

ECG Amplifier and Heart Rate Measurement

Submitted By,
Mandeep Singh (MT2016513)
Prajwal Sharma K (MT2016519)

Submitted To,
Dr. Subajit Sen
Associate Professor,
IIIT, Bangalore

Table of Contents

Chapter No.	Name	Page No.
1	Introduction	1
1.1	Instrumentation Amplifier	1
1.2	ECG	1
2.1	LTspice Circuit Simulation and Results	2
2.2	Waveform of ECG	4
3	Observations and Calculations	5
4	Arduino Code for Digital Filter	6
5.1	Derivations	8
5.1.1	Fourier Transfrom of ECG Signal	8
5.1.2	Common Mode Gain	10

Chapter 1

1 Introduction

1.1 Instrumentation Amplifier

Instrumentation amplifiers are used in any measurement system using electrical transducers to enhance the signal level which is often at low level range. They are also required in certain cases to provide impedance matching and isolation. The characteristics of Instrumentation Amplifier is specified in terms of:

1. Input impedance
2. Output impedance
3. Gain and frequency response.
4. Noise.

1.2 ECG

Electrocardiography (ECG) is the process of recording the electrical activity of the heart over a period of time using electrodes placed on the skin. These electrodes detect the tiny electrical changes on the skin that arise from the heart muscle's electrophysiologic pattern of depolarizing during each heartbeat.

AC Analysis was done of the circuit and Bode Plot of the circuit after filtering and before filtering is shown in Fig.3.

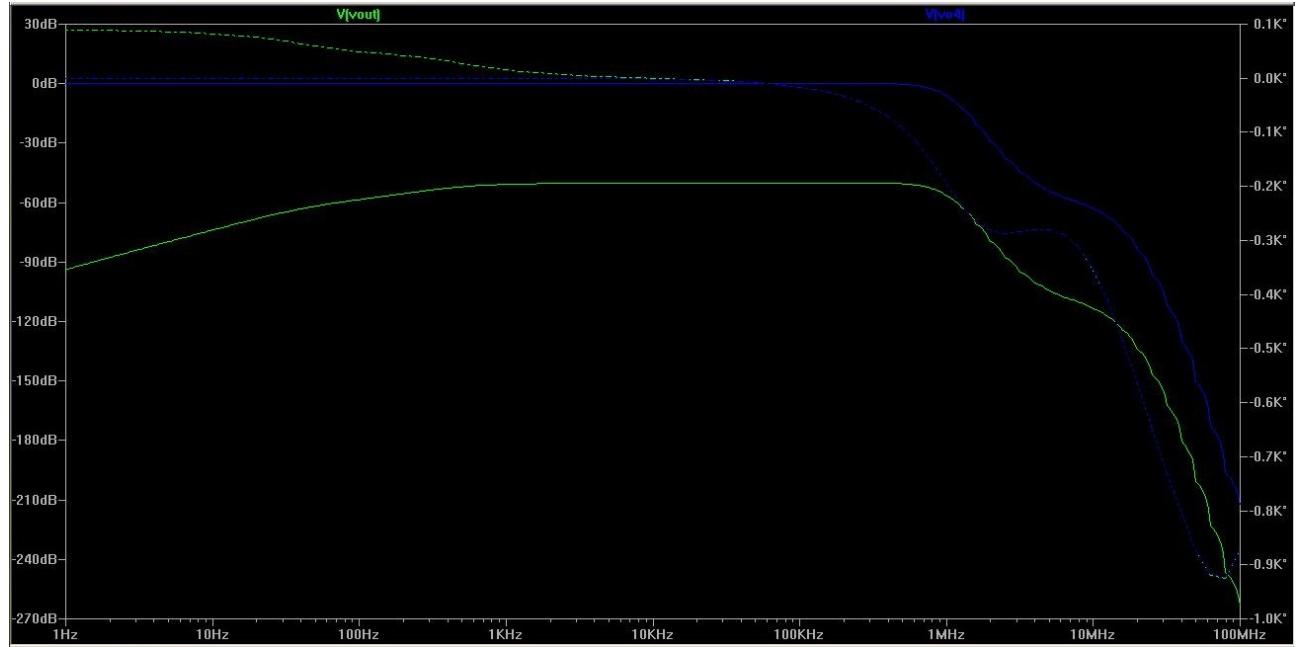


Fig.3: AC Analysis

Transient Analysis with Input Voltage as 1mV and Frequency 100Hz was carried out and the result is shown in Fig.4.

