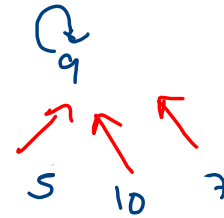
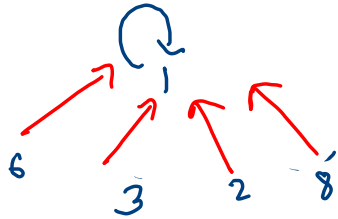


DSU \rightarrow disjoint set union

Parent

| | | | | | | | | | | |
|---|---|--------------|--------------|---|--------------|--------------|--------------|--------------|---|---------------|
| X | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |



relation

✓ 1 - 3

✓ 3 - 2

✓ 5 - 9

✓ 6 - 3

✓ 10 - 5

✓ 7 - 5

✓ 8 - 2

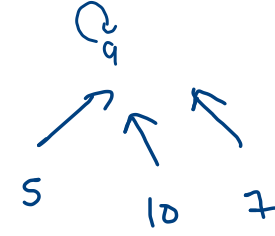
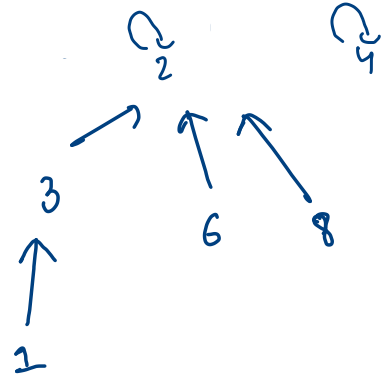
Parent

| | | | | | | | | | | |
|---|---------------------------|---|---------------------------|---|---------------------------|---------------------------|---------------------------|---------------------------|---|----------------------------|
| X | 2 ³ | 2 | 3 ² | 4 | 5 ⁹ | 6 ⁷ | 7 ⁹ | 8 ² | 9 | 10 ⁹ |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

```

find (int x) {
    if (par[x] == x) {
        return x;
    }
    return find(par[x]);
}

```



3 groups

relations

- ✓ 1 - 3
- ✓ 3 - 2
- ✓ 5 - 9
- ✓ 6 - 3
- ✓ 10 - 5
- ✓ 7 - 5
- ✓ 8 - 2

```

}
union (int x, int y) {

```

```

    dx = find(x);

```

```

    dy = find(y);

```

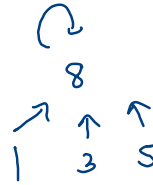
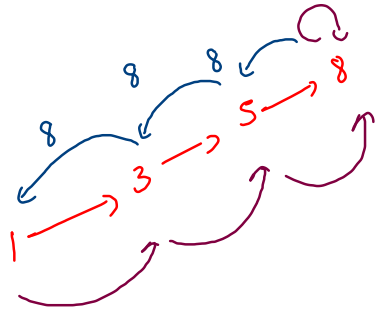
```

    if (dx != dy) {
        par[dx] = dy;
    }
}

```

}

DSU optimisation \rightarrow (i) path compression



parent

$1 \rightarrow 8$

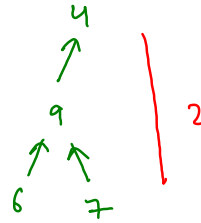
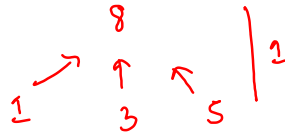
$3 \rightarrow 8$

$5 \rightarrow 8$

$8 \rightarrow 8$

find(1)

(ii) union by rank;

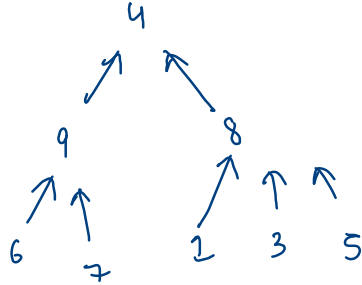


a) $par[8] = 4$

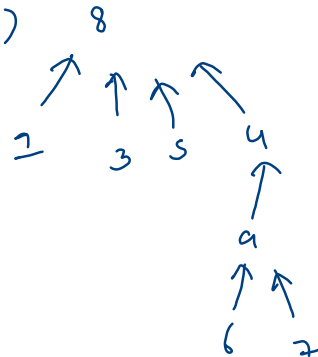
b) $par[4] = 8$

c) both same

a)



b)



