}$  and  $\mu_{g(n)}$  is window mean.
- $\sigma_{f(n)}$  and  $\sigma_{g(n)}$  is window standard deviation.
- $\sigma_{f(n)g(n)}$  is window cross covariance.
- $C_1 = 0.01 * 255$ , (MATLAB default).
- $C_2 = 0.03 * 255$ , (MATLAB default).
- $C_3 = C_2/2$ , (MATLAB default).

Which summarizes to

$$\text{SSIM}[f(x, y), g(x, y)] = \sum_n \frac{(2\mu_{f(n)}\mu_{g(n)} + C_1)(2\sigma_{f(n)g(n)} + C_2)}{(\mu_{f(n)}^2 + \mu_{g(n)}^2 + C_1)(\sigma_{f(n)}^2 + \sigma_{g(n)}^2 + C_2)}. \quad (29)$$

The SSIM index has a max value of 1 when the images are identical which makes it easy to read. [17]

### 3.6.2 Evaluation Using no reference quality assessment

In order to evaluate image quality when there is no reference image to compare against the BRISQUE algorithm is used as a complement. BRISQUE is a no reference image quality assessment model which is based on natural scene statistics and quantifies the "naturalness" of the image. [18]

### 3.6.3 Evaluating Using Edge response

The edge response measures the sharpness of the image by calculating the distance in pixels required for an edge in the image to rise. In this thesis the distance required for the edge response to rise from 10% to 90% was chosen, in figure 12 an illustration of the definition is shown. This evaluation is performed on static images captured in constant light indoors for consistent results, furthermore the motive of the image is slanted geometric objects printed on a sheet of paper.[19]

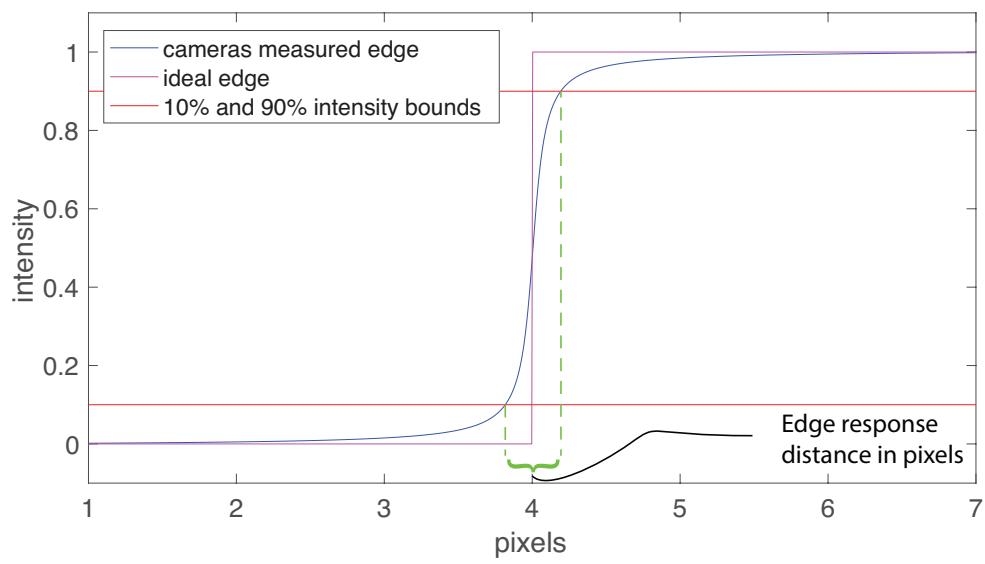


Figure 12: Definition of 10-90% Edge response.

### **3.7 Method criticism**

- No Reference Image Quality Assessment is not designed for SWIR images or SPC:s characteristics noise therefore the results may not reflect how the QA would answer to visual wavelength cameras. BRISQUE definition of "naturalness" may not reflect the images captured by the SPC.

## 4 Evaluation

This section is structured as, for each experiment and setup a detailed explanation and motivation on how and why the experiment is needed followed by the results of that experiment. The experiments are motivated by gathering as much information and results as possible to answer the research questions. The first subsection 4.1 will present the results from experiments with synthetic data where a reference image is available. The second subsection 4.2 will present the result from images reconstructed from the SPC. No perfect reference image is available in those experiments therefore the images will be evaluated against near optimal image, no reference QA and against a state of the art SWIR camera.

### 4.1 Simulated Results

In this section the results produced was simulated by using the reconstructing algorithm and measurement matrix described in section 3.4.1 and 3.3.1 on high quality images captured with a state of the art SWIR camera. The images captured by the SWIR camera acts as a ideal reference to the reconstructed images. By simulating the result from "ideal" images the reconstruction process gets a benchmark independent of the SPC.

#### 4.1.1 Reconstruction performance Using reference image

In these simulation 21 images captured with a state of the art SWIR camera was reconstructed. The performance of the reconstruction was calculated using PSNR and SSIM for different degree of noise and sub sampling ratios.

To reconstruct the images first the measurement vector was created by calculating the inner product between the measurement matrix  $\Phi$  and SWIR image  $\mathbf{x}$ ,

$$\mathbf{y}_{IDEAL} = \Phi \mathbf{x}, \quad (30)$$

where  $\mathbf{y}_{IDEAL}$  is an ideal measurement vector given  $\Phi$  and  $\mathbf{x}$ . In the next step white Gaussian noise was added to the normalized measurement signal. The added noise represent a simple model of the noise perturbing the signal in the SPC.

$$\mathbf{y}_R = \mathbf{y}_{IDEAL\_NORMALIZED} + \epsilon, \quad (31)$$

where  $\mathbf{y}_R$  is the measurement vector used when reconstructing the image and the white Gaussian noise  $\epsilon$  added was scaled with the standard deviation  $\sigma$  between  $0 - 0.2$ .

To create the graphs in figure 14 and 15 this procedure was applied to all 21 images for sub sampling ratio 5% to 30% and added noise with standard deviation between  $0 - 0.2$ . The standard deviation is not increased above 0.2 because the reconstruction fails at that point. In figure 13 a sample of reconstructed image from one of the SWIR images is presented with different amount of noise and sub sampling ratios.



(a) Reference image

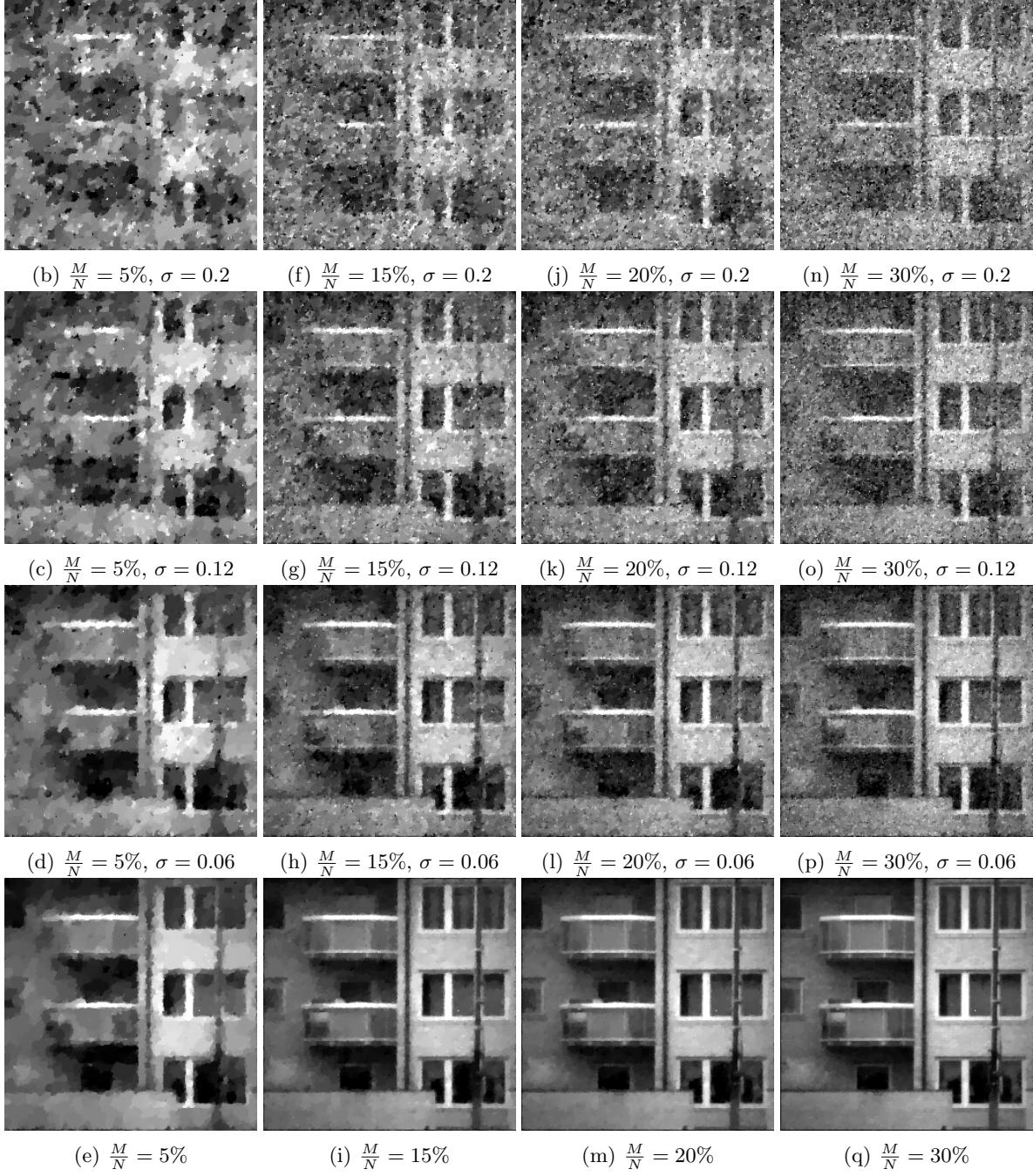


Figure 13: Example of reconstructed images with added noise at different sub sampling ratios.

As seen in figure 13 the reconstructed image quality increases with more measurements and lower noise levels. This observation is confirmed in the graphs i figure 14 and 15 where PSNR and SSIM respectively has been calculated for all 21 reconstructed images and interpolated.

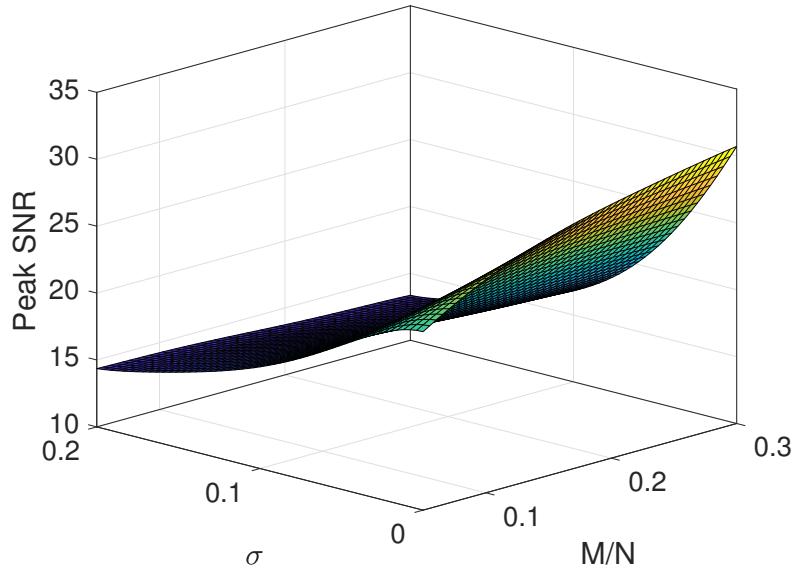


Figure 14: Peak SNR result depending on number of measurements and simulated noise level.