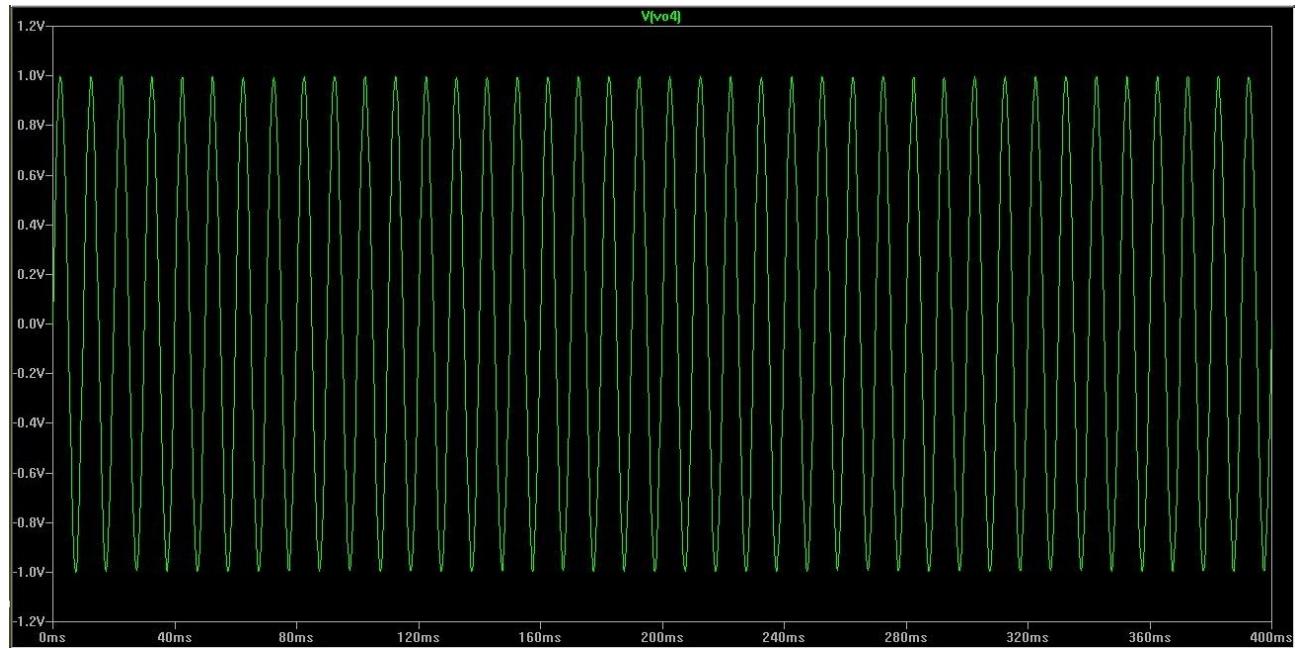


Fig.4: Transient Analysis

Input Impedance and Output Impedance is calculated using Transfer Function and the result is shown in Fig.5.

```
--- Transfer Function ---  
Transfer_function: 3.37071e-011      transfer  
v3#Input_impedance: 2.1e+010          impedance  
output_impedance_at_V(vout): 69.4447   impedance
```

Fig.5: Transfer Function

2.2 Waveform of ECG

ECG waveform is obtained on CRO without filtering by connecting spoons. Since, there was noise notch filter was built to eliminate noise of 50Hz. The output without filter is shown in Fig.6 and output after filtering is shown in Fig.7.

