

## \* Data Structures

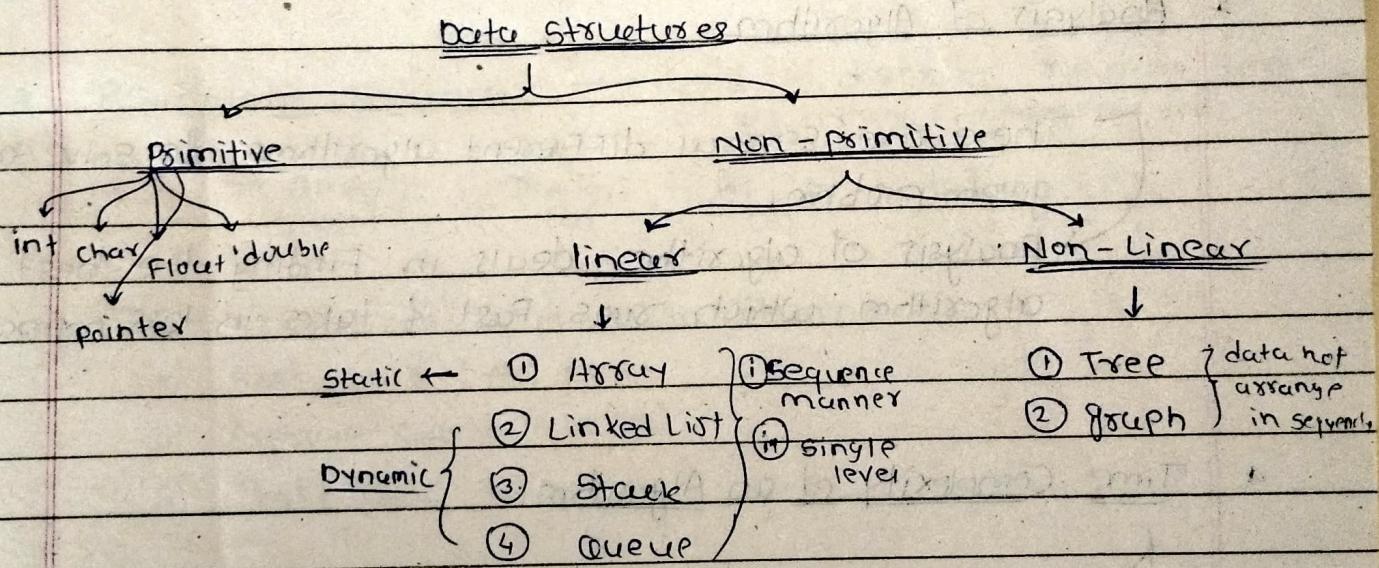
→ It is a way to organize data.

After organizing data it becomes easy to process it.

e.g:-

organized book & unorganized books in library.

## \* Types of Data Structures



## \* Algorithms

→ An Algorithm is a set of instruction to perform a task or to solve a given problem

e.g:- ① A recipe book is a collection of recipes in which each recipe provides a step by step instruction to prepare food.

② Let's say to prepare a tea

① Boil water

② put tea in cup

③ enjoy the tea etc.

e.g:- Print sum of 3 given numbers.

→ Let's write algorithm

- ① Perform sum of 3 numbers
- ② Store it in a variable sum
- ③ Divide sum by 3
- ④ Store the value in variable avg
- ⑤ Print the value stored in avg.

code

```
public void findAvg(int a,
                     int b, int c)
{
    int sum = a+b+c;
    int avg = sum/3;
    System.out.println(avg);
}
```

### \* Analysis of Algorithm

→ These case several different algorithms to solve a given problem.

→ Analysis of algorithm deals in finding the best algorithm which runs fast & takes in less memory.

### \* Time Complexity of an Algorithm

→ The amount of time taken by algorithm to run.

→ The input processed by an algorithm helps in determining the time complexity.

e.g:-

```
public int findsum(int n)
```

{

    return n\*(n+1)/2;

O(1)

↑  
It is Fast

```
public int findsum(int n)
```

{

    int sum = 0;

    for (int i=1; i<=n; i++)

    { sum = sum + i;

}

↑  
It is slow

O(n)

## \* Space Complexity

- The amount of memory or space taken by algorithm to run is called a Space Complexity.
- The memory required to process the input by an algorithm helps in determining the Space Complexity.

\* Asymptotic Notations → used to describe running time of algorithm (mathematical tool).

↳ Omega ( $\Omega$ ), Theta ( $\Theta$ ) & Big 'O' Notation.

These Notations help us in determining

- Best case ( $\Omega$ ) omega
- Average case Theta ( $\Theta$ )
- Worst case (Big O)

1) Omega ( $\Omega$ ) Notation → (Determines best case of an Algorithm)

Very rarely used

because we  
doesn't interest  
to find the  
best case

→ It is the formal way to express the lower bound of an algorithm's running time.

→ Lower bound means for any given input this notation determines best amount of time an algorithm can take to complete.

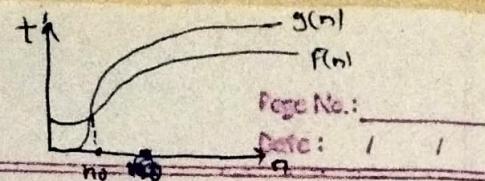
IF we say algorithm takes 100 sec as best amount of time, so, 100 sec will be lower bound of that algorithm.

→ The algorithm can take more than 100 sec but it will not take less than 100 sec.

$$F(n) \leq C + g(n)$$

c = constant

$n > n_0$



## 2] Big O ( $O$ ) Notation.

→ (determine worst case of any algorithm)

(Opposite of  $\Omega$ )

→ It is the formal way to express upper bound of an algorithm's running time

→ Upper bound means for any given input this notation determines longest amount of time an algorithm can take to complete.

For example :-

IF we say certain algorithm takes 100 sec as longest amount of time. So, 100 sec will be upper bound of that algorithm.

→ The algorithm can take less than 100 sec but it will not take more than 100 sec.

→ (Mostly used Algo) → we are very much interested in finding the max<sup>m</sup> amount of time → so we can optimized algorithm to whatever time we want.

## 3] Theta ( $\Theta$ ) Notation

→ (determine Average case)  
(Upper + lower) Bound.

→ It is the formal way to express the upper & lower bound of an algorithm's running time.

→ Determine average amount of time an algorithm can take to complete.

→ Very least used → because there are very rare cases where we actually determine the average time.

## \* Analysis & Rules to calculate Big O Notation.

- \* It's a single processor
- \* It performs sequential execution of statements
- \* Assignment operation takes 1 unit of time (~~like~~  $i=5$ )
- \* Return statement takes 1 unit of time ( $\rightarrow \text{return } x;$ )
- \* Mathematical operation, Logical operation  $\rightarrow$  1 unit of time
- \* Other control / single operation  $\rightarrow$  1 unit of time

### 1) Drop lower order terms

eg:  $T = n^2 + 3n + 1$

lower order ~~of non dominant term~~  $\rightarrow$  Drop

$$T = n^2$$

Time complexity = Big O( $n^2$ )

### 2) Drop constant multipliers

eg:  $T = 3n^2 + 6n + 1$

$$T = n^2 + 6n + 1$$

$$T = n^2$$

Time complexity = Big O( $n^2$ )

### 3) Break the code into Fragments

Finally 
$$T = T_1 + T_2 + T_3$$

## Time complexity of Constant Algorithm

e.g:-

```
① public int sum(int x, int y) {
    int result = x + y;
    return result;
}
```

line no	operation	time
2	$1+1+1+1$	4
3	$1+1$	2
Total		6

$$T = 4 + 2 = 6 \leftarrow \text{It always take the constant amount of time}$$

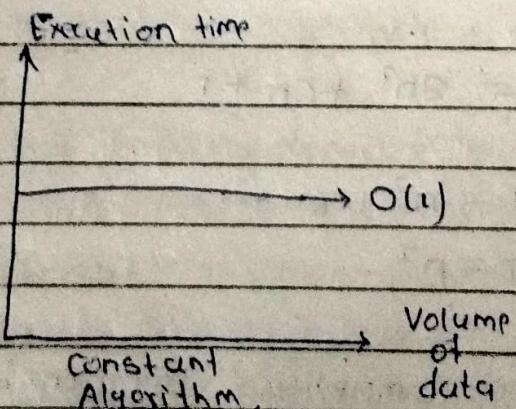
$$T \approx C \text{ (constant)}$$

So, Time complexity = Big O(1)  $\Rightarrow \underline{\mathcal{O}(1)}$

```
② public int get(int[], int i) {
    return arr[i];
}
```

Time complexity  $\Rightarrow \underline{\mathcal{O}(1)}$ .

Graph



## ↑ Time Complexity of Linear Algorithm

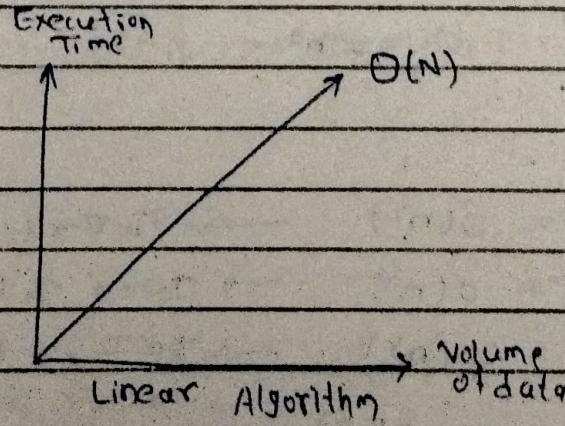
→ Eg:

Find sum of first  $n$  natural no.

```
public void findSum(int n) {  
    int sum = 0; → 1 step (k1)  
    for (int i=1; i<=n; i++) {  
        sum = sum + i; → n step (nk1)  
    }  
    return sum; → 1 step (k2)  
}
```

$$\begin{aligned}\text{Time complexity}(T) &= T_1 + T_2 + T_3 \\ &= k_1 + nk_2 + k_3 \\ &= nk_2 \\ T &= n \\ \boxed{T = O(n)} &\leftarrow \text{Big } O(n)\end{aligned}$$

Graph



## \* Time complexity of polynomial Algorithm

Ex:-

```
For(int i=1; i<=n; it++) {
    For(int j=1; j<=n; jt++) {
        cout ("i=" + it, j=" + jt);
    }
    cout ("End of inner loop");
}
cout ("End of outer loop");
}
```

↓  
defines (For loop inside the For loop)

$$\begin{aligned} \text{Time complexity } T(n) &= K(n+r)n \\ &= n+r+n \cdot (n+1) \\ &= n(1+1+(n-1)) \end{aligned}$$

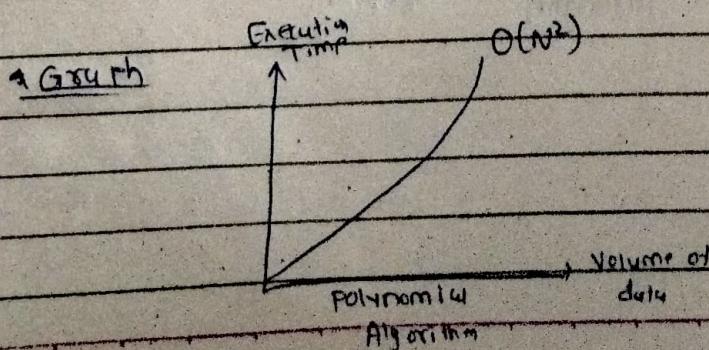
$$\begin{matrix} 0 \rightarrow 0 \\ n \\ 1 \rightarrow 1 \\ \vdots \\ n \end{matrix}$$

$$= n^2$$

$$T = O(n^2) \rightarrow \text{For} \rightarrow 2 \text{ For loop}$$

$$T = O(n^3) \rightarrow \text{IF} \rightarrow 3 \text{ For loop}$$

$$T = O(n^4) \rightarrow \text{IF} \rightarrow 4 \text{ For loop exist}$$



## \* Practice Examples for Time Complexity

1) void Fun(int array[], int length)

```
{   int sum = 0
    int product = 1; }
```

for (int i=0; i < length; i++)

```
{   sum += array[i]; }
```

}

for (int i=0; i < length; i++)

```
{   product *= array[i]; }
```

}

$T_1 = k_1$

$T_2 = nk_2$

$T_3 = nk_3$

→

$$T = T_1 + T_2 + T_3$$

$$= k_1 + nk_2 + nk_3$$

$$= nk_2 + nk_3$$

$$= n(k_2 + k_3)$$

$$T = n$$

$$\boxed{T = O(n)} \rightarrow (\text{Big } O \text{ of } n)$$

2) void Fun(int n)

{

$$\text{int sum} = 0 \quad \left\{ \begin{array}{l} \\ k_1 \end{array} \right.$$

$$\text{int product} = 1; \quad \left\{ \begin{array}{l} \\ k_1 \end{array} \right.$$

for (int i=0; i < n; i++) { → O(n) }

for (int j=0; j < n; j++) { → O(n) }

printf ("%d", i, j);

}

}

$\left. \begin{array}{l} \\ n+n+\dots+(n-1) \end{array} \right\} nk_1$

$$T = k_1 + kn^2$$

$$\boxed{T = O(n^2)}$$

(3) range ( $0, n$ ), average processing time =  $T(n)$   
what is value of  $T(6)$ ?

int Function ( int n )

{      int i ;       $\longrightarrow$   $k_1$

    if (n <= 0)

    {      return 0 ;      }

    else

    {

        i = random (n - 1) ;       $\longrightarrow$  ①

        printf ("this is %d") ;

        return Function (i) + Function (n - 1 - i) ;

    }

}

→

$T_6 \rightarrow 1$  unit of time

$T_5 \downarrow$

$T_5 \rightarrow 1$  unit of time

$T_4 \downarrow$

$T_4 \rightarrow 1$

$T_3 \downarrow$

$T_3 \rightarrow 1$

$T_2 \downarrow$

$T_2 \rightarrow 1$

$T_1 \downarrow$

$T_1 \rightarrow 1$

$T_0 \downarrow$

$T_0 \rightarrow 1$

~~no of calls~~

$|T(6) = 6| \leftarrow$  no of calls

$T = O(n)$

④ Which of the following are equivalent to  $O(N)$ ? Why?

i)  $O(N+P)$ ; where  $P < N/9 \rightarrow$  non dominant term

$$T = O(N+P)$$

$$\boxed{T = O(N)}$$

ii)  $O(9N - k)$

$$T = O(9N - k)$$

$$T = O(9N)$$

$$\boxed{T = O(N)}$$

iii)  $O(N + 8 \log N)$

$$\rightarrow T = O(N + 8 \log N)$$

$$\boxed{T = O(N)}$$

iv)  $O(N + M^2) \rightarrow M$  is not constant

$\rightarrow$

$$T = O(N + M^2)$$

$$T = O(N + M^2)$$

$\rightarrow$  This is not  $O(N)$

⑤ Following code for balanced binary search tree, what is runtime?

$\rightarrow$  int sum(Node node)

```
{ if(node == NULL)
    { return 0; } }
```

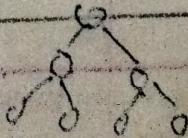
k,

```
} return sum(node.left) + node.value + sum(node.right);
```

3

$$\boxed{T = O(N)}$$

$$\boxed{T = O(N)}$$



Q) Find the complexity of following code which test whether given no is prime or not?

```

int isPrime(int n) {
    if (n == 1) {
        return 0;
    }
    for (int i = 2; i * i < n; i++) {
        if (n % i == 0)
            return 0;
    }
    return 1;
}
  
```

→ Suppose  $i^2 < n$

$$i^2 < n \quad i = 2, 3, \dots, (n-1)$$

$i < \sqrt{n}$

$i = \sqrt{n}$

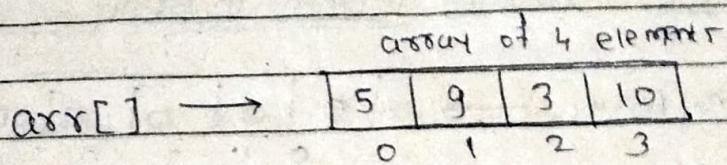
$i = \sqrt{n}$

$$\begin{aligned}
T &= T_1 + T_2 \\
&= k_1 + \sqrt{n} k_2 \\
T &= \sqrt{n} \\
\boxed{T = O(\sqrt{n})}
\end{aligned}$$

## Array

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### \* Array



- \* It's a collection of data elements of specified type
- \* All data have contiguous memory locations.
- \* Each position has two neighbours except first & last one
- \* Size of array is fixed & cannot be modified once it is created
- \* Index starts at 0 and for (1D array) ends at (length - 1)
- \* Declaration (1D)

### Syntax :-

Datatype arrayName [ ] ;

Datatype [ ] array Name ;

e.g:-      int myArray [ ] ;                  { we most for Java  
 or            int [ ] myArray ; }                 } mostly used

- \* Initialization → It gives memory to array elements.

