

* Proof of correctness for selection sort

function SelectionSort(array):
 for i from 0 to length(array) - 1 do:
 minimum_index = i
 for j from i + 1 to length(array) do:
 if array[j] < array[minimum_index] then:
 minimum_index = j
 swap array[i] with array[minimum_index]
 end for
end function

→ Loop Invariant: At the beginning of each iteration the subarray array[0:i] contains the smallest i element from entire array

Base case: 1st iteration, the subarray array[0:0] is empty, it is sorted, the loop invariant is valid at this stage.

Inductive step: for first i iteration. This implies that the subarray array[0:i] consist of smallest element. So loop invariant holds true.

iteration $i+1$:- the algorithm scans the unsorted portion of array $C[i:n]$ to locate smallest element. After swapping, the element 'array $C[i]$ ' is the smallest element

So array $C[0:i+1]$ contains smallest $i+1$ element, so loop invariant continues to hold true after $i+1$ th iteration

Termination:- when $i=n-1$ loop completes execution the array is sorted

Conclusion:- Since the loop invariant holds true throughout the algorithm execution, the algorithm guarantees a sorted output for any valid input array.