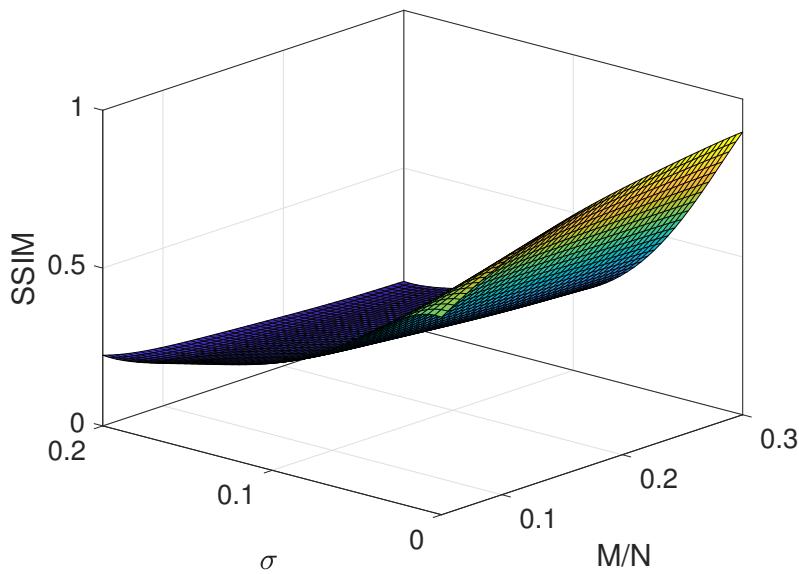


Figure 15: SSIM result depending on number of measurements and simulated noise level.

A second observation is that, when the noise increases the reconstructed image quality is not improved at the same rate as the noiseless case when increasing the sub sampling ratio.

#### 4.1.2 Reconstruction performance Using no reference quality assessment

In this sub section the same reconstructed image set from section 4.1.1 is used to calculate the no reference image quality with the BRISQUE algorithm. This is the same algorithm which will be used to evaluate the results from the SPC therefore this experiments will yield a benchmark on how good results that can be obtained given the measurement matrix and reconstruction algorithm.

The results displayed in the graph in figure 16 shows the same trend as the results from the previous section, less noise and more samples yields better performance in the reconstruction. The figure also contain the mean results from the original SWIR images as the flat blue surface, which has scored a far superior score than the reconstructed images.

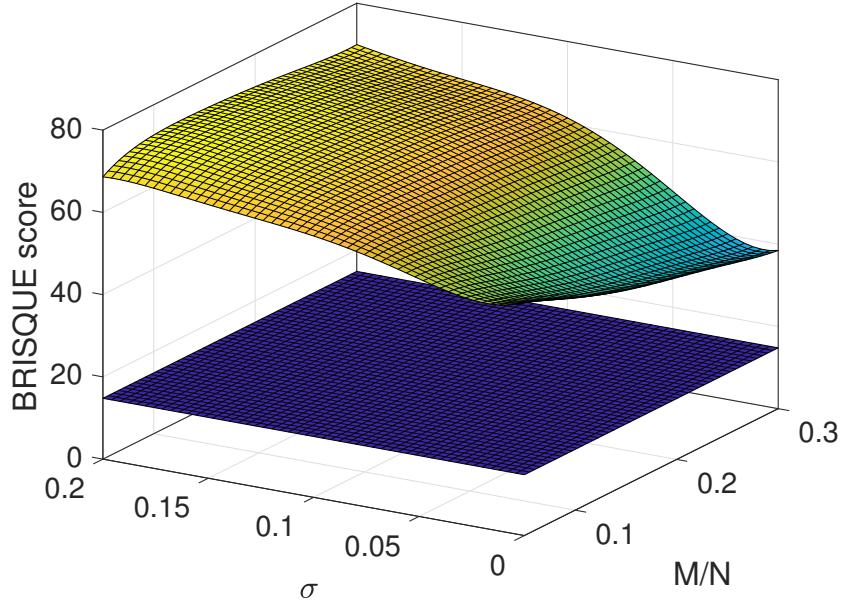


Figure 16: BRISQUE result depending on number of measurements and simulated noise level. Lower surface is reference image score.

In figure 17 the result has been flatten to a 2D graph with fewer selected data points for clarity. Even in the noiseless case the score will not be better then approximately 40 for the reconstructed images while the SWIR images has a mean value of 15. The conclusion from this result is that, with the current measurement matrix and reconstruction method around 40 in BRISQUE score is what to expect as optimum given that the SPC will induce noise to the signal.

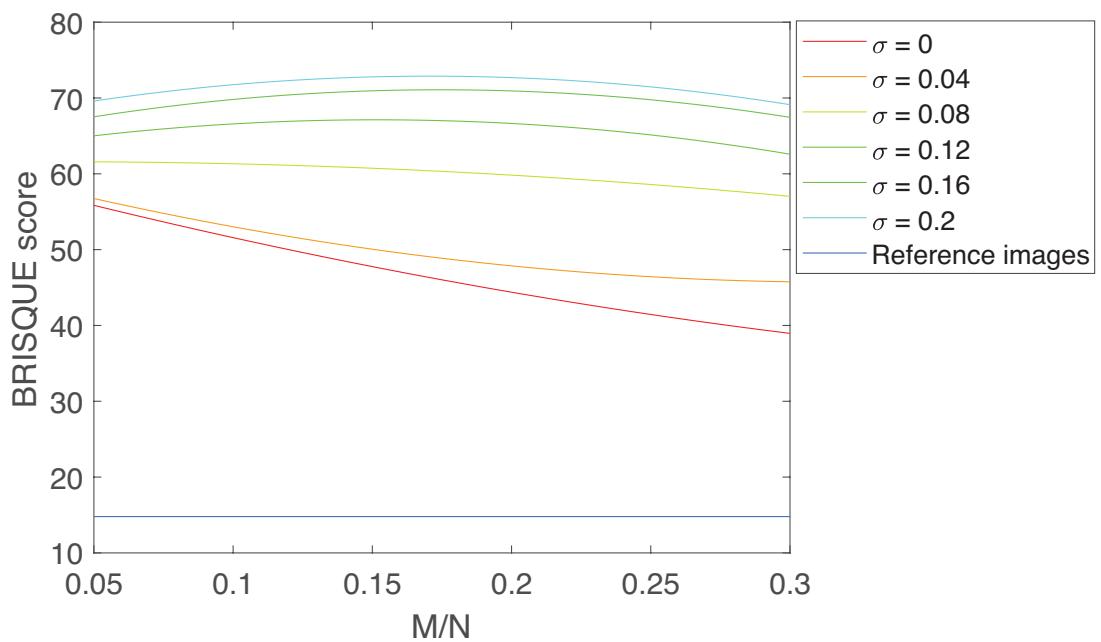


Figure 17: BRISQUE result depending on number of measurements for different simulated noise levels.

#### 4.1.3 Dynamics in scene

In the current experimental SPC setup the exposure time is between 10 to 50 seconds which increases the chance of dynamics in the scene. Dynamics in the scene will reduce the reconstruction performance because the signal is assumed to be constant. By simulating dynamics in a controlled environment the measured signal characteristics for different cases can be identified. Dynamics in the scene can roughly be roughly divided into two separate categories, luminance change and movement. In this section global luminance change and two kinds of motion be simulated. The goal is to interpret how the signal change and if it can be suppressed for better reconstruction.

In the first scenario a object is placed in an image but for each measurement the location of the object will be moved in a bounded area of the image. This model represents a scene where the background is static but a person is standing in the same area but moves around.

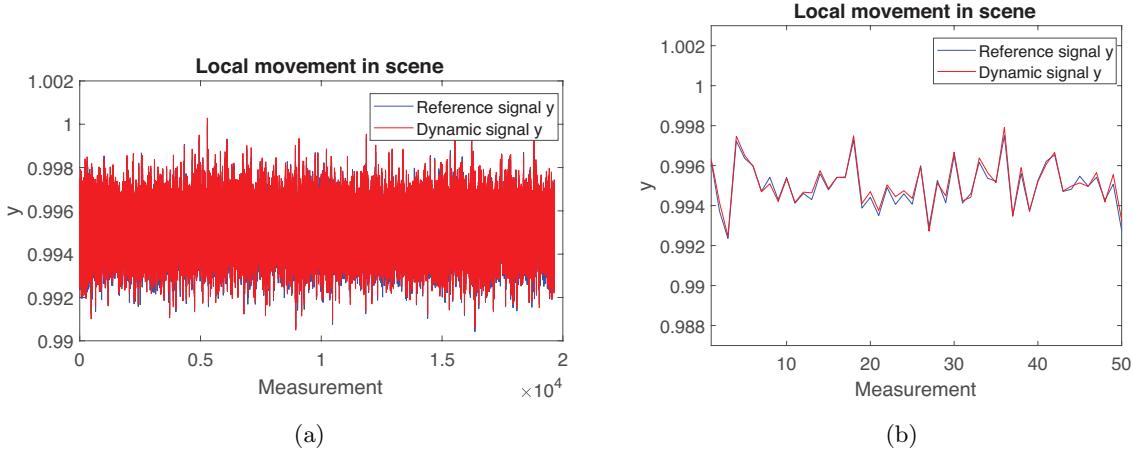


Figure 18: (a) Perturbed signal from local movement on top of reference signal. (b) Zoomed in view of some samples from figure (a).

As seen in figure 18a there is no obvious difference between the non perturbed reference signal and the distorted signal. In figure 18b where some of the samples is displayed no large difference can be seen either.

The reconstructed images from the reference signal and the perturbed signal is displayed in figure 19b and 19c respectively. The difference between the reconstructed images is visible to the naked eye, not only does the object moving around get blurry and noisy but the whole image globally.

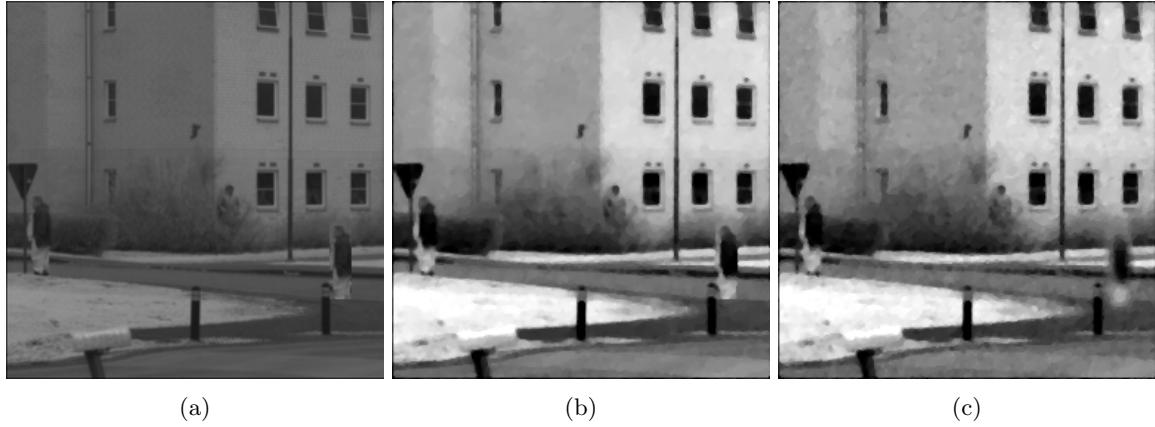


Figure 19: The results of local movement on a reconstructed image, sub sampled at 30%. (a) Original reference image. (b) Reference image reconstructed from the original image without movement. (c) Reconstructed image from a scene with local movement.

