

# PRC Data Challenge

## Method and Results of Team “Likable Jelly”



Richard Alligier, David Gianazza

Ecole Nationale de l'Aviation Civile

# PRC Data Challenge

## Team “Likable Jelly”:

- Richard Alligier, assistant professor at ENAC
- David Gianazza, associate professor at ENAC

## PRC data challenge

Develop an open Machine Learning model to predict Aircraft Take-Off Weight (TOW) based on flight and trajectory data.

Provided Files:

- `challenge_set.csv` and `final_submission_set.csv`
  - flight identification: callsign
  - origin/destination: DEParture (ADEP), and DEStination (ADES)
  - timing: date of flight, actual off-block time, arrival time
  - aircraft: aircraft type code
  - airline: (obfuscated) Aircraft Operator code (airline)
  - operational values: flight duration, taxi-out time, flown distance
- OpenSky Network's ADS-B 2022-XX-XX.parquet files
  - timestamp, latitude, longitude, altitude, groundspeed, ROCD, T and wind

# Machine Learning Model: Our Solution

TOW = model (FlightInfo, WeatherAtAirports, Trajectory)

## model

- **LightGBM** library; an efficient gradient boosted trees library
- Hyper-parameters:
  - Number of boosting iterations (it i.e. number of trees): 50,000
  - Random search to select size of the trees and regularization parameters

## Input Variables

611 input variables extracted from different sources

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FlightInfo: `challenge_set.csv` and `final_submission_set.csv`

- Basic variables from `.csv` files but we did not use the callsign.
- Added variables:
  - Local time of departure/arrival computed from UTC time
  - Great circle distance, latitude/longitude from [\[ourairports.com\]](https://ourairports.com)

WeatherAtAirport: METARs from  
[\[https://mesonet.agron.iastate.edu/ASOS/\]](https://mesonet.agron.iastate.edu/ASOS/)

- Temperature and wind at departure and arrival airport
- Thunderstorms and fog at the arrival airport

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Trajectory: OpenSky Network's ADS-B 2022-XX-XX.parquet files

- 1 ADS-B Trajectory Filtering & Smoothing
- 2 Features Engineering:

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2 Features Engineering:

- Wind along trajectory:

Average value of the wind projected onto the ground speed

$$\text{dot} \left( \vec{wind}, \vec{groundspeed} \right) / \|\vec{groundspeed}\|$$

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### ■ Climb phase:

$$\text{■ energyrate} = \frac{d\text{energy}}{dt}, \text{ with energy} = g_0 \text{Altitude} + \frac{1}{2} \text{TrueAirSpeed}^2$$

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■ Estimated mass using:  $(\text{Thrust} - \text{Drag}) V_a / \text{mass} = \text{energyrate}$

Thrust and Drag model from OpenAP [Sun et al., 2020]

Solving this equation  $\Rightarrow$  roots of a 2nd degree polynomial [Alligier et al., 2013]