### Syntax :-

arrayName = new datatype [size];

e.g:-      myArray = new int [5];

- \* → \* Declaration + Initialization in one step (Java)

datatype [ ] arrayName = new datatype [size];

String e.g:-    int [ ] myArray = new int [5];    // int myArray = {1, 2, 3, 4, 5};

## 2 Adding & Updating element in Array

myArray → [ 0 | 0 | 0 | 0 | 0 ]  
0 1 2 3 4

when  
we  
initialize  
an array

public void constructor()

int[] myArray = new int[5]; → [ 0 | 0 | 0 | 0 | 0 ]

myArray[0] = 5; → [ 5 | 0 | 0 | 0 | 0 ]

myArray[1] = 1; → [ 5 | 1 | 0 | 0 | 0 ]

myArray[2] = 8; → 5 1 8 0 0

myArray[3] = 2; → 5 1 8 2 0

myArray[4] = 10; → 5 1 8 2 1 0

myArray[5] = 9; → 5 1 8 2 1 0

(update) →

}

## 3 Point elements of array in Java

→ public void printArry(int[] arr)

{

int n = arr.length;

for (int i = 0; i < n; i++)

{

System.out.print(arr[i] + " ");

}

System.out.println();

}

## \* Removing integer From an array.

Q Given an array of integers, return an array with even integers removed

Input : arr = {3, 2, 4, 7, 10, 6, 5}

Output : arr = {3, 7, 5}



arr[ ] [ 3 | 2 | 4 | 7 | 10 | 6 | 5 ] (odd count)

removeEven(arr);

result[ ] [ 3 | 7 | ]

0 1 ↑ 2

idx

public static

→ int[] removeEven(int[] arr)

{

int oddCount = 0;

For (int i=0; i<arr.length; i++)

{

if (arr[i] % 2 != 0)

{

oddCount++;

}

}

int[] result = new int[oddCount];

int idx = 0;

For (int i=0; i<arr.length; i++)

{

~~if~~ if (arr[i] % 2 != 0)

{

result[idx] = arr[i];

idx++;

}

return result;

First we count

how many

odd numbers are  
occur in odd  
count

→ create another new  
array.

↑ size  
for passing  
value to it

## ↑ How to Reverse an Array in Java

(Q) Given an array, the task is to reverse array or string

Given - { 2, 11, 5, 10, 7, 8 }

Output - { 8, 7, 10, 5, 11, 2 }



```
reverseArray (int numbers[], int start, int end)
{
```

```
    while (start < end)
```

```
    {
```

```
        int temp = numbers[start];
```

```
        numbers[start] = numbers[end];
```

```
        numbers[end] = temp;
```

```
        start++;
```

```
        end--;
```

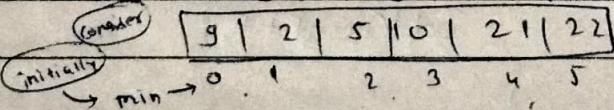
```
}
```

```
}
```

At starting

Start = 0  
end = 5

\* To Find the Minimum value of the Array.



```
public int findMinimum (int[] arr)
```

```
{
```

```
    int min = arr[0];
```

// initially consider first value is min

```
    for (int i; i < arr.length; i++)
```

```
{
```

```
    if (arr[i] < min)
```

```
{
```

```
        min = arr[i];
```

```
}
```

```
}
```

```
return min;
```

Sarit Gupta

\* Find the second maximum value in an array.



arr[] [ 13 | 34 | 2 | 34 | 3 | 3 | 1 ]  
0 1 2 3 4 5

initially second max & max value are take minimum.

### Program

```
public int findSecondMax(int[] arr)
{
    int max = Integer.MIN_VALUE;
    int SecondMax = Integer.MIN_VALUE;
    for (int i=0 ; i<arr.length ; i++)
    {
        if (arr[i] > max)
        {
            Secondmax = max;
            max = arr[i];
        }
        else if (arr[i] > secondmax && arr[i] != max)
        {
            Secondmax = arr[i];
        }
    }
    return Secondmax;
}
```

Q How to move zeroes to the end of Array

→ arr[] [ 8 | 1 | 2 | 1 | 0 | 0 | 3 ]

Output → [ 8 | 1 | 2 | 1 | 3 | 0 | 0 ]

-Program :

```
public void movezeroes(int[] arr, int n)
```

```
    int j = 0;
```

```
    for (int i = 0; i < n; i++)
```

```
        { if (arr[i] != 0 && arr[j] == 0)
```

```
            {
```

```
                int temp = arr[i];
```

```
                arr[i] = arr[j];
```

```
                arr[j] = temp;
```

```
}
```

```
        if (arr[j] != 0)
```

```
{
```

```
        j++;
```

```
}
```

```
}
```

Q Find the missing no in array of given range

(Imp) Q1 → Given an array of  $(n-1)$  distinct numbers in the range of 1 to n. Find the missing number in it.

arr[] [ 2 | 4 | 1 | 8 | 6 | 3 | 7 ]

Output : 5

Explanation :- The missing from range 1 to 8 is 5.

math formula to find the sum of n natural number

$$= \frac{n*(n+1)}{2}$$

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### Program :-

```
public int findMissingNumber(int[] arr)
```

```
{
```

```
    int n = arr.length + 1;
```

```
    int sum = n * (n + 1) / 2;
```

```
    for (int num : arr)
```

```
{
```

```
        sum = sum - num;
```

```
}
```

```
    return sum;
```

```
}
```

1) calculate sum of all values in array and 2) subtract one by one all values in array from sum

we will get the missing no.

## Singly Linked List

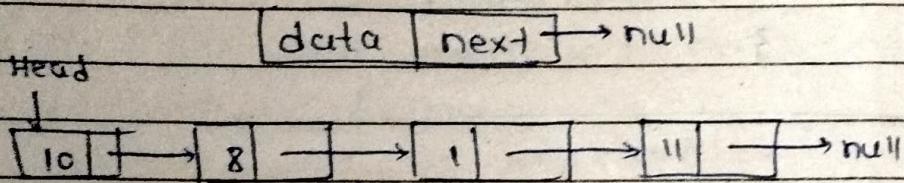
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- \* Singly Linked List → Linear or non-contiguous memory allocation

Singly linked list is a data structure used for storing collection of nodes & has following properties

- stores an object in node.

- \* It contains sequence of nodes
- \* A node has data and reference to next node in a list.
- \* First node is the head node.
- \* Last node has data and points to null.



### \* Implementation of ListNode in Singly Linked List

#### // Generic Type

```

→ public class ListNode < T >
{
    private T data;
    private ListNode < T > next;
}

```

#### // Integer Type

```

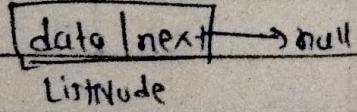
public class ListNode
{

```

```
    private int data;
```

```
    private ListNode next;
```

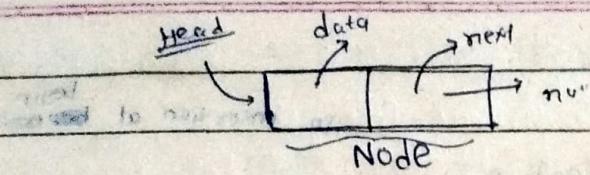
```
}
```



# Rough Implementations

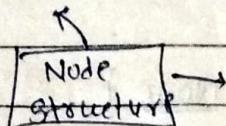
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Static class Node

```
{ int data;
  Node next; }
```



constructor → Node (int data)

```
{ this.data = data;
```

```
this.next = null; }
```

```
Node.head = null;
```

(cond)

① Linked list exist

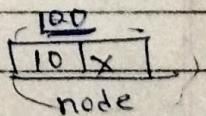
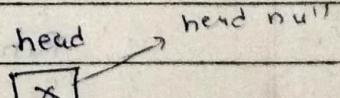
② Linked list does not exist

③ IF (head == null)

{

head = node;

}



node = 100

node.data = 10

node.next = null

else

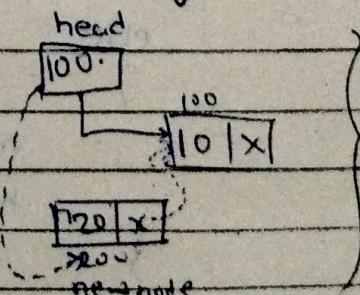
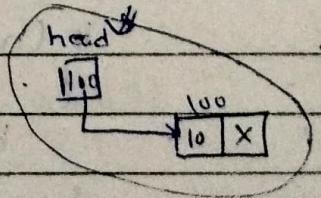
{

head = new\_node;

new\_node.next = head;

head = new\_node;

}



## \* Creation of linked List.

```
public class Single_Creation
```

```
{
```

```
    static void Node {
```

```
        int data;
```

```
        Node next;
```

```
        Node (int data)
```

```
{
```

```
            this.data = data;
```

```
            this.next = null;
```

```
}
```

```
} Node head = null;
```

```
public void creation()
```

```
{
```

```
    int data;
```

```
    Scanner sc = new Scanner (System.in);
```

```
    do { Sout ("Enter data");
```

```
        data = sc.nextInt();
```

```
        Node new-node = new Node (data);
```

```
        if (head == null)
```

```
{
```

```
            head = new-node;
```

```
}
```

```
else
```

```
{
```

```
            new-node.next = head;
```

```
            head = new-node;
```

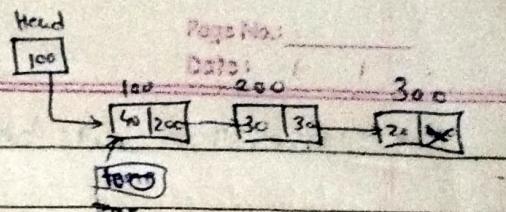
```
}
```

```
Sout ("Do you want to continue. If yes, press 1");
```

```
n = sc.nextInt();
```

```
while (n == 1); }
```

also insertion at begin  
end



For traversing → we use temp

so  
temp creation → Node temp = head;

temp = 100  
temp.data = 40  
temp.next = 200

rest code will continue

```
→ public void traverser()
  {
    Node temp = head;
    if (head == null)
    {
      cout("LL does not exist");
    }
    else
    {
      while (temp != null)
      {
        cout(temp.data);
        temp = temp.next;
      }
    }
  }
```

```
public static void main (String args[])
{
```

```
  Single_Creation l = new Single_Creation();
  l1.create();
  l1.traverser();
}
```

## \* Insertion at begin, end & position of (Single LL)

### At begin

we have  
to w.p.  
new-node  
as a p.t.

new-node.next = head;

head = new-node;

### At end

Node temp = head;

while (temp.next != null)

{

temp = temp.next

}

temp.next = new-node;

we have  
to w.p.  
temp  
as a p.t.

### At position

Sout ("Enter the po of node to be insert");

p = sc.nextInt();

Node templ = head;

for (int i = 0; i < (p - 2); i++)

{

templ = templ.next;

}

new-node.next = templ.next;

templ.next = new-node;

b



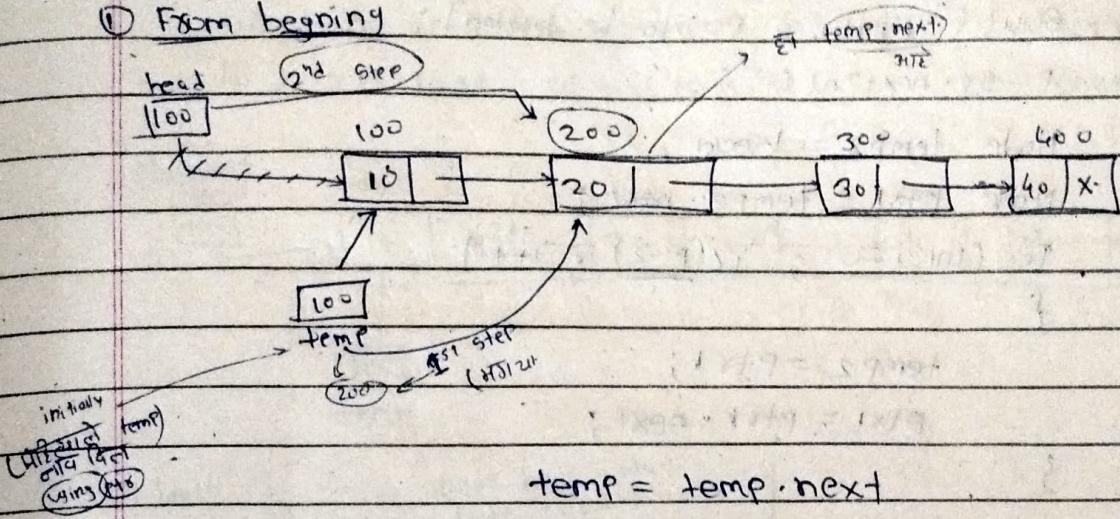
# Boutik Bazaar ( $\sqrt{2}$ )

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## \* Deletion of linked list

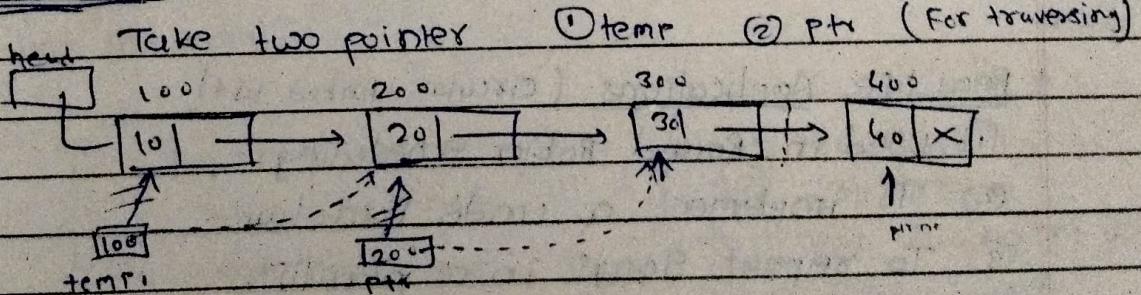
### ① From beginning



### Code

```
{
    Node temp = head;
    temp = temp.next;
    head = temp;
```

### ② From end



Node temp = head;

Node ptr = temp.next;

while (ptr.next != null)

{    temp = ptr;

    ptr = ptr.next;

Step 1

temp.next = null;

temp

### ③ Delete from po

cout ("Enter a po to be deleted");

p = sc.nextInt();

Node temp2 = head;

Node ptx1 = temp2.next;

for (int i=0; i<(p-2); i++)

{

temp2 = ptx1;

ptx1 = ptx1.next;

}

temp2.next = ptx1.next;

## # Circular linked list

The circular linked list is a linked list where all nodes are connected to form a circle.

In a circular linked list, the first node and last node are connected to each other which forms a circle.

→ There is no null at the end.

### \* Real life Applications (circular linked list)

① Used in Round Robin Scheduling

② To implement a undo function

③ To repeat songs in a play list.

④ To keep track of the turn in a multiplayer game.