In table 2 the results from calculating PSNR and SSIM between the reconstructed images is presented. It can be observed that the image has been effected to some degree by the movement.

Peak SNR	SSIM
29	91

Table 2: Effects comparing non perturbed reconstructed image against reconstructed image with local movement

The second scenario is an object passing through, moves out or moves to an other place in the scene far from the original place. The problem is modeled with a static background then as the simulated measurement is acquired the object will cross the scene, like a car, human or animal might do when using the SPC. The object will cross the scene in 1000 measurements of approximately 19000 which corresponds to approximately 0.7 seconds when sampling measurements with the SPC in its current setup.

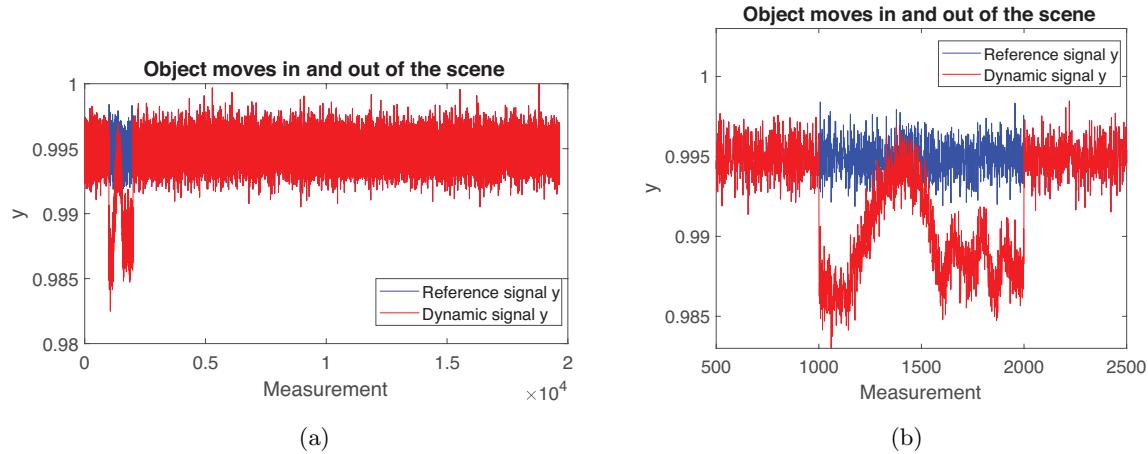


Figure 20: (a) Perturbed signal from large movement on top of reference signal. (b) Zoomed in view of some samples from figure (a).

As seen in figure 20 the exact moment the object enters the scene the signal changes. This is because a completely new structure has entered the scene and therefore changing the DC level. It can also be noted that the object passed something which has approximately the same intensity as the background and therefore the DC signal almost comes back up to its original state for a brief moment.

In figure 21 the effect of the moving object can be seen in the reconstructed image which has gained a lot of global noise. Note that the object passing trough can not be seen because there is more measurements with the background and the object moving creating uncertainty in the whole image.

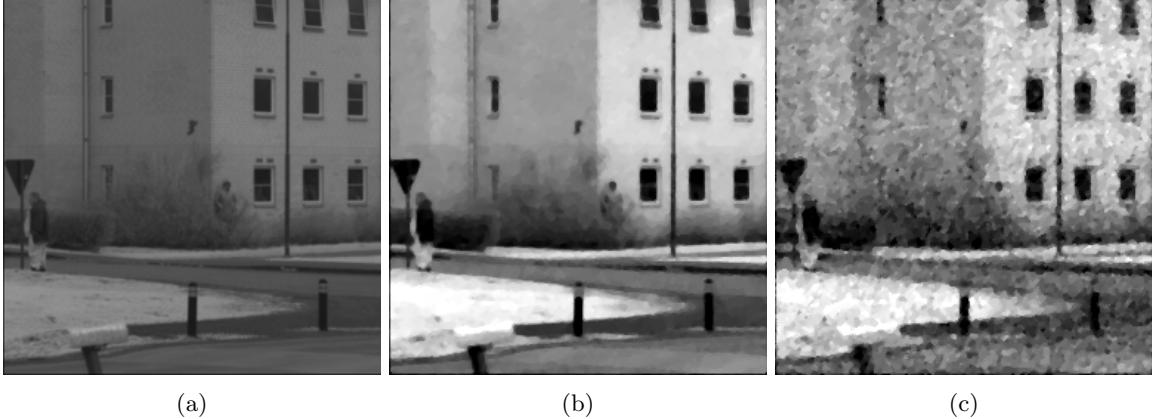


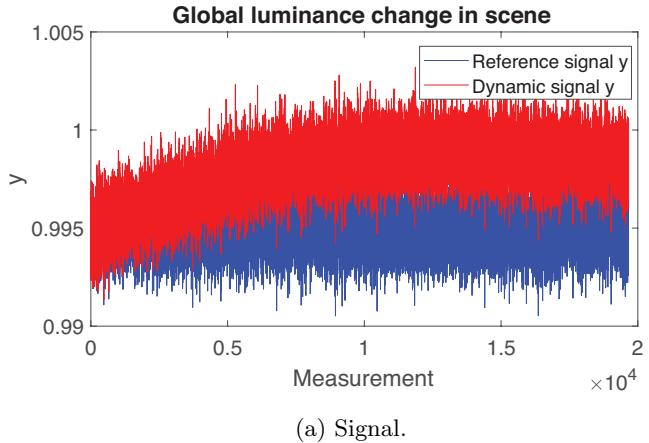
Figure 21: The results of large movement on a reconstructed image, sub sampled at 30%. (a) Original reference image. (b) Reference image reconstructed from the original image without movement. (c) Reconstructed image from a scene with object passing trough.

In table 3 the results from calculating PSNR and SSIM between the reconstructed images is presented. It can be observed that the image has been effected heavily by the movement.

Peak SNR	SNR	SSIM
23	18	58

Table 3: Effects comparing non perturbed reconstructed image against reconstructed image with local movement

The third scenario is luminance change in the scene which is caused by inconsistency of light intensity from the source. Outdoors this means that the light intensity from the sun will vary over time, the most obvious being clouds occluding the sun but even change in air density can change the intensity. This scenario is modeled by adding or subtracting the global intensity in the image over the measurements.



(a) Signal.

As seen in figure 22a the DC level of the signal will slowly change but the stricture of the signal stay the same. In figure 23 the reconstructed images from the perturbed signal and the reference signal is displayed. The reconstructed image from the dynamic signal has gained a lot of global noise even though the structure in the image has not been changed over the measurements.

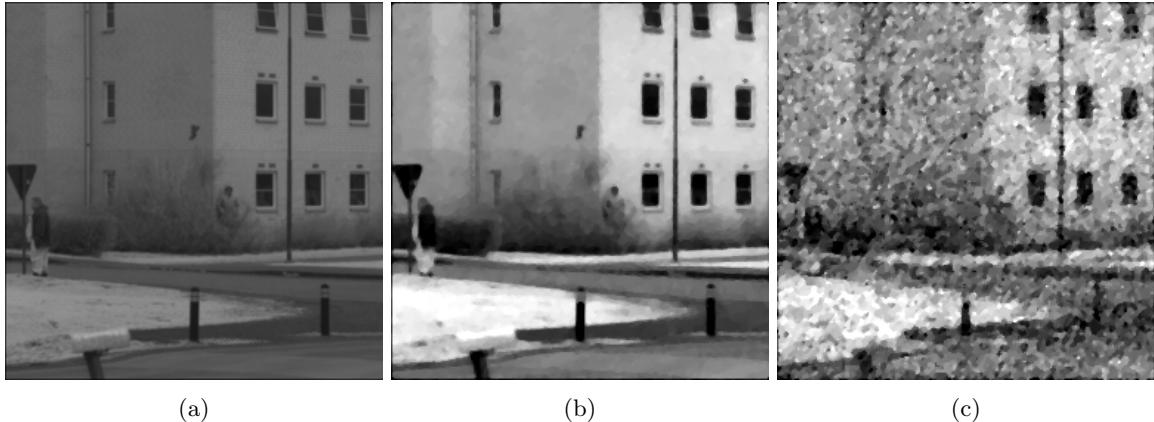


Figure 23: The result of global light intensity change on a reconstructed image sub sampled at 30%  
 (a) Original reference image. (b) Reference image reconstructed from the original image without light  
 intensity change. (c) Reconstructed image from a scene with global light intensity change over the  
 measurements.

In section 3.5.5 a model of this problem was proposed with a algorithm to suppress the impact of global luminance change. The algorithm is applied to this experiment to evaluate its performance. The moving average subtraction method is applied and in figure 24a the resulting signal is plotted over the dynamic signal, the improved signal is stationary again. In figure 24b and 24c where the processed signal is plotted over the reference signal it can be seen that the processed signal has gained its original structure and almost fit exactly to the original.

