



Modeling tools and techniques using R

Paul Esker Pennsylvania State University pde6@psu.edu or paul.esker@gmail.com

> Felipe Dalla Lana Ohio State University

dallalanadasilva.2@osu.edu or felipedallalana@gmail.com

Workshop format

- 8 am to 12 pm
- Mix of some lecture material with hands-on learning in R and Rstudio

►R: www.r-project.org ➤ Rstudio: <u>www.rstudio.com</u>

- Focus is on useful tools for modeling, including examining model assumptions and predictions
- · Examples draw on collaboration and consulting experiences (PDE) as such not all focus on Plant Path examples
- Assumption: some exposure to R and comfort with at least running code and working with different packages

Materials

- Webpage: https://rtools.netlify.com/
- · Github:

https://github.com/PSUPlantEpidemiology/APS2019.git

- Material that is available:
 - R scripts
 - · R markdown documents
 - · Output in word and pdf format for note-taking

Background to notes

- These slides draw on previous teaching experiences including:
 - ➤ Majority of examples (except dose-response additional example) focus on a regression framework assuming continuous-type variables
 - All explanatory variables continuous = regression
 All explanatory variables categorical = ANOVA type methods

 - Combination of continuous and categorical = ANCOVA type methods
 - >The combination of the Rmd output and notes should provide a more complete overview (I hope...)
 - >Two statistics courses geared to graduate students at the University of Costa Rica
 - > Week-long workshops on statistical modeling in epidemiology taught in Toluca, Mexico
 - Consulting across the following programs: plant pathology, agronomy, entomology, soils science, horticulture, biology, molecular biology, plant physiology, engineering, chemistry, and the social sciences

Available material

Background material:

- 1. Introduction (Rmd) to R (from McRoberts and Esker)
- 2. Correlations

Primary material:

- 1. R scripts for linear, multiple, and regression modeling tools.
- 2. Rmd files for same models
- 3. PDF outputs from the models.

Additional material:

1. Rmd files and outputs for examples: quadratic, nonlinear, nonparametric, and generalized linear models

More about ddditional examples and learning goals

- Polynomial regression: examine issues in collinearity in more detail and how to define centered variables
- Mosquito Dose-Response Final: generalized linear model (mixed) example that compares different model types and assumptions
- Nonlinear regression: introduction to defining nonlinear models and initial parameters
- Nonparametric regression: smoothing methods to look at nonlinear responses and the tradeoff with model complexity

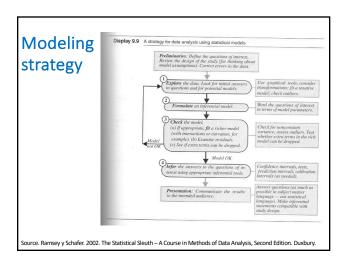
Modeling goals

The first step (of seven – note that we will touch on these others with our examples) Decide on the type of model that is needed in order to achieve the goals of the study. In general, there are five reasons one might want to build a regression model.

- For **predictive** reasons that is, the model will be used to predict the response variable
- from a chosen set of predictors.
 For **theoretical** reasons that is, the researcher wants to estimate a model based on a known theoretical relationship between the response and predictors.
 For **control** purposes — that is, the model will be used to control a response variable by
- manipulating the values of the predictor variables.
- For inferential reasons that is, the model will be used to explore the strength of the relationships between the response and the predictors.
- For **data summary** reasons that is, the model will be used merely as a way to summarize a large set of data by a single equation.
- https://newonlinecourses.science.psu.edu/stat501/node/332/

Modeling thoughts

ource. Gelman y Hall. 2007. Data Analysis Using Regression and Multilevel/Hierarchical Models. Cambridge



Starting from a regression framework

- \bullet We will use the following structure to explore tools in R:
 - Linear model: understand assumptions and tools for prediction
 - Expanding the model with multiple explanatory variables

 - - Generalized linear models to look at model assumptions for things like dose-response curves

Exponential family of distributions $\frac{y^{\varphi-1}}{\Gamma\left(\,\varphi\right)}\!\!\left(\!\frac{\varphi}{\mu}\!\right)^{\!\varphi} \exp\!\left(\!\frac{-\varphi\,y}{\mu}\right)$ $\frac{1}{\mu} exp\left(\frac{-y}{\mu}\right)$ $\frac{\Gamma\big(\,\varphi\big)}{\Gamma\big(\,\mu\varphi\big)\Gamma\big[\!\big(\,1\!-\!\mu\,\big)\varphi\big]}y^{\mu\varphi-1}\big(\,1\!-\!y\big)^{\!\!\big(\,1\!-\!\mu\,\big)\varphi-1}$ $\binom{n}{y}\!\!\left(\!\frac{\mu}{N}\!\right)^{\!\!y}\!\!\left(1\!-\!\frac{\mu}{N}\!\right)^{\!\!n-y}$ $\left(\!\frac{\mu}{1\!+\!\mu}\!\right)^{\!y}\!\left(\!\frac{1}{1\!+\!\mu}\!\right)$ Geometric (μ, φ y = 0, 1, 2, ...