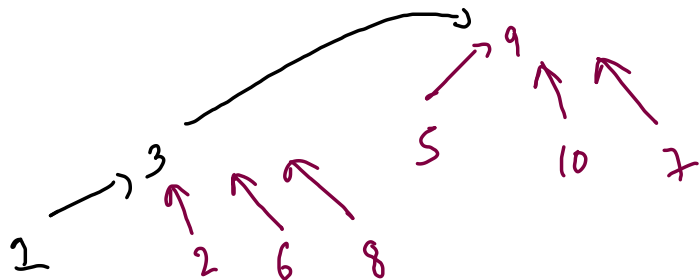
parent

| | | | | | | | | | | |
|---|---------------------------|---------------------------|---------------------------|---|---------------------------|---------------------------|---------------------------|---------------------------|---|----------------------------|
| X | 1 ³ | 2 ³ | 3 ⁹ | 4 | 5 ⁹ | 6 ³ | 7 ⁹ | 8 ³ | 4 | 10 ⁹ |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

rank

| | | | | | | | | | | |
|---|---|---|---------------------------|---|---|---|---|---|---------------------------|----|
| X | 0 | 0 | 0 ¹ | 0 | 0 | 0 | 0 | 0 | 0 ² | 0 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

4



$$x = 5 \quad ux = 9 \quad rx = 1$$

$$y = 2 \quad uy = 3 \quad ry = 1$$

$$1 - 3$$

$$3 - 2$$

$$5 - 9$$

$$6 - 3$$

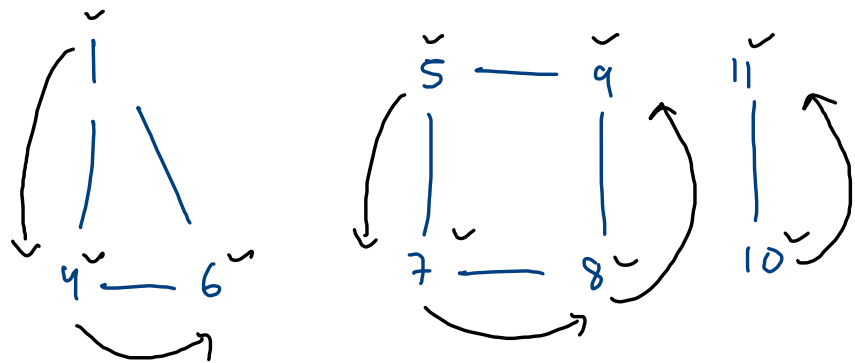
$$10 - 5$$

$$7 - 9$$

$$8 - 2$$

$$5 - 2$$

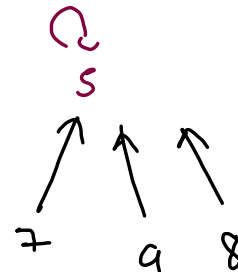
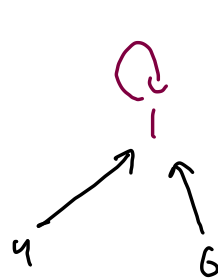
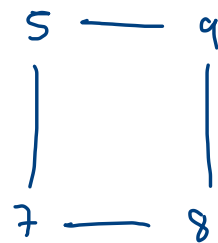
DFS



1 5 10

Count = 2 2 3

DSU



1 -> 4, 6

4 -> 1, 6

6 -> 1, 4

5 -> 7, 9

7 -> 5, 8

9 -> 5, 8

8 -> 7, 9

11 -> 10

10 -> 11

| | 0 | 1 | 2 | 3 | 4 | 5 |
|---|----|----|----|---------------------------|----------------------------|----------------------------|
| 0 | 0 | 1 | 2 | 3 ² | 4 | 5 ¹ |
| 1 | 6 | 7 | 8 | 9 ² | 10 ¹ | 11 ² |
| 2 | 12 | 13 | 14 | 15 | 16 | 17 ² |
| 3 | 18 | 19 | 20 | 21 | 22 | 23 |
| 4 | 24 | 25 | 26 | 27 | 28 | 29 |