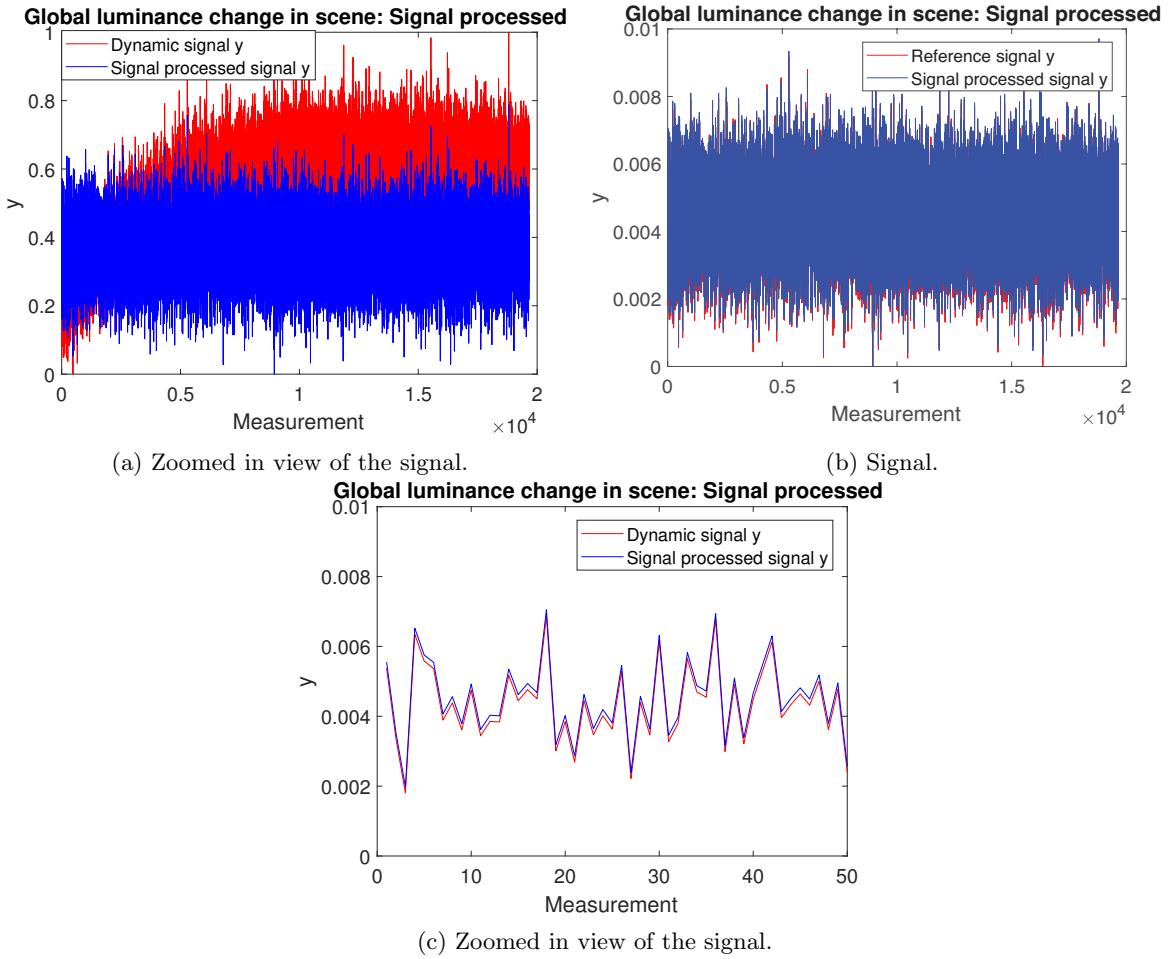
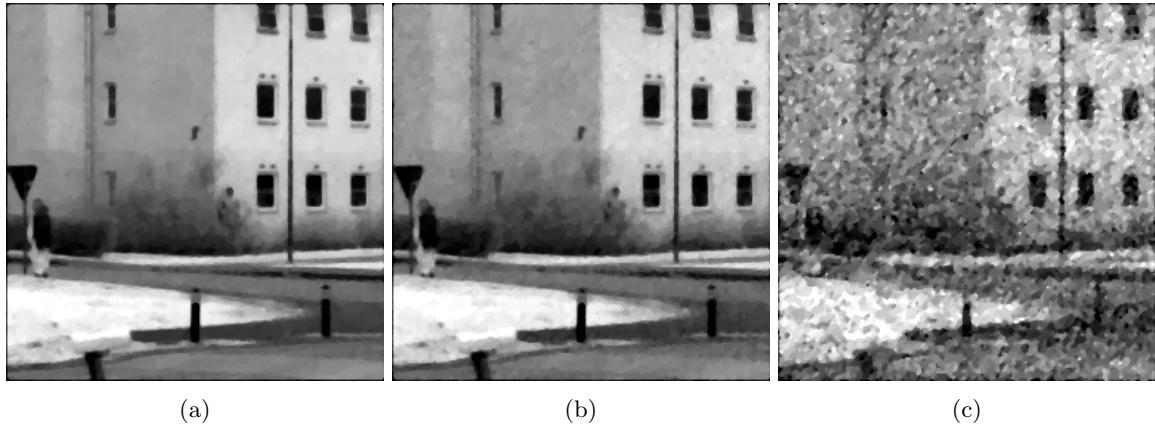


Figure 24: Global movement, acquired signal

In figure 25 the processed signals reconstructed image is displayed between the reference and perturbed signals reconstructed images. The signal processing improve the reconstruction significantly, the image has gained some noise compared to the reference image but over all there is not much difference between them.



(a)

(b)

(c)

Figure 25: The result of processed signal perturbed by light intensity change on a reconstructed image sub sampled at 30% (a) Reference image reconstructed from the non perturbed signal without light intensity change. (b) Reconstructed image from a scene with global light intensity change over the measurements signal processed. (c)Reconstructed image from a scene with global light intensity change over the measurements.

In table 4 the results from calculating PSNR and SSIM between the reconstructed images is presented. As in the images, the results after the signal processing is significantly higher.

	Peak SNR	SSIM
Perturbed signal	19	38
Mean subtracted signal	33	93

Table 4: Effects comparing non perturbed reconstructed image against global luminance change perturbed reconstructed image and mean subtracted signal reconstructed image.

## 4.2 SPC evaluation

The evaluation section is now shifted to examine the images produced by the SPC. The images will be analyzed using a range of methods to examine the performance of the SPC. In this section the BRISQUE algorithm will be used again where connections to the previous result is drawn, a reconstructed image will be compared to an ideal image using homography, a set of images is presented reconstructed at different subsampling ratios, a edge response analysis is performed and the correlation between reconstruction performance and noise is conducted. All images captured by the SPC with natural scenes was taken at a distance between 200 to 900 meter in sunny days with some clouds.

### 4.2.1 Reconstructed performance Using reference image

This evaluation is designed to get a measurement of expected image quality with the same metrics used in the synthetic case. As stated before, it is hard to obtain a reference image to the images produced by the SPC. One solution to obtain a reference image is to calculate a homography between images. But there are two problems of just performing a homography to obtain a reference image, the first one is that, homography estimates the transformation between flat surfaces which excludes most natural images, and the second is that, the estimated homography will not be perfect and thus for example high contrast edges in the images will not match and then produce large errors in the performance measurements. To solve these two problems the scene is a flat surface with a printed pattern and to avoid the error from sharp edges the pattern is constructed without any. To not complicate this experiment the reference image is the computer generated optimal images which is being transformed to fit the image captured by the SPC.

The reference homography transformed image which was created using sine functions to avoid edges can be seen in figure 26 with the reconstructed images with different subsampling ratio.

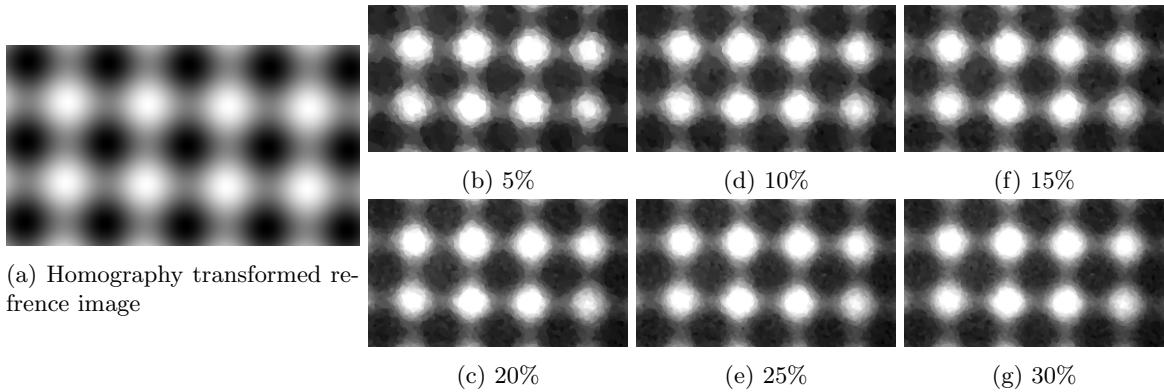


Figure 26: The reconstructed images with different number of measurements and the reference image transformed to fit the SPC images using homography.

Before the results from the evaluation is presented it is worth noting that the reference image is a perfect simulated reference image, which was not effected by the uneven light source and quality of the print as the reconstructed image from the SPC, which for example can be seen in the edges of the reconstructed images in figure 26b to 26g. In figure 27 below the same evaluation method as the reconstructed simulated images in section 4.1 is used, PSNR and SSIM, because there is a reference image again.

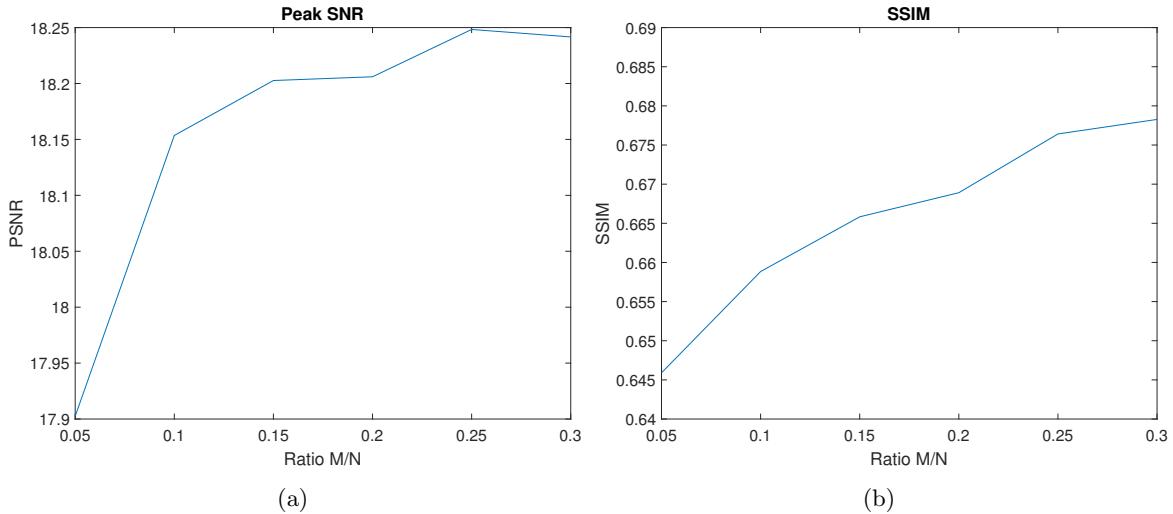


Figure 27: Signal quality of SPC images compared to reference image. (a) Peak SNR for reconstructed images against reference image. (b) SSIM score for reconstructed images against reference image.

The result shows the same expected result as before with increased quality with increased subsample ratio. An second observation confirms the observation made in section 4.2.5, where the image quality is rapidly improves when increasing subsample ratio to to 15%, then the improvement rate stagnates.

#### 4.2.2 Reconstruction performance Using no reference quality assessment

In this section the blind quality assessment tool BRISQUE will be used to score the reconstructed images from the SPC. The same algorithm was used on the simulated data where a benchmark was set as a theoretical limit to the reconstructed images.

Each image is evaluated at subsampling rate from 5% to 30% where the result is presented in figure 28.

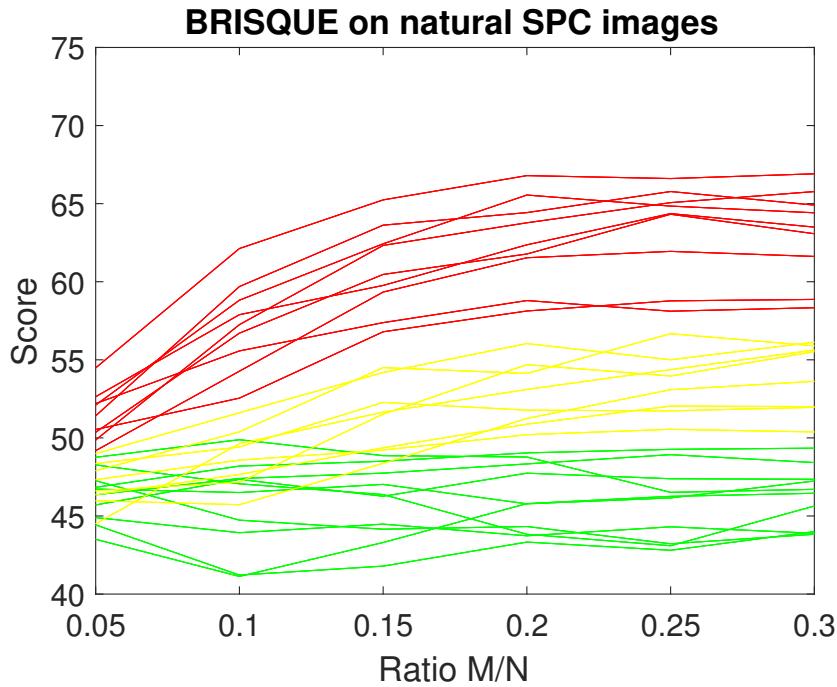


Figure 28: BRISQUE score for images reconstructed from the SPC with subsampling ratios from 5% to 30%. Each line represent one image and is classified with different colors representing start score at smallest subsampling ratio and general trend when subsampling ratio is increased.