Some basic syntax				
Syntax in R form	Interpretation			
Y~A	Linear regression that includes both the intercept and slope			
Y ~ -1 + A	Linear regression that does not include the intercept (= regression forced through intercept)			
Y~A+I(A^2)	Polynomial model [I() = identity function]			
Y ~ A + B	First order model for factors A and B, without interaction			
Y ~ A:B	First order model that only includes the interaction term			
Y~A*B	Full first order model Y~A+B+A:B			
Y ~ (A + B + C) ^2	Model that includes all first order effects plus the interactions through order "X" (= second order in this example): $Y \sim A+B+C+AB+AC+BC$			

Background

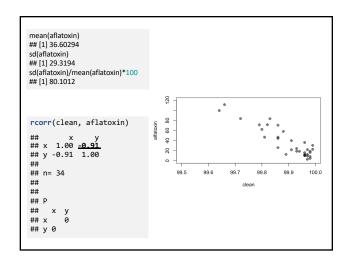
- · Our interest includes:
 - 1. Understanding the inherent relationships between different variables.
 - Developing methods for predictions based on estimating a dependent variable (risk model, forecast model, ...)
- Given that, we are interested in exploring these relationships based on quantitative variables
 - It should be obvious though that we can also incorporate qualitative factors and create conditional models (i.e., dependent on the factor of interest, *dummy variables*)

Starting point...

- We need to define the independent-dependent relationship
 - Dependent variable = response
 - Independent variable(s) = regressor(s), predictor(s), ...
- <u>Linearity assumption</u> = the rate of change (slope) does not change at different levels of *X*

R example 1.

- File name (R script): "Linear regression.R"
 - Data come from the analysis of aflatoxin in peanut
 - o Percentage clean grain
 - o Concentration of aflatoxin
- Objectives:
 - Quantify the relationship between the percentage clean grain and aflatoxin concentration
 - Determine if this model can be used for future predictions

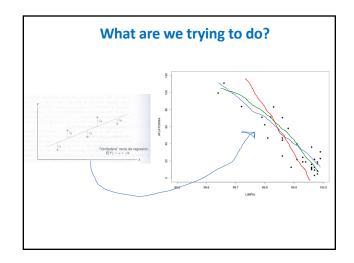


Model structure

$$Y = \beta_0 + \beta_1 X + \varepsilon$$
Response
$$\begin{array}{c} \text{Intercept = } \\ \text{intersection with} \\ \text{vertical axis} \end{array} \qquad \begin{array}{c} \text{Slope = rate of } \\ \text{change} \end{array} \qquad \begin{array}{c} \text{Random variable = error} \\ \text{or residual variance,} \\ \text{which includes a} \\ \text{combination of known} \\ \text{and unknown factors} \end{array}$$

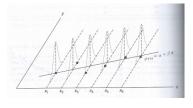
Independent variable as a function of the dependent variable:

- Dependent variable = random variable, since the residual variable is random
- Independent variable = not random, but it is measured with some minimal error



Model assumptions

- · Errores are distributed normally
- Mean error is 0
- Variance is the same for all errors



Modeling fitting method: least squares

- Most common method for the majority of statistical packages
- We can use likelihood based methods (generalized linear models) also
 - Dose-response example illustrates that philosophy
 - $\bullet\,$ Some of our automated methods also are based on this approach
- Objective: Minimize the residual sum of squares
 - Reduce the amount of error between the observed value and the model adjusted value (i.e., predicted or estimated value)

$$e_i = Y_i - \widehat{Y}_i$$

$$\sum_{i} (Y_{i} - \widehat{Y}_{i}) = \sum_{i} [Y_{i} - (\widehat{\beta}_{0} - \widehat{\beta}_{1} \overline{X})]^{2}$$

Estimating the coefficients based on least squares

• Slope:

This is pure mathematics...

$$\widehat{\boldsymbol{\beta}}_1 = \underbrace{\sum_{i=1}^n (X_i - \overline{X})(Y_i - \overline{Y})}_{\sum_{i=1}^n (X_i - \overline{X})^2} \overset{\text{\vee}}{\longrightarrow} \text{Summation of the deviations in X}}_{\text{Summation of the deviations in X values}}$$

