# Assignment 5 sol

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```
df <- Cellphone
head(df)</pre>
```

##		Product_	id	Price	Sale	weight	resoloutio	n ppi	cpu.core	cpu.freq	internal.mem
##	1	2	203	2357	10	135.0	5.	2 424	8	1.35	16
##	2	8	380	1749	10	125.0	4.	233	2	1.30	4
##	3		40	1916	10	110.0	4.	7 312	4	1.20	8
##	4		99	1315	11	118.5	4.	233	2	1.30	4
##	5	8	380	1749	11	125.0	4.	233	2	1.30	4
##	6	9	947	2137	12	150.0	5.	5 401	4	2.30	16
##		ram Re	earC	Cam Fro	ont_Ca	m batt	ery thickne	SS			
##	1	3.000	13.	.00		8 2	310 7	. 4			
##	2	1.000	3.	15		0 1	700 9	. 9			
##	3	1.500	13.	.00		5 20	7 7	. 6			
##	4	0.512	3.	15		0 1	100 11	. 0			
##	5	1.000	3.	15		0 1	700 9	. 9			
##	6	2.000	16.	.00		8 2	500 9	. 5			

plot(df)

		1000		100		100		0.0		0 4		0 20	6 18		
	oduct_		Sp. A.	<b>\$</b>	<b>, , , , , , , , , , , , , , , , , , , </b>	)   	<b>≅</b> o					<b>9</b>	୍ଷ ବ୍ୟ		0
000		Price	<b>8 6</b>	<b>5</b> 00 d	<b>4</b> 500		6		<b>#</b> 0 4				<b>₽</b> %		
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0			<b>D Q</b>	<b>5</b> 0 ¢		<b>4</b>	, o		<b>9</b> 5 °	ram			<u>~</u> %d		
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0	0.80		<b>30</b> Q			ar Ba	°C		8	<b>4</b> 8		ont_Ca	<b>P</b>		
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9				<b>2</b> 0.0										nicknes	W
	0		0		2 12		0 6		0 120		0 20	2	2000		

### summary(df)

```
##
     Product_id
                        Price
                                        Sale
                                                        weight
   Min. : 10.0
                    Min.
                          : 614
                                   Min. : 10.0
                                                    Min. : 66.0
   1st Qu.: 237.0
                    1st Qu.:1734
                                   1st Qu.: 37.0
                                                    1st Qu.:134.1
   Median : 774.0
##
                    Median:2258
                                   Median : 106.0
                                                    Median :153.0
##
   Mean
         : 675.6
                    Mean
                           :2216
                                   Mean : 621.5
                                                    Mean :170.4
   3rd Qu.:1026.0
                    3rd Qu.:2744
                                   3rd Qu.: 382.0
                                                    3rd Qu.:170.0
##
   Max.
          :1339.0
                           :4361
                                         :9807.0
                                                           :753.0
                    Max.
                                   Max.
                                                    Max.
##
    resoloution
                                      cpu.core
                                                      cpu.freq
                        ppi
##
   Min. : 1.40
                   Min. :121.0
                                   Min. :0.000
                                                   Min. :0.000
   1st Qu.: 4.80
                                                   1st Qu.:1.200
                   1st Qu.:233.0
                                   1st Qu.:4.000
##
   Median: 5.15
                   Median :294.0
                                   Median :4.000
                                                   Median :1.400
##
   Mean : 5.21
                          :335.1
                                   Mean :4.857
                   Mean
                                                   Mean :1.503
   3rd Qu.: 5.50
##
                   3rd Qu.:428.0
                                   3rd Qu.:8.000
                                                   3rd Qu.:1.875
##
   Max.
          :12.20
                   Max.
                          :806.0
                                   Max.
                                         :8.000
                                                   Max.
                                                        :2.700
##
    internal.mem
                                      RearCam
                                                     Front Cam
                        ram
##
   Min. : 0.0
                   Min.
                          :0.000
                                   Min. : 0.00
                                                   Min. : 0.000
   1st Qu.: 8.0
                   1st Qu.:1.000
                                   1st Qu.: 5.00
                                                   1st Qu.: 0.000
##
   Median: 16.0
                   Median :2.000
                                   Median :12.00
                                                   Median : 5.000
##
   Mean : 24.5
                   Mean :2.205
                                   Mean :10.38
                                                   Mean : 4.503
##
   3rd Qu.: 32.0
                   3rd Qu.:3.000
                                   3rd Qu.:16.00
                                                   3rd Qu.: 8.000
##
   Max.
          :128.0
                   Max.
                          :6.000
                                   Max.
                                          :23.00
                                                   Max. :20.000
##
      battery
                    thickness
##
   Min. : 800
                  Min.
                         : 5.100
```

