

Name: Alok Bhawankar
Roll: PA06
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Lab Assignment 2

AI

Title : Implantation of minimax algorithm for Tic-Tac-Toe game.

Aim : Solve Tic-Tac-Toe using minimax Algorithm

Objective : To study and implement minimax algorithm for Tic-Tac-Toe

Theory :

Adversarial Search :

- examine the problem contain we by to plan ahead of world and others agents plans againsts me.
- Searches in which 2 or more players with compictly goals are trying to explore same space for solution.
- "opponent" changing state of problem every step in a direction we do not want.
- eg. chess, Tic-Tac-Toe.
- includes - minimax algorithm
- alpha beta Pruning

Tic - Tac - Toe

- 2 Players x 2 0
- turn-by-turn play in 5x3 and
- 3 in a row, column or diagonal first wins
- Considering minimax algorithm

- 2 players max and min.
- players have an alternate turn & start with max.

Max \rightarrow maximum result of game here

Min \rightarrow minimise result

- Utility function $f(p)$ 'p' be position / state in game

$$f(p) = \begin{cases} \text{largest positive number, if p is win for computer.} \\ \text{smallest negative number, if p is win for opponent RCDc - RCDo.} \end{cases}$$

RCDc = no. of rows, columns, diagonals, in which computer would still win.

RCDo = no. of rows, columns, diagonals in which opponent could still win.

O	O	X
X	X	O
X	O	X

Minimum Algorithm

- recursive / backtracking algorithm used in decision making & game theory.
- provides optimal move for player assumes opponent playing optimally.
- 2 players play to get maximum benefit, max & min

- Max will select maximum value, Min selects minimized.
- performs 'DFS' for exploration of complete game here.
- It proceeds always down to terminal node of tree, then back track the tree as recursion.
- Minimax strategy:
 - MIN value taken every other level of tree which represent opponent's choice of move.
 - Computer assumes that human will choose more, of least value to computer.

Properties :

- Complete, optimal.
- T.C & S.C is $O(b^d)$ min max depth of tree.

Limitations :

- gets slow for complex games.

Input : Initial state.

Output : Solution / goal state with optimal path.

Algorithm : Minimax

Platform : Linux

FAQs

1) Compared informed search and adversarial search.

A) Informed Search

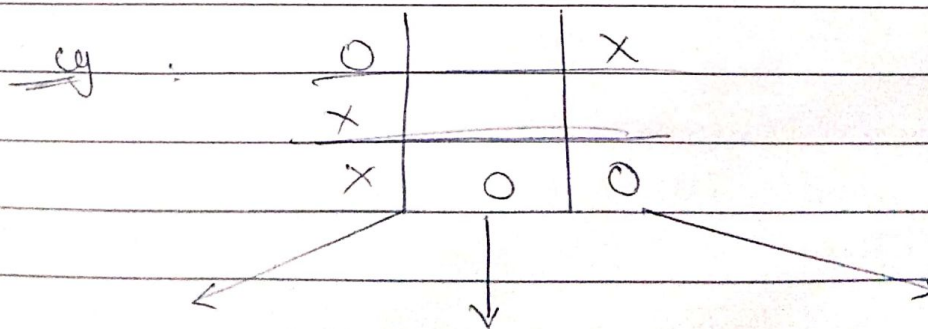
- Problem-specific knowledge that helps agents to explore less the search space and find more efficiently goal node.
- Uses idea of heuristics to identify most promising search path.
- includes BFS & A* algorithm.