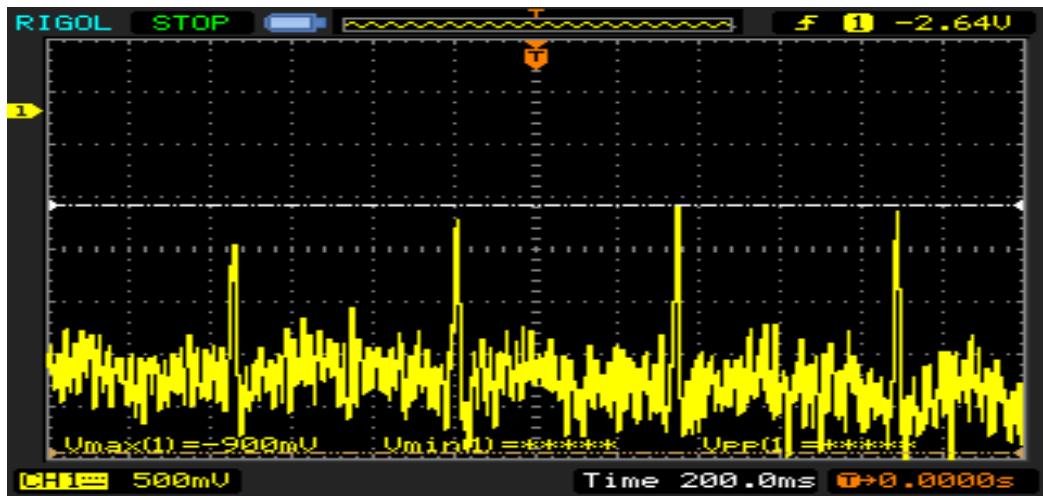


Fig.6: ECG Waveform without filter

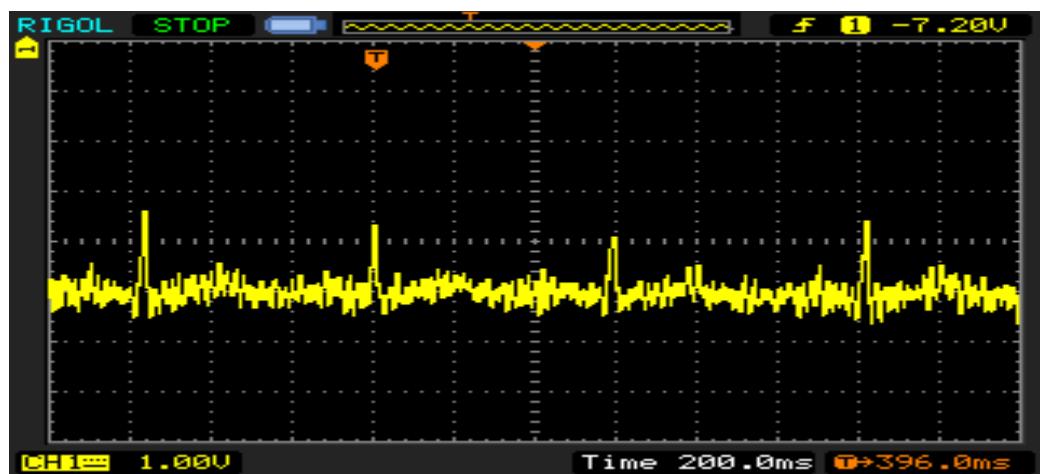


Fig.7: ECG Waveform after Filtering

Chapter 3

Observations and Calculations:

1. Offset Voltage:

1st Stage:

Voltage at pin1 = -7.3mV

Voltage at pin7 = -1.2mV

Offset at 1st stage = -6.1mV

2nd Stage:

Offset at 2nd Stage = 87mV

3rd Stage:

Offset at 3rd Stage = -850mV

2. Common Mode Gain:

Input Voltage = 0.716 Vrms

Output Voltage = 0.086 Vrms

Common Mode Gain = $0.086 / 0.716 = 0.12$

3. Differential Gain:

Input Voltage = 20mV

1st Stage = 170mV

2nd Stage = 2.18V

3rd Stage = 20.6Vp-p

Gain = 1030

Common Mode Rejection Ratio (CMRR) = $20 \log(1030 / 0.12) = 78.67\text{dB}$

Chapter 4

Arduino Code for Digital Filter

```
/*
Simple FIR filter implementation
*/
#define FILTERTAPS 5           // The number of taps in your filter, or better the number of coefficients

// declare array for values
float values[FILTERTAPS] = {0, 0, 0, 0, 0}; // to have a nice start up, fill the array with 0's
// NOTE: this could be 1 shorter, as we already have the input in a variable. This would save stack
size/memory

// declare input and output variables
float input = 1; // without a real input, looking at the step respons (input at unity, 1) would be nice to see
float output = 0; // output as a 0, but that doesn't really matter

// our counter, real life applications won't need this
byte n = 0;

void setup() {
    Serial.begin(115200); // open the serial port, I like them fast ;-
}

float fir(float in){
    static byte k;          // k stores a pointer to create a circular memory through the array. This
variable remains its value the next time we call the fir routine (hence 'static')
    byte i = 0;             // i is a counter to step through the filter coefficients and stored values
    float out = 0;           // out is the return variable. It is set to 0 every time we call the filter!

    values[k] = in;          // store the input of the routine (contents of the 'in' variable) in the array
at the current pointer position

    // declare variables for coefficients
    // these should be calculated by hand, or using a tool
    // in case a phase linear filter is required, the coefficients are symmetric
    // for time optimization it seems best to enter symmetric values like below
    float coef[FILTERTAPS] = { 0.021, 0.096, 0.146, 0.096, 0.021};

    //declare gain coefficient to scale the output back to normal
    float gain = 0.38; // set to 1 and input unity to see what this needs to be

    for (i=0; i<FILTERTAPS; i++) { // we step through the array
        out += coef[i] * values[(i + k) % FILTERTAPS]; // ... and add and multiply each value to
accumulate the output
        // (i + k) % FILTERTAPS creates a cyclic way of getting through the array
    }
    out /= gain; // We need to scale the output (unless the coefficients provide unity gain in
the passband)

    k = (k+1) % FILTERTAPS; // k is increased and wraps around the FILTERTAPS, so next time we
will overwrite the oldest saved sample in the array

    return out; // we send the output value back to whoever called the routine
}
```

```
void loop() {  
    // This is the loop that takes care of calling the FIR filter for some samples  
  
    for (n = 0; n < FILTERTAPS + 2; n++) {          // If you like to see the step response, take at least as  
    many cycles as the length of your FIR filter (FILTERTAPS + 1 or 2)  
        Serial.print("n= ");           // print the sample number  
        Serial.println(n, DEC);  
        Serial.println("Now calling fir...");  
        output = fir(input);         // here we call the fir routine with the input. The value 'fir' spits out is  
    stored in the output variable.  
        Serial.print("fir presented the following value= ");  
        Serial.println(output);      // just for debugging or to understand what it does, print the output  
    value  
    }  
    while (true) {};           // endless loop  
}
```

Chapter 5

5.1 Derivations:

5.1.1 Fourier Transform of ECG Signal

\rightarrow Fourier needs to find the bandwidth of $E(t)$:

$$n(t) = \begin{cases} A & 0 \leq t < 0.05T_H \\ -A & 0.05T_H \leq t < 0.1T_H \\ 0 & \text{otherwise} \end{cases}$$

$$C_n = \frac{1}{T_H} \int_0^{0.05T_H} \frac{A + t}{0.05T_H} e^{-j \frac{2\pi n t}{T_H}} dt + \frac{1}{T_H} \int_{0.05T_H}^{0.1T_H} \left(2A - \frac{A + t}{0.05T_H} \right) e^{-j \frac{2\pi n t}{T_H}} dt$$

