

10-2. 1(4) 2(3), 1(4), 4(2), (4),
6, 9, 12, 13, 14, 15, 17.

1. (4). 解: 由题得, $0 \leq y \leq x, x \in [0, \pi]$.

$$\iint_D x \cos(x+y) d\sigma = \int_0^\pi x dx \cdot \int_0^x \cos(x+y) dy$$

$$= \int_0^\pi x [\sin(x+y)]_0^x dx$$

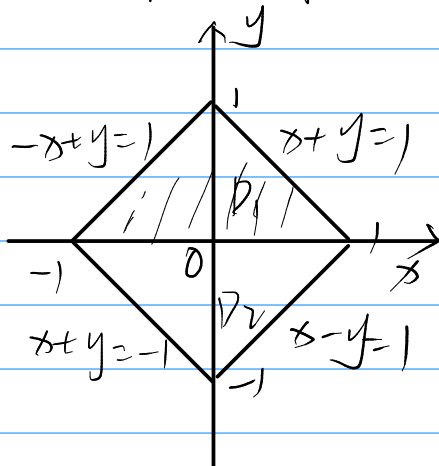
$$= \int_0^\pi x \cdot (\sin 2x - \sin x) dx$$

$$= \int_0^\pi x \cdot d(\cos x - \frac{1}{2} \cos 2x)$$

$$= -\frac{3}{2}\pi - \int_0^\pi (\cos x - \frac{1}{2} \cos 2x) dx$$

$$= -\frac{3}{2}\pi.$$

2. (3). 解: 如图:

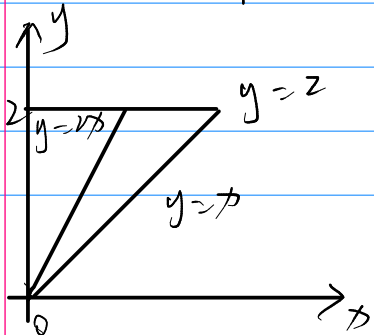


$$\text{则 } \iint_D e^{x+y} d\sigma = \iint_{D_1} e^{x+y} d\sigma + \iint_{D_2} e^{x+y} d\sigma$$

$$= \int_{-1}^0 e^x dx \int_{-x-1}^{x+1} e^y dy + \int_0^1 e^x dx \int_{x-1}^{-x+1} e^y dy$$

$$= e - \frac{1}{e}$$

2. (4). 解: 如图:



$$\text{则 } \iint_D (x^2 + y^2 - x) d\sigma = \int_0^2 dy \int_{\frac{y}{2}}^y (x^2 + y^2 - x) dx$$

$$= \int_0^2 \left[\frac{x^3}{3} + y^2 x - \frac{x^2}{2} \right]_{\frac{y}{2}}^y dy = \frac{13}{6}$$

$$\frac{19}{24} y^3 - \frac{2}{8} y^2 \quad 0, 2.$$

4 (2). $0 \leq y \leq \sqrt{r^2 - x^2}$, $-r \leq x \leq r$ 时,

$$Z = \int_{-r}^r dx \int_0^{\sqrt{r^2 - x^2}} f(x, y) dy$$

$-\sqrt{r^2 - y^2} \leq x \leq \sqrt{r^2 - y^2}$, $0 \leq y \leq r$ 时,

$$Z = \int_0^r dy \int_{-\sqrt{r^2 - y^2}}^{\sqrt{r^2 - y^2}} f(x, y) dx.$$

1 (4) - 对图 1.11 中圆作两条切线得,

$$Z = \int_{-2}^{-1} dx \int_{-\sqrt{4-x^2}}^{\sqrt{4-x^2}} f(x, y) dy + \int_{-1}^1 dx \int_{-\sqrt{4-x^2}}^{-\sqrt{4-x^2}} f(x, y) dy$$

$$+ \int_{-1}^1 dx \int_{\sqrt{4-x^2}}^{\sqrt{4-x^2}} f(x, y) dy + \int_1^2 dx \int_{-\sqrt{4-x^2}}^{\sqrt{4-x^2}} f(x, y) dy.$$

对圆作切线分割得:

$$Z = \int_{-2}^{-1} dy \int_{-\sqrt{4-y^2}}^{\sqrt{4-y^2}} f(x, y) dx + \int_{-1}^1 dy \int_{-\sqrt{4-y^2}}^{-\sqrt{4-y^2}} f(x, y) dx$$

$$+ \int_{-1}^1 dy \int_{\sqrt{4-y^2}}^{\sqrt{4-y^2}} f(x, y) dx + \int_1^2 dy \int_{-\sqrt{4-y^2}}^{\sqrt{4-y^2}} f(x, y) dx.$$