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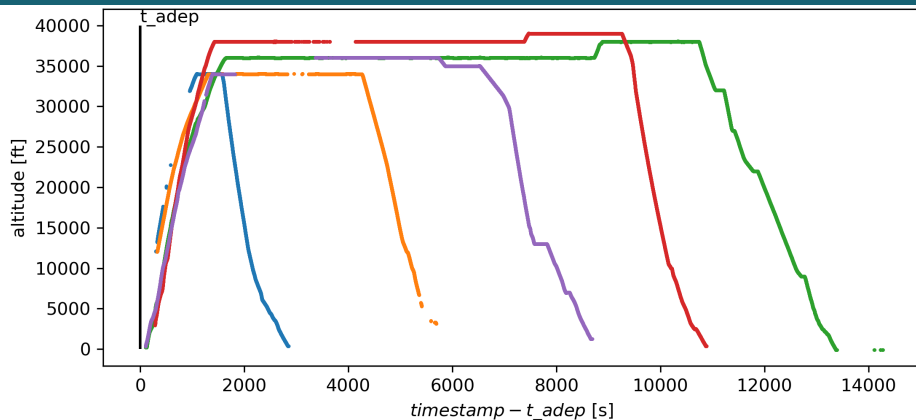
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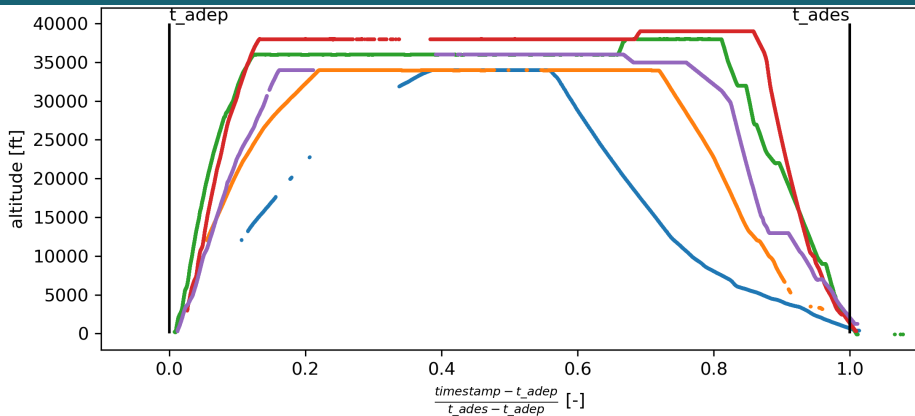
Solving this equation  $\Rightarrow$  roots of a 2nd degree polynomial [Alligier et al., 2013]

