

1、若 $F(x)$ 的原函数为 $\sin x$ ，则 $\int dF(x) = \underline{\hspace{2cm}}$.

2. $\int \frac{\sin 2x}{1 + \sin^2 x} dx = (\quad C \quad)$.

- A. $\ln(1 + \sin 2x) + C$ B. $\ln(1 + \cos 2x) + C$
C. $\ln(1 + \sin^2 x) + C$ D. 以上答案都不对

3. $\int \frac{2x+5}{x^2+4x+13} dx$

4. $\int \frac{1}{(1+e^{-x})} dx$

5、计算： $\int \operatorname{arccot} \sqrt{x} dx$

6. 求 $\int x^2 \cos x dx$.

7. $\int \sin^3 t \cdot \cos t \cdot dt$

8. $\int \sin^3 t \cdot \cos^2 t \cdot dt$

9. 求 $\int \frac{dx}{\sqrt{(x^2+1)^3}}$. 解：令 $x = \tan u$, $dx = \sec^2 u du$

$$\int \frac{dx}{\sqrt{(x^2+1)^3}} = \int \frac{\sec^2 u du}{\sec^3 u} = \int \frac{1}{\sec u} du = \int \cos u du = \sin u + C = \frac{x}{\sqrt{x^2+1}} + C$$

10. 求 $\int \frac{1}{x\sqrt{x^2-1}} dx$.

解：设 $x = \sec u$, $dx = \sec u \tan u du$

$$\text{原式} = \int \frac{1}{\sec u \tan u} \sec u \tan u du = \int du = u + C = \arccos \frac{1}{x} + C$$

11. $\int \frac{1}{\sin^2 x \cos^2 x} dx = \int \frac{\sin^2 x + \cos^2 x}{\sin^2 x \cos^2 x} dx = \int (\sec^2 x + \csc^2 x) dx = \tan x - \cot x + c$

12. $\int \frac{x^2+x-1}{(x^2-1)^2} dx$