

Proof Method & Propositional Resolution (Latihan 2)

1) Premis: $(\text{malas} \wedge \text{bolos}) \rightarrow \neg \text{lulus}$ Kesimpulan: $\neg \text{malas}$
 $\neg \text{lulus} \rightarrow \text{marah}$

$\text{bolos} \wedge \neg \text{marah}$

Réduktion $\{(\text{lulus} \wedge \text{bolos}) \rightarrow \neg \text{lulus}, \neg \text{lulus} \rightarrow \text{marah}, \text{bolos} \wedge \neg \text{marah}\} \models \neg \text{malas}$

Danak: generalisasi inferensi

1 $(\text{malas} \wedge \text{bolos}) \rightarrow \neg \text{lulus}$ (premis)

2 $\neg \text{lulus} \rightarrow \text{marah}$ (premis)

3 $\text{bolos} \wedge \neg \text{marah}$ (premis)

4 bolos (simplification 3)

5 $\neg \text{marah}$ (simplification 3)

6 $\text{lulus} \rightarrow \neg (\text{malas} \wedge \text{bolos})$ (transposition 1)

7 $\neg \text{marah} \rightarrow \text{lulus}$ (transposition 2)

8 lulus (modus ponens 5 & 7)

9 $\neg (\text{malas} \wedge \text{bolos})$ (modus ponens 6 & 8)

10 $\neg \text{malas} \vee \neg \text{bolos}$ (de Morgan's Law 9)

11 $\neg \text{malas}$ $\frac{\neg \text{bolos}}{\neg \text{bolos}}$ (disjunctive syllogism 10 & 4)

2) Buktikan $\{p \rightarrow q, q \rightarrow r\} \models (q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p)$

$$a) ((p \rightarrow q) \wedge (q \rightarrow r)) \rightarrow ((q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p))$$

p	q	r	$((p \rightarrow q) \wedge (q \rightarrow r)) \rightarrow ((q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p))$
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T T T T T T F T F T F

T T F T F F T F T T F F

T F T F F T T T F T F

T F F F F T T F T F F

F T T T T T T T T T T

F T F T F F T F T T T

F F T T T T T T T T

F F F T T T T T T T

Karena valid, maka $\{p \rightarrow q, q \rightarrow r\} \models (q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p)$ \blacksquare

$$b) (p \rightarrow q) \wedge (q \rightarrow r) \wedge \sim ((q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p))$$

p	q	r	$(p \rightarrow q) \wedge (q \rightarrow r) \wedge \sim ((q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p))$
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T T T T T T F F T F T F

T T F T F F F F T T F F

T F T F F T F F T T F T F

T F F F F T F T F T F F

F T T T T T F F T T T T

F T F T F F F F T T T T

F F T T T T F F T T T T

(KIKY)
F F F T T T F F T T T T

Karena unsatisfiable, maka $\{p \rightarrow q, q \rightarrow r\} \models (q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p)$ $\boxed{\text{V}}$

c) premis: $p \rightarrow q, q \rightarrow r$; konklusi: $(q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p)$

(i) $p \rightarrow q$ premis (viii) $(p \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p)$ CR(vii)

(ii) $q \rightarrow r$ premis (ix) $(p \rightarrow \neg r) \rightarrow \neg p$ modus ponen (viii), (vii)

(iii) $(q \rightarrow r) \rightarrow (p \rightarrow (q \rightarrow r))$ II (ii) (x) $(q \rightarrow r) \rightarrow ((p \rightarrow \neg r) \rightarrow \neg p)$ II (ix)

(iv) $p \rightarrow (q \rightarrow r)$ modus ponen (ii), (iii) $\boxed{\text{VI}}$

(v) $(p \rightarrow (q \rightarrow r)) \rightarrow ((p \rightarrow q) \rightarrow (p \rightarrow r))$ ID (iv)

(vi) $(p \rightarrow q) \rightarrow (p \rightarrow r)$ modus ponen (iv), (v)

(vii) $p \rightarrow r$ modus ponen (i), (vi)

5) Buktikan set klasa berikut bersifat unsatisfiable!

a) $\{p, q\}, \{\neg p, r\}, \{\neg p, \neg r\}, \{p, \neg q\}$

(i) $\{p, q\}$ premis (v) $\{p\}$ (i), (iv)

(ii) $\{\neg p, r\}$ premis (vi) $\{\neg p\}$ (ii), (iii)