• Intercept:

$$\widehat{oldsymbol{eta}}_0 = \overline{Y} - \widehat{oldsymbol{eta}}_1 \overline{X} = rac{\sum\limits_{i=1}^n Y_i - \widehat{oldsymbol{eta}}_1 \sum\limits_{i=1}^n X_i}{n}$$


```
Regression results

> linreg <- with(peanut, lm(aflatoxin-clean)) #Format, Y <- X
> anova(linreg) #ANOVA table to see how the model fit looks
Analysis of Variance Table

Response: aflatoxin

Df Sum Sq Mean Sq F value Pr(>F)
clean 1 23334,5 23334,5 148.36 1.479e-13 ***

Residuals 32 5033.2 157.3

Signif. codes: 0 '**** 0.001 '** 0.01 '* 0.05 '.' 0.1' '1
> summary(linreg) #Another way to see results of the model, with a few more details.

Call:

Im(formula = aflatoxin - clean)

Min 10 Median 30 Max
-25.843 -7.997 -2.771 6.835 27.665

Coefficients:

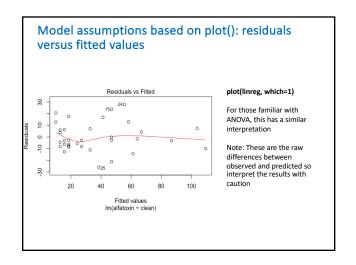
(Intercept) 28443.18 2332.21 12.20 1.43e-13 ***

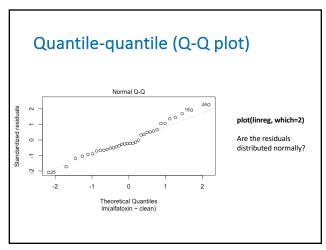
clean -284.36 23.35 -12.18 1.48e-13 ***

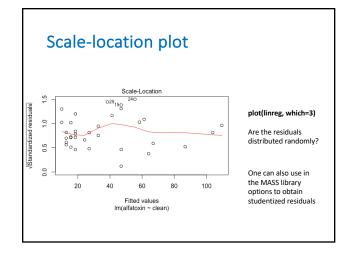
Residual standard error: 12.54 on 32 degrees of freedom
Multiple R-squared: 0.8226, Adjusted R-squared: 0.817
F-statistic: 188.4 on 1 and 32 DF, Povalue: 1.479e-13
```

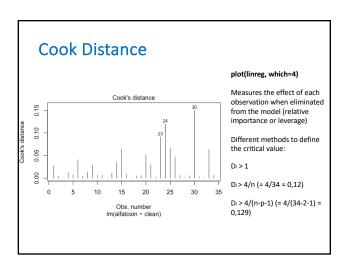
Interpretation for R²

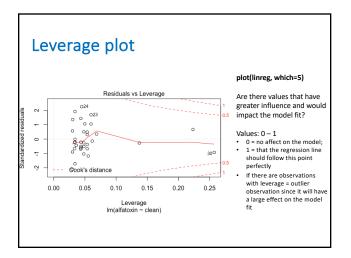
- Realibility for R² is a function of:
 - Database size
 - Type of application
- Final interpretation will vary depending on the system under study:
 - 0.95 (biology) = good model fit
 - 0.95 (chemistry) = poor model fit

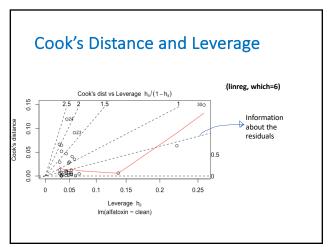












Estimation and prediction

- Estimation = we are interested in study the response variable for specific values of X that are within the range of observed values
- Example: What is the mean concentration of aflatoxin when the percentage clean seed is 99.68%?
- Based on confidence intervals for probable values
 >x=x₀
 - >Y is distributed as follows:
 - Mean = $\beta_0 + \beta_1 X$
 - Standard deviation = σ

Estimation and prediction

- Prediction = the objective is to predict a new value(s) assuming a future occurrence (new lots, new forecast year, etc.)
 - Example: What is the mean concentration of aflatoxin when the percentage clean seed is 99.68% is we obtained an unknown sample from a different location?
 - ➤In this case, the prediction takes into account two sources of uncertainty:
 - About the general location of population mean
 - About the location of the new value in the future as related to the mean value

$$Pred[Y \mid X_0] = \widehat{\mu}\{Y \mid X_0\} = \widehat{\beta}_0 + \widehat{\beta}_1 X_0$$

Confidence intervals

$$EE[\widehat{\mu}\{Y \mid X_0\}] = \sigma^2 \sqrt{\frac{1}{n} + \frac{(X_0 - \overline{X})^2}{(n-1)s_X^2}}, g.l. = n-2$$