(I) (II)

$$\stackrel{?}{=} \frac{1}{T_H} \int_0^{0.05T_H} \frac{A + t}{0.05T_H} e^{-j \frac{2\pi n t}{T_H}} dt$$

$$= \frac{20A}{T_H^2} \left[\int_0^{0.05T_H} + e^{-j \frac{2\pi n t}{T_H}} dt \right]$$

$$= \frac{20A}{T_H^2} \left[\frac{t e^{-j \frac{2\pi n t}{T_H}}}{-j \frac{2\pi n}{T_H}} - \frac{e^{-j \frac{2\pi n t}{T_H}}}{\left(\frac{2\pi n}{T_H} \right)^2} \Big|_0^{0.05T_H} \right]$$

$$= \frac{20A}{T_H^2} \left[\frac{0.05T_H e^{-j \frac{2\pi n}{20}}}{-j \frac{2\pi n}{T_H}} + \frac{e^{-j \frac{2\pi n}{20}}}{\left(\frac{2\pi n}{T_H} \right)^2} - \frac{1}{\left(\frac{2\pi n}{T_H} \right)^2} \right]$$

$$= 20 \left[\frac{j 0.05 e^{-j \frac{2\pi n}{20}}}{-j 2\pi n} + \frac{e^{-j \frac{2\pi n}{20}}}{\left(2\pi n \right)^2} - \frac{1}{\left(2\pi n \right)^2} \right]$$

$$= e^{-j \frac{2\pi n}{20}} \left[\frac{8A}{20\pi n} + \frac{20A}{\left(2\pi n \right)^2} \right] - \left[\frac{20A}{\left(2\pi n \right)^2} \right] -$$

$$\textcircled{I} \Rightarrow (2A - \frac{At}{0.05T_H})$$

$$\begin{aligned}
\textcircled{II} &\Rightarrow \frac{1}{T_H} \int_{0.05T_H}^{0.1T_H} \left(2A - \frac{At}{0.05T_H} \right) e^{-\frac{i2\pi nt}{T_H}} dt \\
&= \frac{1}{T_H} \left[\left(2A - \frac{At}{0.05T_H} \right) \frac{e^{-\frac{i2\pi nt}{T_H}}}{-\frac{i2\pi n}{T_H}} - \left(\frac{A}{0.05T_H} \right) \frac{e^{-\frac{i2\pi nt}{T_H}}}{\left(\frac{2\pi n}{T_H}\right)} \right] \\
&= \frac{1}{T_H} \left[\frac{-20A}{T_H} \frac{e^{-\frac{i2\pi n}{10}}}{\left(\frac{2\pi n}{T_H}\right)^2} - \left(\frac{A}{\frac{-i2\pi n}{20}} - \frac{20A}{T_H} \frac{e^{-\frac{i2\pi n}{10}}}{\left(\frac{2\pi n}{T_H}\right)^2} \right) \right] \\
&= \frac{-20A}{(2\pi n)^2} e^{-\frac{i2\pi n}{5}} - \frac{Ai}{20n} e^{-\frac{i2\pi n}{10}} + \frac{20A}{(2\pi n)^2} e^{-\frac{i2\pi n}{20}} \\
&= e^{-\frac{i2\pi n}{5}} \frac{20A}{(2\pi n)^2} + e^{-\frac{i2\pi n}{10}} \left(\frac{20A}{(2\pi n)^2} - \frac{Ai}{20n} \right) -
\end{aligned}$$

$$C_n = \textcircled{I} + \textcircled{II}$$

$$\begin{aligned}
&= \left[-\frac{20A}{(2\pi n)^2} + e^{-\frac{i2\pi n}{10}} \left[\frac{Ai}{20n} + \frac{20A}{(2\pi n)^2} - \frac{Ai}{20n} + \frac{20A}{(2\pi n)^2} \right. \right. \\
&\quad \left. \left. - e^{-\frac{i2\pi n}{5}} \frac{20A}{(2\pi n)^2} \right] \right]
\end{aligned}$$

$$C_n = -\frac{20A}{(2\pi n)^2} + e^{-\frac{i2\pi n}{10}} \frac{40A}{(2\pi n)^2} - e^{-\frac{i2\pi n}{5}} \frac{20A}{(2\pi n)^2}$$