1 Time complexity → ① For traversing in singly linked list = O(n)

② In circular linked list (For traversing) = O(1)

Because in circular linked list, we have known the address of last node (tail)

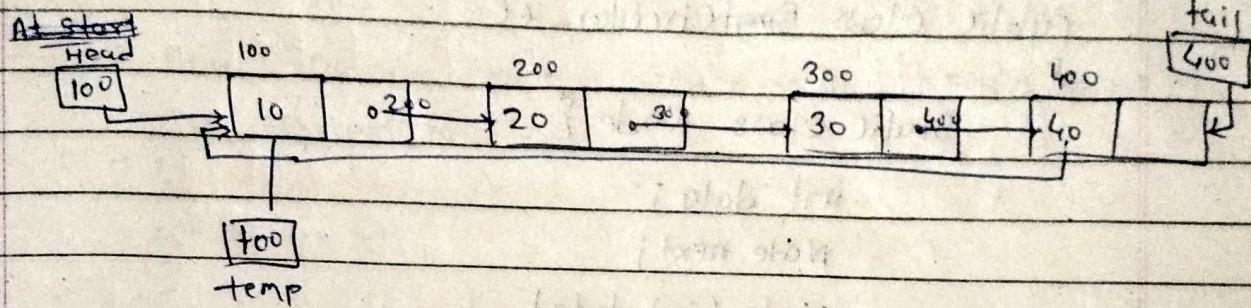
(Rough Work)

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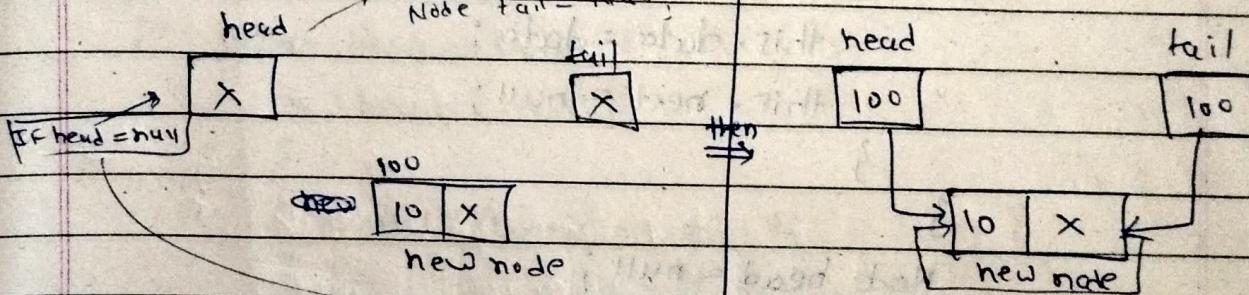
## + Creation

- Creation is same as an linear linked list, only we have create extra point 'tail' at end.
- And In last assign tail = head. IF insertion takes place.



At begin

Node head = null;  
Node tail = null;



head = new-node  
tail = new-node

new-node.next = Head/tail/

If link list exist

else part

{

new-node.next = head  
head = new-node  
tail.next = head;

\* Only tail part extra  
3112 3114444444  
tail.next & starting mt  
join anaq m1111111111

at begin  
Code : Creation & traversing

→ import java.util.Scanner;

public class ~~for~~ Circular\_LL  
{

    static class Node {

        int data;

        Node next;

        Node (int data)

    {

        this.data = data;

        this.next = null;

    }

    Node head = null;

    Node tail = null;

    public void creation()

    {

        int data, n;

        Scanner sc = new Scanner(System.in);

        do

        { System.out.print("Enter data");

            data = sc.nextInt();

            Node newNode = new Node(data);

            IF (head == null)

            {

                head = newNode;

                tail = newNode;

                newNode.next = Head;

            }

        out Head, tail, newNode  
        कोई भी प्राप्ति

② \*

③ \*

```

    else
    {
        new-node.next = head;
        head = new-node;
        tail.next = head;
    }

    ④
    cout("Do you want to add more data. If yes press Y!");
    n = sc.nextInt();
}

while(n == 1);
}

```

```

public void traverse()
{
    Node temp = head;
    if (head == null)
    {
        cout("LL does not exist");
    }
    else
    {
        do {
            cout(temp.data + " ");
            temp = temp.next;
        } while (temp != head);
    }
}

```

⑤ temp = head

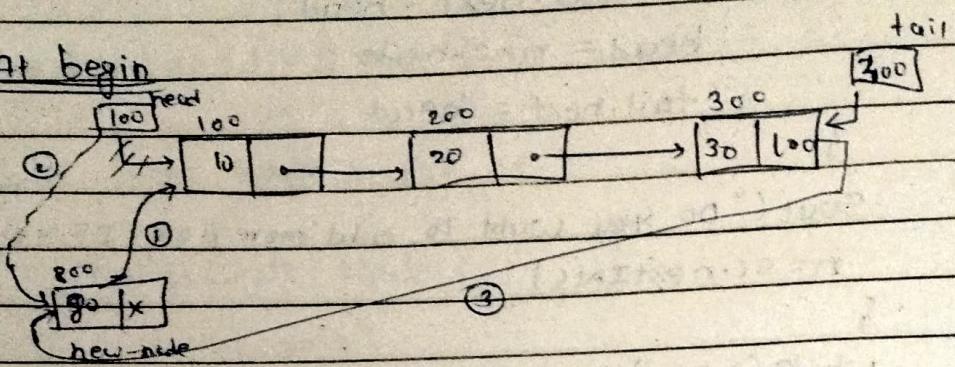
```

public static void main(String args[])
{
    Circular_ll *a = new Circular_ll();
    a.create();
    a.traverse();
}

```

## \* Circular LL (Insertion)

### ① At begin



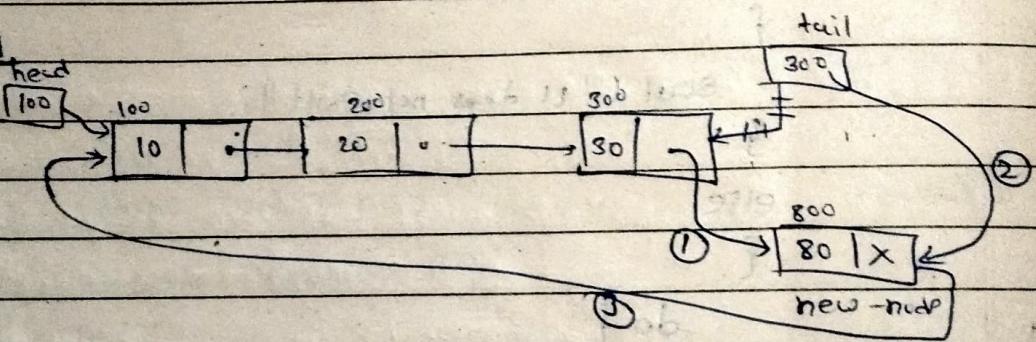
Code

```
new-node.next = head;
```

```
head = new-node;
```

```
tail.next = head;
```

### ② At end



Code

```
tail.next = new-node;
```

```
tail = new-node;
```

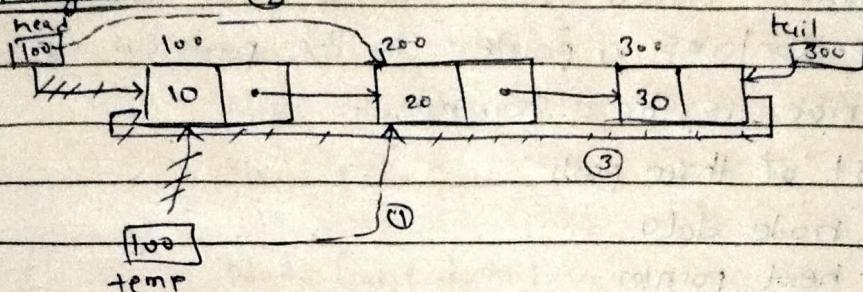
```
new-node.next = head;
```

### ③ Insert at Po

→ It is same as insertion of linear linked list  
(no change).

## Circulation II (Deletion)

① At begin



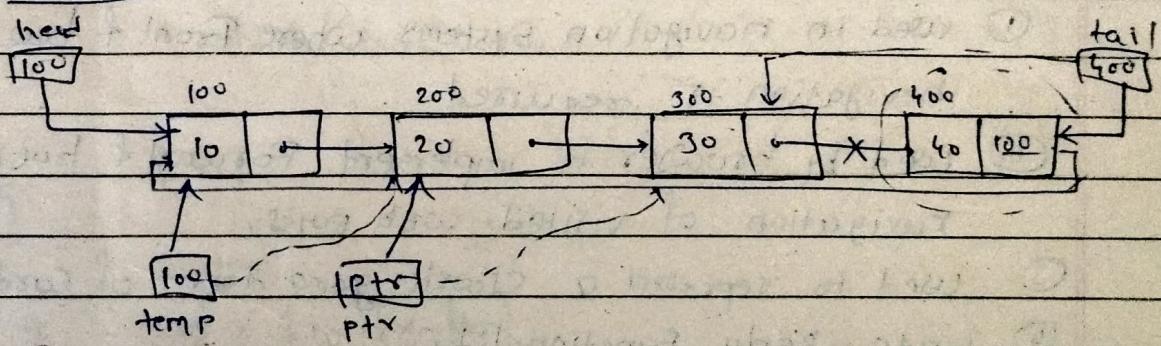
Code

```
temp = temp.next;
```

```
head = temp;
```

```
tail.next = head;
```

② At end



Code

```
Node temp = head;
```

```
Node ptrr = temp.next;
```

```
while (ptrr.next != head)
```

```
{
```

```
    temp = ptrr;
```

```
    ptrr = ptrr.next;
```

```
}
```

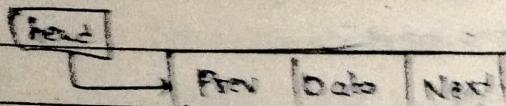
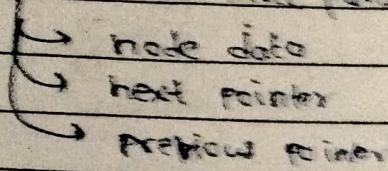
```
temp.next = head;
```

```
tail = temp;
```

## # Doubly linked lists

Doubly linked list is a complex linked list in which a node contains a pointer to the previous as well as the next node in the sequence.

- Consist of three parts



## 2 Real life Applications

- ① Used in navigation systems where forward & backward navigation is required.
- ② Used by browser to implement forward & backward navigation of visited web pages.
- ③ Used to represent a classic game deck of cards.
- ④ Undo - Redo functionality.

## 3 Time Complexity

$$\text{Insertion} = O(1)$$

$$\text{Traversal} = O(n)$$

$$4 \text{ Space Complexity} = O(1)$$

Structure

```
Static class Node {
```

```
    int data;
```

```
    Node next;
```

```
    Node prev;
```

```
Node (int data)
```

```
{
```

```
    this.data = data;
```

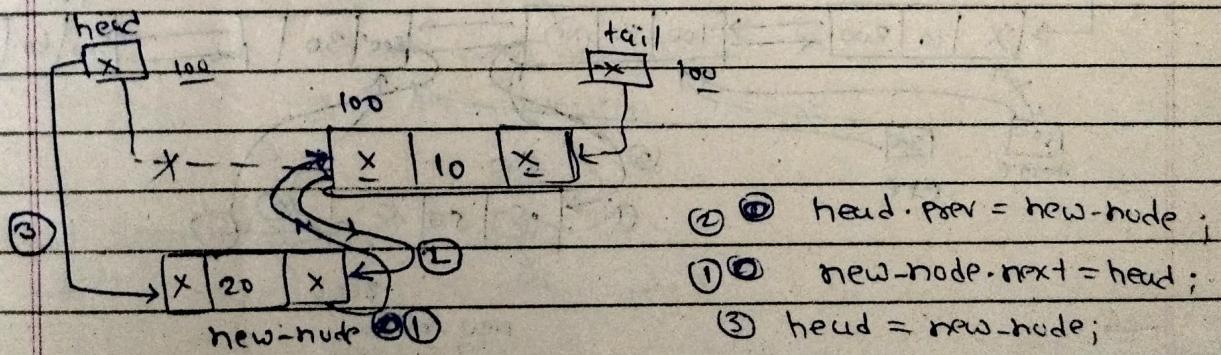
```
    this.next = null;
```

```
    this.prev = null;
```

```
}
```

```
Node head = null;
```

```
Node tail = null;
```

Creation

```
IF (head = null)
```

```
{ head = new-node;
```

```
tail = new-node;
```

```
}
```

```
else { head.prev = new-node; } → वाले ओर खाले
```

```
new-node.next = head;
```

```
}
```

```
head = new-node;
```

Note

traversing  
downwards singly

## Insertion (doubly)

### (1) At begin

new-node.next = head;

head.prev = new-node;

head = new-node;

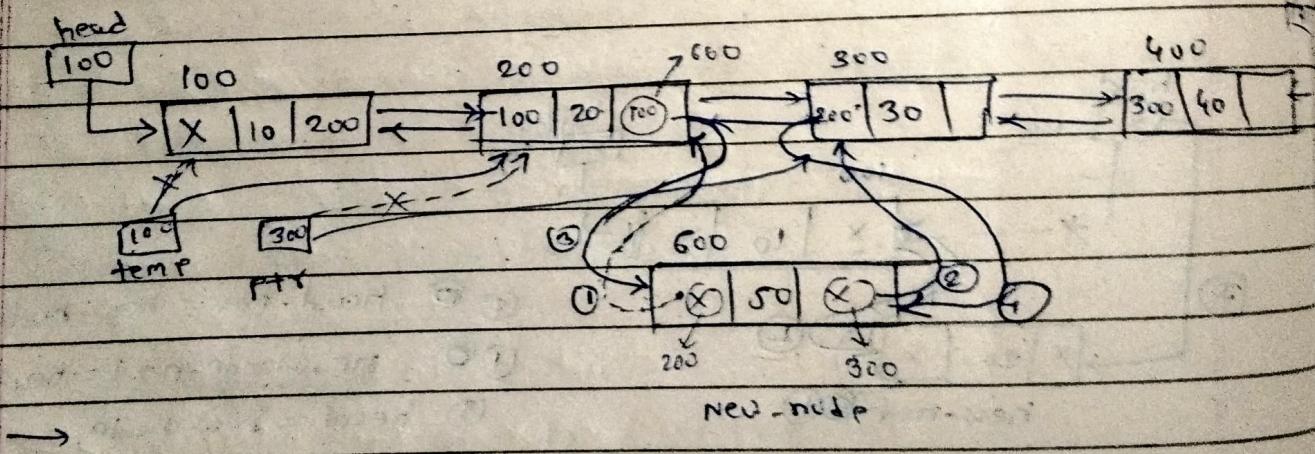
### (2) At end

tail.next = new-node;

new-node.prev = tail;

tail = new-node;

### (3) Specific location



. For(*i*=1 ; *i*<*P*-1 ; *i*++)

{ *temp* = *ptr*;

*Ptr* = *Ptr*.*next*;

}

*new-node*.*prev* = *temp*;

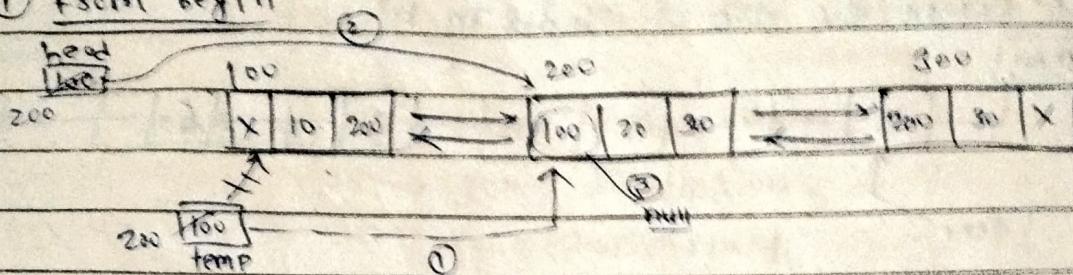
*new-node*.*next* = ~~*ptr*~~ *ptr*;

*temp*.*next* = *new-node*;

*ptr*.*prev* = *new-node*;

## \* Deletion (Doubly)

### ① From begin



Node temp = head;

① temp = temp.next;

head = temp;

head.prev = null;

### ② From end

Node temp = tail;

temp = temp.prev;

temp.next = null;

tail = temp;

### ③ Specific location

→ For (i=1; i < p-1; i++)

{ temp = ptr;

ptr = ptr.next;

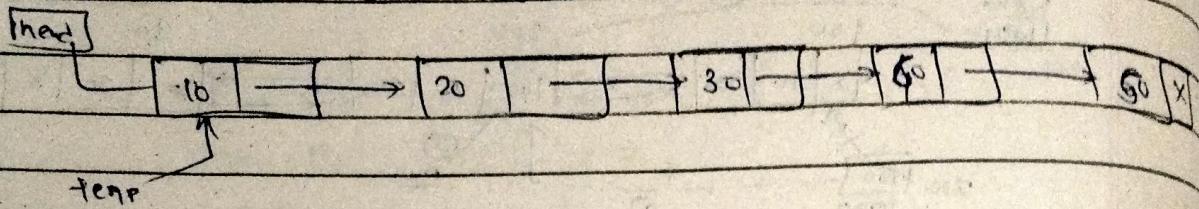
}

temp.next = ptr.next;

ptr.next.prev = temp;

## Practice Questions

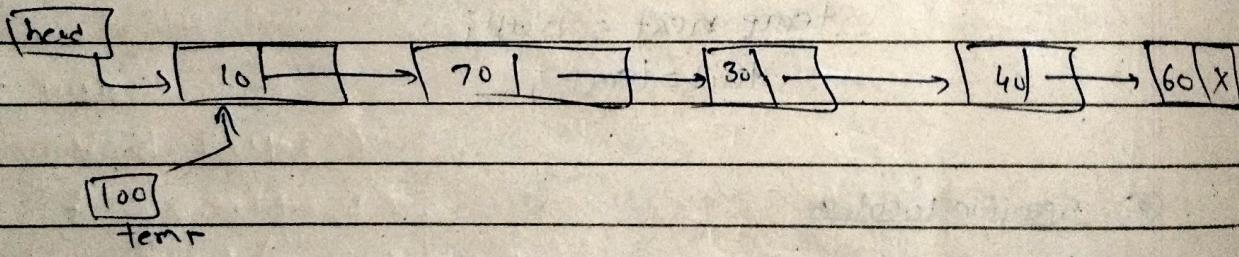
- ① Count the no of Nodes in LL



```

int c = 0;
Node temp = head;
while (temp != null)
{
    c++;
    temp = temp.next;
}
cout(c);
    
```

- ② Find maximum element



```

int max = 0;
Node temp = head;
while (temp != null)
{
    if (temp.data > max)
        max = temp.data;
    temp = temp.next;
}
    
```

## Stack

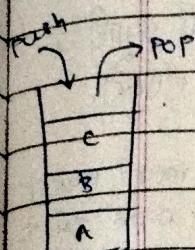
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LIFO (Last in First out)

Stack :- Stack is a linear datastructure

Follows LIFO order for performing Operations



operations

Push = insertion

Pop = deletion.