### ■ Flight profile: Cruise altitude and speed

# Trajectory Features: Flight Profile

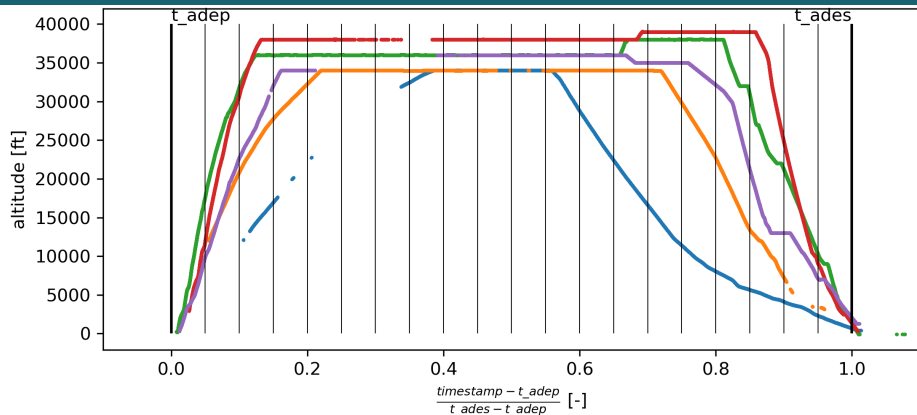


# Trajectory Features: Flight Profile



Flight duration  $t_{ades} - t_{adeq}$

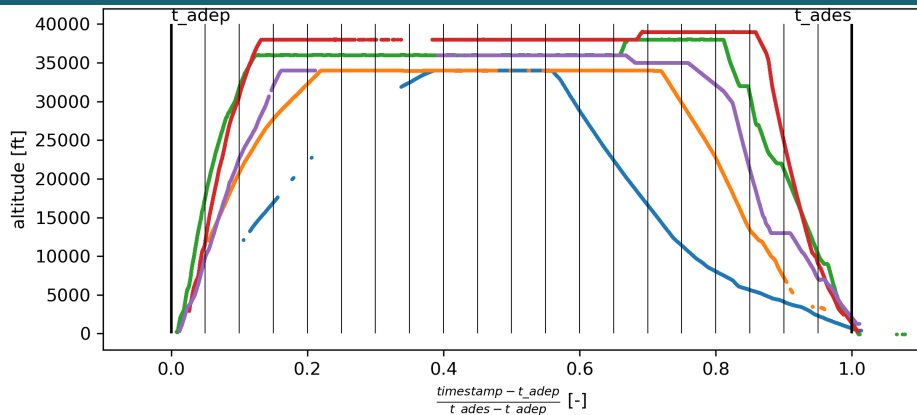
# Trajectory Features: Flight Profile



Flight duration  $t_{ades} - t_{adeP}$ , and 20 scaled temporal slices along the trajectory, starting from [0,5%] to [95%,100%]

- Cardinal (slice)
- $\text{median}_{i \in \text{slice}} \text{altitude}_i$
- $\text{median}_{i \in \text{slice}} \text{Mach}_i$
- $\text{altitude}_{\text{last}(\text{slice})} - \text{altitude}_{\text{first}(\text{slice})}$

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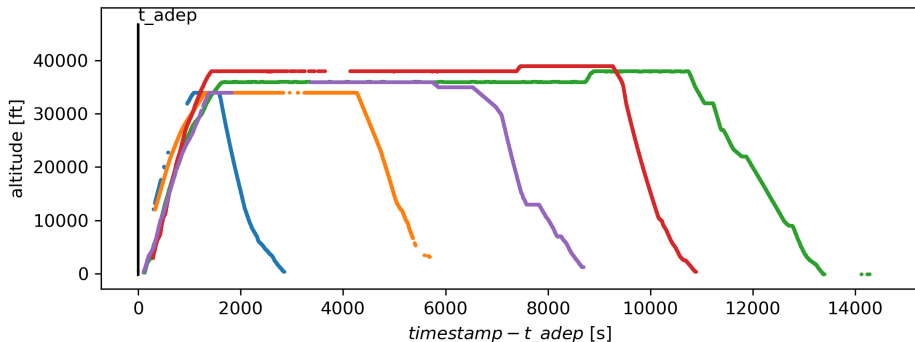


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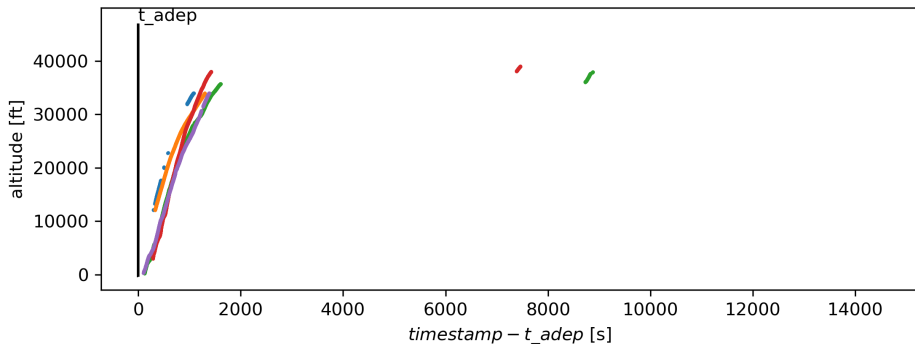
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This process generates  $1 + 4 \times 20$  features