(iii) $\{\neg p, \neg r\}$ premis (vii) $\{\}$ (v), (vi) $\boxed{\text{VII}}$

(iv) $\{p, \neg q\}$ premis

b) $\{p, q, \neg r, s\}, \{\neg p, r, s\}, \{\neg q, \neg r\}, \{p, \neg s\}, \{\neg p, \neg r\}, \{r\}$

(i) $\{p, q, \neg r, s\}$ premis (vii) $\{q, s\}$ (i), (ii)

(ii) $\{\neg p, r, s\}$ premis (viii) $\{\neg q\}$ (iii), (vi)

(iii) $\{\neg q, \neg r\}$ premis (ix) $\{\neg r, \neg s\}$ (iv), (v)

(iv) $\{p, \neg s\}$ premis (x) $\{\neg s\}$ (vi), (ix)

(v) $\{\neg p, \neg r\}$ premis (xi) $\{\neg s\}$ (vii), (viii)

(vi) $\{r\}$ premis (xii) $\{\}$ (x), (xi) $\boxed{\text{VIII}}$

6) Premis: $p \rightarrow q$, $\neg p \rightarrow \neg t$, $\neg s \rightarrow \neg r$, $q \rightarrow r$; Konklusi: $t \rightarrow s$

Buktikan dengan proposisional reduction!

$\Delta \cup \{\neg p\}$ unsatisfiable

$$\Delta = \{p \rightarrow q, \neg p \rightarrow \neg t, \neg s \rightarrow \neg r, q \rightarrow r\} \quad \{\neg p\} = \{\neg(t \rightarrow s)\}$$

$$I \{ \neg p \vee q, p \vee \neg t, s \vee \neg r, \neg q \vee r \} \quad I \{ \neg(\neg t \vee s) \}$$

$$O \{ \{\neg p, q\}, \{p, \neg t\}, \{s, \neg r\}, \{\neg q, r\} \} \quad N \{ t \wedge \neg s \}$$

$$O \{ \{t\}, \{\neg s\} \}$$

$$\Delta \cup \{\neg p\} = \{ \{\neg p, q\}, \{p, \neg t\}, \{s, \neg r\}, \{\neg q, r\}, \{t\}, \{\neg s\} \}$$

(i) $\{\neg p, q\}$ premis (v) $\{t\}$ premis (ix) $\{q\}$ (i), (vii)

(ii) $\{p, \neg t\}$ premis (vi) $\{\neg s\}$ premis (x) $\{\neg q\}$ (iv), (viii)

(iii) $\{s, \neg r\}$ premis (vii) $\{p\}$ (ii), (v) (xi) $\{\}$ (ix), (x)

(iv) $\{\neg q, r\}$ premis (viii) $\{\neg r\}$ (iii), (vi)

Karena $\Delta \cup \{\neg p\}$ unsatisfiable maka $\{p \rightarrow q, \neg p \rightarrow \neg t, \neg s \rightarrow \neg r, q \rightarrow r\} \models t \rightarrow s$

g) a: Ang tidak bersalah; b: Bng tidak bersalah; c: Cng Adah bersalah

a) $\neg b \wedge c$, $\neg a \rightarrow \neg c$, $c \wedge (\neg a \vee \neg b)$

b) Premis: a, b, c; Cari kllmat yang benar dan tidak benar pada pdm a.

a	b	c	$\neg b \wedge c$	$\neg a \rightarrow \neg c$	$c \wedge (\neg a \vee \neg b)$
T	T	T	F	T	T F F

Kllmat benar: $\neg a \rightarrow \neg c$: Bng jujur

Kllmat tidak benar: $\neg b \wedge c$, $c \wedge (\neg a \vee \neg b)$: Ang dan Cng berolahraga

c) Premis: $a \leftrightarrow (\neg b \wedge c)$, $b \leftrightarrow (\neg a \rightarrow \neg c)$, $c \leftrightarrow (c \wedge (\neg a \vee \neg b))$

a	b	c	$a \leftrightarrow (\neg b \wedge c)$	$b \leftrightarrow (\neg a \rightarrow \neg c)$	$c \leftrightarrow (c \wedge (\neg a \vee \neg b))$
T	T	T	T	F	T
T	T	F	F	F	F
T	F	T	F	T	T
T	F	F	F	F	F
F	T	T	F	F	T
F	T	F	T	F	F
F	F	T	F	T	T
F	F	F	F	F	F

Ketika seluruh premis benar, a bernilai salah, b bernilai benar, dan c bernilai salah.

Schinjor yang tidak berasal adalah Bang