Peak (top of stack)

## Stack

### \* Real World Application of Stack

- ① Used in Recursion
- ② Undo operation
- ③ Web browser (history)
- ④ Tower of Hanoi (Algorithm of Stack)
- ⑤ Functions calls.

→ \* Explain why Stack is a recursive datastructure?

→ Recursion :- It is a technique of solving any problem by calling same function again & again until some breaking condition where recursion stops & it starts calculating the solution from there.

→ ② Thus, In recursion last function called needs to be completed first.

③ So, Stack is a LIFO data structure (last in first out) & hence, it is used to implement in recursion.

### \* Time & space complexity of Stack

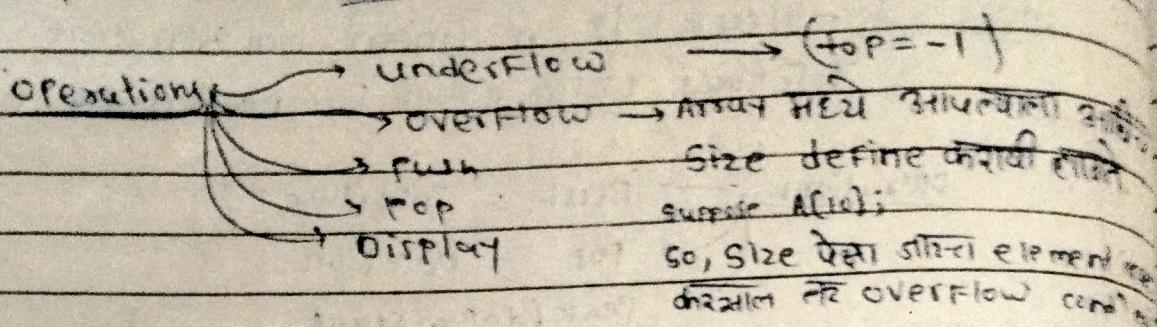
	Time	Space
Push	$O(1)$	$O(1)$
Pop	$O(1)$	$O(1)$
Peak	$O(1)$	$O(1)$

Microprocessor

Time

Space

## Implementation of Stack (Using Array)



→ underflow cond' → Check in case of (pop)

→ overflow cond' → Check in case of (push)

1) void underFlow()

{

if ( $top == -1$ )

{

Sout ("underflow cond'");

}

2) void overFlow()

{

if ( $top == (n-1)$ )

{

Sout ("overflow");

}

3) for push

void Push()

{ overflow();

→ First check overflow cond'  
IF part

Sout ("Enter data");

int i = sc.nextInt();

} else part

top = top + 1;

a[top] = i;

array  
we declare

}

$$\left. \begin{array}{l} \text{pop} = \text{top} - - \\ \text{push} = \text{top} + + \end{array} \right\}$$

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### 3) For pop

Void Pop()

{

if (top == -1)

{

Sout ("Underflow");

}

else

{

top = top + 1;

}

### 3) For display

Void display()

{

Sout ("Items are");

For (int i = top ; i >= 0 ; i++)

{

Sout (a[i]);

}

}

### Time complexity

	Best	Worst
push	$O(1)$	$O(n)$
pop	$O(1)$	$O(n)$
display	$O(n)$	$O(n)$

## Implementation of stack (using linked list)

Note :- ① Stack के linked list को implementation करता है। जो 'Head' असीमित (Top) संहिता है।

② Insertion (push) और deletion (pop) से begining लाये जाते हैं।

③ Linked list में overflow condition घटना होती है। कारण stack 3-12 के linked list में size आधिक नहीं बढ़ावी जाती।

④ Time complexity पर linked list की O(1) है। कारण, जबकि push operation करने के लिए beginning की operation करनी

### ① underflow

```
if (top == -1)
{
    cout("Underflow");
```

}

for (i = 0; i < 10; i++)

### ② void push()

{

cout("Enter data");

int data = sc.nextInt(); // Scanner class

Node new-node = new Node(data);

if (top == null)

{

top = new-node;

}

else

{

new-node.next = top;

top = new-node;

③ void pop()

```

{
    if (top == null)
    {
        cout ("Stack empty");
    }
    else
    {
        temp = temp->next;
        top = temp->next;
    }
}

```

→ यह 31/40 के  
Pointer द्वारा  
एक Delete करने  
का काम है।

④ void display()

```

{
    Node temp = top;
    while (temp != null)
    {
        cout (" " + temp->data);
        temp = temp->next;
    }
}

```

Time complexity	Best case	Worst case
push()	O(1)	O(1)
pop()	O(1)	O(1)
display()	O(n)	O(n)

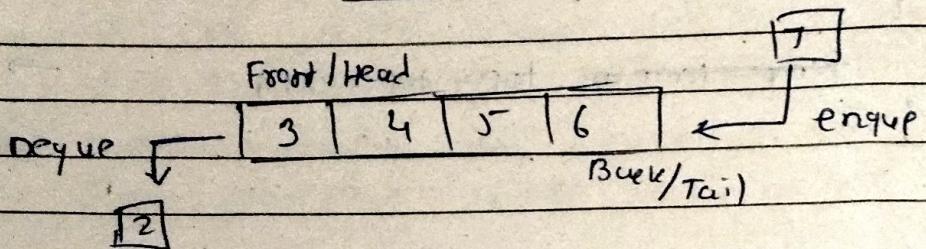
## Queue

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\* Queue :- Queue is a linear data structure that is open at both ends.  
Follows First in first out order for performing operations (FIFO)

\* Addition of element is done at one end & deletion is done at another end.

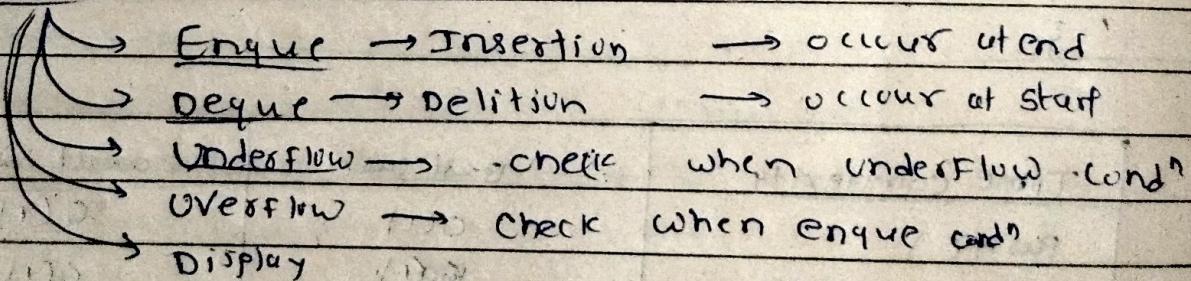


## Queue Data Structure

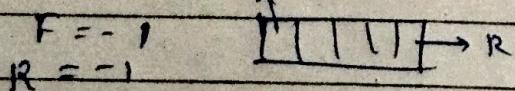
\* Characteristic

- \* Queue can handle multiple data.
- \* We can access both ends.
- \* They are fast & flexible.

## Operations



### ① Underflow cond



IF ( $F == -1 \text{ and } R == -1$ )  
{  
    // Underflow

### ② Overflow



IF ( $R == (N-1)$ )  
{  
    // Overflow

```
int F = -1, R = -1;  
int n = 10;  
int q[] = new int[n];
```

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### ③ Enque (using Array)

```
Void enqueue()
```

```
{
```

```
if (x == (n - 1))
```

```
{ sout ("overflow");
```

```
}
```

```
else
```

```
{ sout ("Enqueueing element");
```

```
if (F == -1 && R == -1)
```

```
{
```

```
F = 0;
```

```
R = 0;
```

```
q[x] = i;
```

```
else
```

```
{ x = x + 1;
```

```
q[x] = i;
```

```
} }
```

### ④ Deque

```
Void Dequeue()
```

```
{
```

```
if (F == -1 && R == -1)
```

```
{
```

```
sout ("underflow");
```

```
}
```

```
else
```

```
F = F + 1;
```

```
}
```

```
Void display()
```

```
{
```

```
sout ("Items are");
```

```
for (int i = F; i <= R; i++)
```

```
{
```

```
sout (q[i]);
```

```
}
```

```
}
```

Node F = Null;  
Node R = Null;

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## \* Queue (using Linked List)

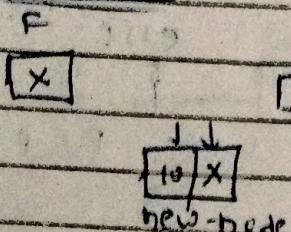
### ① Underflow

```
if (F == null & R == null)  
{  
    cout ("underflow");  
}
```

### ② overflow

```
if (new == null)  
{  
    cout ("overflow");  
}
```

### ③ Enqueue



```
public void enqueue()
```

```
{ if (F == null)
```

```
    F = new-node;
```

```
    R = new-node;
```

```
}
```

```
else
```

```
    cout ("Enter data");
```

```
    int data = sc.nextInt();
```

```
    Node new-node = new Node(data);
```

```
    if (F == null)
```

```
{
```

```
    F = new-node;
```

```
    R = new-node;
```

```
}
```

```
else
```

```
{
```

```
    R.next = new-node;
```

```
    R = new-node;
```

```
}
```

④ public void Deque ()

{

if ( $F == null$ )

{

cout ("Underflow");

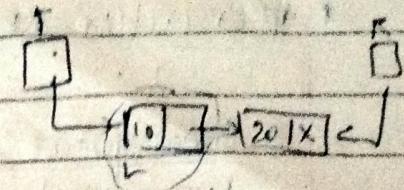
}

else

{

$F = F.next;$

}



$(F = F.next)$

### ⑤ Display

Node temp =  $F$ ;

while ( $temp != null$ )

{

cout( $\circ$ , temp.data);

temp = temp.next;

}

### \* Time Complexity (Queue)

Queue

Array

LL

Enqueue

$O(1)$

$O(1)$

Dequeue

$O(1)$

$O(1)$

Display

$O(n)$

$O(n)$



Fix(size)

## # Circular Queue using Arrays

- Linear queue  
(using array)

0	1	2	3	4	5	6
10	20	30	40	50	60	70
F=0						R=6

(AFTER DELETION)  
First two  
element

0	1	2	3	4	5	6
0	0	30	40	50	60	70
F=2						R=6

(only exist in case of arrays) → Wastage of Space occur in linear queue.

(The use of circular que can overcome this problem)

## Circular Queue

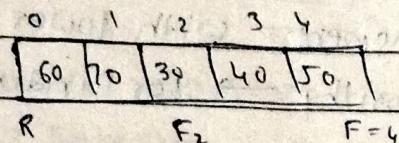
Front end is connected to rear end.

\* Cond' For the que to be circular que

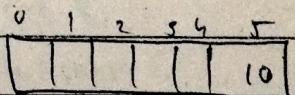
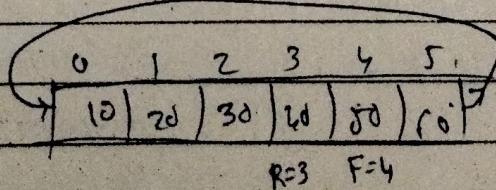
- ① Front = 0 & rear = (n - 1)
- ② front = rear + 1

### Comparison

	Linear	Circular
① Insertion & Deletion	Insertion is done at rear end, deletion is done at front end	Insertion & deletion can take place at any end
② Memory space	Require more space than circular que	Require less space compared to linear que
③ Memory utilization	The use of memory is inefficient	The memory can be more efficiently utilized
④ Order	Follows FIFO	No specific order for execution

\* Linear Queue1) Enqueue  $\Rightarrow R = R + 1$ 2) Dequeue  $\Rightarrow F = F + 1$ \* Circular Queue1) Enqueue  $\Rightarrow R = (R + 1) \% \text{ max size}$ 2) Dequeue  $\Rightarrow F = (F + 1) \% \text{ max size}$ 

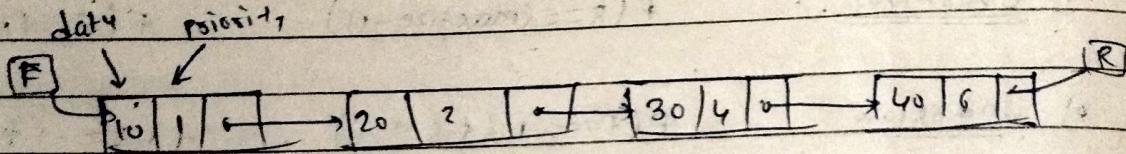
$$R = (6+1)\%5 = 15 \% 5 = 0$$

Linear1) Overflow $f(R == (\text{max size} - 1))$ circular queue $f(F == (R + 1) \% \text{ max size})$ 2) Underflow $f(f == -1 \text{ } \& \text{ } R == -1)$  $f(F == -1 \text{ } \& \text{ } R == -1)$ (if  $F == R$ )For ( $F=12$ )  $\rightarrow$  since only one element is present in queue3) DisplayFor ( $i=F ; i < R ; i = (i+1) \% n$ ){  
cout( $q[i]$ );

}

## Priority Queue → implements min Heap

- ① A priority queue is a type of queue that organizes elements based on their priority values.
- ② Elements with higher priority values are typically retrieved before elements with lower priority values.
- ③ Used in Dijkstra's Algorithm → For finding shortest path
- ④ Prim's Algorithm
- ⑤ Heap sort → (use in implementation)
- ⑥ Operating system → we use it for load balancing.