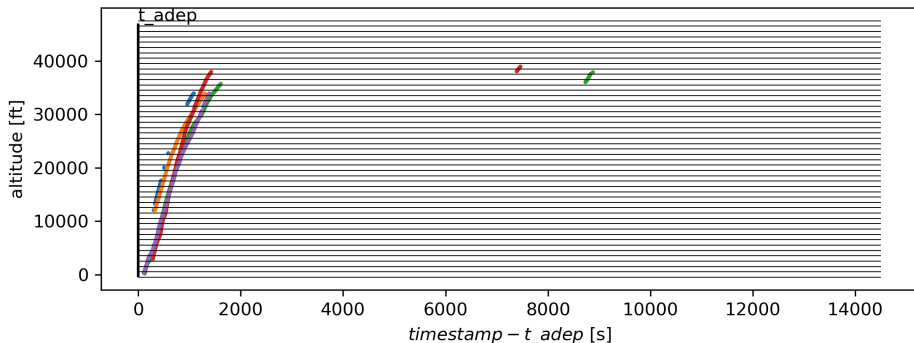
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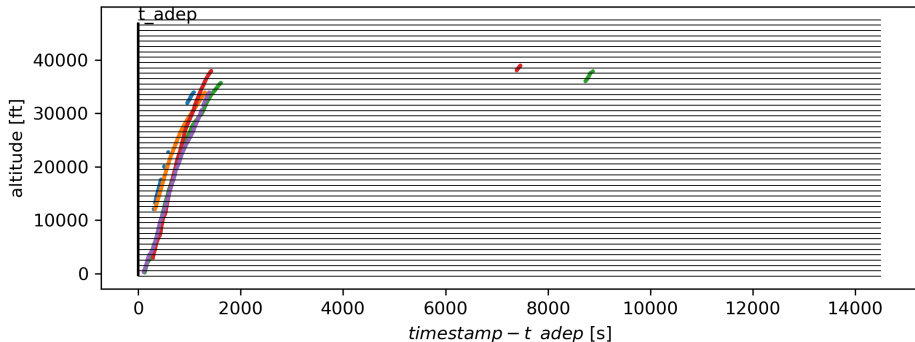


48 vertical slices starting from  $[-500\text{ft}, 500\text{ft}]$  to  $[46500\text{ft}, 47500\text{ft}]$

- Cardinal (slice)
- $\text{median}_{i \in \text{slice}} \Delta T_i$
- $\text{median}_{i \in \text{slice}} \text{TrueAirSpeed}_i$
- $\text{median}_{i \in \text{slice}} \text{ROCD}_i$
- $\max_j \text{ROCD}_j - \min_i \text{ROCD}_i$
- $\text{median}_{i \in \text{slice}} \text{mass}_i$
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- $\min_{i \in \text{slice}} \text{timestamp}_i - t_{adeq}$
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⇒ Generates  $11 \times 48$  features 7 / 11

# Results

Using all these 611 input variables, we have an RMSE of 1,611 kg

Improved results through averaging models different random seeds:

- 10 Models (RMSE: 1,564 kg)
- 20 Models (RMSE: 1,561 kg)

# Follow-up: Ablation Study of the Built Features

Which features do the heavy lifting ?

- Thunderstorm and fog variables ?
- Cruise variables ?
- General climb variables (ROCD,etc) ?
- Mass estimates ?
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TS & Fog	Cruise	Climb			RMSE [kg]
		Other	Mass	energy_rate	
X	X	X	X	X	3147
✓					3147
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				✓	1686
✓	✓	✓	✓	✓	1611

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# Conclusion

Predicting TOW with a good accuracy is possible

## What Worked ?

- Information extracted from climb phase (energy rate !)
- Filtering and smoothing (??) + many slices (??)

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## Features Not so Useful in our Solution ?

- Thunder and fog at arrival airport
- Cruise features

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- Thunder and fog at arrival airport
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## Perspective ?

- Is it possible to extract more info from cruise and descent phases ?
- A benchmark that will be used by researchers on future study ?!

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## Perspective ?

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Thanks to the organizers for this nice data challenge, it has been fun ! :-)

Thank you for your attention





[Alligier et al., 2013]

Ground-based estimation of aircraft mass, adaptive vs. least squares method.

[Sun et al., 2020]

Openap: An open-source aircraft performance model for air transportation studies and simulations.

