

Assignment 1

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Download all python codes from

https://github.com/pranav-159/ai1103_Probability_and_Random_variables/blob/main/Assignment_1/codes/experimental_verification_2.4.py

and latex-tikz codes from

https://github.com/pranav-159/ai1103_Probability_and_Random_variables/blob/main/Assignment_1/main.tex

1 PROBLEM(2.4)

Suppose that 5% of men and 0.25% of women have grey hair. A grey haired person is selected at random. What is the probability of this person being male? Assume that there are equal number of males and females.

2 SOLUTION(2.4)

Let $A=0,1$ represent the random variable for being male or female and $G=0,1$ represent having grey hair or not. Then,

$$P(A = 0) = 50\% = \frac{1}{2} \quad (2.0.1)$$

$$P(A = 1) = 50\% = \frac{1}{2} \quad (2.0.2)$$

$$P(G = 1|A = 0) = 5\% = \frac{1}{20} \quad (2.0.3)$$

$$P(G = 1|A = 1) = 0.25\% = \frac{1}{400} \quad (2.0.4)$$

By Bayes rules,

$$P(A = 0|G = 1) = \frac{P(0) \times P(G = 1|0)}{\sum_{i=0}^1 \Pr(G)} \quad (2.0.5)$$

$$\therefore \sum_{i=0}^1 \Pr(G) = P(0) \times P(G = 1|0) + P(1) \times P(G = 1|1) \quad (2.0.6)$$

$$P(A = 0|G = 1) = \frac{\frac{1}{2} \times \frac{1}{20}}{\frac{1}{2} \times \frac{1}{20} + \frac{1}{2} \times \frac{1}{400}} \quad (2.0.7)$$

$$P(A = 0|G = 1) = \frac{20}{21} \quad (2.0.8)$$

Probability that the grey haired person selected at random is male is 0.952380952.