# Java collection framework

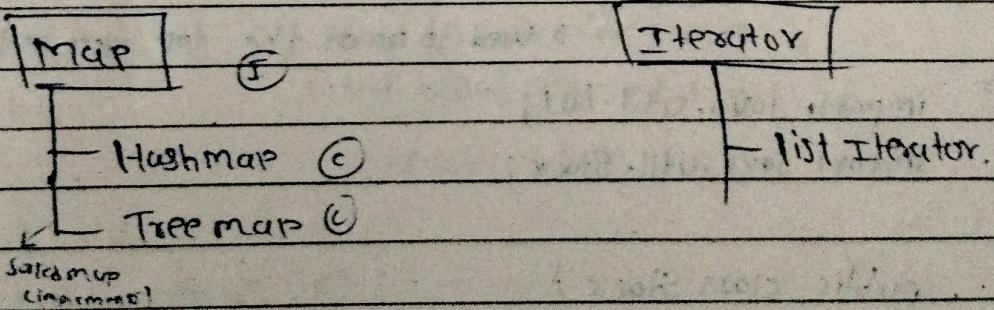
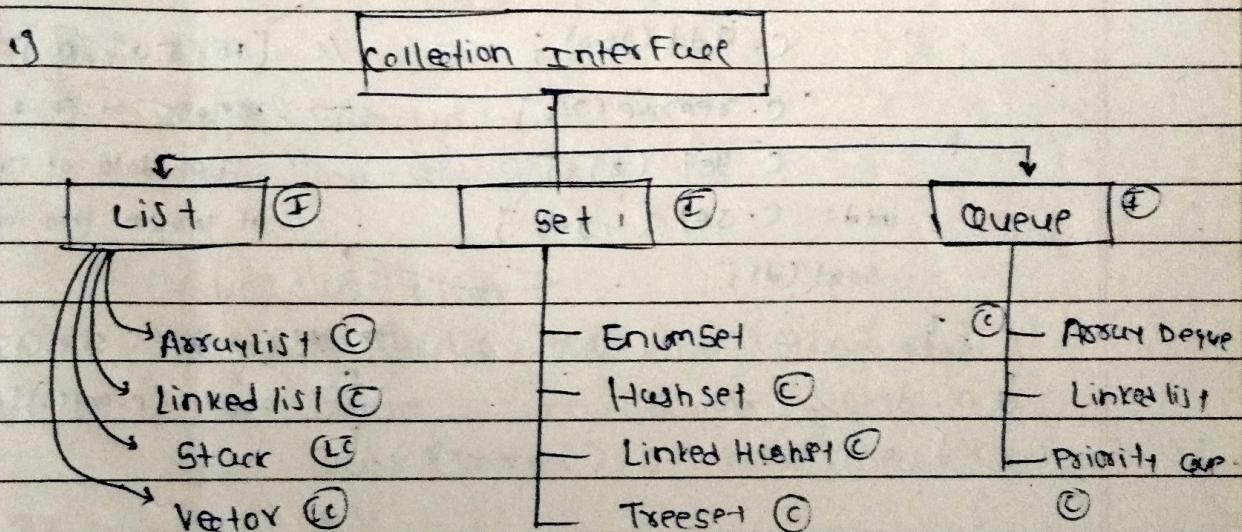
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The Java Collections framework provides a set of interfaces & classes to implement various data structures & algorithms.

## \* Three types of collection Framework

- 1] Collection interface                          `java.util.Collection`
- 2] Map interface                                `java.util.Map`
- 3] Iterator



Collection Framework :- It is the set of predefined classes and interfaces which is used to store multiple data.

# 1) ArrayList

```
import java.util.ArrayList;
```

```
public class ArrayList {
    public static void main (String args[])
    {
        List<Integer> c = new ArrayList<>();
        c.add(10);
        c.add(50);
        c.add(100); // [10, 50, 100]
        c.remove(2); // remove at pos 2 i.e. 100
        c.get(2); // Print data at position 2
        int d = c.set(1, 90); // at location they insert 90
        System.out.println(d);
    }
}
```

```
for (int i=0; i < c.size(); i++)
{
    System.out.println(c.get(i));
}
```

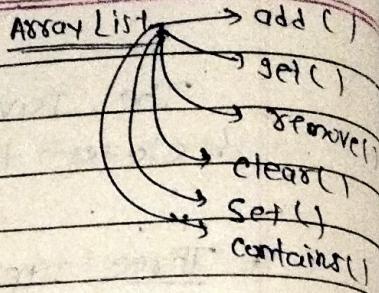
# 2) Stack

```
import java.util.List;
import java.util.Stack;
```

```
public class Stack
```

```
public static void main (String args[])
{
```

```
    Stack<Integer> c = new Stack<Integer>();
```



```
c.push(100);  
c.push(200);  
c.push(300);  
c.push(400); // [100, 200, 300, 400]  
int d = c.peek(); // 400  
int e = c.search(200);  
cout < e;  
}  
}
```

### Input From User

```
→ import java.util.List;  
import java.util.Stack;
```

```
public class Stack {  
    public static void main(String args[]) {  
        Scanner sc = new Scanner(System.in);  
        Stack<Integer> c = new Stack<Integer>();  
        for (int i=0; i<5; i++) {  
            System.out.print("Enter your number:");  
            int value = sc.nextInt();  
            c.push(value);  
        }  
        cout < c;  
        if (!c.isEmpty()) {  
            c.pop();  
        }  
    }  
}
```

## ① In Collection Framework Assoc & LL are same. 3] LinkedList

→ ~~import~~

import java.util.LinkedList;

public class linklist {

    public static void main(String args[]) {

        LinkedList<Integer> c = new LinkedList<>();

        c.add(10);

        c.add(50);

        c.add(100);

        c.add(60);

        → c.remove(2)

        c.clear(); → clear all the data

        boolean d = c.contains(50)

→ check whether that particular value is present or not in LL

}

## ② Queue using linked list

queue

→ Linked list

→ Priority Queue

### ↳ Linked list

→ OFFER → used to enqueue  
→ POLL → used to dequeue  
→ PEEK

### ↳ Priority Queue

→ OFFER  
→ POLL

\* ~~ArrayList~~ Collection Framework use करा किया simple way से program करा time complexity Same रहती, Page No.: \_\_\_\_\_ Date: / /

→ import java.util.Queue  
import java.util.LinkedList;

```
public class queue {
    public static void main (String args[])
    {
        Queue<Integer> c = new LinkedList<>();
        c.offer(10);
        c.offer(20);
        c.offer(30);
        c.offer(60); // [10, 20, 30, 60]

        System.out.println(c.peek()); // 10
        c.poll(); // 60 is deleted
        c.poll(); // 30 is deleted
        System.out.println(c); // [10, 20]
    }
}
```

#### \* Priority Queue

→ import java.util.PriorityQueue;

import java.util.Queue;

public class priority\_queue {

public static void main (String args[])
{
 Queue<Integer> c = new PriorityQueue<>();

c.offer(60);

c.offer(89);

~~System.out.println(c);~~

c.poll();

System.out.println(c);

use min heap

java.util.concurrent;

Note :-

For max heap  $\Rightarrow$  Queue<Integer> c = new PriorityQueue<>(<> (comparator : reverse order))

## # Set Interface

- set interface does not allow duplicate.
- because it's storing the data in hashes & hash table does not allow duplicate values.
- Unordered set of items.

### 1] HashSet

- add()
- remove()
- contains()
- size()
- clear

(unordered collection)

### 2] LinkedHashSet

- add()
- remove()
- contains()
- size()
- clear

(ordered collection)

### 3] TreeSet

- add()
- remove()
- contains()
- size()
- clear

(sorted collection)

### 4] HashSet

```
import java.util.HashSet;  
import java.util.Set;  
public class HashSet {  
    public static void main (String args[]) {  
        }
```

```
        Set<Integer> c = new HashSet<>();
```

```
        c.add(10);
```

```
        c.add(50);
```

```
        c.add(100);
```

```
        c.add(60);
```

// [50, 100, 10, 60] → Unordered collection of data

```
c.remove(50); // [100, 10, 60]
```

```
c.size() → return no. items available
```

(main diff b/w  
ArrayList & HashSet)

}

}

2) LinkedHashSet → Display the data in sequence as we insert.

→ Same as HashSet (but difference is LinkedHashSet is implemented using linkedlist)

→ LinkedHashSet maintain the property of both set as well as linkedlist.

→ `Set<Integer> c = new LinkedHashSet<>();`

3) TreeSet → Display Data in sorted form.

→ maintaining the property of linked list & Binary Tree.

→ `Set<Integer> c = new TreeSet<>();`

# Map Interface → A map contains values on the basis of key i.e key & value pair

### HashMap

- put()
- putIfAbsent()
- isEmpty()
- remove()

### TreeMap

- put()
- putIfAbsent()
- isEmpty()
- remove()

→ Each key & value pair is known as an entry.

→ A map contains unique keys.

Note → A map doesn't allow duplicate keys, but you can have duplicate values

→ HashMap & LinkedHashMap allow null keys & value but TreeMap doesn't allow any null key or value.

String   
 \* (key is unique)

## 1) HashMap

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→  $\text{Map<Integer, String>} c = \text{new HashMap<>()};$

c. Put(1, 'A');

c. Put(2, 'B');

c. Put(3, 'C');

c. Put(4, 'D');

c. PutIfAbsent(4, 'D'); → data absent 2nd time for order  
क्षेत्री अस्ति विकास के रूप  
रह देते.

for (Integer d : c.keySet())

{  
 System.out.println(d);

System.out.println(c.get(d)); // for accessing the keys

for (String d : c.values())

{  
 System.out.println(d);

System.out.println(c.get(d)); // for only accessing the values.

## 2) TreeMap: → Sorted order (uses Binary Search concept)

$\text{Map<Integer, String>} c = \text{new TreeMap<>()};$

# List Iterator → list iterator is used to traverse all the elements in the list

\* Forward traversing      ↘ hasNext( )  
                                   ↗ next( )

\* Backward traversing      ↗ hasPrevious( )  
                                   ↘ previous( )

→ ex:

```
List<Integer> c = new ArrayList();
c.add(10);
c.add(20);
c.add(100);
c.add(60);
```

ListIterator<Integer> d = c.listIterator();

while (d.hasNext())

{

    cout(d.next());

}

while (d.hasPrevious())

{

    cout(d.previous());

}

## \* Non-Linear Data Structures

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### Binary Tree.

#### \* Types of Binary Tree

① Binary Tree

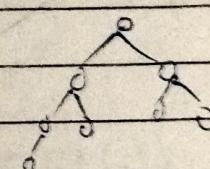
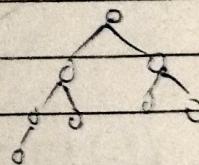
→ only two child are present.

② complete BT

→ two child complete वित्ती

आवाज तक करता complete सेता

ही पातें, पर नहीं मात्र पाते



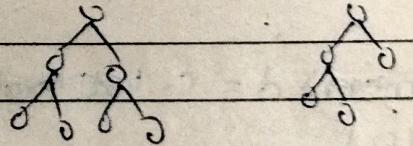
→ this is complete BT

③ Full BT | 2-Tree | Proper BT | Strict BT

कोणता यंत्र नोड हे 0 किंवा 2 चिल्ह असतील

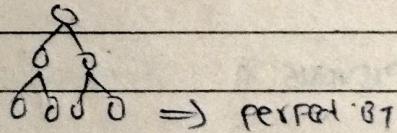
पूर्ण BT

e.g.



⇒ Full BT

④ Perfect BT → यंत्री लेवल पूरी कॉम्प्लीट असतील



\* Formulas

?

### Formula

1] Max no of nodes possible at level  $i = \underline{2^i}$

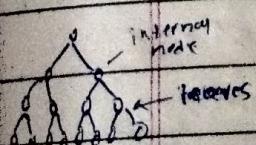
2] Max. no of nodes possible in a B.T of height  $h = \underline{2^{h+1} - 1}$

3] Min no of nodes possible in a B.T of height  $h = (h+1)$

4] Max height of B.T having  $n$  nodes =  $[\log_2(n+1) - 1]$

5] Min ~~no of nodes~~<sup>height</sup> possible in B.T having  $n$  nodes  
 $= \underline{(n-1)}$

In full binary tree of height  $h$



$$l = 2^h \text{ leaves} \quad \text{and} \quad m = 2^h - 1 \text{ internal nodes}$$

binary tree of height 3

8 leaves  $\rightarrow$  internal nodes.

Motivation, IF you want to be programmer  $\rightarrow$  you do not need to learn recursive approach  
But, IF you want to be good programmer  $\rightarrow$  you must learn recursive approach

\* Recursion  $\rightarrow$  efficient approach in order to solve the Problem

Recursion is the technique of making a function call itself.

① When a Function call's itself

Note: Base condition is must. (कोणत्याही Problem मधील base cond" exist करत नसेल तर, आण्याची व्याप्ती recursive method ने use करत नसेल.)

e.g:-  $A(n)$   $\Rightarrow$  Get  $n=4$   
Function calls  $\rightarrow A(n-1);$  {  
recursion  
  
Hi  $n=4-1=3$   
Hi  $n=3-1=2$   
Hi  $n=2-1=1$   
Hi  $n=1-1=0$   
Hi  $n=0-1=-1$   
There is no termination condn (base cond") on Program goes to infinite loop

for e.g:-  
 $A(n)$   
{ if( $n==1$ )  
{ return 1; } } Base cond" (terminating cond)  
else {  
sout("Hi");  
 $A(n-1);$   
}

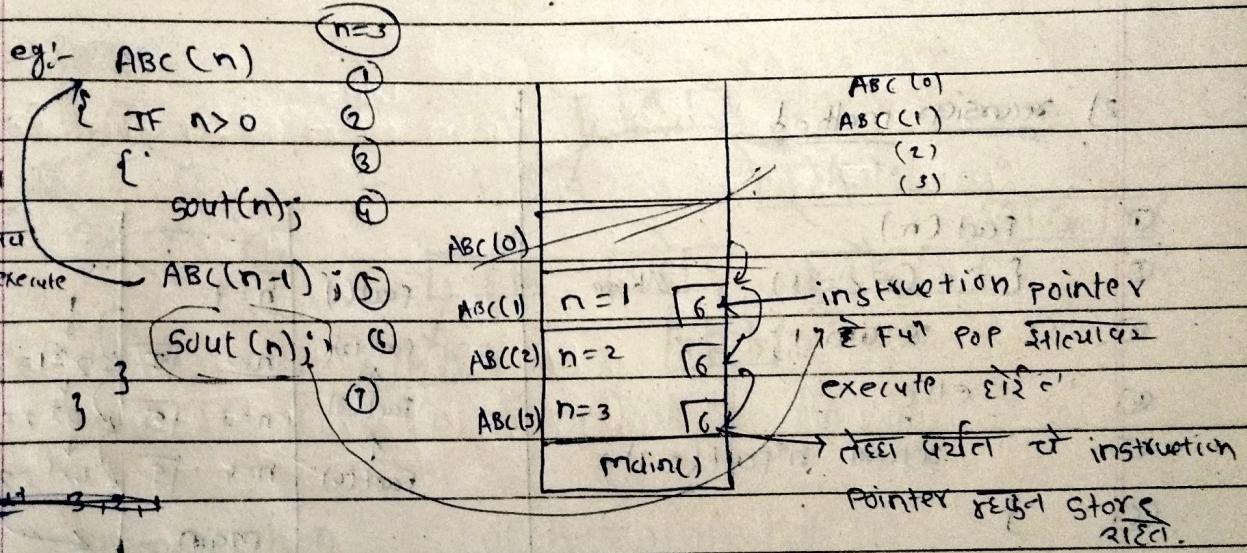
③ Use to solve bigger problem after breaking it down in smaller Problem

e.g. Factorial of 50  $\rightarrow$  we break the Problem  
First we find Factorial 1 then 2, 3 - 4, 5 then ... 49, 50

④ Iterative Problems  $\leftrightarrow$  Recursive Problems

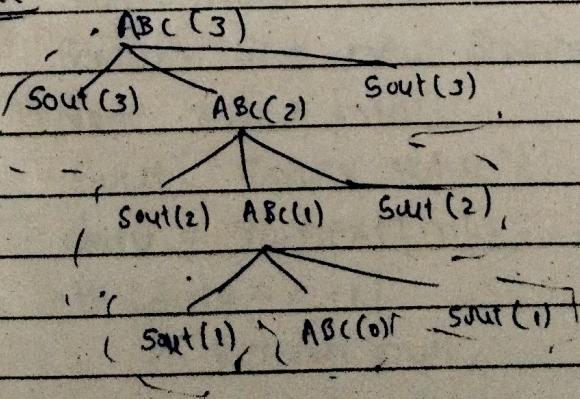
RecursionStackTree1) Stack

instruction pointer & The program Counter, called instruction pointer, is a processor register that indicates the current address of program being executed.