```
## 1st Qu.:2040
                  1st Qu.: 7.600
## Median :2800
                  Median: 8.400
## Mean
          :2842
                  Mean
                         : 8.922
   3rd Qu.:3240
                  3rd Qu.: 9.800
   Max.
           :9500
                  Max.
                         :18.500
library(ggplot2)
library(corrplot)
```

#### ## corrplot 0.95 loaded

cor\_matrix <- cor(df[, sapply(df, is.numeric)], use = "complete.obs")# Correlation matrix
cor\_matrix</pre>

```
##
                 Product_id
                                                        weight resoloution
                                Price
                                             Sale
## Product id
                1.000000000
                             0.1651358
                                      0.21854822
                                                   0.035868997 -0.01781743
## Price
                0.165135812
                            1.0000000 0.27326252 0.144555117 0.40400956
## Sale
                0.218548215
                            0.2732625 1.00000000 0.016114462 0.01715418
## weight
                            0.1445551 0.01611446
                                                  1.000000000 0.89041650
                0.035868997
## resoloution -0.017817433 0.4040096 0.01715418 0.890416497 1.00000000
## ppi
                0.207270573 0.8176145 0.23589646 -0.054682633 0.18129159
## cpu.core
               -0.008634003 \quad 0.6868106 \quad 0.06951745 \quad 0.216257283 \quad 0.47222591
## cpu.freq
                0.092427978  0.7273828  0.09913282  0.222729918  0.50545380
## internal.mem 0.261186427
                            0.7767378  0.48930802  0.098849256  0.20265951
## ram
                0.236194427
                            0.8969151 0.37312667 0.149283264 0.32721632
## RearCam
                0.172811675
                            0.7395376  0.29216432  -0.029448190
                                                               0.24989197
## Front_Cam
                0.071020207
                             0.6752864   0.43723322   -0.005970849
                                                               0.20272023
## battery
                0.031744856
                            0.5599457 0.12033837 0.833782666 0.84346176
## thickness
                0.039807160 -0.7167731 -0.04799095 -0.185262384 -0.53370786
##
                               cpu.core
                                          cpu.freq internal.mem
                       ppi
                                                                      ram
                0.20727057 -0.008634003 0.09242798
## Product_id
                                                     0.26118643
                                                                0.2361944
## Price
                0.81761445
                           0.686810645 0.72738283
                                                     0.77673777
                                                                0.8969151
## Sale
                0.23589646 0.069517451 0.09913282
                                                     0.48930802
                                                                0.3731267
## weight
               -0.05468263 0.216257283
                                        0.22272992
                                                     0.09884926
                                                                0.1492833
## resoloution
                0.18129159
                           0.472225906
                                        0.50545380
                                                     0.20265951
                                                                0.3272163
## ppi
                1.00000000 0.487990138 0.71316830
                                                     0.61855960 0.7487245
## cpu.core
                0.48799014 1.000000000
                                        0.49151900
                                                     0.27625082 0.4831275
## cpu.freq
                0.71316830 0.491518995
                                       1.00000000
                                                     0.44140011
                                                                0.6335475
## internal.mem 0.61855960 0.276250819 0.44140011
                                                     1.00000000 0.8753536
## ram
                0.74872447   0.483127510   0.63354749
                                                     0.87535357
                                                                1.0000000
## RearCam
                0.77400811 0.611352632 0.62510407
                                                     0.45191665
                                                                0.6480732
## Front_Cam
                0.49137066
                           0.586698382
                                        0.35831903
                                                     0.55573337
                                                                0.6474698
## battery
                           0.459728437 0.47313689
                0.30251667
                                                     0.46150566
                                                                0.5410011
## thickness
               -0.49679079 -0.697935474 -0.61445827
                                                    -0.36741160 -0.5210736
##
                   RearCam
                              Front_Cam
                                           battery
                                                     thickness
## Product_id
                0.17281168
                           0.071020207
                                        0.03174486
                                                    0.03980716
## Price
                0.73953757 \quad 0.675286410 \quad 0.55994569 \ -0.71677306
## Sale
                0.29216432 0.437233222
                                        0.12033837 -0.04799095
## weight
               -0.02944819 -0.005970849
                                        0.83378267 -0.18526238
## resoloution
                           0.202720227
                                        0.84346176 -0.53370786
                0.24989197
## ppi
                0.77400811 \quad 0.491370660 \quad 0.30251667 \ -0.49679079
## cpu.core
                ## cpu.freq
```