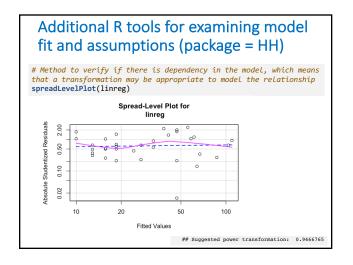
Prediction intervals

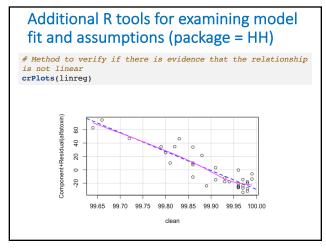
$$EE[Pred\{Y \mid X_0\}] = \sqrt{\widehat{\sigma}^2 + EE[\widehat{\mu}\{Y \mid X_0\}]^2}$$

Peanut example observation <- data.frame(clean=99.68) predict(object=linreg, newdata=observation, interval="confidence") ## fit lwr upr ## 1 98.15855 86.97085 109.3462 predict(object=linreg, newdata=observation, interval="predict") ## fit lwr upr ## 1 98.15855 70.27011 126.047</pre>

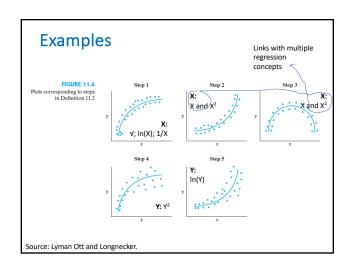
Additional R tools for examining model fit and assumptions (package = HH) ci.plot(linreg) 95% confidence and prediction intervals for linreg observed fit confint confint pred int pred int

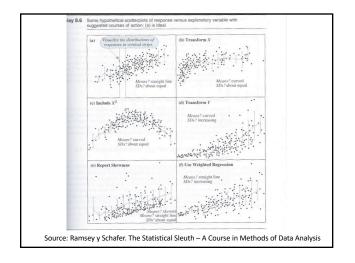
Additional R tools for examining model fit and assumptions (package = HH) # Method to look for outliers using a Bonferroni adjustment outlierTest(linreg) ## No Studentized residuals with Bonferroni p < 0.05 ## Largest | rstudent|: ## rstudent unadjusted p-value Bonferroni p ## 24 2.425727 0.021292 0.72394 # Test of homoscedasticity ncvTest(linreg) ## Non-constant Variance Score Test ## Variance formula: ~ fitted.values ## Chisquare = 0.183475, Df = 1, p = 0.6684

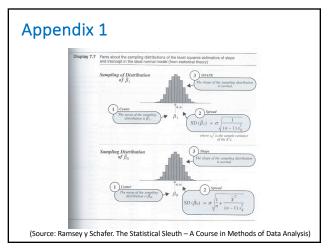


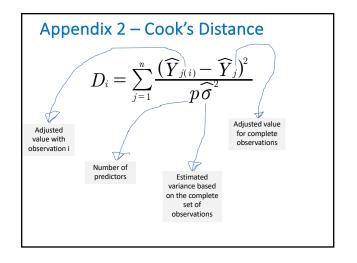


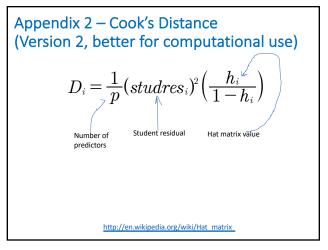
Transformations Can involve transforming: Response variable Predictor variable Both variables For further information, see: 11.1 = Lyman Ott and Longnecker. https://onlinecourses.science.psu.edu/stat501/node/48











Multiple regression modeling as a next step

- Components:
 - Response variable (dependent variable)
 - >1 independent varible (multiple factors)
- Model types include:

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \varepsilon$$

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_1 X_2 + \varepsilon$$

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_1^2$$

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_1^2 + \beta_3 X_1^3$$

Assumptions

- Model is properly defined
- Assumptions about the errors:

$$\varepsilon_i \sim Normal$$

$$Var(\varepsilon_i) = \sigma_{\varepsilon}^2$$

 ε_i = independent

Partial slopes

- Parameters for the independent variables:
 - Are called partial slopes because these values represetn the change in Y as a unit change in X_i (factor i) but by maintaining constant the other factors

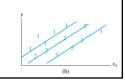
Additive effects

• When the effects between the X factors are independents

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \varepsilon$$

(a) Scatterplot of y versus x_1 ; (b) scatterplot of y versus x_1 , indicating additivity of effects for x_1 and x_2

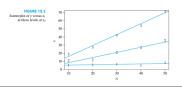
(a) (a)



Interactions

• When there are changes in Y with different levels of X_1 , but the magnitud of this change depends on the level of X_2

