Assignment 4

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Download all python codes from

https://github.com/PRABHATH-cs20-11038/ AI1103/tree/main/Assignment 4/codes

and latex-tikz codes from

https://github.com/PRABHATH-cs20-11038/ AI1103/tree/main/Assignment_4

1 Problem

(GATE(CS)2013 - 2Q) Suppose p is the number of cars per minute passing through a certain road junction between 5 PM and 6 PM, and p has a Poisson distribution with mean 3. What is the probability of observing fewer than 3 cars during any given minute in this interval?

- (A) $8/(2e^3)$
- (B) $9/(2e^3)$
- (C) $17/(2e^3)$
- (D) $26/(2e^3)$

2 Solution

Probability of Poison Distribution is,

$$\Pr(X = p) = \frac{e^{-\mu}\mu^p}{p!}$$
 (2.0.1)

Here, p refers to no. of cars per minute, $p \in \{0, 1, 2, ..., \infty\}$

Mean of poison distribution,

$$\mu = 3 \tag{2.0.2}$$

$$\Pr(X = p) = \frac{e^{-3}3^p}{p!}$$
 (2.0.3)

 $\label{table 4} TABLE\ 4$ Table of probability of no. of cars passing per minute

p	0	1	2	3	
Pr(X = p)	$1/e^{3}$	$3/e^{3}$	$9/(2e^3)$	$9/(2e^3)$	

by Boolean logic,

$$Pr(X < 3) = Pr(X = 0) + Pr(X = 1) + Pr(X = 2)$$
(2.0.4)

$$\Pr\left(X < 3\right) = \frac{17}{2e^3} \tag{2.0.5}$$

Option (C) is correct

Probability simulated:0.42209 theoretical:0.42319