```
## internal.mem 0.45191665 0.555733370 0.46150566 -0.36741160

## ram 0.64807316 0.647469774 0.54100108 -0.52107357

## RearCam 1.00000000 0.596373692 0.28782142 -0.55099793

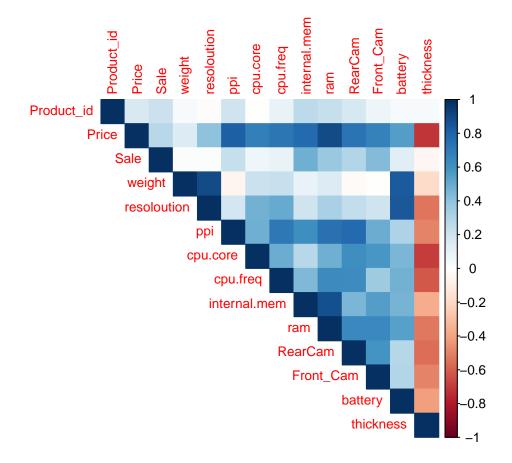
## Front_Cam 0.59637369 1.000000000 0.29528337 -0.49354169

## battery 0.28782142 0.295283372 1.00000000 -0.41268185

## thickness -0.55099793 -0.493541691 -0.41268185 1.00000000
```

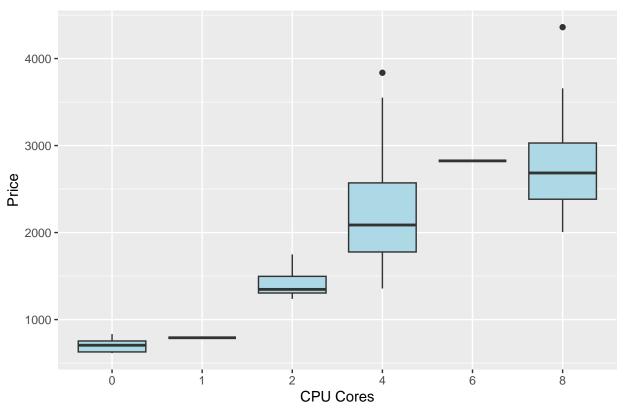
From the output we can see that, Columns like PPI , CPU core , Cpu.freq, internal.mem, ram,  ${\tt RearCam,Front\_Cam},$  thickness have high correleation with the  ${\tt Price}$ 