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 (X_1 X_2) + \varepsilon$$



Dummy variables

- Qualititative factors: We can use a 0-1 representtion to define the variable
 - Example: for two factors, A and B,
 - X₁ = 1 if treatment A
 - X₁ = 0 if treatment B
 - Which results in a model form:

$$Y = \beta_0 + \beta_1 X_1 + \varepsilon = \begin{cases} Y = \beta_0 + \varepsilon, & \text{if treatment} = B \\ Y = \beta_0 + \beta_1 X_1 + \varepsilon, & \text{if treatment} = A \end{cases}$$

General linear model form

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_k X_k + \varepsilon$$

- For the independent variables, we can have:
 - Quantitative factors
 - · Qualitative factors
 - Quadratic forms for the factors
 - Interactions among factors (multiplicative form)

Estimation

- Is based on the use of normal equations
 - Which are simultaneously solved

TABLE 12.5 Normal equations for a multiple regression model

	y_i	$\hat{oldsymbol{eta}}_0$	$x_{i1}\hat{\beta}_1$		$x_{ik}\hat{\boldsymbol{\beta}}_k$
1	$\sum y_t =$	$n\hat{\beta}_0$	$+ \sum x_{i1}\hat{\beta}_{1}$	+ · · · +	$\sum x_{ik}\hat{\beta}_k$
x_{i1}		$\sum x_{t}\hat{\beta}$	$_0 + \sum x_{t1}^2 \hat{\beta}_1$	+ · · · +	$\sum x_{t1}x_{tk}\hat{\beta}_k$
: x _{ik}	$\sum x_{ik}y_i =$	$\sum x_{tk}\hat{\beta}$	$0 + \sum x_{ik}x_{il}\hat{\beta}_1$	+ · · · +	$\sum x_{tk}^2 \hat{\beta}_k$

Tests $H_0: \beta_1 = \beta_2 = ... = \beta_k = 0$ $H_1: \text{at least one } \beta \neq 0$

$$F = \frac{SS_{regression}/k}{SS_{error}/[n-(k+1)]} = \frac{MS_{regression}}{MS_{error}}$$

Reject H_0 means that there is some degree of predictive value, meaning some of the factors are important (statistically)

Let's move into R to see this...

- · Data source: aphid counts in different lots
- Additional measures include:
 - Average daily temperature (C)
 - · Average daily relative humitidy (%)
- Can we define a "best" model that describes aphid numbers as a combination of these two factors?

> summary(aphids data)								
lot	aphids	temperature	humidity					
Min. : 1.00	Min. : 6.00	Min. :16.30	Min. : 6.00					
1st Qu.: 9.25	1st Qu.: 27.75	1st Qu.:26.00	1st Qu.:21.88					
Median:17.50	Median : 62.00	Median:28.30	Median :32.50					
Mean :17.50	Mean : 61.91	Mean :28.09	Mean :35.19					
3rd Qu.:25.75	3rd Qu.: 92.00	3rd Qu.:31.95	3rd Qu.:46.38					
Max. +34.00	Max. :118.00	Max. :34.50	Max. :79.50					

Let's move into R to see this...below is the additive model

```
> model3<-with(aphids_data, lm(aphids-temperature+humidity))
> anova(model3)
Analysis of Variance Table

Response: aphids
Df Sum Sq Mean Sq F value Pr(>F)
temperature 1 15194.8 15194.8 28.7765 7.554e-06 ***
humidity 1 4813.1 4813.1 9.1151 0.005038 **
Residuals 31 16368.9 528.0
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

SSregression = 15194,8 + 4813,1 = 20007,9 dfregression = 2

F = (20007,9/2) / 528 = 18,946 Prob(F) = 8,42 x 10⁻⁶ Evidence that there is a relationship between aphid numbers and temperature and relative humidity

Model standard deviation

Residuals

$$Y_i - \widehat{Y}_i = Y_i - (\widehat{\boldsymbol{\beta}}_0 + \widehat{\boldsymbol{\beta}}_1 X_{i1} + \widehat{\boldsymbol{\beta}}_2 X_{i2} + ... + \widehat{\boldsymbol{\beta}}_k X_{ik})$$

Model standard deviation

$$S_{\varepsilon} = \sqrt{MS_{error}} = \sqrt{\frac{SS_{error}}{n - (k+1)}}$$

Also known as: residual standard error, standard error of the estimate, root mean square error

Coefficient of determination

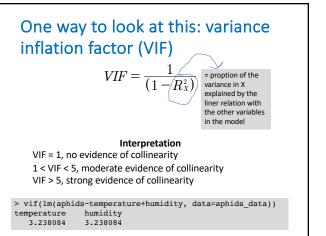
$$R_{Y \cdot X_1 \cdot \cdot \cdot X_k}^2 = \frac{SS_{total} - SS_{error}}{SS_{total}}$$

- Interpretation is the same as a simple linear model
- \bullet By default, R^2 will increase with the additional of further factors
- If the factors are not correlated, this represents the summation of each individual R²
- When the variables are correlated = collinearity

Collinearity

- When there exists some correlation between independent variables
 - One factor may be explained well by another factors
 - May not impact model if the correlations are small
 - When correlation is high, could impact model fit (overfitted)

Back to the example aphids a



Model comparision: nested models

- F-test: complete model versus reduced model
 - Question, is there still predictive value?

$$F = \frac{\left[SS_{full} - SS_{reduced}\right]/(k-g)}{SS_{full}/\left[n-(k+1)\right]}$$
With,
$$df_1 = k - g$$

$$df_2 = \left[n-(k+1)\right]$$

anova(model3, model4)

