

$$U'(C_t) = C_t^{(-\phi_c)}$$

$$U'(C_{t+1}) = C_{t+1}^{(-\phi_c)}$$

$$U''(C_t) = (-\phi_c) C_t^{(-\phi_c)-1}$$

$$U''(C_{t+1}) = (-\phi_c) C_{t+1}^{(-\phi_c)-1}$$

$$g(\mu) = \mu_t^{\theta_2} \theta_1$$

$$g'(\mu) = \theta_2 \theta_1 \mu_t^{\theta_2-1}$$

$$h(Y) = Y_t^{1-\gamma}$$

$$h'(Y) = (1-\gamma) Y_t^{(-\gamma)}$$

$$d(X_t) = d_2 X_{t-1}^2 + X_{t-1} d_1 + d_0$$

$$d(X_{t+1}) = d_0 + d_2 X_t^2 + d_1 X_t$$

$$d'(X_T) = d_1 + X_{t-1} 2 d_2$$

$$Z_\tau = \frac{Z_t \frac{\theta_2}{\theta_2-1}}{\tau_t}$$

$$Z_Y = \frac{Z_t \frac{\theta_2 (1-\gamma)-1}{\theta_2-1}}{Y_t}$$

$$E_\tau = \frac{\frac{(-1)}{\theta_2-1} \mu_t Y_t^{1-\gamma}}{\tau_t}$$

$$E_y = (1-\gamma) Y_t^{(-\gamma)} - Y_t^{(-\gamma)} \mu_t \left(1 + \frac{(-\gamma)}{\theta_2-1} - \gamma \right)$$

$$R_\tau = (1-\gamma) \alpha + K_{t-1}^{(-1)} Y_t^{1-\gamma} (1-\gamma) (-\alpha) + K_{t-1}^{(-1)} Y_t^{1-\gamma} \mu_t \left(1 + \frac{1}{\theta_2-1} \right) - \mu_t^{\theta_2} K_{t-1}^{(-1)} Y_t \frac{\theta_2 \alpha \theta_1}{\theta_2-1} \tau_t^{(-1)}$$

$$R_Y = \alpha K_{t-1}^{(-1)} - K_{t-1}^{(-1)} Y_t^{(-\gamma)} \tau_t \alpha (1-\gamma)^2 + K_{t-1}^{(-1)} Y_t^{(-\gamma)} \mu_t \tau_t (1-\gamma) \alpha \left(1 - \gamma - \frac{\gamma}{\theta_2-1} \right) - \mu_t^{\theta_2} K_{t-1}^{(-1)} \alpha \theta_1 \left(1 - \frac{\theta_2 \gamma}{\theta_2-1} \right)$$

$$R_K(\tau_t, y_t, k_{t-1}) = Y_t (-\alpha) K_{t-1}^{(-2)} + K_{t-1}^{(-2)} Y_t^{1-\gamma} \tau_t (1-\gamma) \alpha - K_{t-1}^{(-2)} Y_t^{1-\gamma} \mu_t \tau_t (1-\gamma) \alpha + \mu_t^{\theta_2} K_{t-1}^{(-2)} Y_t \alpha \theta_1$$

$$R_K(\tau_{t+1}, y_{t+1}, k_t) = (-\alpha) Y_{t+1} K_t^{(-2)} + K_t^{(-2)} (1-\gamma) \alpha \tau_{t+1} Y_{t+1}^{1-\gamma} - K_t^{(-2)} Y_{t+1}^{1-\gamma} (1-\gamma) \alpha \tau_{t+1} \mu_{t+1} + K_t^{(-2)} \alpha \theta_1 Y_{t+1} \mu_{t+1}^{\theta_2}$$

$$\log(A_t) = \rho \log(A_{t-1}) + \epsilon_t \quad (1)$$

$$R_t = \frac{Y_t \alpha K_{t-1}^{\alpha-1}}{K_{t-1}^\alpha} (1 - \tau_t (1 - \mu_t) h'(Y) - g(\mu)) \quad (2)$$

$$\tau_t h(Y) = Y_t g'(\mu) \quad (3)$$

$$U'(C_t) = \beta U'(C_{t+1}) (R_{t+1} + 1 - \delta) \quad (4)$$

$$C_t = Y_t - K_t + K_{t-1} (1 - \delta) - Z_t \quad (5)$$

$$X_t = X_{t-1} \eta + (1 + \nu) E_t \quad (6)$$

$$Y_t = K_{t-1}^\alpha A_t (1 - d(X_t)) \quad (7)$$

$$E_t = (1 - \mu_t) h(Y) \quad (8)$$

$$Z_t = Y_t g(\mu) \quad (9)$$

$$U'(C_t) Z_\tau = Z_\tau \lambda_t U''(C_t) + \lambda_{t-1} (U''(C_t) (-Z_\tau) (1 + R_t - \delta) + U'(C_t) R_\tau) + \zeta_t (-E_\tau) \quad (10)$$

$$\beta \eta \zeta_{t+1} = \zeta_t + (d_1 + X_{t-1} 2 d_2) K_{t-1}^\alpha A_t \omega_t \quad (11)$$

$$\zeta_t E_y = \omega_t + U'(C_t) (1 - Z_Y) + (1 - Z_Y) \lambda_t (-U''(C_t)) + \lambda_{t-1} ((1 + R_t - \delta) U''(C_t) (1 - Z_Y) + U'(C_t) R_Y) \quad (12)$$

$$U'(C_t) = \beta U'(C_{t+1}) (1 - \delta) + \lambda_{t+1} \beta (1 - \delta) (-U''(C_{t+1})) + \lambda_t (U''(C_t) + (1 - \delta) \beta U''(C_{t+1}) (1 + R_{t+1} - \delta) + \beta U'(C_{t+1}) R_K(\tau_{t+1}, y_{t+1}, k_t))$$

$$+ \lambda_{t-1} (1 + R_t - \delta) (-U''(C_t)) - \alpha \beta \omega_{t+1} (1 - d(X_{t+1})) A_{t+1} K_t^{\alpha-1} \quad (13)$$