As seen in figure 28 each image has been plotted separately, this is because the high variance in the scores and the distinct different trends in the score. Furthermore the images has been classified into three different classes depending on the initial score at 5% subsampling and the trend when increasing the subsampling ratio. The classes has been color coded where:

- Red means bad score from the first subsampling ratio and a trend line where the score gets worse with more samples.
- Yellow represent good initial score but the trend line indicates worse image quality when subsampling ratio is increased.
- Green represent both good initial score and better or stationary score when subsampling ratio is increased.

an visually inspecting the images

When studying the BRISQUE score plot in figure 28 from the SPC and comparing to the plot of BRISQUE scores from simulated images in figure 17 some similarities can be found. The first one is that, the best scores from the SPC has the same score as the simulated images with small or no noise added, which means that the SPC can compare to the benchmark set by the simulated images and thus gives theoretical optimal reconstruction given the measurement matrix and reconstruction algorithm. The second similarity is the trend of the "bad" images which has approximately the same score and trend as the simulated images with larger noise added to the sampled signal. In the last part of this subsection the reconstructed images will first be presented and analyzed followed by a noise analysis to conclude if there is a correlation between noise level and BRISQUE score.

In figure 29 to 31 a sample of reconstructed images are presented from each class with subsampling ratio 30%.

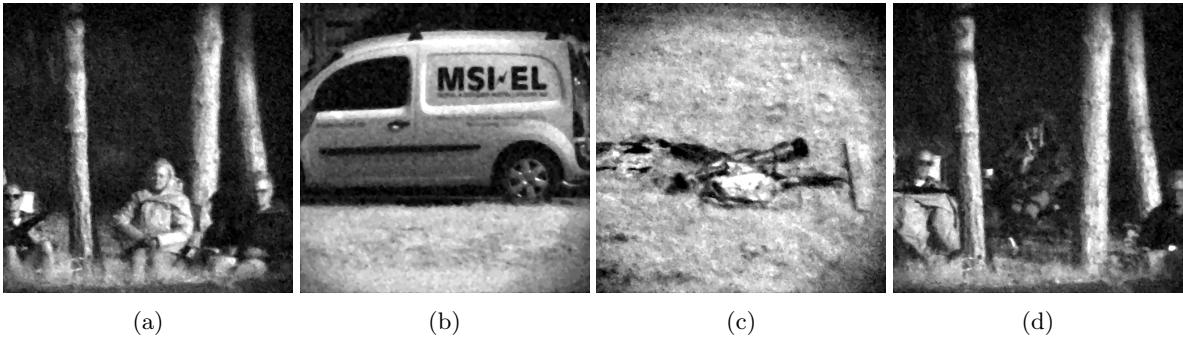


Figure 29: Sample of "good" images corresponding to the green lines in figure 28. (a) and (d) People sitting in the edge of a forest. (b) Stationary car. (c) Camouflage jackets and a AT-4 anti-tank weapon on the ground.

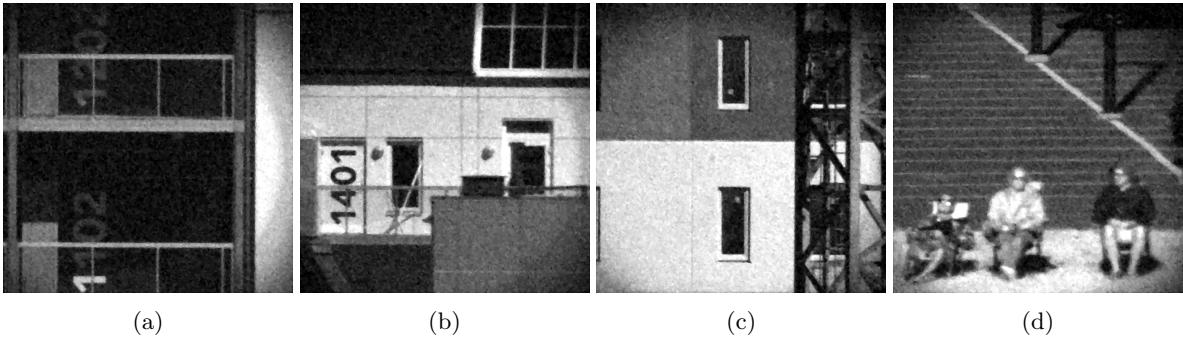


Figure 30: Sample of "medium good" images corresponding to the yellow lines in figure 28. (a) People sitting next to a parking lot. (b) - (d) House facades.

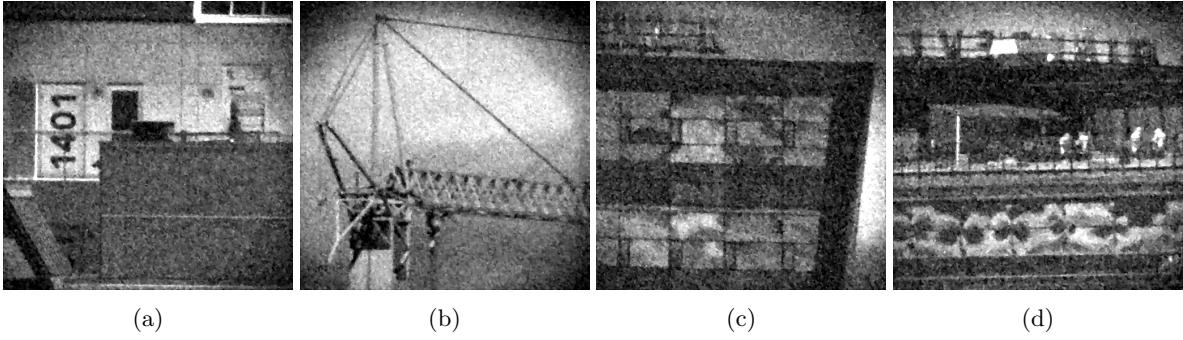


Figure 31: Sample of "bad" images corresponding to the red lines in figure 28. (a) House facade. (b) Crane (Moving clouds in background). (c) Mjärdevi Center facade (Moving clouds reflection in windows). (d) Mjärdevi Center balcony with people having a break (Moving clouds reflection in windows).

Lets study the images in figure 29 to 31, the difference between "good" and "half good" images are very subtle, the intensity and visible noise level is a bit better in the "good" images. Between the "good"/"half good" and "bad" images there is a more noticeable difference, the images in the "bad" set has more distinct noise and lower over all intensity.

When the images was sampled a correlation between the mean signal strength and reconstruction performance was noticed, this is due to the constant background noise from the SWIR photo diode. In figure 32 the mean sampled signal strength was plotted against SNR and signal variance calculated from normalizing the sample signal and background noise. The variance was calculated in the same way as the simulated signals in section 4.1. Each signal has the same corresponding color code from the BRISQUE plot in figure 28.

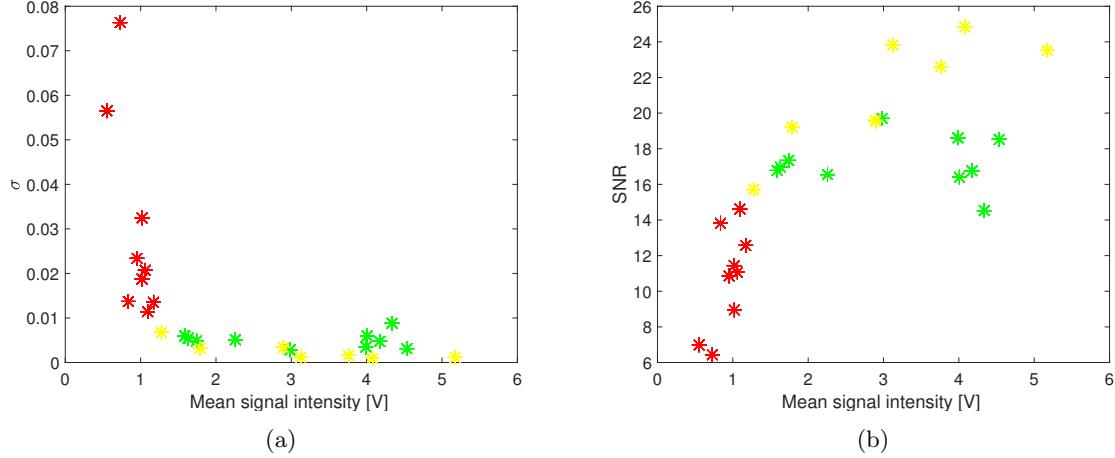


Figure 32: Mean sampled signal intensity compared to normalized signal and background noise where each signal has the same corresponding color code from the BRISQUE plot in figure 28. (a) Signal intensity against normalized variance from background noise. (b) Signal intensity against SNR from normalized signal and background noise.

From the two plots in figure 32, some observations can be made:

- From both plots in figure 32 there is a quite distinct threshold where the signals intensity overcomes the noise level to reconstructed "good" images around 1.2 volt. None of the "good"/"half good" images are below this signal intensity but are mixed over the threshold.
- In the plots there are only two signals with higher variance than 0.04.
- There are three red images with almost the same SNR and mean signal intensity as yellow and green images but yields a worse BRISQUE score anyway.
- The yellow and green images is mixed for all mean signal strengths.

Finich this section?

#### 4.2.3 Luminance Change in scene

As predicted in section 3.5.5, dynamics in the scene could result in poor reconstruction performance and an algorithm to suppress this distortion was proposed and tested with good result in the simulated case in section 4.1.3. With a exposure time of just under one minute for the SPC this problem turned out to be constantly present when taking photos at natural scenes outdoors, and the luminace change over time was more complex then the simulated test case. It turned out that the sensor was highly sensitive to luminace change which could not be perceived with the naked eye. This observation should not be unanticipated, the sensor sums up half the scenes light which make the tiniest intensity change for each pixel a large global change. So how did the algorithm hold up for

the real application? In figure 33 the raw sampled signal is colored red which clearly is not a stationary signal, with the moving average in green and the final improved signal in blue.