Take $n=0$

$$\begin{aligned}
C_0 &= \frac{20A}{T_H^2} \int_0^{0.05T_H} dt + \frac{1}{T_H} \int_{0.05T_H}^{0.1T_H} \left(2A - \frac{At}{0.05T_H} \right) dt \\
&= A [0.025] + 0.1A - 0.075A
\end{aligned}$$

$C_0 = 0.05A$

— *

5.1.2 Common Mode Gain

COMMON MODE GAIN

$$R_{\text{in}} = R_{11} + \Delta R, \quad R_{21} = R_{22}, \quad R_{32} = R_{12}$$

Ist stage :-

$$\frac{V_{o1}}{V_{in}} = 1 + \frac{2R_{11}}{R_{12}}$$

$$\frac{V_{o2}}{V_{in}} = 1 + 2 \frac{(R_{11} + \Delta R)}{R_2}$$

$$\Rightarrow \frac{V_{o1} - V_{o2}}{V_{in}} = -\frac{2 \Delta R}{R_{12}} = \frac{\Delta V}{V_{in}}$$

IInd stage :-

$$\frac{V_{o3}}{\Delta V} = -\frac{R_{32}}{R_{21}}$$

IIIrd stage :-

$$\frac{V_{o4}}{V_{o3}} = -\frac{R_5}{R_4}$$

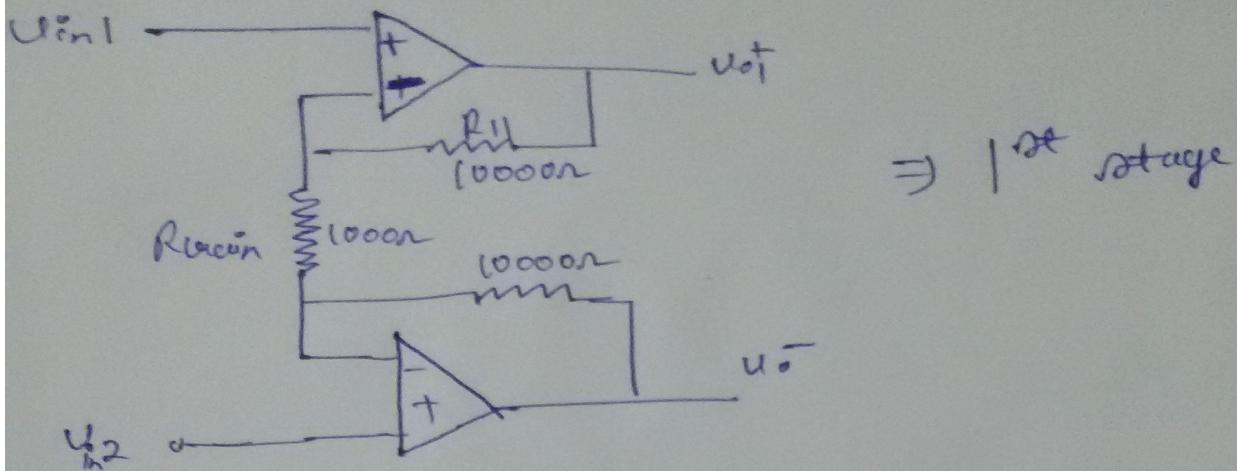
$$\text{Total common mode gain} = \frac{V_{o4}}{V_{in}} = -\left(\frac{2 \Delta R}{R_{in}}\right) \left(\frac{R_{32}}{R_{21}}\right) \left(\frac{R_5}{R_4}\right)$$

$$CMRR = \frac{A_{CM}}{A_{CM}}$$

$$CMRR = - \left(\frac{1 + \frac{2R_{11}}{R_{12}}}{\left(2 \frac{\Delta R}{R_{12}} \right)} \right) = - \left(\frac{R_{12} + 2R}{2 \Delta R} \right)$$