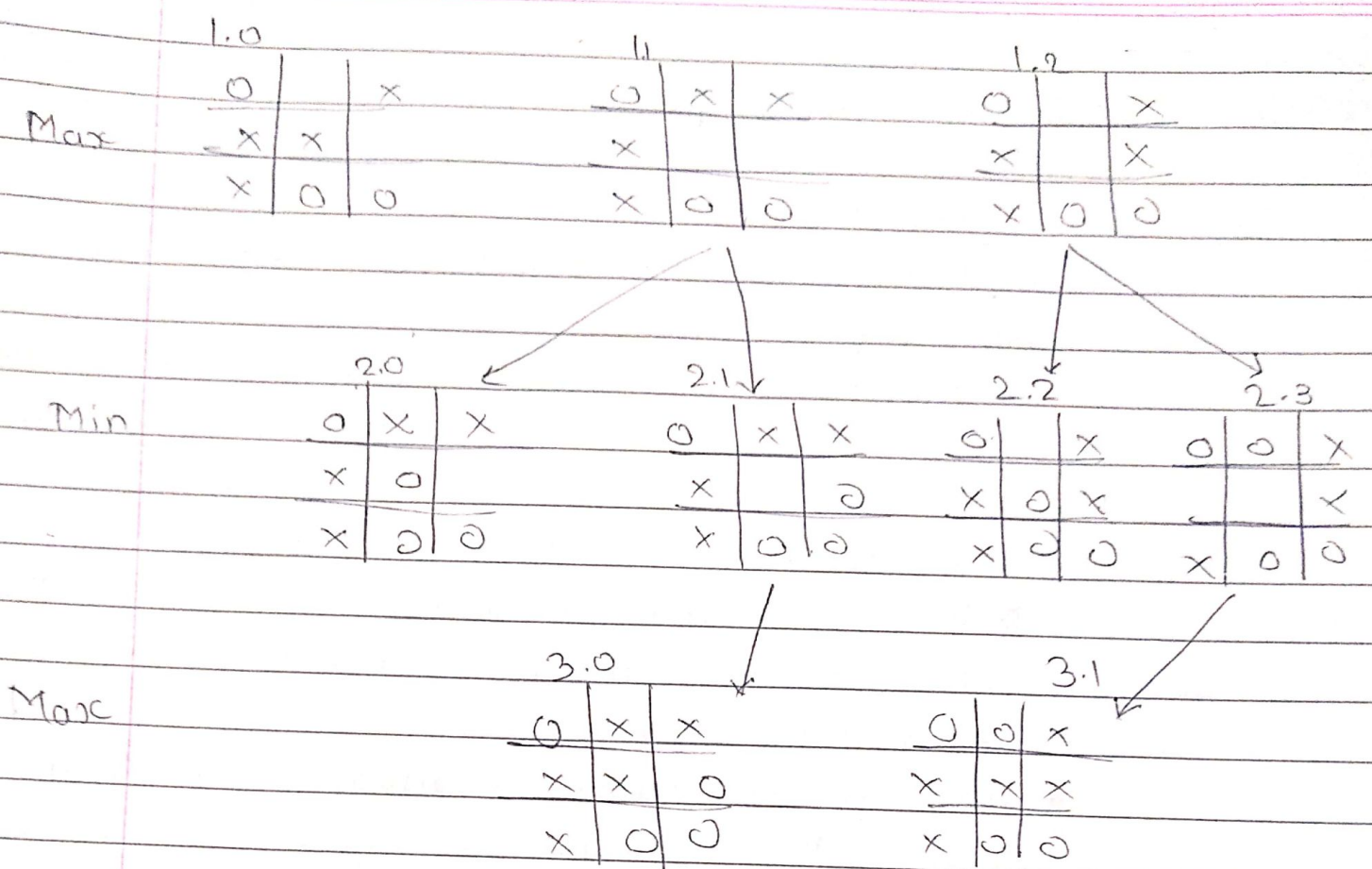
Adversarial Search

- examines problems which are when we try to plan ahead of world & others agents planning against us.
- include multi-agent environment.
- includes games like chess.

Q2] Explain minimax algorithm with example.

A) • recursive / back tracking algorithm used in sequentiality & game theory.



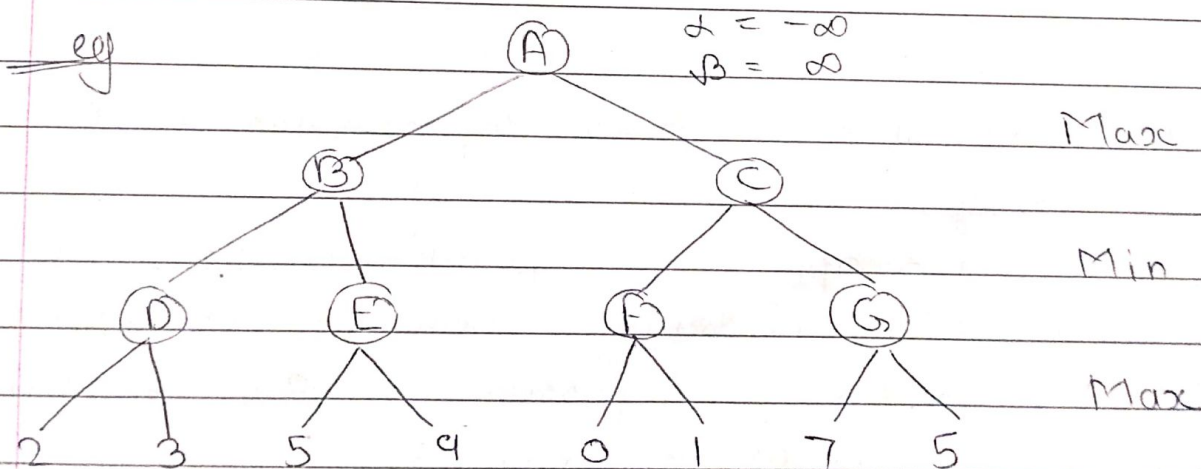


- Initial state 0.0 gives 3 possibilities (1.0, 1.1, 1.2)
- 1.0 gives computer win (+1)
- 1.1 gives opponent 2 possibilities (2.0, 2.1)
 - 2.0 is winning state for our opponent
 - 2.1 gives possibilities, 3.0 in which computer is win (+1)
- 1.2 gives 2 possibilities (2.2, 2.3)
 - 2.2 is winning state for opponents, so losing for computer is win (+1)

