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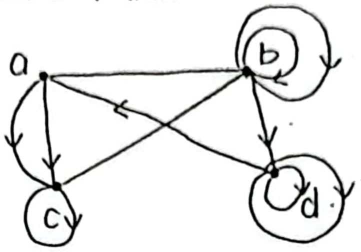
Problem 1

左侧图的邻接矩阵:

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 \\ 1 & 1 & 0 & 0 \end{bmatrix}$$

右侧邻接矩阵有向图:



Problem 2.

1) a) $K_{3,2}$

$$A = \begin{bmatrix} 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \end{bmatrix} \quad D = \begin{bmatrix} 2 & 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & 0 & 0 & 3 \end{bmatrix}$$

b) $\overline{K_{2,3}}$

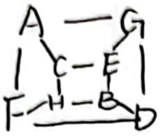
$$A = \begin{bmatrix} 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad D = \begin{bmatrix} 2 & 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

2) D为原图的度矩阵.

Problem 3.

证明：由题易知 下右图的补图中的边集为：[{A,C}, {A,F}, {A,G}, {B,E}, {B,D}, {B,H}, {C,H}, {C,E}, {D,F}, {D,G}, {E,G}, {F,H}].

即当存在双射函数 ϕ，使得：$\phi(a)=A$，$\phi(b)=G$，$\phi(c)=D$，$\phi(d)=F$，$\phi(e)=C$，$\phi(f)=E$，$\phi(h)=H$，$\phi(g)=B$，即其补图为：



时，该图与左图同构，得证.

Problem 4.

(1) 8个.

(2). 3个.

(3) 3个.

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Problem 5.

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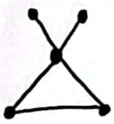
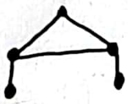
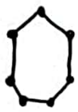
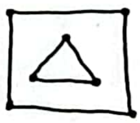
Problem 6.

(1)  和 

(2).  和 

Problem 7.

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