```
corrplot(cor_matrix, method = "color", type = "upper", tl.cex = 0.8)
```



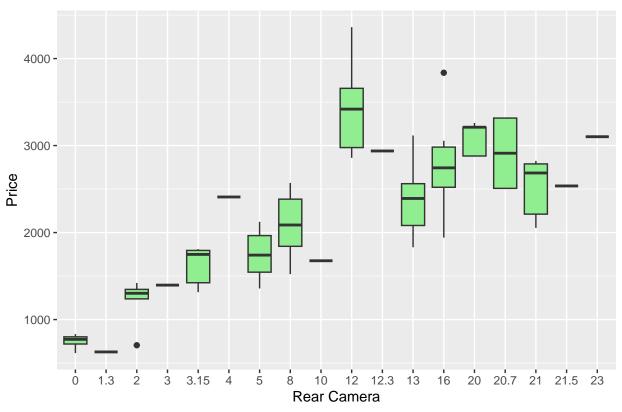
```
ggplot(df, aes(x = as.factor(cpu.core), y = Price)) +
  geom_boxplot(fill = "lightblue") +
  labs(title = "CPU Cores vs Price", x = "CPU Cores", y = "Price")
```

### **CPU Cores vs Price**



```
ggplot(df, aes(x = as.factor(RearCam), y = Price)) +
  geom_boxplot(fill = "lightgreen") +
  labs(title = "Rear Camera vs Price", x = "Rear Camera", y = "Price")
```

### Rear Camera vs Price



```
# Performing Best Subset selection
library(leaps)
df <- df[, !names(df) %in% "Product_id"]</pre>
best_model <- regsubsets(Price ~ ., data = df, nvmax = 12) # Total 13 cols , taking all cols
summary(best_model)
## Subset selection object
## Call: regsubsets.formula(Price ~ ., data = df, nvmax = 12)
## 12 Variables (and intercept)
##
                Forced in Forced out
## Sale
                    FALSE
                               FALSE
                    FALSE
                               FALSE
## weight
## resoloution
                    FALSE
                               FALSE
## ppi
                    FALSE
                               FALSE
                    FALSE
                               FALSE
## cpu.core
## cpu.freq
                    FALSE
                               FALSE
                               FALSE
## internal.mem
                    FALSE
## ram
                    FALSE
                               FALSE
## RearCam
                    FALSE
                               FALSE
## Front_Cam
                    FALSE
                               FALSE
## battery
                    FALSE
                               FALSE
## thickness
                    FALSE
                               FALSE
## 1 subsets of each size up to 12
## Selection Algorithm: exhaustive
             Sale weight resoloution ppi cpu.core cpu.freq internal.mem ram
## 1 (1) "" ""
                        11 11
```

```
11 11 11 11
                                                                 11 11
## 2 (1)
                                                                               11 4 11
                                         "*" " "
                                                                 11 11
                                                                               "*"
     (1)
                           11 11
                                        11 * 11 11 * 11
     (1)
                                                                 "*"
                                                       "*"
## 6
      ( 1
## 7
     (1)
                                                                 "*"
                                                                 "*"
      (1)
                                                       "*"
                                                                 "*"
                                                                               "*"
## 9
                           "*"
                                                                 "*"
## 10
       (1)
                                                       11 * 11
                                                                               11 * 11
      (1)"*"
                                                                 "*"
## 11
                                                       "*"
                                                                 "*"
                                        "*" "*"
                                                                               "*"
              RearCam Front_Cam battery thickness
              11 11
                       11 11
                                  11 11
## 1
     (1)
              11 11
                                          "*"
## 2 (1)
     (1)
                                          "*"
                                           "*"
## 4
      (1)
                       11 11
     (1)
              11 11
     (1)
## 6
## 7
     (1)
                                  11 * 11
                                           11 * 11
## 8 (1)
## 9 (1)
                       "*"
                                  "*"
## 10 (1)""
## 11 ( 1 ) "*"
                       "*"
                                           "*"
                       "*"
                                  "*"
                                           "*"
## 12 ( 1 ) "*"
```

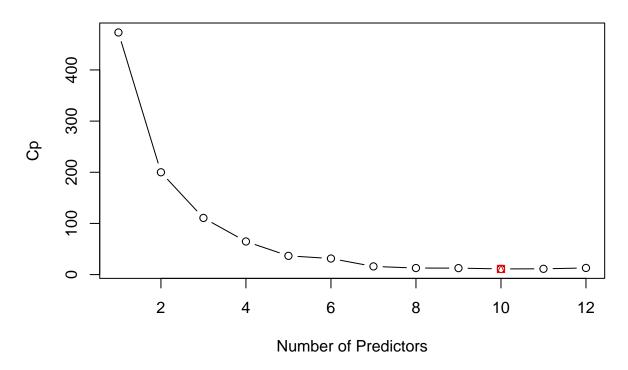
From the Above output we can say that if we only consider one column then best column is "ram" and if we have to select two best columns then we will take "ram" and "thickness". Similarly, it goes and according to our best no. of variables to select, we can select using this model summary.