Output :- 3, 2, 1, 1, 2, 3

POP stack

2) Tree

3, 2, 1, 1, 2, 3

## Program to Find the Factorial

### ① Iterative method

$F = 1 ; n = 4$

for( $i=1 ; i \leq n ; i++$ )  
{

$F = F * i;$

-3

$$1 * 1 = 1$$

$$1 * 2 = 2$$

$$2 * 3 = 6$$

~~$$6 * 4 = 24$$~~

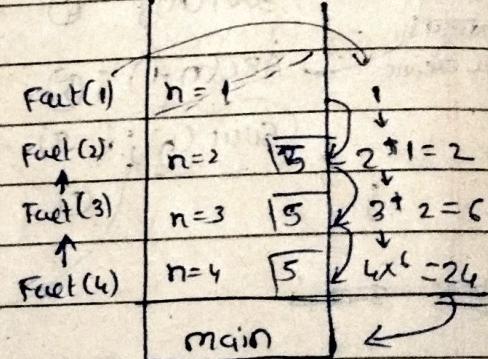
So  $\boxed{\text{Fact}(4) = 24}$

### ② Recursion method

```

① Fact(n)
② { if (n <= 1) // base
③     return 1;
④ else
⑤     return n * Fact(n-1);
⑥ }

```



So  $\boxed{\text{Fact}(4) = 24}$

• Binary Tree Traversal: (Left, Root, Right) Inorder

• Binary left child

(Left child) =  $2i + 1$

• Binary right child

index (Arr) =  $2i + 2$  = Right child

Left child =  $2i + 1$

Right child =  $2i + 2$  } Binary tree data formula  $\frac{1}{2}$

Store करा जाए (i.e. tree में left child के right

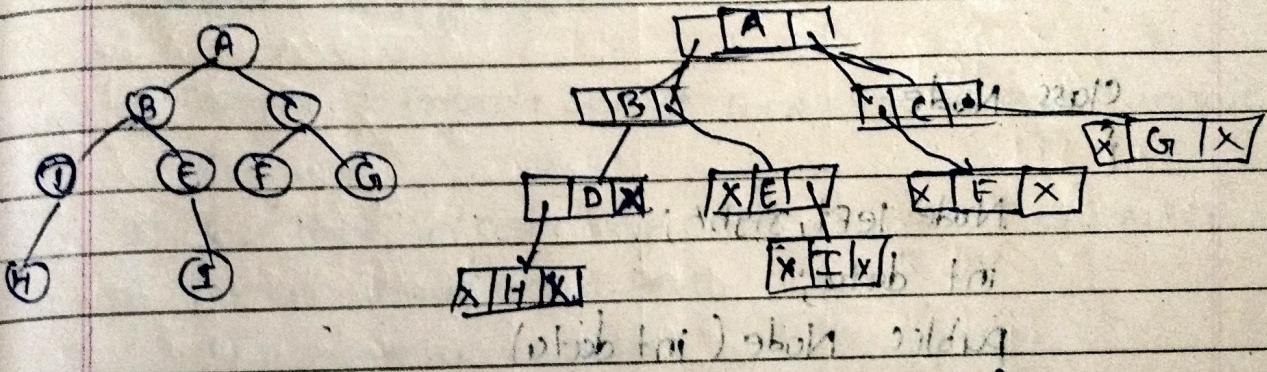
( $i+1$  वाले पार्ट) नए बिन लिए जाएँ

?

• Using linked list

(Left child) =  $2i + 1$

### \* Concept



### \* Implementation

public class tree-creation

{

    Static Node Create() {

        Scanner sc = new Scanner(System.in);

        Node root = null;

        System.out.print("Enter value");

        data = sc.nextInt();

        if (data == -1)

            return null;

        root = new Node(data);

```
System.out.print("enter left child of " + root.data);
```

```
root.left = create();
```

```
System.out.print("enter right child of " + root.data);
```

```
root.right = create();
```

```
return root;
```

}

```
public static void main(String args[])
```

{

.

}

```
Node root = create();
```

Class Node {

```
    Node left, right;
```

```
    int data;
```

```
    public Node(int data)
```

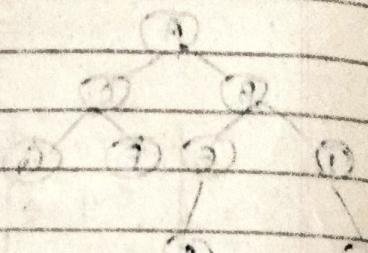
```
        this.data = data;
```

```
        left = null;
```

```
        right = null;
```

}

1 2 3 4



```
    if (left == null) left = new Node(data);
```

```
    if (right == null) right = new Node(data);
```

```
    if (data < left.data) left =
```

```
    if ("what is this") right =
```

```
    if (data > right.data) right =
```

```
    if (data == left.data) if
```

```
    if (data == right.data) if
```

```
    if (data == left.data) if
```

$O(n \log n)$  ↪ Huffman Coding → David Huffman

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\* Application of Binary Tree → Huffman Coding

↪ used to compress the data

Huffman Coding



Compress ↗ Fixed length → simple  
↘ Variable length.

Frequently occurring characters

→ Huffman Coding is a technique of compressing data to reduce its size without losing any of the details.

## # Huffman Coding Algorithm

- 1) Create a Priority Queue consisting of each unique character
- 2) Sort them in ascending order of their frequencies.
- 3) For all unique characters
  - i) Create a NewNode
  - ii) extract minimum value from Q and assign to left child
  - iii) extract minimum value from Q & assign to right child of NewNode
  - iv) calculate the sum of these two minimum value and assign it to the value of NewNode
- v) Insert this NewNode into the tree
- 4) return rootNode.

eg:- ① | 1 | 6 | 5 | 3 | → Calculate Frequency  
B C A D → Form string

↓  
Sort, in increasing order (In Priority queue)

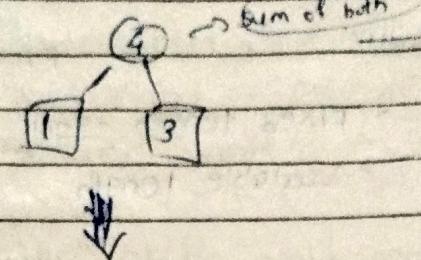
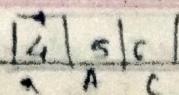
| 1 | 3 | 5 | 6 |  
B D A C

↓  
Add lower child of max smaller to left

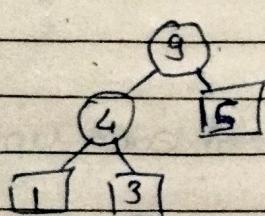
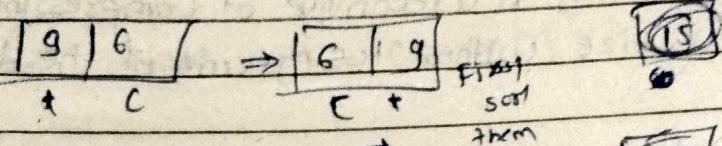
## # Huffman Coding Complexity

① Time complexity =  $O(n \log n)$

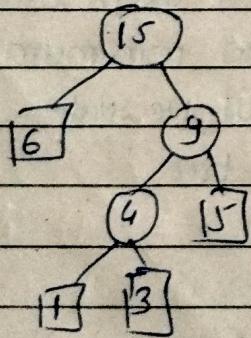
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more lower as left node  
& higher as right node of tree



Character	Freqn	Cdpr	Size
A	5	11	$3 \times 2 = 6$
B	1	100	$1 \times 3 = 3$
C	6	0	$6 \times 1 = 6$
D	3	101	$3 \times 3 = 9$



$$4 \times 8 = 32 \text{ bits}$$

15 bits

28 bits

without ending total size = 120 bits

After encoding =  $32 + 15 + 28 = 75$  bits

↓ Decode It

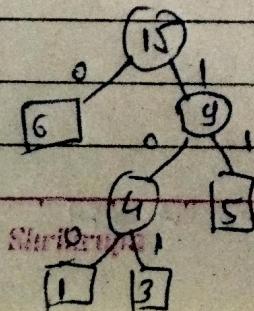
left child = 0  
right child = 1

↓ Compress

## # Applications

① used in conventional compression formats like GZIP, BZIP2, PKZIP etc.

② for text & Fax transmission



# Graph

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Graph :- A graph is a nonlinear structure, like linear data structures (lists), it can be implemented with either an indexed or a linked building data structure.

- \* Non-linear Data Structures
- 
- \* A graph  $G(V, E)$  consists of
- 1] a set of objects  $V = \{v_1, v_2, v_3, \dots, v_n\}$  called vertices.
  - 2] a set of  $E = \{e_1, e_2, e_3, \dots, e_m\}$  called edges.

## # Applications

- 1) Facebook, Twitter accounts → graphs suggest mutual friends.
- 2) Telecommunication Network.
- 3) Google maps → used for building transportation system.
- 4) Computer Science → used to represent flow of computation.
- 5) World wide web →
- 6) Operating System → Process & resources are considered as vertices of graph, & edges can draw resources to allocated processes.
- 7) Mapping System → In GPS we also use graphs.
- 8) Microsoft Excel → use DAG means Directed Acyclic graphs.
- 9) Dijkstra Algo → use graph, to find shortest path between nodes.
- 10) Social media sites → we use graph to track choice of users.

## # Graph Representation in Memory

1) Adjacency Matrix [Array]

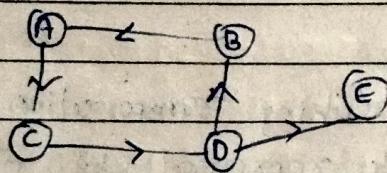
2) Adjacency List {Link list}

3) Multi List

1) Adjacency Matrix → using Array

$A_{ij} = 1$ , if there is an edge from  $v_i$  to  $v_j$

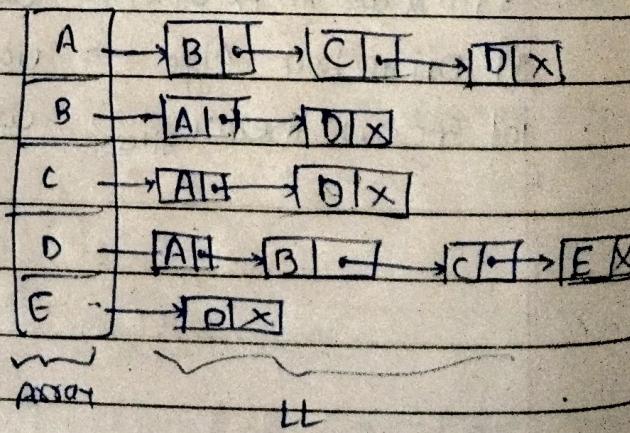
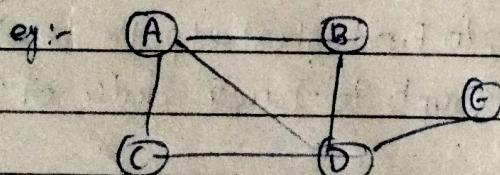
$A_{ij} = 0$ , if there is no edge



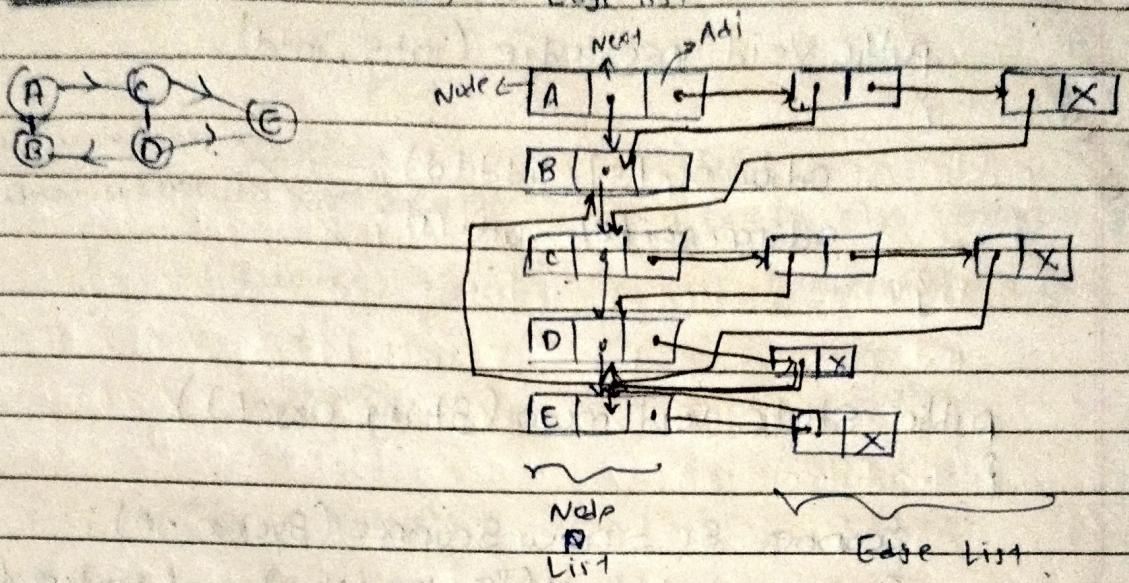
	A	B	C	D	E
A	0	0	1	0	0
B	1	0	0	0	0
C	0	0	0	1	0
D	0	1	0	0	1
E	0	0	0	0	0

Weighted graph  $3 \times 2 \times 11$ ,  $\text{RT}^2 = 1227$   
STP pure weight  $1227$ .

2) Adjacency List (using Linklist) → combination of (Array + LL)



3) Multilist (using LL)  $\xrightarrow{\text{Node List}}$   $\xleftarrow{\text{Edge List}}$



## \* Graph Implementation using Adjacency List

### \* Program

```

import java.util.LinkedList;
import java.util.Scanner;

public class graph-implement {
    private LinkedList<Integer> adjacency[]; use  
collection  
framework
    public graph-implement(int v) {
        adjacency = new LinkedList[v];
        for (int i = 0; i < v; i++)
            adjacency[i] = new LinkedList<Integer>();
    }
}
  
```

3

Only for  
 graph  
 & graph  
 traversal  
 BFS & DFS  
 Done using  
 implementation

public void insertedge (int s, int d)

adjacency [s]. add (d);  
 adjacency [d]. add (s);

source (adjacency [s]);  
 sink (adjacency [d]);

public static void main (String args[])

{ Scanner sc = new Scanner (System.in);

System.out.print ("Enter Number of Vertices & Edge");

int v = sc.nextInt();

int e = sc.nextInt();

graph implement g = new graph-implement (v);

System.out.print ("Enter edge");

for (int i=0; i<e; i++)

{

int s = sc.nextInt();

// Source edge

int d = sc.nextInt();

// Destination

g.insertedge (s,d);

}

## Graph Traversal

### BFS

(Breadth First Search)

(Queue)  $\rightarrow$  [FIFO]



Slower



Time Complexity =  $O(V+E)$



require more  
memory space  $\Theta(OV)$

### DFS

(Depth First Search)

(Stack) [LIFO]



Faster



$O(V+E)$

$V = \text{Vertices}$   
 $E = \text{Edges}$

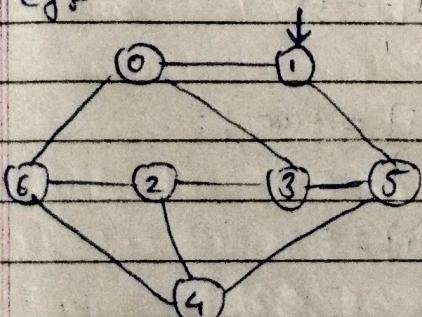


less memory space  
require

+ BFS → uses Queue

BFS is a vertex-based technique for finding the shortest path in the graph.

e.g.



we have to create 3 arrays.

For visited  $V[7] =$ 

True	T	T	T	T	T	T
------	---	---	---	---	---	---

 & queue

array

boolean type

$P[7] =$ 

1	0	5	6	3	4	2
---	---	---	---	---	---	---

 & integer type

queue = 

1	0	8	8	3	4	2
---	---	---	---	---	---	---

AFTER PUSHING

Form true value  
is printed one  
by one  
 $= 1, 0, 5, 6, 3, 4, 2$

→ One vertex is selected at a time when it is visited & marked then its adjacent are visited & stored in the queue.

## \* Implementation BFS

public void bfs(int source)  
{

boolean visited-node[] = new boolean[adjacency.length];

int parent-nodes[] = new int[adjacency.length];

Queue<Integer> q = new LinkedList<>();  
q.add(source);

visited-nodes[source] = true;

parent-nodes[source] = -1;

while (!q.isEmpty())

{

int p = q.poll();

System.out.print(p);

for (int i : adjacency[p])

{

if (visited-node[i] != true)

{

visited-node[i] = true;

q.add(i);

parent-nodes[i] = p;

}

3

3

3

public static void main(String args[])

{ System.out.println("Enter Source for bfs traversal");

int source = sc.nextInt();

g.bfs(source);

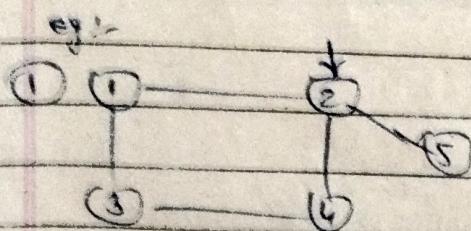
~~DFS~~ (Depth First Search) → uses Stack  $\rightarrow$  push last element (LIFO)

The DFS is an edge-based technique

two stages

- ① First visited vertices are pushed into the stack &
- ② Second if there are no vertices then visited vertices are popped.