# Trajectory features

## Climbing phase

48 vertical slices starting from [-500ft,500ft] to [46500ft,47500ft]

For each slice:

- Cardinal(slice) - number of points in the slice
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- $\text{median}_{i \in \text{slice}} \text{mass}_i$

# Trajectory features

## Flight profile

20 scaled temporal slices along the trajectory, starting from [0,5%] to [95%,100%]

For each slice:

- $t_{ades} - t_{adep}$  - the scaling factor and flight duration
- Cardinal(slice) - number of points in the slice
- $\text{median}_{i \in \text{slice}} \text{Mach}_i$
- $\text{median}_{i \in \text{slice}} \text{altitude}_i$
- $\text{altitude}_{last(slice)} - \text{altitude}_{first(slice)}$

# Machine Learning Model

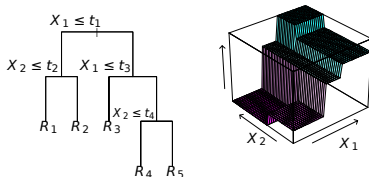
- Theoretical framework: stochastic gradient boosting

[1]

- Gradient-boosted regression trees:

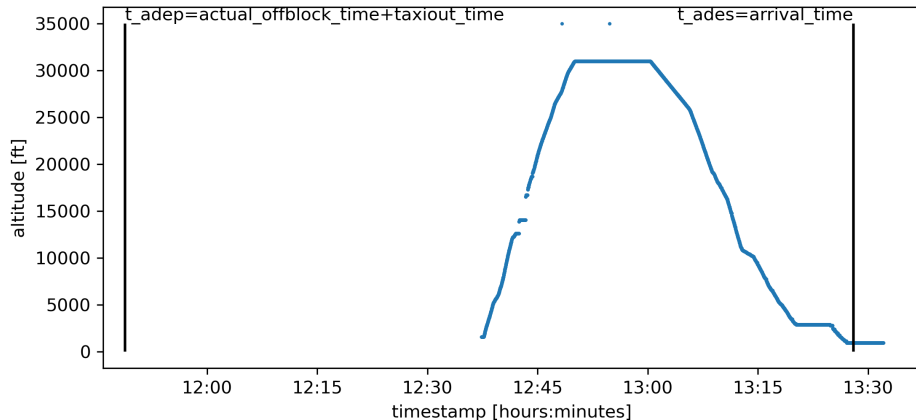
- Sum of weak prediction models  $h_m(x) = h_{m-1}(x) + \nu t_m(x)$
- with  $t_m(x) = \sum_{R_j \in T_m} \gamma_{mj} \mathbb{1}_{R_j}(x)$  a small tree

Elements of Statistical Learning (2nd Ed.) © Hastie, Tibshirani & Friedman 2009 Chap 9

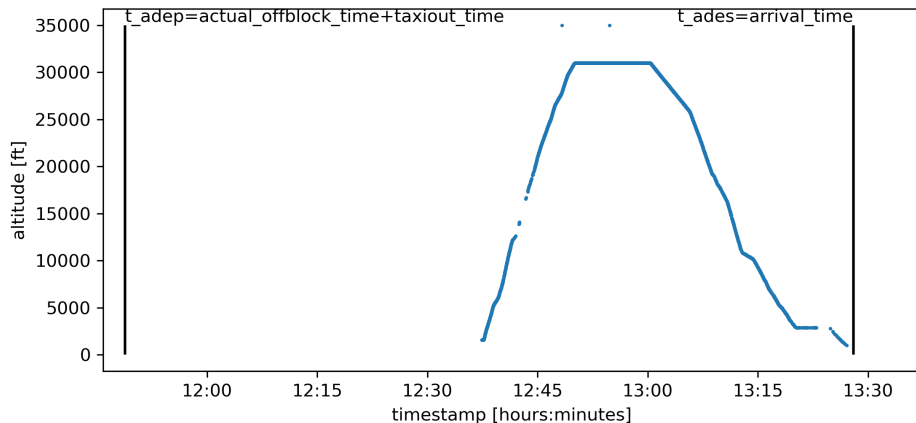


- Iterative training: small tree  $t_m(x)$  tuned on residuals of previous model  $h_{m-1}$ , with random sampling

