

Code structure

Both parts of the assignment have been structured similarly. First of all, the `matrix_io.h` header and source file `matrix_io.c` has been used as required by CodeJudge. The test case for the first part has been separated into the source file for the function call `call_dgesv.c` and a main function for testing, `call_dgesv_test.c`. A makefile has been included to link the files as well as `dgesv_` from LAPACK and run the program. The second part has been structured similarly, linking `call_dgesv.c`, `solve.c` as well as the `matrix_io.c` source and `matrix_io.h` header files.

Numerical considerations and error handling

Numerical assessments are mostly left to LAPACK's `dgesv_` function, although the function has been thoroughly tested to ensure that the function properly handles the following numerical considerations: 1) Non-numeric input such as INFINITY and NaN values and 2) ill conditioned matrices.

The first scenario is included as an addition in the `call_dgesv` function, as the `dgesv_` function itself did not seem to deal properly with this scenario. The exact test is elaborated further under "Test cases".

Ill conditioned matrices are handled through the `dgesv_` function. Hence, if `dgesv_` returns a value (through the `info` argument) above 0, the matrix is said to be exactly or near singular, which may result from an ill conditioned matrix.

Errors are returned as requested for NULL pointers for A and b, a non-square matrix A, incompatible dimensions between A and b and finally memory allocation errors. The remainder, except the above described part of non-numeric input, is left for the `dgesv_` function but considered as described above as well as tested, which will be elaborated next.

Test cases¹

In the first part, two test cases were performed. One with pseudo-randomly generated numbers and one with a value replaced by INF in matrix A to check the `call_dgesv` function's return value (screenshot of result from command line in appendix – `Invalid_input_A.png`).

Three test cases were performed with different inputs of matrix A for the second part. One with a well-conditioned matrix, an ill-conditioned matrix and a matrix containing numerical errors (INF and NaN values) to test the programs (attached in appendix as Case 1, 2 and 3, respectively). All matrices are attached in the appendix and the solution x for the well-conditioned matrix is included as well

The ill-conditioned matrix, correctly, returns the exactly/near singular error message from `dgesv_`. The matrix containing numerical errors is handled correctly in the first part, but in the second part, the `read_matrix` function does not appear to deal with "incorrect" input in the same way the `read_vector` function does, and e.g. INF and NaN values are converted to 0's (returning in an "incorrect" result in `x.txt`, as seen from Case 2 in the appendix). The `read` function could be amended to check the input and return NULL in case of invalid content in the file. An example with an INF value in vector b is also included in the appendix (attached as Case 4).

The well-conditioned matrix returns a quite accurate result too (based on `x.txt`), and the program therefore appears to work as expected, given a proper input.

¹ All functions, header and Makefile used for test cases are included in the appendix as .zip files under names "Part 1" and "Part 2", respectively.