

## Week 10 — November 15, 2018

### Homework

- Read chapter 13 in “Beginning C”
- Read sections 9.1-9.5 (pp. 118-130) in “Writing Scientific Software”

### Exercises

In an earlier exercise, we worked with a structure `struct sparse_triplet` representing a sparse matrix in triplet form. This week we are going to work with a small library that implements basic linear algebra operations for vectors, matrices, and sparse matrices in triplet form.

1. Download `week10.zip` from Inside and unzip it. The file contains several files:
  - a source file `matrix_io.c` and a header file `matrix_io.h` which provide a basic set of data structures and functions
  - a source file `test_basic.c` which is a short program with some test cases
  - a makefile that can be used to compile the test program
  - four templates (`dot.c`, `norm2.c`, `norm_fro.c`, and `norm_fro_sparse.c`).

Look through the header file `matrix_io.h` to familiarize yourself with the data structures and functions that the library provides. Notice that there are three data structures:

- `vector_t` represents a vector of length  $n$  and is defined as:

```
typedef struct vector {  
    unsigned long n; /* length of vector */  
    double * v; /* pointer to array of length n */  
} vector_t;
```

- `matrix_t` represents a matrix of size  $m \times n$  and is defined as:

```
typedef struct matrix {  
    unsigned long m; /* number of rows */  
    unsigned long n; /* number of columns */  
    double ** A; /* pointer to two-dimensional array */  
} matrix_t;
```

- `sparse_triplet_t` represents a sparse matrix in triplet form of size  $m \times n$  and is defined as:

```
typedef struct sparse_triplet {
```

```

    unsigned long m;    /* number of rows          */
    unsigned long n;    /* number of columns        */
    unsigned long nnz;   /* number of nonzeros       */
    unsigned long * I;   /* ptr to array with row indices */
    unsigned long * J;   /* ptr to array with col. indices */
    double * V;          /* ptr to array with values    */
} sparse_triplet_t;

```

Notice also that for each of these data types, there are functions for the following operations:

- memory allocation/deallocation (e.g., `malloc_vector()` and `free_vector()`)
- file input/output (e.g., `read_vector()` and `write_vector()`)
- console output (e.g., `print_vector()`).

The functions that start with `malloc_` and `read_` allocate memory and return a pointer. This means that each call to one of these functions should be matched with a call to the corresponding function that starts with `free_`. For example, if your program contains a call to `read_matrix()`, there should also be a call to `free_matrix()` in order to deallocate the memory that was allocated by `read_matrix()`.

If you want to know more about the functions defined in `matrix_io.h`, open the source file `matrix_io.c` and take a look at the implementation of the different functions. The source file also includes basic documentation in the form of comments.

2. Open the `test_basic.c` source file and inspect the code. Compile the test program and run it:

```
$ make run
```

The test program should print a vector, a matrix, a sparse matrix, and some error messages. The program should also create three files: `test_vector.txt`, `test_matrix.txt`, and `test_sparse_triplet.txt`. Open each of these files in a text editor and compare with the screen output.

3. Extend the library with a function that computes and returns the Euclidean norm of a vector  $x$ , i.e.,

$$\|x\|_2 = \left( \sum_{i=1}^n x_i^2 \right)^{1/2}.$$

The function should have the following prototype

```
int norm2(const vector_t * px, double * nrm);
```

and the implementation should be documented with comments in the source file. The Euclidean norm should be stored in the second argument `nrm`, and the functions should return one of the following values:

- `MATRIX_IO_ILLEGAL_INPUT` if one of the inputs is `NULL`

- `MATRIX_IO_DIMENSION_MISMATCH` if the length of the vector is 0
- `MATRIX_IO_SUCCESS` if the function returns without any errors.

Use the template `norm2.c` for your implementation.

Write a short program (say, `test_norm2.c`) to test the Euclidean norm function. The program should test that the different error cases are handled correctly.

**Remark:** This exercise is also available on [CodeJudge](#).

4. Extend the library with a function that computes the Frobenius norm of a matrix of size  $m \times n$ , i.e.,

$$\|A\|_F = \left( \sum_{i=1}^m \sum_{j=1}^n A_{ij}^2 \right)^{1/2}.$$

The function should have the following prototype

```
int norm_fro(const matrix_t * pA, double * nrm);
```

and the implementation should be documented with comments in the source file. The Frobenius norm should be stored in the second argument `nrm`, and the functions should return one of the following values:

- `MATRIX_IO_ILLEGAL_INPUT` if one of the inputs is `NULL`
- `MATRIX_IO_DIMENSION_MISMATCH` if either  $m$  or  $n$  is zero
- `MATRIX_IO_SUCCESS` if the function returns without any errors.

Use the template `norm_fro.c` for your implementation.

Write a short program (say, `test_norm_fro.c`) to test the Frobenius norm function. The program should test that the different error cases are handled correctly.

**Remark:** This exercise is also available on [CodeJudge](#).

5. Extend the library with a function that computes the Frobenius norm of a sparse matrix of size  $m \times n$ . The function should have the following prototype

```
int norm_fro_sparse(const sparse_triplet_t * pA, double * nrm);
```

and the implementation should be documented with comments in the source file. The Frobenius norm should be stored in the second argument `nrm`, and the functions should return one of the following values:

- `MATRIX_IO_ILLEGAL_INPUT` if one of the inputs is `NULL`
- `MATRIX_IO_DIMENSION_MISMATCH` if either  $m$  or  $n$  is zero
- `MATRIX_IO_SUCCESS` if the function returns without any errors.

Use the template `norm_fro_sparse.c` for your implementation.

Write a short program (say, `test_norm_fro_sparse.c`) to test the function. The program should test that the different error cases are handled correctly.

**Remark:** This exercise is also available on [CodeJudge](#).

6. Extend the library with a function that computes the inner product of two vectors  $x$  and  $y$  of length  $n$ , i.e.,

$$x^T y = \sum_{i=1}^n x_i y_i.$$

Your function should have the following prototype:

```
int dot(const vector_t * px, const vector_t * py, double * xy);
```

The inner product should be stored in the third argument `xy`, and the return value should be equal to

- `MATRIX_IO_ILLEGAL_INPUT` if one of the inputs is `NULL`
- `MATRIX_IO_DIMENSION_MISMATCH` if the input vectors are of different length or if both vectors have length 0
- `MATRIX_IO_SUCCESS` if the function returns without any errors.

Your implementation should include sufficient documentation in the form of comments.

Use the template `dot.c` for your implementation.

Write a short program (say, `test_dot.c`) to test the inner product function. The program should test that the different error cases are handled correctly.

**Remark:** This exercise is also available on [CodeJudge](#).