Q3] Explain Alpha Beta pruning

A) Alpha Beta Pruning

- modified version of minimum & optimization technique
- correct minimax decision without checking each node of game here has 2 threshold parameters alpha & beta.
- main condition for pruning is $\alpha \geq \beta$.
- return same move as regular, removes all nodes which are not really affecting final decision but many algo slow
- * max player update & alpha values & min player beta values.



1] Max player will start for Root A where $\alpha = -\infty$ & $\beta = \infty$ and same value passed to its child and subchild.

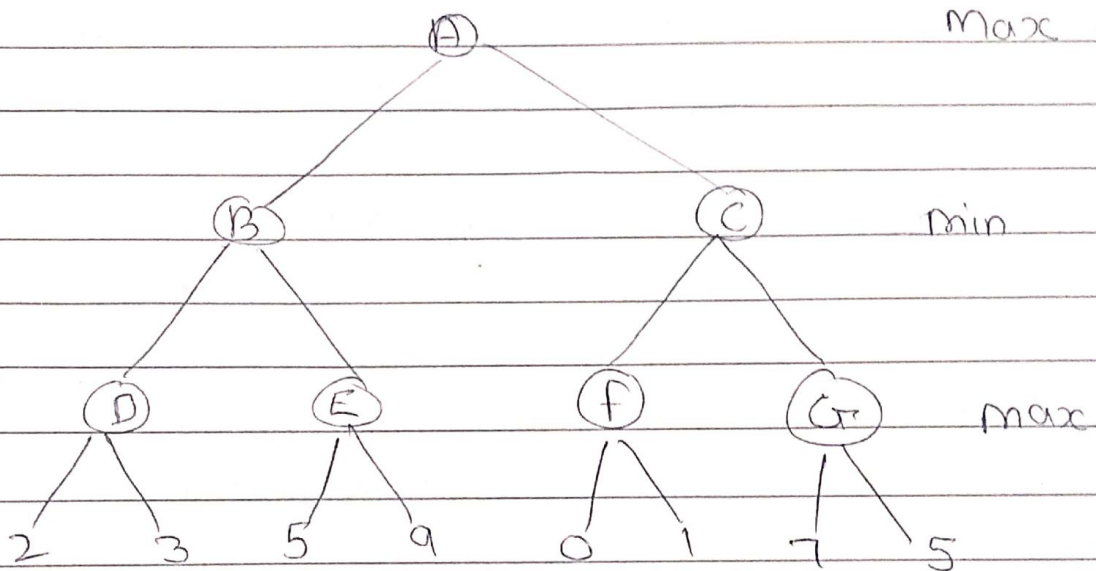
g) At Node 'E' $[3, \infty)$

$$\alpha = \max(3, 0) = 3 = \max(3, 1)$$

$$\beta = \min(\infty, 1) = 1$$

h) At 'A' $[3, \infty]$

Best value for A is $\max(3, 1) = 3$



2] a) At Node 'D' $[-\infty, \infty]$

$$\alpha = \max(2, 3) = 3$$

Node Val = 3

$$\beta = \infty$$

b) A Node 'B' $[-\infty, \infty]$

$$\alpha = -\infty$$

$$\beta = \min(\infty, 3) = 3$$

These values of β will be passed by next successor of B i.e.

c) At Node 'E' $[-\infty, 3]$

$$\alpha = \max(-\infty, 5) = 5$$

Node Val = 5

$$\beta = 3$$

$\alpha > \beta$ \therefore right successor of E will be pruned & not traversed

d) At Node 'A' $[-\infty, \infty]$

$$\alpha = \max(-\infty, 3) = 3$$

$$\beta = \infty$$

These value of α is passed to next successor of A i.e., c

e) At Node 'E' $[3, \infty]$

- Same values will be passed to its next successor

f) At Node 'F' $[3, \infty]$

$$\alpha = \max(3, 0) = 3 = \max(3, 1)$$

$$\beta = \infty$$

Node value = 1