Adjacency



2	1	4	5	3
V[s]	true (t)	T	T	T

2	5	4	3	1
P[s]				

2	1	4	5
Stack <sub>1</sub>			

see 2 adjacent node

Printing: → 2, 5, 4, 3, 1

1	4	8
Stack <sub>2</sub>		

see 5 adjacent node

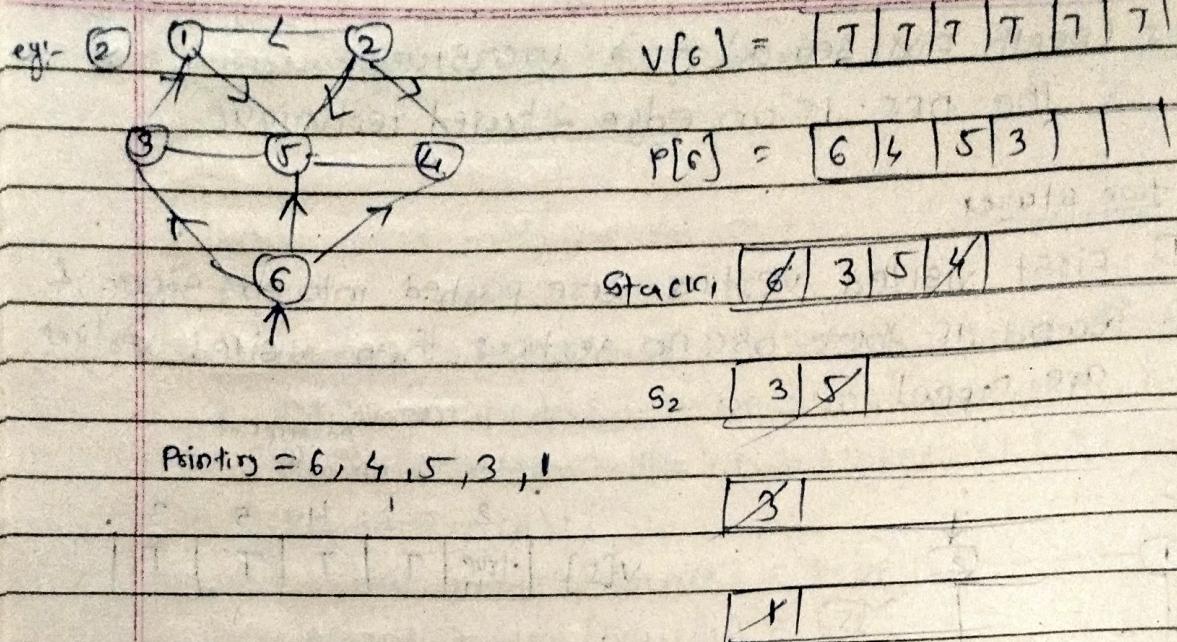
1	4
Stack <sub>3</sub>	

adjacent of 4 are 2, 3 → 2 is visited by 3 is no so add 3

1	3
Stack <sub>4</sub>	

see adjacent of 3 → all are visited

1	4
Stack <sub>5</sub>	



Pointing = 6, 4, 5, 3, 1

2 is not visited

because there is  
no path to find 2

So, 2 cannot be traversed here.

## # Implementation DFS

```
public void DFS(int source)
```

```
{
```

```
boolean visited_nodes[] = new boolean[adjacent.length]
```

```
int parent_nodes[] = new int[adjacent.length];
```

```
Stack<Integer> q = new Stack<>();
```

```
q.add(source);
```

```
visited_nodes[source] = true;
```

```
parent_nodes[source] = -1;
```

```
while (!q.isEmpty())
```

```
{
```

```
int p = q.pop();
```

```
System.out.print(p);
```

```
for (int i = adjacency[r])  
{  
    if (visited_nodes[i] == true)  
    {  
        visited_nodes[i] = false;  
        q.add(i);  
        parent_nodes[i] = r;  
    }  
}  
}  
}
```

```
public static void main (String [] args)  
{
```

```
    System.out ('Enter source. For DFS traversal')
```

```
    int source = sc.nextInt();
```

→ g.bFS (source);

→ g.dFS (source);

```
}
```

(last  
prob) m  
(sumes  
part)

## # Spanning Tree ( $n-1$ )edges

A Spanning tree is a subset of the graph (subgraph) that does not have cycle, and it also cannot be disconnected. (which has all vertices covered with minimum possible no of edges).

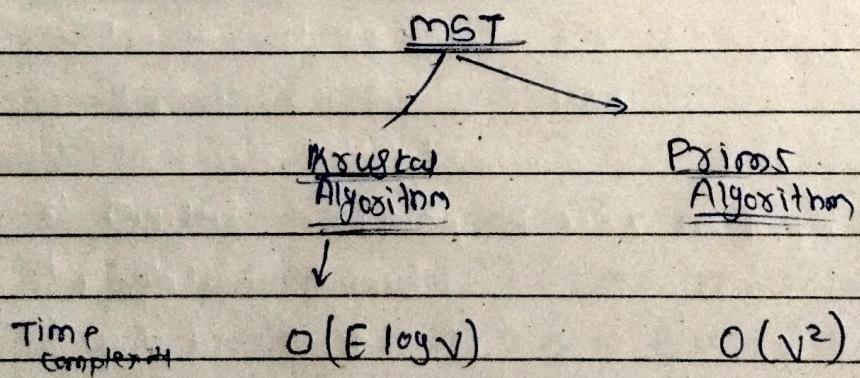
### Applications

A Spanning tree used to find minimum path to connect all nodes of graph

- ① Computer network routing
- ② Civil network planning
- ③ Cluster Analysis

## # minimum spanning Tree (MST)

The MST is the one whose cumulative edge weights have the smallest value!



\* Relaxation → used in Dijkstra's algorithm

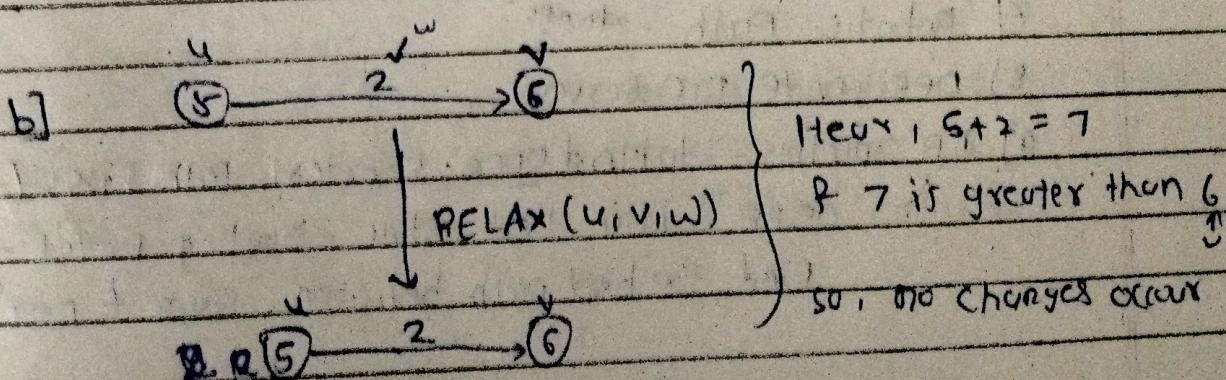
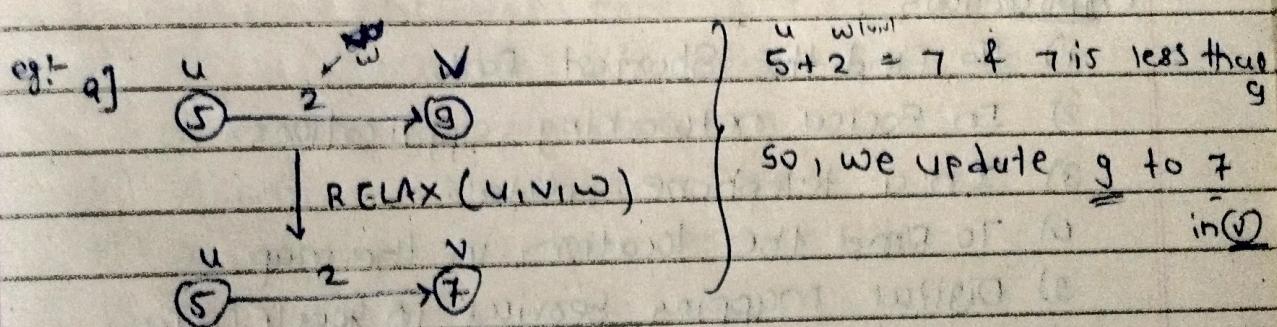
The single-source shortest path case based on a technique known as relaxation.

→ A method that repeatedly decreases an upperbound on actual shortest path weight of each vertex until the upper bound is equivalent to the shortest-path weight.

Code Algo

RELAX ( $u, v, w$ )

- 1) IF  $d[v] > d[u] + w(u,v)$
- 2). then  $d[v] \leftarrow d[u] + w(u,v)$
- 3).  $\pi[v] \leftarrow u$



## II Dijkstra's Algorithm $\rightarrow$ uses greedy approach

It is an algorithm for finding the shortest path between nodes in a weighted graph.

### Complexity

$$\text{Time Complexity} = O(E \log V)$$

$$\text{Space complexity} = O(V)$$

where

$E$  = no of edges,

$V$  = no of vertices

### Applications

- 1) To find the Shortest Path
- 2) In Social networking applications
- 3) In a telephone network
- 4) To find the location in the map.
- 5) Digital mapping services in google maps
- 6) Flighting Agenda
- 7) Robotic Path  $\rightarrow$  drones
- 8) Designate File Server
- 9) IP routing - to find shortest path first (OSPF)  
 $\hookrightarrow$  "OSPF" is a link state routing protocol  $\rightarrow$  used to find the best path between source + dest?

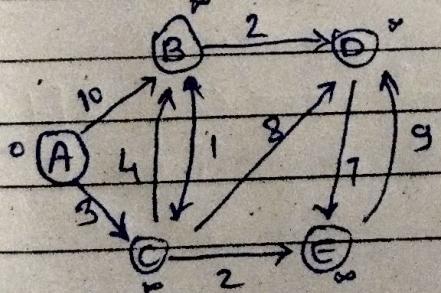
## \* Algorithm (Dijkstra's)

(Precond :-  $G = (V, \omega)$  is a weighted graph with initial vertex  $v_0$ )

(Post cond:-)

- 1) Initialize the distance field to 0 for  $v_0$  & to  $\infty$  for each of the other vertices.
- 2) Enqueue all the vertices into a priority queue  $\mathbb{Q}$  with highest priority being the lowest distance field value.
- 3) Repeat Steps 4-10 until  $\mathbb{Q}$  is empty
- 4] Deque the highest priority vertex into  $x$
- 5] Do Steps 7-10 for each vertex  $y$  that is adjacent to  $x$  & in the priority queue.
- 6] Let  $s$  be the sum of  $x$ 's distance field plus the weight of the edge from  $x$  to  $y$ .
- 7] If  $s$  is less than  $y$ 's distance field, do steps 8-9.  
otherwise go back to Step 3
- 8] Assign  $s$  to  $y$ 's distance field
- 9] Assign  $x$  to  $y$ 's back reference field.

e.g:-



→ Initialize - Single - sum  
 → relax()  
 → Extract min( $\mathbb{Q}$ )

	A	B	C	D	E
Distn	0	$\infty$	$\infty$	$\infty$	$\infty$
	0	10	3	$\infty$	$\infty$
	0	7	3	11	5
Updated Value using Relaxation	0	7	3	11	5
10 $\rightarrow$ 7	0	7	3	11	5
	0	7	3	11	5

After small steps  
टी ये वे हैं  
देखते ही देखते

so, the shortest distn for

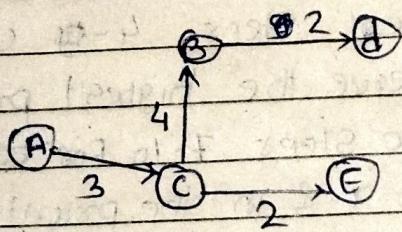
$$A = 0$$

$$B = 7$$

$$C = 3$$

$$D = 9$$

$$E = 5$$



## \* Leetcode #200 / Number of Islands

- Given an  $m \times n$  2D binary grid, which represent a map of 1's (land) & 0's (water), return the number of islands.

An island is surrounded by water & is formed by connecting adjacent lands horizontally or vertically.

You may assume all four edges of the grid are all surrounded by water.

Input -

	1's	1's	0	0	
0's	1	0	0	0	
0's	0	0	1	0	
0's	0	0	0	1	

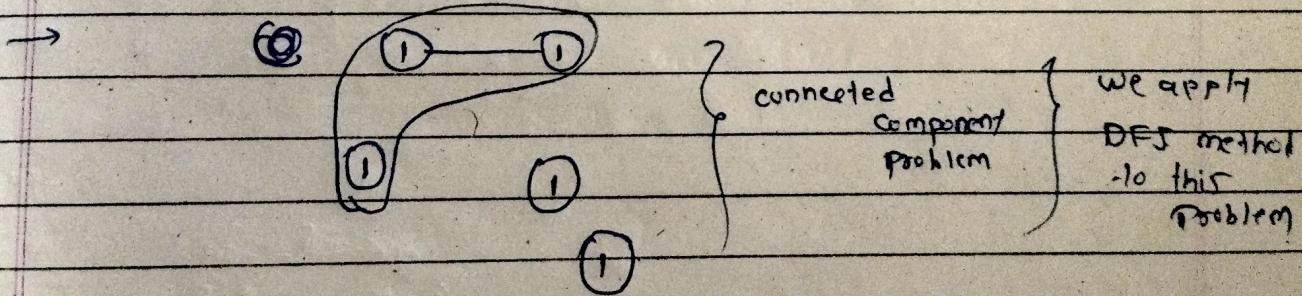
grid[][]

Land → 1  
Water → 0

Water & air  
are surrounded

Output = 3 → upper 3(1's) form 1 land &

other lower two lands ⇒ Total = 3 lands



Algorithm to find the no of Islands are given by DFS.

## # Floyd Warshall Algorithm

→ All Source Shortest Path Algorithm

The problem is to find the shortest distance between every pair of vertices in a given edge-weighted directed Graph.

→ Follow's dynamic programming approach.

a - b = 1	a - c = 1	a - d = 1	a - e = 1
b - c = 1	b - d = 1	b - e = 1	c - d = 1
c - d = 1	c - e = 1	d - e = 1	
d - e = 1			

Distance

b - a = 1	b - c = 1	b - d = 1	b - e = 1
c - a = 1	c - b = 1	c - d = 1	c - e = 1
d - a = 1	d - b = 1	d - c = 1	d - e = 1
e - a = 1	e - b = 1	e - c = 1	e - d = 1

Distance

c - a = 1	c - b = 1	c - d = 1	c - e = 1
d - a = 1	d - b = 1	d - c = 1	d - e = 1
e - a = 1	e - b = 1	e - c = 1	e - d = 1
a - b = 1	a - c = 1	a - d = 1	a - e = 1

Distance

d - a = 1	d - b = 1	d - c = 1	d - e = 1
e - a = 1	e - b = 1	e - c = 1	e - d = 1
a - b = 1	a - c = 1	a - d = 1	a - e = 1
b - c = 1	b - d = 1	b - e = 1	c - d = 1

Distance

e - a = 1	e - b = 1	e - c = 1	e - d = 1
a - b = 1	a - c = 1	a - d = 1	a - e = 1
b - c = 1	b - d = 1	b - e = 1	c - d = 1
c - d = 1	c - e = 1	d - e = 1	

Distance

a - b = 1	a - c = 1	a - d = 1	a - e = 1
b - c = 1	b - d = 1	b - e = 1	c - d = 1
c - d = 1	c - e = 1	d - e = 1	
d - e = 1			

Distance

b - a = 1	b - c = 1	b - d = 1	b - e = 1
c - a = 1	c - b = 1	c - d = 1	c - e = 1
d - a = 1	d - b = 1	d - c = 1	d - e = 1
e - a = 1	e - b = 1	e - c = 1	e - d = 1

Distance

c - a = 1	c - b = 1	c - d = 1	c - e = 1
d - a = 1	d - b = 1	d - c = 1	d - e = 1
e - a = 1	e - b = 1	e - c = 1	e - d = 1
a - b = 1	a - c = 1	a - d = 1	a - e = 1

Distance

d - a = 1	d - b = 1	d - c = 1	d - e = 1
e - a = 1	e - b = 1	e - c = 1	e - d = 1
a - b = 1	a - c = 1	a - d = 1	a - e = 1
b - c = 1	b - d = 1	b - e = 1	c - d = 1

Distance

DP : Recursive soln → memorization (DP) → Top-down approach  
Page No.: \_\_\_\_\_ Date: \_\_\_\_\_ (DP)

## # Dynamic Programming $\Rightarrow$ Recursion + Storage

Dynamic programming is a technique for solving a complex problem by first breaking it into a collection of simpler subproblems, solving each problem just once, & then storing their solutions to avoid repetitive computations.