```
> anova(model3, model4) # the interaction improved the model
Analysis of Variance Table

Model 1: aphids - temperature + humidity
Model 2: aphids - temperature + humidity + temperature:humidity
Res.Df RSS Df Sum of Sq F Pr(>F)
1 31 16369
2 30 13605 1 2764 6.095 0.01947 *
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

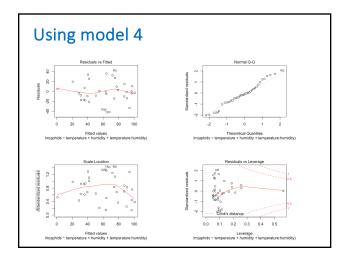
Diagnostics

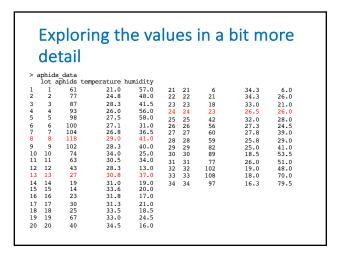
- plot()
- rstudent()
- dbetas()
- dffits()
- covratio()
- cooks.distance()

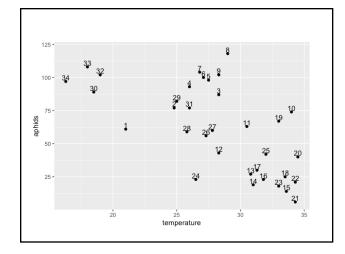
Plot provides the graphical

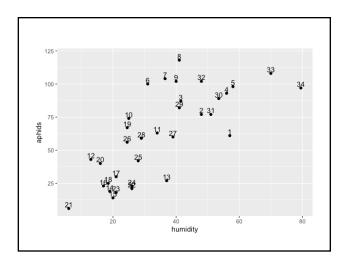
The other functions provide calculated values (and graphical tools with olsrr) for the respective measures, which can be useful if you would like to search for specific values that are beyond threshold values, etc.

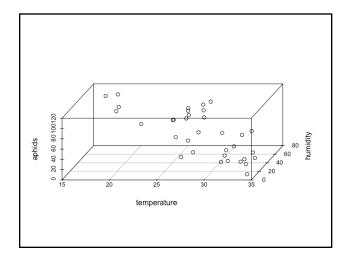
Follows from the same ideas in our peanut example, are there outliers, influential points, etc.?





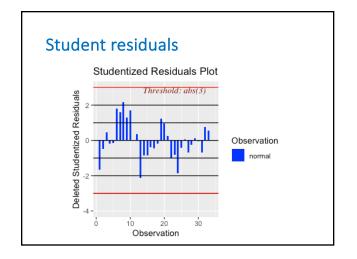


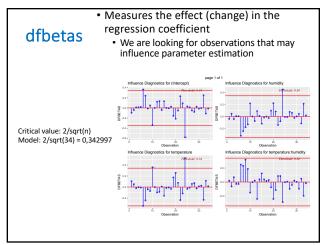




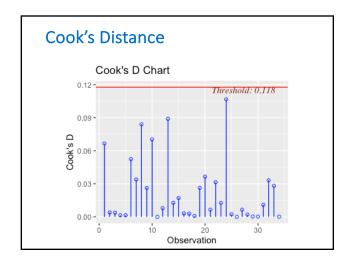
Visual examination of key measures using *olsrr* package

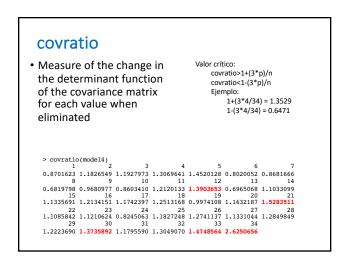
- Interesting package that takes the calculations and offers graphical visualization of the results for each assumption (you can teach an old dog new tricks...)
- https://www.rdocumentation.org/packages/olsrr/v ersions/0.5.2
 - Recommended for the beginner/intermediate R user and focused on ordinary least square regression models