```
which.min(summary(best model)$cp) # The model which contains the lowest cp variables
## [1] 10
coef(best_model, which.min(summary(best_model)$cp)) # The 10 selected variables coefficients
##
    (Intercept)
                         Sale
                               resoloution
                                                     ppi
                                                              cpu.core
                  -0.02074425 -96.01276129
## 1812.04486648
                                              1.13475997
                                                           57.06636066
##
       cpu.freq internal.mem
                                             Front Cam
                                                               battery
                                       ram
##
  143.83971623
                 5.93891924 98.77624751 10.60825400
                                                            0.11428398
      thickness
##
## -77.65115406
```

These above are coefficients of 10 best selected columns

```
plot(summary(best_model)$cp, type = "b", main = "Cp Plot", xlab = "Number of Predictors", ylab = "Cp")
points(10, summary(best_model)$cp[10], pch = 14, col = "red")
```

### **Cp Plot**

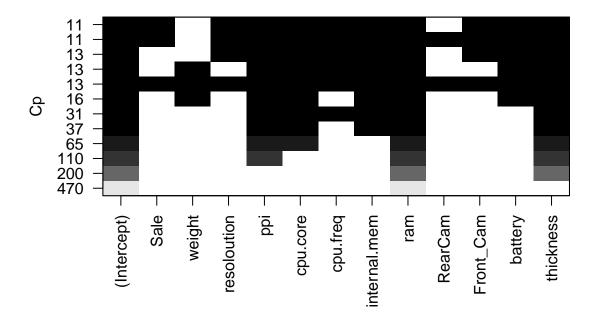


```
summary(best_model)$cp[10]
```

## [1] 11.10326

So, the value of Cp at number of predictors = 10 is 11.10326. So, we can clearly see that for no of predictors = 10 we get the lowest Cp

```
plot(best_model, scale = "Cp")
```



# So this graph show that when we include very few variables like ram then we are getting Cp of 470 and as we are including more variables like 10 important variables which is shown in the black on the top rows then we are getting the minimum Cp of 11 and even it will reduce when we will increase more no of variables and that can be case of overfitting.

#### library(pls)

```
## Warning: package 'pls' was built under R version 4.4.3

##
## Attaching package: 'pls'

## The following object is masked from 'package:corrplot':

##
## corrplot

## The following object is masked from 'package:stats':

##
## loadings

pcr_5 <- pcr(Price ~ ., data = df, scale = TRUE, validation = "CV", ncomp = 5)
pcr_7 <- pcr(Price ~ ., data = df, scale = TRUE, validation = "CV", ncomp = 7)

## Check variance explained by the first 5 and 7 components
explained_variance_5 <- summary(pcr_5)$explvar</pre>
```

```
X dimension: 161 12
## Data:
## Y dimension: 161 1
## Fit method: svdpc
## Number of components considered: 5
## VALIDATION: RMSEP
## Cross-validated using 10 random segments.
          (Intercept) 1 comps 2 comps 3 comps 4 comps 5 comps
## CV
                770.6
                         278.5
                                  236.3
                                           232.7
                                                    226.5
                                                             187.1
## adjCV
               770.6
                         278.1
                                  236.0
                                           232.5
                                                    226.1
                                                             186.5
## TRAINING: % variance explained
          1 comps 2 comps 3 comps
                                    4 comps 5 comps
## X
            48.24
                     67.71
                              78.61
                                       85.55
                                                90.02
## Price
           87.40
                     90.91
                              91.15
                                       91.92
                                                94.50
```

So, here with 5 components total variance that is explained is 94.50% which is not greater than 95% but good enough because more than 90% variance is explained by only 5 Principal components