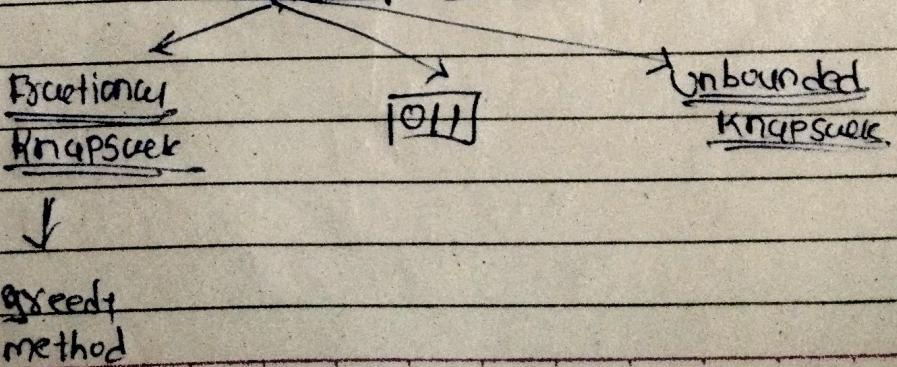
- ① It simply breaks the problems into sub-problems & saves the result for future purpose.
- ② Find the optimal solutions of these problems.
- ③ Stores the result of subproblem  $\rightarrow$  Memorization
- ④ Reuses them so that same sub-problem is calculated more than once.

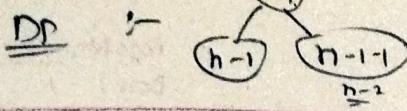
~~INFO~~

## # 0/1 Knapsack Problem

- 1] Subset sum
- 2) Equal sum partition
- 3) Count of Subset Sum
- 4) minimum Subset Sum Difference
- 5] Target Sum
- 6] no of Subsets of given difference.

### Knapsack Problem (Types)





## Fractional knapsack

## 0/1 knapsack

① using greedy Approach

① using Dynamic programming approach

② This problem either takes an item or not.

② This problem either takes an item or not.

② We can also take a fraction of item

② an item or not. If does not take part of it.

③ It has an optimal structure

③ It also has optimal structure.

eg:- we have 10 amount of Space. & The Amount A = 5, B = 4 & C = 3

First we put A & then B

So ~~we~~  $5+4=9$  so (AFB) so

only 1 space is remain &

C = 3. so what will D

↓

→ 0/1 knap

④ In this situation Fractional knapsack divide C & fill the space of 1 to 10

But the 0/1 knapsack dose not devide C. it add whole C or remain empty space (does not add C).

## # 0/1 Knapsack (DP) →

\* How to Identify

weight	$\rightarrow w[0] = 2$	$3, 4, 5, 6$	}
value	$\rightarrow v[ ] = 1, 4, 5, 7$		

O/P → max ratio

$$\text{Capacity} \rightarrow W = 7 \text{ kg}$$

For DP

Choice

optimization

max, min, largest, greatest etc.

## # 0/1 Knapsack Recursive code

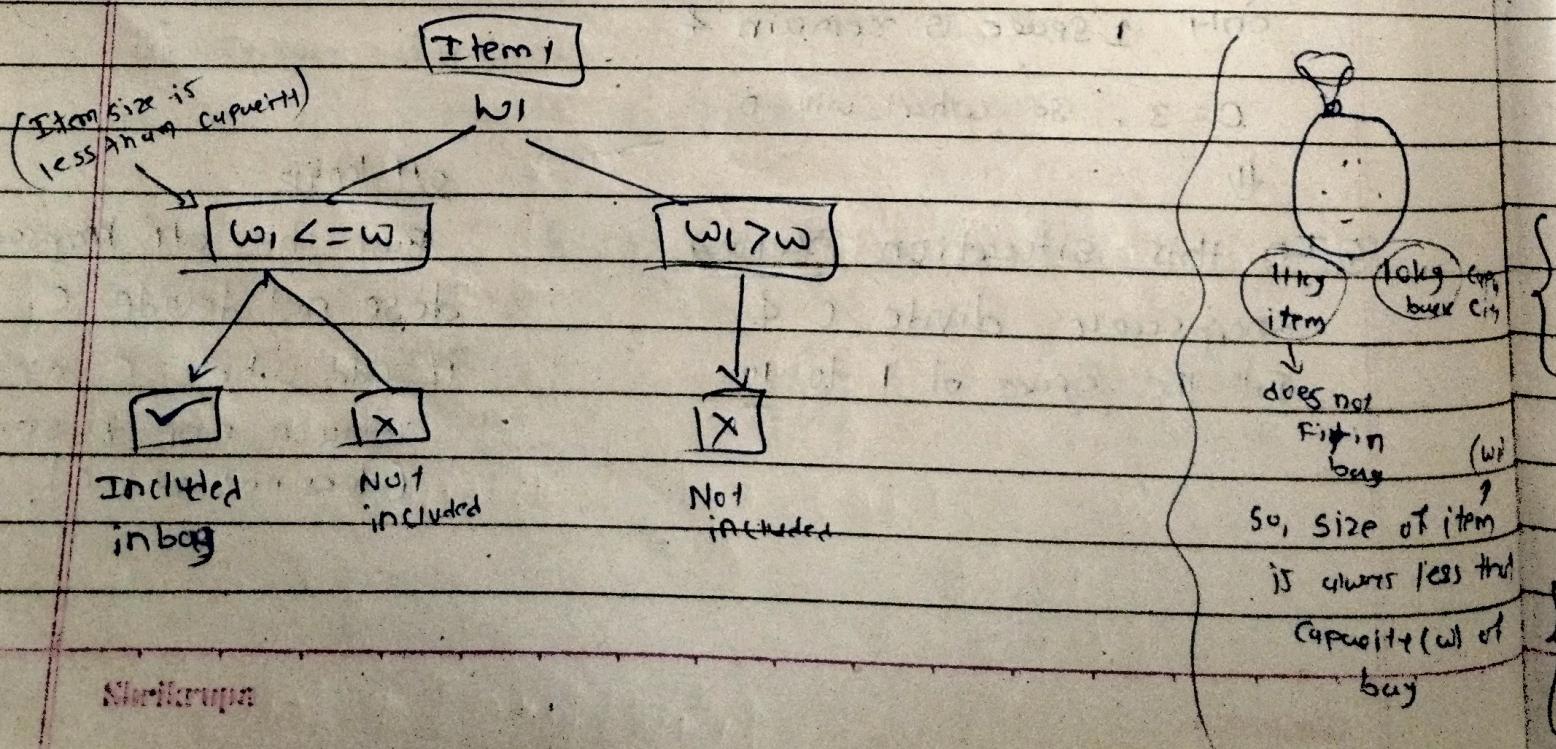
Recursive

we have to return

max profit

choice

choice diagram



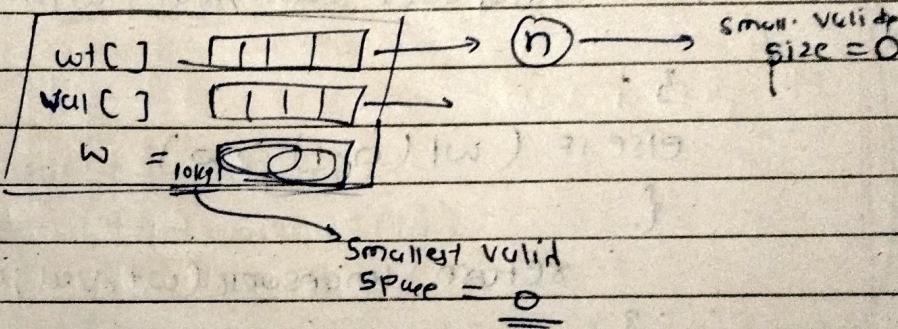
(a) Program Approach → soln

objn. ← int Knapsack (int wt[], int val[], int W, int n)  
 max profit  
 { I/P  
 Base Cond'n  
 choice diagram  
 } 3

\* Base Cond'n → important in recursive approach

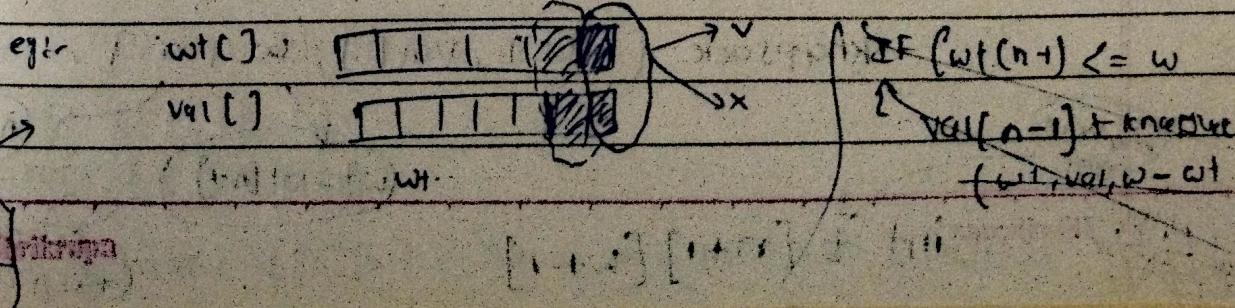
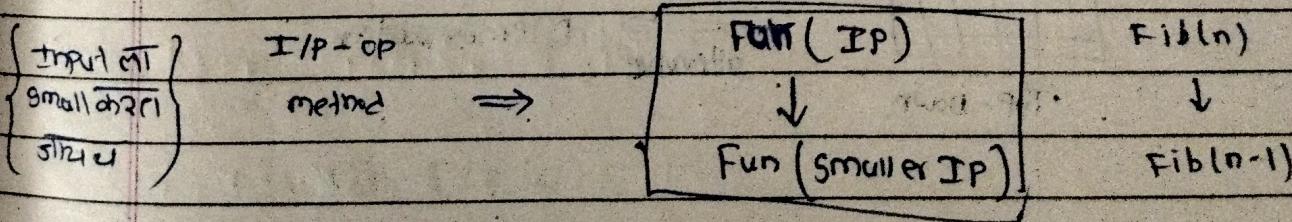
→ Think of the smallest valid I/P.

e.g:-



so; IF ( $n = 0 \text{ or } w = 0$ ) } base cond'n  
 { return 0 }

\* Recursive Fns



Code :-

```

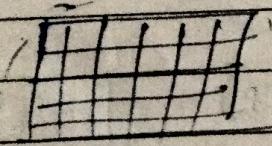
int knapsack (int wt[], int val[], int w, int n)
{
    if (n == 0 || w == 0) { // Base cond'n
        return 0;
    }

    if (wt[n-1] <= w)
        return max (val[n-1] + knapsack(wt, val,
                                         w-wt[n-1], n-1),
                    knapsack(wt, val, w, n-1));
    else if (wt[n-1] > w)
        return knapsack(wt, val, w, n-1);
}

```

# Memorization

Recursive code  
↓  
memorize



Top-Down

↓  
alternative

Memorization

Knapsack (wt[], val[], w, n)

wt - wt[n-1]

n-1

↓ change first  
(first 2 rows) matrix  
of size

int t[n+1][w+1]

matrix  
name

Srilakshmi

memset() → function in ~~top2D array~~

memset(arr, 0, size of arr);

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w+1

int t[n+1][w+1]	↑	1	-1	-1	1
memset(t, -1, size of (t))	↓	-1	-1	-1	1
	recursive form	-1	-1	-1	1
		3	-1	-1	1

$$t[3][2] = \text{recurForm}(2, 3)$$

दूसरी स्तर 3118 value  
3121 की रीटर्न  
को ही 3121 की 3118

(-1) 3121 की रीटर्न recursive  
form

### \* Code changes (DP) (memorization)

globally declare → int t[102][1002];  
memset(t, -1, size of (t))

int knapsack(int wt[], int val[], int w, int n)  
{  
 if (n == 0 || w == 0)  
 { return 0; }

→ if (t[n][w] != -1)  
{  
 return t[n][w]; }  
(value in stack)

if (wt[n-1] <= w)  
{  
 return t[n][w] = max(      sum as before  
 )  
}

else if (wt[n-1] > w)  
{  
 return t[n][w] = knapsack(wt, val, w, n-1);  
}

## # Time Complexity (knapsack), $O(n^2)$

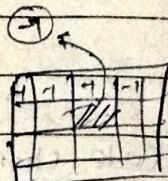
(Two iteration form)

memorization or Top Down =  $\underline{\underline{O(n^2)}}$

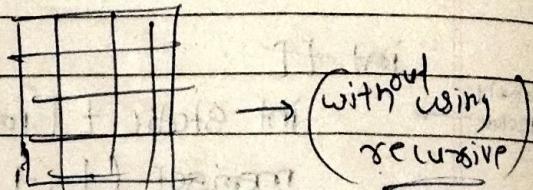
### \* Top-Down Approach ( $O(n)$ knapsack)

1) Recursive approach

2) Memorization  $\Rightarrow$  recursive +



3) Top-Down  $\Rightarrow$



$\rightarrow$  For changing recursive fun, (First we remove base condn)

$(\text{IF } (n == 0) \text{ || } (w == 0)) \Rightarrow$  recursive  
Base condn  $\xrightarrow[\text{into}]{\text{converted}}$  Top-Down  
return 0 Initialization

	$w$	$i$
$n$	$w=0 w=1 w=2$	$i=0 i=1 i=2 i=3 i=4$
$n=0$	1 1 1	1 1 1
$n=1$	1 1 1	1 1 1
$n=2$	1 1 1	1 1 1
$n=3$	1 1 1	1 1 1
$t[n][i]$	1 1 1	1 1 1

$\rightarrow$  (Initialization)

For ( $i=0; i<(n+1); i++$ )  
 {  
 For ( $int j=0; j<(w+1); j++$ )  
 {  
 IF ( $i==0 \text{ || } j==0$ )  
 $t[i][j] = 0;$   
 }
 }

$$\text{curr} \rightarrow \left\{ \begin{array}{l} \lfloor w - wt[n-1] \rfloor \Rightarrow \text{if } w = \text{wt}[n-1] \\ \text{else } \end{array} \right. \quad \left. \begin{array}{l} \text{reg 1: } \\ \text{Data: } \end{array} \right\}$$

\* Now, From choice diagram code of memorization, we have to remove recursion.

$$+ [n][w]$$

$$vai[n-1] + knapsack(wt, vai, w-wt[n-1], n-1)$$

$\downarrow$

$$vai[n-1] + \underline{+ [n-1][w - wt[n-1]]}$$

third part  $w$ , 3rd for  $n$   
change  $\downarrow$  here

so, IF ( $wt[n-1] \leq w$ )

$$+ [n][w] = \max \left( \begin{array}{l} vai[n-1] + + [n-1][w - wt[n-1]] \\ + [n-1][w] \end{array} \right)$$

else

$$+ [n][w] = + [n-1][w]$$

3.

$\downarrow$

Add this code with initialization

$\Downarrow$

we get code at Top-Down approach

Dynamic Programming

&

0/1 knapsack

\* Program → O/P knapsack (DP) → Top-Down

import java.util.\*;

Class TOP-DOWN {

    Static int knapsack( int wt[], int val[], int W, int n )  
    {

        int[] t = new int[W+1];

        For ( int i=1 ; i<(n+1) ; i++ )

        {

            For ( int j=1 ; j<=W ; j++ )

            {

                if ( wt[i-1] <= j )

                    t[i][j] =

                        max ( val[i-1] + t[i-1][j-wt[i-1]] ,  
                        t[i-1][j] )

            else

            {

                t[i][j] = t[i-1][j]

            }

        return t[i][j];

}

    Public static void main( String[] args )

    {

        int profit[] = { 60, 100, 120 };

        int weight[] = { 10, 20, 30 };

        int N = 50;

        int n = profit.length;

        Sout( knapsack( weight, profit, N, n ) );

        Sout( knapsack( weight, profit, W, n ) );

Fratik Bagade (20112) SLR To be continued...  
Date: \_\_\_\_\_ 

\* Subset Sum Problem