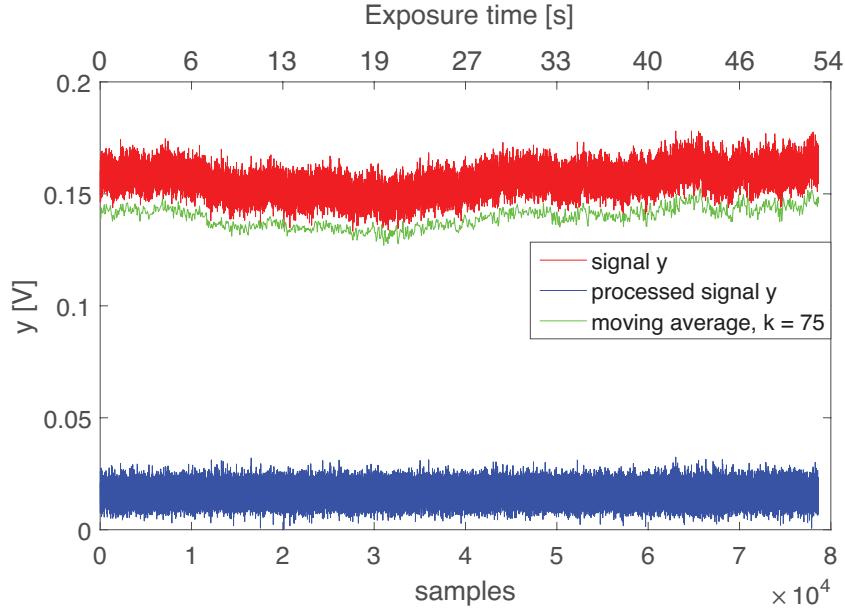
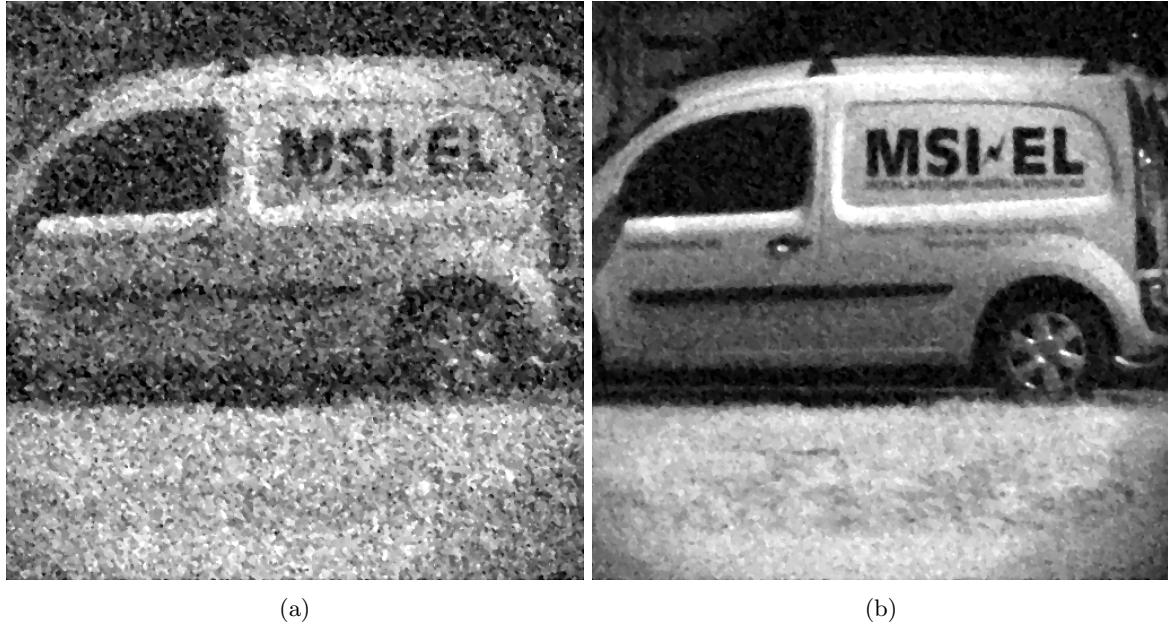


Figure 33: Sampled signal from SPC with light intensity change and the improved moving mean processed signal.

As can be seen on the moving average plotted, the intensity change is very fast and can change in matter of a split of a second, "k" which is the number of neighboring samples to calculate the average was set to 75 to match the fast change which corresponds to a window of 50 milliseconds.

In figure 34 a reconstructed image without the method used and one with the method used is displayed.



(a)

(b)

Figure 34: Reconstructed images, (a) before and (b) after applying moving mean average method.

As can be seen in the figure, the method produces good result, the image reconstructed without the signal processing has a severe global noise due to the non stationary signal and the reconstruction performance significantly significantly lower. This images is actually one of the images captured in good conditions with strong lighting and mild intensity change overall.

#### 4.2.4 Edge response

The edge response is used to comparing the sharpness of cameras and lenses. The edge response from the SPC is compared to a state of the art SWIR camera. Two scenes was captured by the SPC and a conventional SWIR camera containing printed sheath of paper with simple tilted shapes on them, see figure 35. The scene was lit by a 135 Watt halogen lamp placed two meters from the sheath.

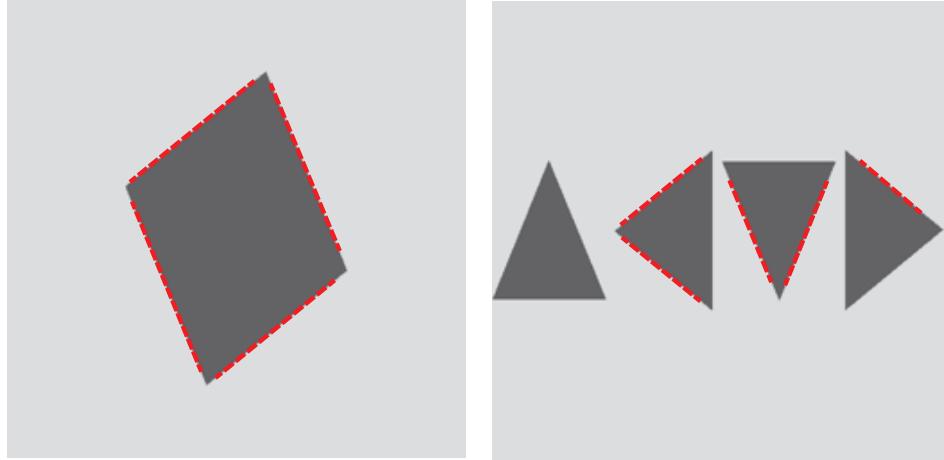


Figure 35: Printed targets with markings where the edge response measurements was performed

In the resulting images, edge response measurements was gathered from the specified edges in

figure 35, with the result from all edges and both images for respective cameras, a mean and standard deviation is calculated. For the SPC, images reconstructed from 5% to 30% was tested in order to see if the subsampling ratio effected the MTF result. In figure 36 the images from the SWIR camera and SPC are presented.

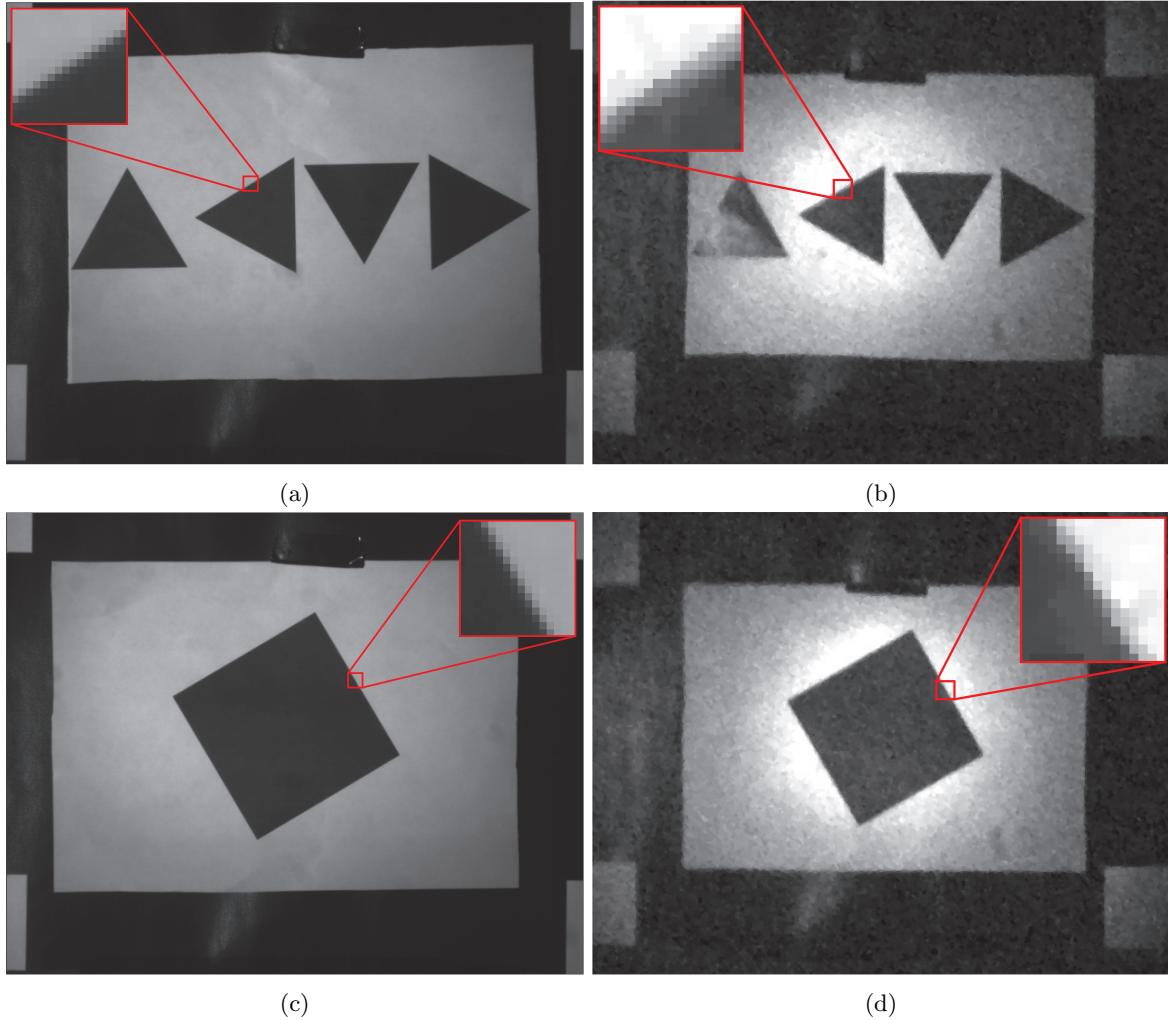


Figure 36: SPC and state of the art SWIR camera images. (a) and (c) from the conventional SWIR camera and (b) and (c) captured with the SPC.

The edge response is measured in the distance (pixels) required for a edge to rise from 10% to 90% intensity change. In figure 37 the result from the experiment in presented.

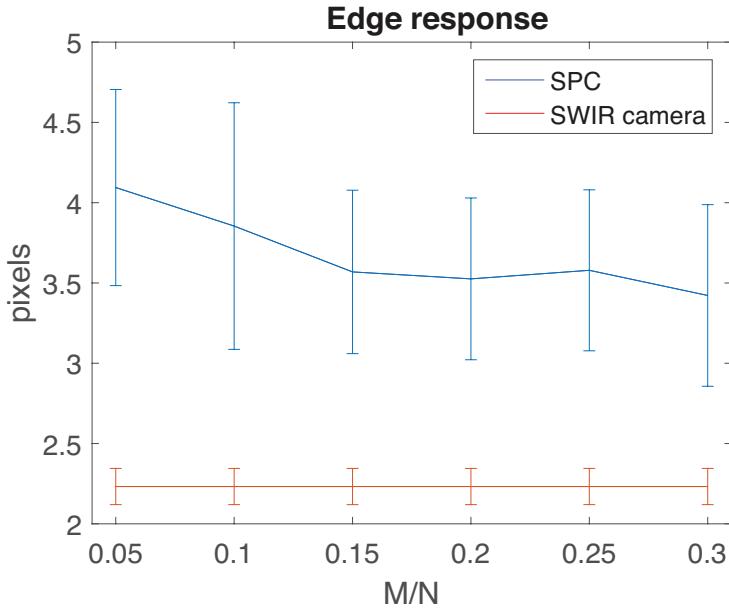


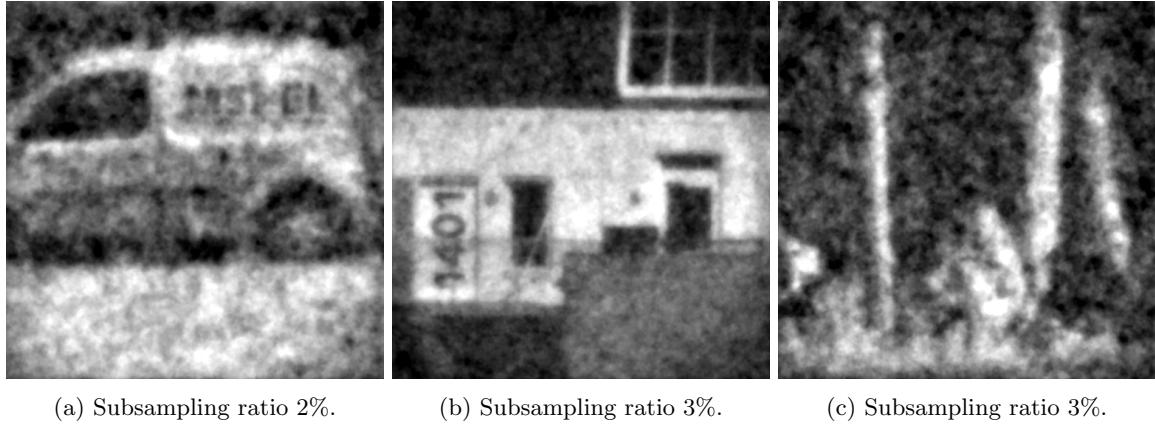
Figure 37: Edge response, distance (pixels) to rise from 10-90% in average for an edge.