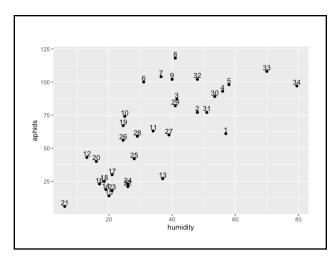




dffits Standardized measure (scaled) that represents the change in predicted value for each observation when it is eliminated Large value = high influence Crticial value: 2 2*sqrt(p/n) Ejemplo: 2*sqrt(4/34) = 0.69







Let's take a pause...next step

- Aphid example: how well does this model look?
- Are there other models we should consider?
- In the next step, we will expand on the model by looking at different tools to identify "best" models and compare those based on tools like AIC, BIC, and Mallow's Cp

Let's build this considering what we have seen so far...

• Model a (additive):

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \varepsilon$$

• Model b (full model with quadratic terms):

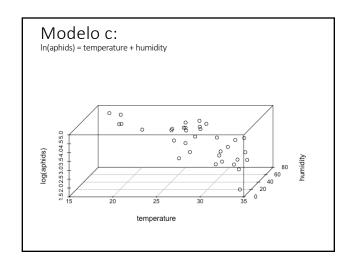
$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_1^2 + \beta_4 X_2^2 + \beta_5 X_1 X_2 + \varepsilon$$

• Transformation? Model c [count data -> ln()]

$$\ln(Y) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \varepsilon$$

Model a (additive model):

Model b (full model):



Comparison of model a and b

Indicates that model b does not significantly improve the model (over-parameterized?)

Summary (partial)

- Of the three models (a, b, and c)
 - a versus b: while the model improved some of the predictive value with b, there are probably factors that are not needed to best explain the relationship
 - $\bullet\,$ a and c: the transformation did not improve the model
 - One possibility to consider with count data would be to switch to a generalized linear model and use a Poisson distribution

Is there a model that better represents the observations?

- Given our two models (a and b), is there a better model that reflects the process?
- Our full model includes: main effect terms, interaction term, and quadratic model terms (based on the graphical
- We will apply three methods to build the models:
 - Manually = add model parameters at each step and make decisions about the relative fit
 - Here, we will rely extensively on anova(model X, model Y) to compare the models since there is a natural nesting of one model within another
 - Stepwise method (forward, backward, both)
 - · Best subsets (takes the full model and looks at different combinations of factors)

Stepwise methods

- · Uses a search algorithm
 - Forward selection: starting from a null model, add variables based on some inclusion critera to keep or remove the variable, and the process continues for the rest of the variables until we arrive at the defined full model
 - · Backward selection: similar, but this time we start from the full model and work towards a simpler model
 - · Both directions: we apply the search algorithm working simultaneously with a forward and backward mindset
 - Ideally: all methods end the same model (we will see this is not always the case)
 - In R: Variable selection is based on AIC (Akaike Information Criterion)

Best subsets

- · Method that looks at different models by considering combinations of the independent variables
 - For example, if we have four possible factors for a model,
 - This approach will look at the best models for only one, for two, for three, and with all factors
 - Comparison methods in R (package = leaps, function = regsubsets):
 - · Adjusted coefficient of determination
 - Mallow's Cp
 - Schwartz criterion (Bavesian information criterion)

AIC

- Measure of the relative quality of a statistical model
- · Balance the trade-off between the model fit and model complexity

$$AIC = 2p - 2\ln(L)$$

Number of parameters

Maximum value for the likelihood function of the estimated model

"General" = the preferred model will have the minimum AIC value, what we are doing is penalizing the model for having greater numbers of factors

BIC

- Like AIC this is a method that provides a selection criterion for a finite number of models
 - Based on likelihood functions

$$BIC = -2* \ln(L) + p \ln(n)$$
Maximum value for the likelihood function of an estimated model

"General" = the preferred model will have the minimum value for BIC and the formula penalizes more complex models (i.e., greater number of parameters)

Mallow's C_p

• Equivalent method to AIC

$$C_{p}=rac{SC_{error,p}}{CM_{error}}-n+2p$$

"General" = preferred model with have a minimum value for C_p

Manually (see R notes)

Model		
	ajustado	
Temperature + Humidity + Temperature ² + Humidity ² + Temperature:Humidity	0.5617	
Temperature + Humidity + Temperature ² + Humidity ²	0.5752	
Temperature + Humidity + Temperature ²	0.565	
Temperature + Humidity + Humidity ²	0.5832	
Humidity + Humidity ²	0.5869	
Temperatura + Humedad	0.521	

This is a systematic approach to comparing the models. Right now, the best model may be: aphids~temperature + humidity + humidity². We could consider a humidity-only model as well?