```
explained_variance_7 <- summary(pcr_7)$explvar
```

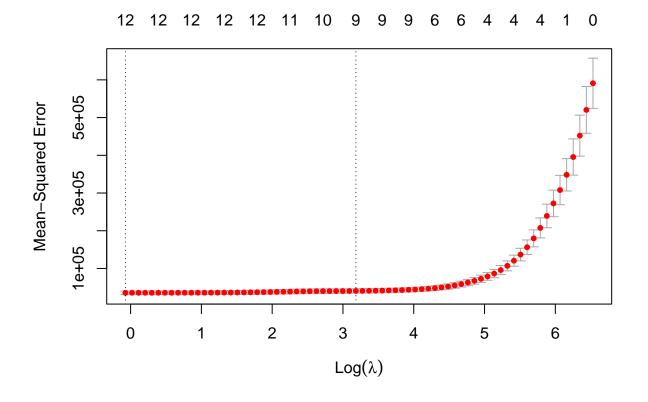
```
X dimension: 161 12
## Data:
## Y dimension: 161 1
## Fit method: svdpc
## Number of components considered: 7
## VALIDATION: RMSEP
## Cross-validated using 10 random segments.
          (Intercept) 1 comps 2 comps 3 comps 4 comps 5 comps 6 comps
                770.6
                         282.6
                                  246.4
                                                    243.8
                                                             189.4
## CV
                                           245.8
                                                                      189.6
                770.6
                         282.0
                                                                      188.8
## adjCV
                                  245.3
                                           244.7
                                                    242.4
                                                             188.5
##
         7 comps
## CV
            185.9
## adjCV
            185.2
## TRAINING: % variance explained
         1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps
## X
            48.24
                     67.71
                              78.61
                                       85.55
                                                90.02
                                                         93.40
                                                                  95.59
## Price
           87.40
                     90.91
                              91.15
                                       91.92
                                                94.50
                                                         94.52
                                                                  95.01
```

So, here with 7 components total variance that is explained is 95.01% which is greater than 95%. So, Good enough because more than 95% variance is explained by only 7 Principal components

```
## Loading required package: Matrix

## Loaded glmnet 4.1-8

X <- as.matrix(df[, !names(df) %in% "Price"]) # Predictors
y <- df$Price # Response variable
# Fit Lasso model with cross-validation to find best lambda
set.seed(3) # Ensure reproducibility
cv_lasso <- cv.glmnet(X, y, alpha = 1, standardize = TRUE, nfolds = 10)
plot(cv_lasso)</pre>
```



```
# Best lambda value
best_lambda <- cv_lasso$lambda.min
best_lambda</pre>
```

## [1] 0.9293484

Since we are getting high value of lambda, so we can say that stronger regularization, shrinking more coefficients to zero

```
lasso_model <- glmnet(X, y, alpha = 1, lambda = best_lambda, standardize = TRUE)</pre>
lasso_coef <- coef(lasso_model)</pre>
lasso_coef[lasso_coef != 0]
    [1] 1705.74933498
                        -0.02135994
                                       -0.45523499
                                                     -66.71562740
                                                                      1.02291850
## [6]
          54.11494752 125.48189555
                                        6.19528538
                                                      95.91893217
                                                                      4.68732450
## [11]
           8.58641496
                          0.12081951 -71.71894132
```

So We can clearly see from above that , there are some variables whose coefficients are very close to zero which means they are irrelevant columns . Like that 2nd coefficient etc.

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