From the plot in figure 37, a clear difference between the SPC and state of the art SWIR camera can be seen, where the conventional SWIR camera has in average half the distance against the SPC images. Some improvement is seen when the subsample ratio is increased, but the standard deviation is almost constant, meaning that the difference between the state of the art SWIR camera and the SPC, in best case only differ about 0.5 pixels, but in the worst case differ about 1.7 pixels and in average 1.2 pixel.

#### 4.2.5 Subsampling ratio

From the theory of compressive sensing the number of measurements needed to reconstruct an image is correlated with the sparsity or compressibility of the image, therefore it is hard to give a good estimate of a subsampling ratio needed to obtain a desired quality of the reconstruction. In addition, using a SPC where noise contaminate the signal and the scene may not be completely stationary, the number of measurements needed will increase in proportion to the noise and the change in the scene. In this subsection the minimum subsampling ratio will be presented followed by how the reconstructed image quality is effected by an increase of subsampling ratio.

The minimum number of measurements to reconstruct a image where the motive can be recognized is also effected by the factors described, trying to reconstruct an image under the minimum subsampling ratio results in an image with just noise. A survey of the minimum subsampling ratio was performed on all images captured by the SPC in this thesis, and the result ranged from 2% to 4% to obtain a recognizable images, in figure 38 a sample of three images with varying minimum subsampling ratios is displayed.



(a) Subsampling ratio 2%. (b) Subsampling ratio 3%. (c) Subsampling ratio 3%.

Figure 38: Varying minimum subsampling ratios to reconstruct sample images captured by the SPC.

In the sample images in figure 38 the minimum subsampling ratio varied between 2% to 3%, but as can be seen, this is only the minimum subsampling ratio where the motive is merely recognizable, large structure can be identified but detail is lost. In general a subsampling ratio of 5% has always succeeded to reconstruct a identifiable image with some fine details, moving along this topic the results from higher subsampling ratios is presented.

In figure 39 three scenes is reconstructed using different subsample ratios ranging from 5% to 30%, for each row the subsampling ratio is increased by 5% and at the top a reference image from a visual camera is presented. What should be expected is increased image quality with increased subsampling ratio, this result can give an perception of which subsampling ratio is good enough for a given purpose, and as can be seen, the increase of subsampling ratio is not linear proportional to the increase in perceived image quality, just like regular image compression.



(a) Visual camera image.



(b) Subsampling ratio 5%



(c) Subsampling ratio 10%



(d) Subsampling ratio 15%



(e) Subsampling ratio 20%



(f) Subsampling ratio 25%



(g) Subsampling ratio 30%

Figure 39: Reconstructed images captured by the SPC with increasing subsampling ratios. First row showing a reference visual spectrum image followed by SPC images reconstructed with 5% from top then increased subsampling ratio by 5% for each row to 30% on the last row.

There are a few things that can be noted in the images in figure 39,

- the reconstructed images behave as expected, when the subsample ratio increases the image quality increases.
- Already at 5% subsampling ratio the scene can be properly identified unlike the case in minimal subsamples ratio. The images have some artifacts that can be linked to the reconstruction algorithm, the images look like they are made of small patches.
- Between 10-15% the finer details start to appear, like the gap between the panels in the facade, the text on the car and door are getting sharper and the structure of the faces start to appear.

- As stated before, the image quality does not increase at the same rate as the subsampling ratio, this is most noticeable when increasing the subsampling ratio above 15%. The improvement after 15% is not as easy to spot as from the increments before, but they can be found in the details.

## 5 Discussion

In this section the results and method is analyzed and discussed. When discussing results a focus on consistency, relation to theory and real world applicability is held. In the discussion of method an analysis of replicability, reliability and validity is held.

### 5.1 Result

Overall the results obtained in this thesis reflects what has been stated in the theory and research, but no reference to the use of SPC in natural environment could be found and thus this thesis will present the link between real world application and theory/lab results and the challenges that come with it.

#### 5.1.1 Reconstruction performance Using reference image

In the simulated reconstruction the results behaved in most part as expected given the CS theory, with increased subsampling ratio the performance increased. But the interesting part of this results is whats happening when increasing the noise, not only does the general performance drop for all subsample ratios, but also the improvement rate by increasing the subsample ratio drops, which figure 32 and 15 shows. This result tells us that if the signal contains a high degree of noise, a larger subsampling ratio may not improve the reconstructed image as mush as expected.

When obtaining the same measurements with the SPC one low frequency image was captured and reconstructed, with near optimal SNR and environment such that a homography between the reconstructed image and reference image could be made with good precision. In figure 27a and 27b we can see the PSNR and SSIM of the image given the reference image, as expected from theory and confirmed in the simulated case the performance increases when the subsampling ratio increases. But if we look closer at the PSNR plot we can see that the largest increase in performance is up to 15% subsampling ratio, which can be confirmed when inspecting the images in figure 26b-26g, where the image quality rapidly improves when increasing subsample ratio up to 15%, then the improvement rate stagnates.

#### 5.1.2 Reconstruction performance Using no reference quality assessment

For the simulated reconstruction in figure 16, we can see that the graph looks like a upside down version of the PSNR and SSIM graphs of the simulated images. This results alone is positive for this theses because it was unknown if this method would work well for SWIR images and reconstructed images. An observation that can be made, is that the reference images score about 20 BRISQUE points better then the best reconstructed images and we can conclude that the sampling and reconstruction even in the best case scenario without noise, will not be as good as an conventional camera. We can see from the plot that in the ideal case the score will not be better then approximately 40 BRISQUE points for the reconstructed images while the SWIR images has a mean value of 15. We can concluded from this result that, with the current measurement matrix and reconstruction method, around 40 in BRISQUE score is what to expect as optimum given that the SPC will induce some noise to the signal.

When studying the plot with BRISQUE score given by the results from images reconstructed from the SPC in figure 28, we can see that the best images score just over 40 BRISQUE points, which is the same score as score as simulated images with small or no noise added, which means that the SPC can compare to the benchmark set by the simulation and thus gives a theoretical optimal reconstruction given the measurement matrix and reconstruction algorithm. Furthermore we can see that the trend of the images follows the same characteristics as the simulation in figure 17 for different noise levels, thus we can conclude that simulations gives a good indication of where the real images will score given a noise level.

In figure 29 to 31, we see the images divided into three classes given their BRISQUE score and trend as described in section 4.2.2. As the BRISQUE score tells, the quality of the images should vary a lot, and when taking a closer look the "bad" data set in figure 31 stands out the most. My analysis of why the BRISQUE score and image quality differ is,

- first if we take a look at the images in figure 29 and 30, where the image quality and lighting look quiet the same but yet differ so much in the BRISQUE score, it might be a property of the BRISQUE classifier. The BRISQUE classifier is built to assess image quality in natural images, and if we take a look at the main difference between these two data sets we can see that one is pictures of a car, humans, forest and clothing and the other mainly of buildings and large structure in the images with little change i.e. not so natural, which can effect the score.
- The major difference between figure 29 - 30 and 31 is that the latter appears to contain a lot more global noise. The increase in global noise arises from two separate sources, the fist one being luminance in the scene, we can see that the images in figure 30a and 31a is practically the same motive, but the latter is darker. The darker scene was shot in morning when the sun was not so bright and did not luminate the facade directly and thus the signal was weaker and the resulting reconstruction was effected more by the sensors background noise and gave rise to global noise in the produced image.
- The second reason is large structure movement in the scene, most of the images in the "bad" image set had movement mainly from clouds when sampled which definitely increased global noise in the reconstructed images as concluded in section 3.5.5 and therefore decreased the BRISQUE score significantly.

In the last part of section 4.2.2 the results from plotting SNR and standard deviation against mean signal intensity in figure 32, was presented. Each data point had also been color coded to match the classification made previously, the plots gave more information on why the BRISQUE score was so deviated. From the plot in figure 32a it becomes very clear at which mean signal intensity we can expect to produce good images given that the background noise becomes insignificant. But in the plots there are only two signals with higher variance than 0.04, which is the threshold where the simulated images started to get both worse initial BRISQUE score and worse trend when increasing the subsampling ratio in figure 17. This implies that there probably must be at least one additional factor at play to reduce the image quality in the "bad" set.

We can see that there are a subset of red images with almost the same SNR and mean signal intensity as yellow and green images but yields a worse BRISQUE score anyway, this strengthening the statement the there is probably at least on more factor that reduces reconstruction performance. And as stated in the last paragraph this is probably due to motion in the scene when sampling the signal. Unfortunately for this experiment, it seams like the images containing motion also had a low mean signal intensity, otherwise we would probably also have "bad" images for stronger mean signals.

The last observation in these plots are the mix of "good" and "half good" images in the whole mean intensity span, which tells that a strong signal will not yield a good BRISUQE score, which implies that the motive in the images effecting the BRISQUE score as suspected in when inspecting the reconstructed image sets.

### 5.1.3 Dynamics in scene

In this category there are results both from the simulated images and from the SPC, where the results was divided into three characteristic dynamics: small local changes in the scene, large global changes and luminance change.

The effect on the signal of local movements result shown in figure 19, we can see that there is no significant difference between the non perturbed reference signal and the distorted signal. It can even

be interpreted as added noise to the signal and it is barely detectable even if the signal is known. The effect on the reconstructed image, seen in figure 19a, looks like global noise is added. The conclusion of that test implies that local movement in a scene will distort the reconstructed image globally and especially locally where the movement occurred. It also tells that local movement is very hard to detect in the signal even if a reference signal is available.

When increasing the movement and modeled an unseen object pass through, the samples with movement was very easy to spot, which figure 18b shows. The effect in the reconstructed image is as expected even worse than local movement, with a global distortion, seen in figure 19b. In this simple isolated case the image could be saved by removing the measurements when the object was moving, reconstructing an image with fewer measurements. The resulting image would not be as good as the image in figure 21b but it would not contain the noise present in figure 21c.

In the case of luminance change, the effect on the reconstructed image is even worse than scenes containing movement, which figure 19c and comparing table 2, 3 and 4. Because we know that this problem is real and can not be avoided in natural scenes, a model to suppress this issue was tested with good result, but as can be seen in figure 24b, 23 and table 4, the method will not suppress the effect completely even on a simulation and thus add some global noise in the same form as local movement will.