Stepwise algorithms (based on AIC)

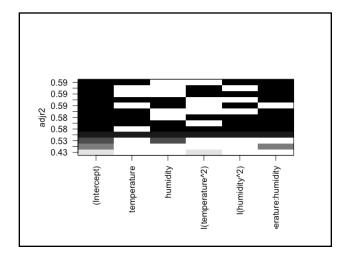
model_null <- lm(aphids~1, data=aphids_data)
model_full <- model_b</pre>

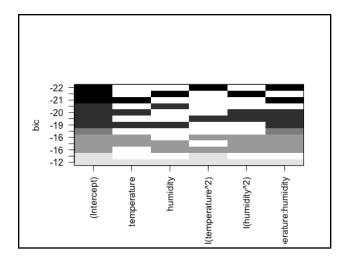
- Forward:
 - aphids ~ humidity + humidity² (AIC = 210.97)
- Backwards:
 - aphids ~ humidity + humidity2 (AIC = 210.97)
- Both directions
 - aphids ~ humidity + humidity² (AIC = 210.97)

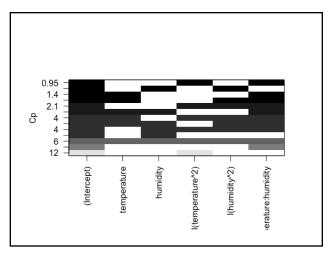
Best subsets (nbest=3)

- R²-ajustado (~0,59 para todo):

 - Temperature + Humidity² + Temperature:Humidity Temperature² + Temperature:Humidity
 - Temperature² + Humidity² + Temperature:Humidity • Temperature + Humidity + Temperature: Humidity
 - Humidity + Humidity²
- BIC (-22):
 - Temperature² + Temperature:Humidity
 - Humidity + Humidity²
- C_p:
 - #1: Temperature² + Temperature: Humidity
 - #2: Humidity + Humidity²







Modeling thoughts

General principles

Our general principles for building regression models for prediction are as follows:

1. Include all input variables that, for substantive reasons, might be expected to
be important in predicting the outcome.

be important in predicting the outcome.

It is not always necessary to include these inputs as separate predictors—for example, sometimes several inputs can be averaged or summed to create a "total

For inputs that have large effects, consider including their interactions as well.
 We suggest the following strategy for decisions regarding whether to exclude a

cance (typically measured at the 5% level; that is, a coefficient is "statistically significant" if its estimate is more than 2 standard errors from zero):

(a) If a predictor is not statistically significant and has the expected sign, it is generally fine to keep it in. It may not help predictions dramatically but is also probably not hurting them.

(b) If a predictor is not statistically significant and does not have the expected sign (for example, incumbency having a negative effect on vote share), consider removine it from the model (that is, setting its coefficient to zero).

(e) If a predictor is statistically significant and does not have the expected sign, then think hard If it makes sense. (For example, perhaps this is a country such as India in which incumbents are generally unpopular; see Linden, 2006.) Try to gather data on potential burking variables and include them in the analysis.

to gather data on potential lurking variables and include them in the analysis.

i) If a predictor is statistically significant and has the expected sign, then by all means keep it in the model.

These strategies do not completely solve our problems but they heep keep not making mistakes such as discarding important information. They are predicated o having thought hard about these relationships before fitting the model. It's always used ret justiff a coefficient's sign after the fact than to think hard about of misbout what we expect. On the other hand, an explanation that is determined after misming the model can still be valid. We should be able to adjust our theories i

Source. Gelman y Hall. 2007. Data Analysis Using Regression and Multilevel/Hierarchical Models. Cambridge.

Which is the best model and why?

- All models have moderate predictive value
- One model consistently found was based on humidity with a quadratic term
- · Biologically, does this model make sense?
- We can go back and study the behaviour on the final model using the various tools we saw earlier

Exercise: Fusarium modeling exercise.R

- To put into practice what we saw in the last section
- Data includes:
 - lot = represents an individual plot level observation
 - yield = kilograms per hectare
 - fdk = fusarium damaged kernels (%)
 - incidence = incidence of Fusarium head blight (%)
 - severity = severity of Fusarium head blight in heads (%)
 - moisture = grain moisture (%)
- don = concentration of vomitoxin (ppm)
- We will read the data into R using "Import Dataset"
- Focus here is on using the automated algorithms

Concluding thoughts

- R has numerous tools to effectively develop, test, and validate models (always has been the software's strength)
- Effective modeling requires decisions based on the overall goal of the model (predictive, theoretical, summary, etc.)
- What are the parameters and what do they mean in the context of the measured variable of interest?
 - Our current work (machine/deep learning) has required substantial time focused on identifying the proper parameters to avoid the "junk in, junk out" result
- What will define a good model is a function of the model goal