$C = \text{cols}$

i, j

$\text{bno.} = i \times \text{cols} + j$

updates:

$(0,3)$ $(0,5)$ $(1,3)$ $(2,5)$ $(1,4)$ $(1,5)$

2

2

2

3

3

1

$C = \text{cols}$

~~2~~

~~3~~

~~2~~

~~3~~

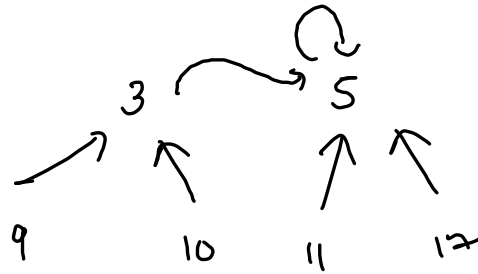
4

~~3~~

4

~~3~~

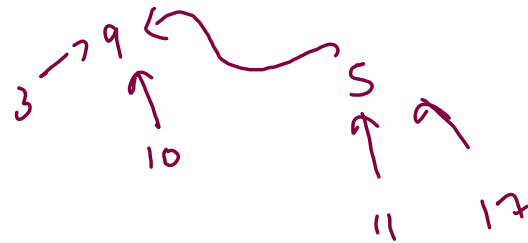
1



conn. comps

graph dynamic \rightarrow DSU

| | 0 | 1 | 2 | 3 | 4 | 5 |
|---|----|----|----|--------------|---------------|---------------|
| 0 | 0 | 0 | 0 | 1 | 0 | 2 |
| 1 | 6 | 7 | 8 | 9 | 10 | 11 |
| 2 | 12 | 13 | 14 | 15 | 16 | 17 |
| 3 | 18 | 19 | 20 | 21 | 22 | 23 |



1 2 2 3 3 3 1

(0,3) (0,5) (1,3) (2,5) (1,3) (1,4) (1,5)



count = 2
3
4
3
2
1

```

for(Point p : operators) {
    int px = p.x;
    int py = p.y;

    if(grid[px][py] == 1) {
        ans.add(count);
        continue;
    }

    grid[px][py] = 1;
    count++;

    //merge if required with nbr
    for(int[] d : dir) {
        int nx = px + d[0];
        int ny = py + d[1];

        if(nx >= 0 && nx < n && ny >= 0 && ny < m && grid[nx][ny] == 1) {
            int bnp = px*m + py; //box number parent
            int bnn = nx*m + ny; //box number number

            //union
            int lp = find(bnp);
            int ln = find(bnn);

            if(lp != ln) {
                //merging is required
                if(rank[lp] < rank[ln]) {
                    parent[lp] = ln;
                }
                else if(rank[lp] > rank[ln]) {
                    parent[ln] = lp;
                }
                else {
                    parent[lp] = ln;
                    rank[ln]++;
                }
                count--;
            }
        }
    }

    ans.add(count);
}

return ans;
  
```

| | 0 | 1 | 2 | 3 | 4 | 5 |
|---|----|----|----|----|----|----|
| 0 | 0 | 1 | 2 | 3 | 4 | 5 |
| 1 | 6 | 7 | 8 | 9 | 10 | 11 |
| 2 | 12 | 13 | 14 | 15 | 16 | 17 |
| 3 | 18 | 19 | 20 | 21 | 22 | 23 |



$C = 2, 2, 2$
 1
 2
 1

1 2 2 1 1

0, 3

0, 5

1, 3

0, 4

1, 4



```

for(Point p : operators) {
    int px = p.x;
    int py = p.y;

    if(grid[px][py] == 1) {
        ans.add(count);
        continue;
    }

    grid[px][py] = 1;

    count++;

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            int lp = find(bnp);
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                    parent[lp] = ln;
                }
                else if(rank[lp] > rank[ln]) {
                    parent[ln] = lp;
                }
                else {
                    parent[lp] = ln;
                    rank[ln]++;
                }
                count--;
            }
        }
    }

    ans.add(count);
}

return ans;
  
```