When capturing images using the SPC, the luminance change became a larger problem than anticipated. All image captured in natural lighting had luminance change and it changed at a higher frequency and larger amplitude even in scenes where the intensity seemed stationary. This is of course due to the fact that the intensity change from every mirror in the DMD is summed in the sensor, so even for small changes the sum will change the signal significantly, as seen in figure 33. But as seen in the results in figure 34, the moving average method worked despite the more complex changes to the signal. Considering that this problem was consistent for all natural images this method became essential for this thesis to produce any good result at all. As stated before, this method is a model of global luminance change in the image, and therefore it is hard to know which side effects this method have on image quality. But as the test show, the method is essential and was used for all images captured by the SPC and presented and evaluated in this thesis.

This method was mainly constructed because I knew the SPC would have a long exposure time, but even if the exposure time is reduced to a few seconds or less, there is some indication that the luminance change will still effect the result. In this thesis, the moving average window corresponded to 50 milliseconds which indicates that the luminance change is so fast that even reducing exposure time could benefit to this method.

Basically all scenes in natural environment contained both dynamics from local movement and luminance change, local movement often arose from vegetation, objects or clouds moving in the wind but also from turbulence which not move the object but how it is perceived on the DMD. Because of all the dynamics presented that is persistent even in a "static" scene, I decided to not photograph scenes where large movement occurred as a car, object or human, even though it could be detected, because it could also be detected as luminance change.

As stated, even "static" scenes will with high probability contain both movement and luminance change which will effect the reconstructed images. Therefor I can conclude that all reconstructed images in this thesis has to some degree added global noise from local movement and the signal processing to counter luminance change.

#### 5.1.4 Edge response

When comparing the edge response between the conventional camera against the SPC the results was very clear, the conventional camera outperformed the SPC with one to two pixels in distance. I think

there are multiple factors why the results from the SPC differed so much from the conventional camera, and have listed them below,

- The largest impact on image quality is probably the reconstruction algorithm which produces "patches", which can be seen in the SPC images in figure 36, especially in the contrast of the white background where the light intensity drops. The "patch" artifact from the reconstruction algorithm can effect the sharpness of the image. We can also see from previous test that even from synthetic data the BRISQUE score is significantly worse then the original image.
- The pixel grid setup in the DMD has two problems that could effect the sharpness. In the DMD the mirrors is aligned in a diamond shape of pattern and in the current setup to fix the ratio and index two mirrors is merged to form one pixel. The reconstruction algorithm will still interpret the measurement as a regular square pixel which can distort the image.
- The focus in the DMD is set manually.
- In this thesis no significant image improvement from post processing such as denoise or sharpening was performed unlike the conventional camera.
- And as stated before, with the long exposure, vibrations and light intensity change effected the results (the SPC could detect significant light intensity change from the halogen lamp powered by a DC-unit), which contribute to global noise in the reconstruction.

### 5.1.5 Subsampling ratio

The first results from section 4.2.5 was the minimum subsampling ratio required to reconstruct a merely recognizable image, for the whole image set the results varied between 2-4%. The variance could be effected by several factors such as image complexity, SNR and dynamics in the scene, which contribute to add uncertainty to the equation system. With the knowledge of minimum subsampling ratio a fast exposure and thus a fast reconstruction could be applied to form a test image, which could be used to calibrate and make decision how to sample the long exposure real image.

In the second part of section 4.2.5, a set of images reconstructed with different subsampling ratio was presented. The result is presented for the reader to obtain a more concrete perception of the generated image quality and a supplement to the numerical results given subsampling ratio, but also overall expected image quality.

## 5.2 Method

The methods used in thesis can be divided into four categories, the SPC hardware, the sampling matrix and reconstruction, post processing and the method used to capture the images. Two of these categories, the hardware setup and the sampling matrix and reconstruction was heavily influenced and implemented by widely accepted methods from articles and experiments. While the two other categories, the post process and the image capturing dependent more on the hardware limitation and competence achieved from the university.

The first method in the chain was feeding the DMD measurement matrices and sampling the signal. Because of the interface to the DMD, which acted as a second monitor to the computer, the method to stream the measurement matrices as a video was thought to be a good method because it was easy to implement. In the early stages of this thesis a much smaller resolution of  $128 \times 128$  pixels was thought to be a feasible maximum and thus much less measurement matrices needed to be streamed to the DMD while having the same exposure time. With that initial goal in mind the video player steaming method would have worked well. But when the target resolution was pushed the video players frame rate had to be pushed to its limits in an application it was not designed to handle. This resulted in a higher probability that the video player would go out of sync and thus ruin the

reconstruction and there was no way of knowing if this had happen. By the time this issue was discovered there where no time of changing and implement a new method but was much needed.

The sampling matrix chosen in this thesis was the sequency ordered Walsh Hadamard measurement matrix, this sampling matrix in unison with implemented fast transform in the reconstruction algorithm enabled the huge increase in image resolution. This method of using structurally random matrices is the only feasible method today to enable high resolution and fast reconstruction with low memory usage in the computer thus if implemented optimally both the feeding of measurement matrices to the DMD and reconstruction could be calculated in run time in a memory efficient program.

The reconstruction algorithm TVAL3 was used throughout this masters thesis and was chosen after the literature study where several articles mentioned total variation as a good optimization algorithm for compressive imaging. The algorithm worked as described and according to the developer and is one of the fastest and best reconstruction algorithms that are free to use and available. The only negative criticism of using this algorithm is that it seems to produce a dark tint in the edges of the reconstructed images.

In the post process quite basic signal and image processing was performed and was intentional designed that way in order to present the result as true as possible. One algorithm was developed specific for the SPC which was the average mean algorithm to suppress the impact of lumination change in the sampled signal. The algorithm showed great result and became essential when taking photos of scenes outdoor. Both hardware and software signal denoising was implemented to the architecture but had to be changed every time the DMD update rate was changed, which happened a couple of times. Finding a new solution every time was a time consuming task and dropped completely in the end when good results was achieved anyway. If I had more time or a target DMD rate would have been set earlier a good signal denoising implementation could have improve the result.

### **5.2.1 Replicability, reliability & validity**

Given the description of method in this thesis I think it would be quiet straight forward to replicate this experimental setup and architecture. The setup is quiet simple and the software developed is not so heavy, therefor I think this experiment have good replicability.

In the case of compressive imaging the reliability and validity goes hand in hand, if whats being measured is not the correct data the reconstruction will fail and if the reconstruction succeed the measurement must be correct. Therefore compressive sensing is very binary, ether you get it right or you fail and thus I think my result have both high validity and reliability.

## 6 Conclusion & Future Work

Explicit answers to research questions and a summary of the whole masters thesis.

In this thesis a complete compressive imaging SWIR SPC architecture was implemented and evaluated. The aim was to find out which image quality could be achieved in natural images captured in daylight, the results produced in thesis both presented evaluation from simulated images and images captured by the SPC to show both how the chosen sampling method and reconstruction algorithm performed and how the whole architecture performed in unison.

The sampling strategy using the structural random matrices method with sequency ordered Walsh Hadamard measurement matrix solved the problems of scaling the reconstructed images to high definition photos and enabled the image resolution  $512 \times 512$  pixels in this thesis, the same resolution as the state of the art reference SWIR camera.

The total variation solver TVAL3 was used as reconstruction algorithm which took advantage of SRM with a FWHT to reconstruct the images fast and with good preservation of edges. Using the chosen sampling and reconstruction method could potentially make for a very lightweight sampling and reconstruction procedure with few variables stored in memory and calculations made in real time.

Feeding the measurement matrices to the DMD through a HDMI cable and video software was an easy method to start with. The first set of measurements was performed with low frame rate and blank frames for control. But when maximizing the frame rate the risk of duplicate or frame drops increased which made it hard to pair each measurement to the correct measurement matrix.

In post processing an algorithm to correct the signal effected by luminance change was implemented, this algorithm showed to be of outmost importance to this thesis. Long exposure time in natural scenes always gave a significant DC change in the sampled signal which should be stationary. Result showed in both simulation of luminance change and in real scenes a significant improvement of image quality when using this method and the analysis indicate that the algorithm may be relevant even if the exposure time gets reduced to near a second.

The resulting images produced by the SPC shows that high quality and high resolution images can be acquired in natural daylight scenes. In good conditions with enough intensity to overcome the sensors background noise and relatively stationary scenes detailed images where even people could be identified could be reproduced. Given the result and further work and improvement if the hardware compressive imaging and the SPC architecture have potential in real world applications.

The resulting reconstructed images from both simulations and the SPC was evaluated with a range of methods. When a reference image was available standard image evaluation techniques, PSNR and SSIM was used. In the subsampling range 5-30% as was used throughout the thesis showed that image quality increased with increasing subsampling ratio but stagnated around subsampling ratio between 15-20%. The BRISQUE no reference image quality assessment algorithm indexed based on statistics of "naturalness" in the images and it could be seen that the SPC could get the same results as the best in the simulations indicating that the sampling and reconstruction is the main source of image degradation and that the SPC hardware in the right conditions do not affect the resulting image quality negatively.

The edge response algorithm

- How can the quality of images reconstructed by CS or a SPC be evaluated?
- What is the state of the art method to capture and reconstruct images using a SPC architecture?
- What image quality is achieved using state of the art methods applied to the SPC?

What image quality can be achieved in natural images captured with a single pixel camera in daylight using state of the art methods?

## 6.1 Conclusion

## 6.2 Future work

This thesis shows that there is possible to use the SPC architecture to capture and reconstruct natural scenes in daylight, but for the technology to be used in a realistic application some improvements need to be made. And I think the most crucial problems could be "bought out" by more sophisticated hardware.

As identified multiple times in this thesis, the largest contributor to decreased image quality is exposure time and noise. The exposure time can be decreased by a faster DMD, today there exist a DMD:s with 8 times the maximum pattern rate of the DMD used in this thesis (which was operated at half the maximum speed), which would enable an exposure time of 1.125 seconds at 10% subsampling ratio. This upgrade would however require a new approach to feeding the measurements matrices to the DMD because of the limitations of the HDMI cables transfer speed.

Ether if a new transfer approach is implemented or not, a more sophisticated method of generating each measurement matrix should be implemented, the current method of generating all measurement matrices offline to a video file and then playbacked by a third Party video player has a limitation of FPS but also a reliability problem. The software was not designed to necessarily show every frame in the video file, which is a problem where each measurement needs to be paired with the correct measurement matrix. My suggestion would be a program which would calculate all matrices at start up and upload them to video memory ready for to display at the DMD. This solution would also be more agile where subsampling ratio, which type of measurement matrix and exposure time could easily be adjusted prior to sampling.

The second hardware upgrade, to reduce noise, would be to replace the photo diode used in this thesis to a more appropriate sensor for the application. The new sensor should have less background noise and the surface area of the doid should be analyzed to match the rest of the architecture to maximize the incoming light onto the sensor through the focusing lens. This upgrade could also unlock the true potential of the SWIR spectrum where images could be captured in dark environments illuminated by the moon, stars and night glow.

New research shows promising results by adding a second sensor which measures the intensity of the mirrors representing zero or turned away from the sensor and being dumped in the current architecture. The compliment of each unique measurement matrix could also be seen as a unique measurement matrix and thus more information is collected in each measurement and thus reduce the subsampling ratio needed to reconstruct a corresponding single sensor image.[24]

The last future work proposition will not increase image quality but would simplify research or usage and time consumption taking pictures with the SPC. The second and third most time consuming task after exposure time is the complexity of sampling the scene and the reconstruction algorithm in the post process. A fully integrated capturing and reconstruction chain with a gpu accelerated reconstruction algorithm should ease the work and save a lot of time for the user.

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