V_{in1} V_{in2} R_4

INSTRUMENTATION AMPLIFIER



$$\frac{V_{o1}}{U^+} = 1 + \frac{2R_{11}}{R_2}$$

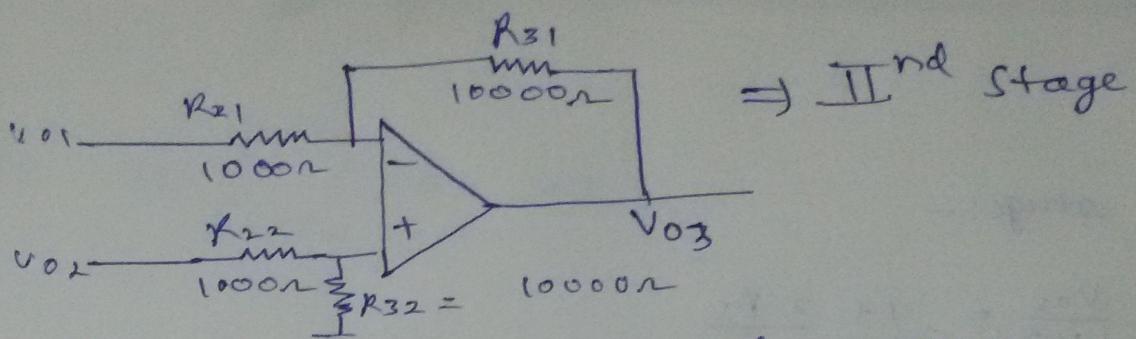
$$\frac{V_{o2}}{U^-} = 1 + \frac{2R_{\text{fb}}}{R_2}$$

$$\frac{V_{o1}}{U^+} = 1 + \frac{2R_{11}}{R_{12}} \Rightarrow V_{o1} = \left(1 + \frac{2R_{11}}{R_{12}}\right) U^+$$

$$\frac{V_{o2}}{U^-} = 1 + \frac{2R_{11}}{R_{12}} \Rightarrow V_{o2} = \left(1 + \frac{2R_{11}}{R_{12}}\right) U^-$$

$$\Rightarrow \frac{V_{o1}}{U_{in1}} = \frac{V_{o2} - V_{o1}}{U^+ - U^-} = 1 + \frac{2R_{11}}{R_{12}} = 1 + \frac{2(1000)}{1000}$$

Gain of 1st stage = 21

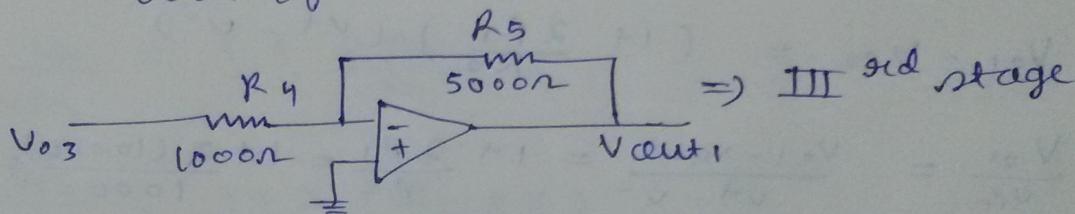


$$\Rightarrow R_{21} = 1000 \Omega, R_{22} = 1000 \Omega, R_{31} = 10000 \Omega$$

$$V_{03} = \left(-\frac{R_{32}}{R_{21}} \right) V_{01} + V_{02} \left(\frac{R_{32}}{R_{21}} \right)$$

$$2) \frac{V_{03}}{V_{01} - V_2} = -\frac{R_{32}}{R_{21}} = -\frac{10000}{1000} = -10$$

Gain of IInd stage = -10



$$\frac{V_{out}}{V_{03}} = -\frac{R_5}{R_4} = -\frac{5000}{1000} = -5$$

Gain of IIIrd stage = -5