Solutions - Series 4

Genomics and bioinformatics - Week 4

October 11, 2011

1 Sequence alignment

Match: +1, *Mismatch:* -1, *Gap:* 0

Sequence 1: GAATTCAGA Sequence 2: GGATCGA.

Step 1: INITIALIZATION

Create a matrix with m+1 columns and n+1 rows where m and n correspond to the sizes of Sequences 1 and 2, respectively.

Step 2: SCORING

Using the given scoring scheme, at each cell, 3 scores are calculated:

- \bullet Upper neighbour score + Gap cost
- Left neighbour score + Gap cost
- Upper-left neighbour score + Match score (if nucleotides match), OR

 Upper-left neighbour score + Mismatch cost (if nucleotides do not match)

The highest score is retained and the arrow is labelled. The resulting scoring matrix should look something like this,

	_	G	A	A	Т	Т	С	А	G
_	0	-2	-4	-6	-8	-10	-12	-14	-16
G	-2	1 —	→- 1	→ -3	→- 5	→ -7	> -9	 11	→-13
G	-4	-1	0	-2—	→ -4—	→ -6—	>- 8	- 10	-10
A	-6	- 3	0	1 —	→ -1	> -3—	→ -5	→-7	→ _9
Т	-8	- 5	-2	-1	2 —	> 0 —	→ -2—	→ - 4 —	→ -6
С	-10	- 7	-4	-3	Ŏ	1	1 _	→ -1 —	→ –3
G	-12	↓ -9	- 6	→ -5	-2	-1	0	0	0

Step 3: BACKTRACKING

The process of deduction of the best alignment from the score matrix is known as traceback. The traceback begins with the last cell to be filled, i.e. the bottom-right cell, and is completed when the first, i.e. the top-left cell of the matrix is reached. Several traceback paths are possible. The solution resulting in the best final score is selected to deduce the optimum alignment. It is possible to have more than one optimum alignment.

A traceback path for the scoring matrix generated in Step 2 is highlighted below,

	_	G	A	A	Т	Т	С	A	G
_	0	-2	-4	-6	-8	-10	-12	-14	-16
G	-2	1 -	→- 1	→ -3	>- 5	>- 7	→ -9	- 11	→-13
G	-4	-1	0	-2—	> -4	→ -6—	→ -8	- 10	-10
A	-6	- 3	0	1 —	→ -1	→ -3—	→ -5	→ -7	→ _9
Т	-8	- 5	-2	→ -1	2 —	→ 0 <u> </u>	→ -2—	→ -4 —	→ -6
С	-10	- 7	-4	-3	ŏ	1	1 —	→ -1 —	→ –3
G	-12	- 9	- 6	4 - 5	-2	-1	0	0	0

Step 4: ALIGNMENT

After backtracking, the optimal alignment is easy to recover using following the rule, Left = Gap, Up = Insertion, and Diagonal = Match

The optimum alignment for the two sequences GAATTCAGA and GGATCGA is,

2 Pair HMM

The corresponding HMM is given by where, p(x,y)=0.125 and p(x,y)=0.04 for mismatch p(x,_)=q(_,y)=0.25

If we consider all probability values with repesct to a random model in log-odds

$$S(x,y) = log \frac{p(x,y)}{p(x) \ p(y)}$$

$$S(x,y) = 1$$
 for match and $s(x,y) = -1$ for mismatch

The we can consruct the three matrices for VM, VX and VY by the Viterbi algorithm There are two possible optimal alignments

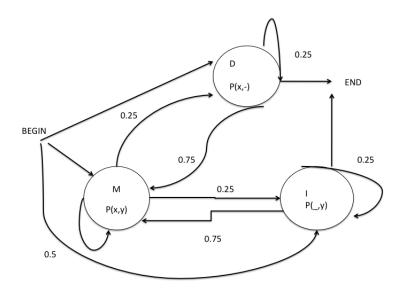


Figure 1: The HMM mpdel for sequence alignment

$$\begin{split} \log V^{M}(i,j) &= \max \begin{cases} \log V^{M}(i-1,j-1) + s(x_{i},y_{j}) \\ \log V^{I}(i-1,j-1) + s(x_{i},y_{j}) \\ \log V^{I}(i-1,j-1) + s(x_{i},y_{j}) \end{cases} \\ \log V^{I}(i,j) &= \max \begin{cases} \log V^{M}(i-1,j) - d \\ \log V^{I}(i-1,j) - e \end{cases} \\ \log V^{I}(i,j) &= \max \begin{cases} \log V^{M}(i,j-1) - d \\ \log V^{I}(i,j-1) - e \end{cases} \end{split}$$

Figure 2: Viterbi Algorithm

		G	Α	A	Т	Т	С	A	G
	0	-∞	-∞	-∞	-∞	-∞	-∞	-∞	-∞
G	-∞	1	-3	-5	-7	-9	-11	-13	-13
G	-00	-1	0	-2	-4	-6	-8	-10	-10
A	-00	-5	0	1	-3	-5	-7	-7	-11
Т	-∞	-7	-4	-1	2	O	-4	-6	-8
С	-∞	-9	-6	-3	-2	1	1	-3	-5
G	-00	-9	-8	-5	-4	-1	0	0	0

Figure 3: The matrix for the match state

		G	Α	Α	Т	Т	С	A	G
	-∞	-2	-4	-6	-8	-10	-12	-14	-16
G	-∞	-∞	-1	-3	-5	-7	-9	-11	-13
G	-00	-00	-3	-2	-4	-6	-8	-10	-12
Α	-00	-00	-7	-2	-1	-3	-5	-7	-9
Т	-∞	-∞	-9	-6	-3 →	0	-2	-4	-6
С	-∞	-∞	-11	-8	-5	-4	-1	- 1	-3
G	-∞	-00	-11	-10	-7	-6	-3	-2	-2

Figure 4: Matrix for deletion state

Figure 5: Matrix for insertion state

		G	Α	Α	Т	Т	С	A	G
	- ∞	-00	-∞	-00	-00	-00	-∞	-∞	-∞
G	-2	-00	-∞	-00	-00	-00	-00	-00	-∞
G	-4	-1	-5	-7	-9	-11	-13	-15	-15
Α	-6	-3	-2	-4	-6	-8	-10	-12	-12
Т	-8	-5	-2	-1	-5	-7	-9	-9	-13
С	-10	-7	-4	-3	0	-2	-6	-8	-10
G	-12	-9	-6	-5	-2	-1	-1	-5	-7

		G	Α	A	Т	Т	С	A	G
	0	-2	-4	-6	-8	-10	-12	-14	-16
G	-2	1	-1	-3	-5	-7	-9	-11	-13
G	-4	-1	0	-2	-4	-6	-8	-10	-10
Α	-6	-3	0	1	-1	-3	-5	-7	-9
Т	-8	-5	-2	-1	2	0	-2	-4	-6
С	-10	-7	-4	-3	0	1	1	-1	-3
G	-12	-9	-6	-5	-2	-1	0	0	0

Figure 6: Alignment by backtracking

G A A T T C A G C G A T _ C _ G M M M M D M D M G A A T T C A G C G A _ T C _ G M M M D M M D M

Figure 7: The alignments