# ADS-B Trajectory Filtering & Smoothing

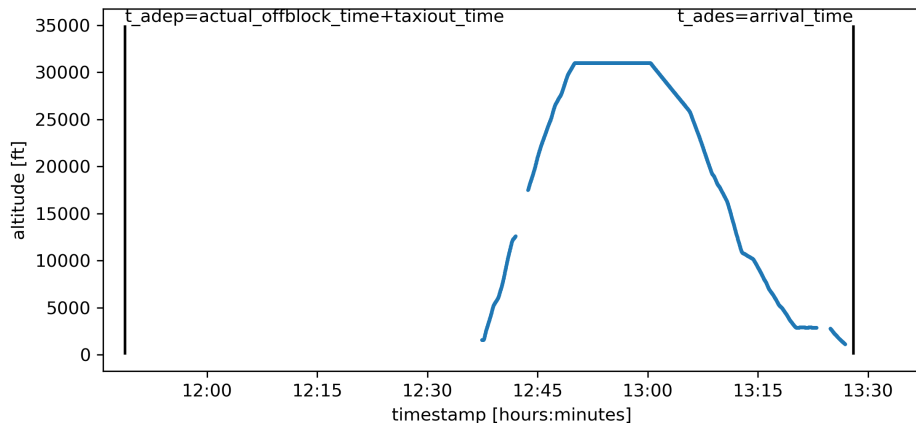


# ADS-B Trajectory Filtering & Smoothing



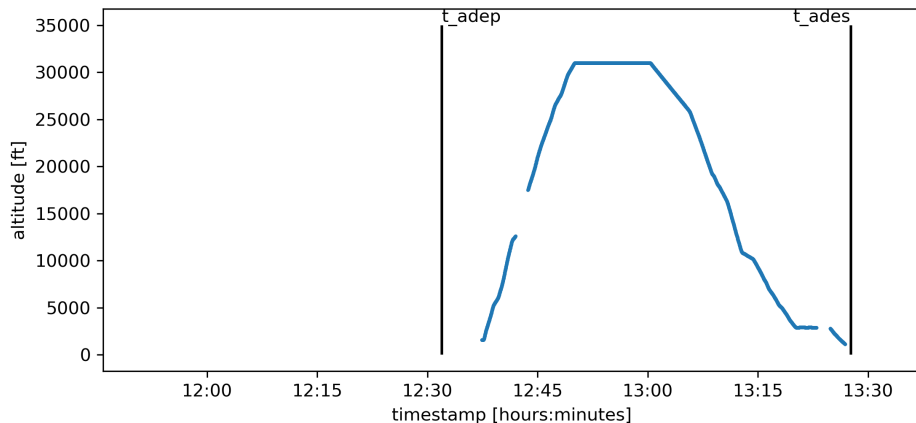
## 1 Filtering out repeated measurements

# ADS-B Trajectory Filtering & Smoothing



- 1 Filtering out repeated measurements
- 2 Filtering out measurements associated with a second order derivative above a threshold
- 3 Trajectories are smoothed using cubic splines ([csaps](#) library)

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- 1 Filtering out repeated measurements
- 2 Filtering out measurements associated with a second order derivative above a threshold
- 3 Trajectories are smoothed using cubic splines ([csaps](#) library)
- 4 Correct take-off/landing datetimes



## Follow-up: Ablation Study of the Built Features

Which features do the heavy lifting ?

- Thunderstorm and fog, No !
- Do cruise variables are that useful ? not that much
- Do mass estimates are that useful ? Yes, somewhat
- Do energy rate variables are that useful ? Yes !!

TS & Fog	Cruise	Climb			RMSE [kg]
		Other	Mass	energy_rate	
✓	✓	✓	✓	✓	1611
X					1606
	X				1610
			X		1609
				X	1721
X	X	X	X	X	3147
✓					3147
	✓				2489
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