

# 基本导数公式记忆.

$$(x^n)' = nx^{n-1}$$

$$(\sin x)' = \cos x$$

$$(\cos x)' = -\sin x$$

$$(\tan x)' = \sec^2 x$$

$$(\cot x)' = -\csc^2 x$$

$$(\sec x)' = \sec x \cdot \tan x$$

$$(\csc x)' = -\csc x \cdot \cot x$$

$$(a^x)' = a^x \ln a$$

$$(e^x)' = e^x$$

$$(\log_a x)' = \frac{1}{x \ln a}$$

$$(\ln x)' = \frac{1}{x}$$

$$(\arcsin x)' = \frac{1}{\sqrt{1-x^2}}$$

$$(\arccos x)' = -\frac{1}{\sqrt{1-x^2}}$$

$$(\arctan x)' = \frac{1}{1+x^2}$$

$$(\operatorname{arccot} x)' = -\frac{1}{1+x^2}$$

$$\operatorname{arctan} x = \frac{1}{1+x^2}$$

$$\operatorname{arccot} x = -\frac{1}{1+x^2}$$

$$\operatorname{arcsin} x = \frac{1}{\sqrt{1-x^2}}$$

$$\operatorname{arccos} x = \frac{1}{\sqrt{1-x^2}}$$

$$\sec x = \frac{1}{\cos x}$$

$$\csc x = \frac{1}{\sin x}$$

$$1 + \tan^2 x = \sec^2 x$$

$$1 + \cot^2 x = \csc^2 x$$

$$\tan x = \left( \frac{\sin x}{\cos x} \right)' = \frac{\cos^2 x + \sin^2 x}{\cos^2 x} = \frac{1}{\cos^2 x} = \sec^2 x$$

$$\cot x = \left( \frac{\cos x}{\sin x} \right)' = \frac{-\sin^2 x - \cos^2 x}{\sin^2 x} = -\frac{1}{\sin^2 x} = -\csc^2 x$$

$$(\sec x)' = \left( \frac{1}{\cos x} \right)' = \left( \frac{\sin^2 x + \cos^2 x}{\cos x} \right)'$$

$$= \left( \frac{\sin^2 x}{\cos x} + \cos x \right)'$$

$$= \left( \frac{2 \sin x \cos x + \sin^3 x}{\cos^2 x} - \frac{\sin x}{\cos^2 x} \right)$$

$$= \frac{\sin x \cos^2 x + \sin^3 x}{\cos^2 x}$$

$$= \frac{\sin x (\cos^2 x + \sin^2 x)}{\cos^2 x} = \frac{\sin x}{\cos^2 x} = \frac{1}{\cos x} \cdot \frac{\sin x}{\cos x} = \sec x \cdot \tan x$$

$$= \sec x \cdot \tan x$$

$$(\csc x)' = \left( \frac{1}{\sin x} \right)' = \left( \frac{\sin^2 x + \cos^2 x}{\sin x} \right)'$$

$$= \left( \frac{-2 \sin^2 x \cos x - \cos^3 x}{\sin^2 x} + \frac{\sin^3 x}{\sin^2 x} \right)$$

$$= \frac{\sin^2 x}{\sin^2 x}$$