Code description for

On the locality of local neural operator in learning fluid dynamics

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Program structure

- *Train_Validation*: training and validation of LNO
 - main.py: main program to run the training or validation of LNO, including 3 functions:
 - ◆ train test save(): train, validate, and save an LNO
 - load test(args.out name): load and validate a trained LNO
 - test receptive(args.out name): load a trained LNO and analyze its receptive field
 - receptive.py: analyze the receptive field of an initialized LNO
 - *lib*: supportive functions and supportive data
 - legendres: the discrete kernel $\varphi_{m,i}$ and $\psi_{m,i}$ for 5th~41st-order Legendre polynomials used in the spectral path
 - networksNS.py: the network of local neural operator for 2D compressible Navier-Stokes equation
 - ♦ *train*.py: functions to train LNO
 - ◆ *test*.py: functions to test trained LNO
 - *utils*.py: supportive functions to generate the kernel of spectral path
 - *Data*: functions to generate and extract data for training
 - ◆ DatasetNS.py: generate dataset for Navier-Stokes equations
 - **receptives**: saved data of receptive field
 - models: the trained LNO models
 - outputs: predicted results on validation samples by trained LNOs
 - *logs*: the output logs during the training process
- *Application*: apply pre-trained LNO to solve unseen problems
 - mainCircularCylinder.py: main program to solve the flow around a circular cylinder
 - mainVehicle.py: main program to solve the flow around a vehicle
 - *IBM*.py: function to implement immersed boundary method
 - **geometry**: geometry files of circular cylinder with different diameters and different shapes of vehicles
 - *lib*: supportive functions
 - ◆ networkNS.py: the network of local neural operator for Navier-Stokes equation, almost the same as networks LNO.py but padding operations are removed
 - utils.py: supportive functions to generate the kernel of spectral path

- *models*: pre-trained LNO models for solving the unseen problems
- CircularCylinder & Vehicle: folders to store the predicted flow fields of the two examples

How to use

• To train a new LNO and then test:

Enable train_test_save() in *main*.py and run command:

```
nohup python -u main.py -n run_name > logs/run_name.log 2>&1 &
```

The trained LNO will be in models named *run_name_model*.pp and the training log will be in *logs* named *run_name*.log.

• To test a trained LNO:

Enable load_test(args.out_name) in *main*.py and run command:

```
nohup python -u main.py -n run_name > logs/run_name.log 2>&1 &
```

The results of predicting the validation data samples will be in *outputs* named *run name*.mat.

• To calculate the receptive field of a trained LNO:

Enable test_receptive(args.out_name) in *main*.py and run command:

```
nohup python -u main.py -n run_name > logs/run_name.log 2>&1 &
```

The results of predicting the validation data samples will be in *receptives* named *run name receptive*.mat.

• To calculate the receptive field of an initialized LNO:

Run command:

python receptive.py

The results of predicting the validation data samples will be in *receptives* named initial n{} N{} M{} K{}.mat.

• To solve the flow around a square cylinder:

Put a pre-trained LNO model file into *models* or select one from *models*, change model_file in *mainSquareCylinder*.py and run command:

```
python mainCircularCylinder.py
```

The predicted flow fields at different time levels will be named CC timelevel.mat.

• To solve the flow around a vehicle:

Put a pre-trained LNO model file into *models* or select one from *models*, change model_file in *mainVehicle*.py and run command:

```
python mainVehicle.py
```

The predicted flow fields at different time levels will be named *Vehicle timelevel*.mat.

Dataset description

Data samples

Data samples for each learning task to be learned are stored in one independent folder named $ComNS128Re\{\}Ma\{\}\}$. In each folder, data samples are stored in pieces with name $folder_name_order$.mat, e.g., $ComNS128Re100Ma2_1$.mat is the 1st data sample for Re = 100, Ma = 0.2, which is the physical field calculated from one random initial condition. Each data file includes all the physical fields required for training, and each physical field is in the format [total_time_steps×field_value_in_a_time_level]. The example data samples can be found in https://pan.baidu.com/s/13ZRXGuaBujk6zlA98tWIIQ

Code: sy84

Unzip the folder at /Train_Validation/Data/

Main adjustable parameters

Parameter	Description	Options	
Train_Validation			
data_dir	Path of dataset	/	
data_name	Name of folder according to Table 1	/	
Re	Reynolds number of Navier-Stokes equation to be	1	
	learned	I	
Ма	Mach number of Navier-Stokes equation to be		
	learned		
t_interval	Controlling the time step Δt of the learning task,		
	$\Delta t = \Delta \tau \times t_interval$, where $\Delta \tau = 0.01$ is the	Positive integer	
	time step of training data samples		
learning_rate	Initial learning rate	0.001 (recommend)	
reccurent	Round number for recurrent training,	10 (recommend)	
epochs_overall	Epoch number of training	200 (recommend)	
iterations	Iteration number in each epoch	500 (recommend)	
orders_all	Orders of all used data samples, including both	/	
or der s_all	training and validation samples		
orders_train	Orders of training data samples	/	
num_blocks	Number of blocks n	4 (recommend)	
N	Order of spectral transform N	5~41	
М	Selected first m lowest modes M	≤ n	
K	Number of repetitions K	2 (recommend)	
Norm_facotrs	Factors to normalize the input according to Appendix E	[0.5, 0.5, 5, 10] (recommend)	
Init_weight	Factors to initialize the weights in LNO according to Appendix E	$[\sqrt{3}, \{\}, \sqrt{6}, \sqrt{3}, \sqrt{6}, \sqrt{3}]$	
		(recommend, see Table E1 for the	
		2 nd value)	
if_ln	Set input ρ, T to their logarithm for	True (recommend)	
	normalization according to Appendix E		
Application			
N	Order of spectral transform for choosing LNOs		
	with different receptive ranges, 8 for insufficient,	8,12,20	
	12 for compatible, 20 for excessive range		
model_file	File name for the pre-trained LNO model	/	
NG_L,NG_D,NG_U,NG_R	The size of the computational domain from the	/	

	center of the solid wall geometry in the left, down, up, and right sides	
delta_x	Size of spatial discretization according to the training samples	1/64 (default)
u_lid	Velocity of the inflow	1 (recommend)
filename	Geometry file name of the solid obstacle	'CircularCylinderD{}.mat' for circular cylinder 'vehicle_sports.mat' for vehicle
p_1	Equidistant points on the solid wall of the obstacle	/
delta_s	Distance between points in p_1, should be around delta_x	/
ShapeNum	Number of obstacles	/
d	Diameter of circular cylinder	/
cycle_num	Total number of time-marching steps	/