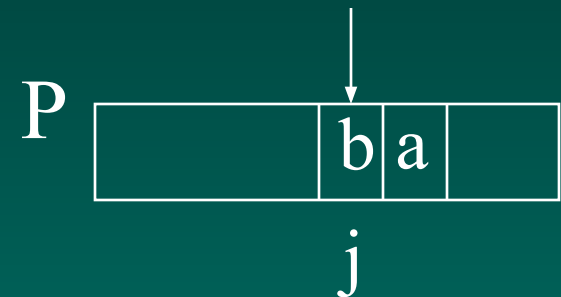
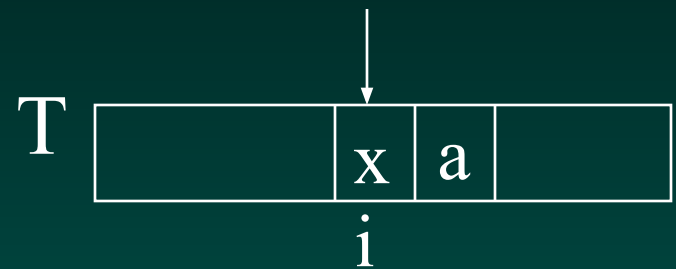


3. *The Boyer-Moore Algorithm*

- The Boyer-Moore pattern matching algorithm is based on two Phases.
- 1. The *looking-glass* phase
 - find P in T by moving *backwards* through P, starting at its end

3. The Boyer-Moore Algorithm

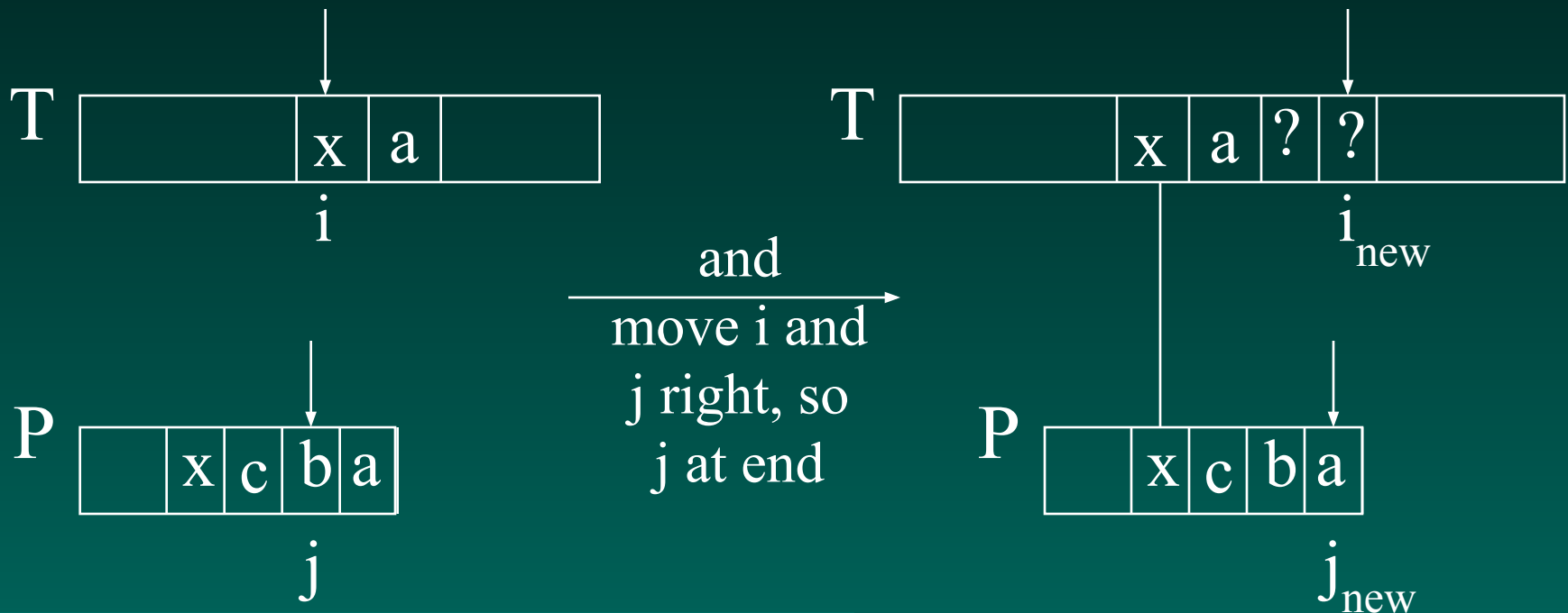
- 2. The *character-jump* phase
 - when a mismatch occurs at $T[i] \neq x$
 - the character in pattern $P[j]$ is not the same as $T[i]$
- There are 3 possible cases, tried in order.



3. The Boyer-Moore Algorithm

Case 1

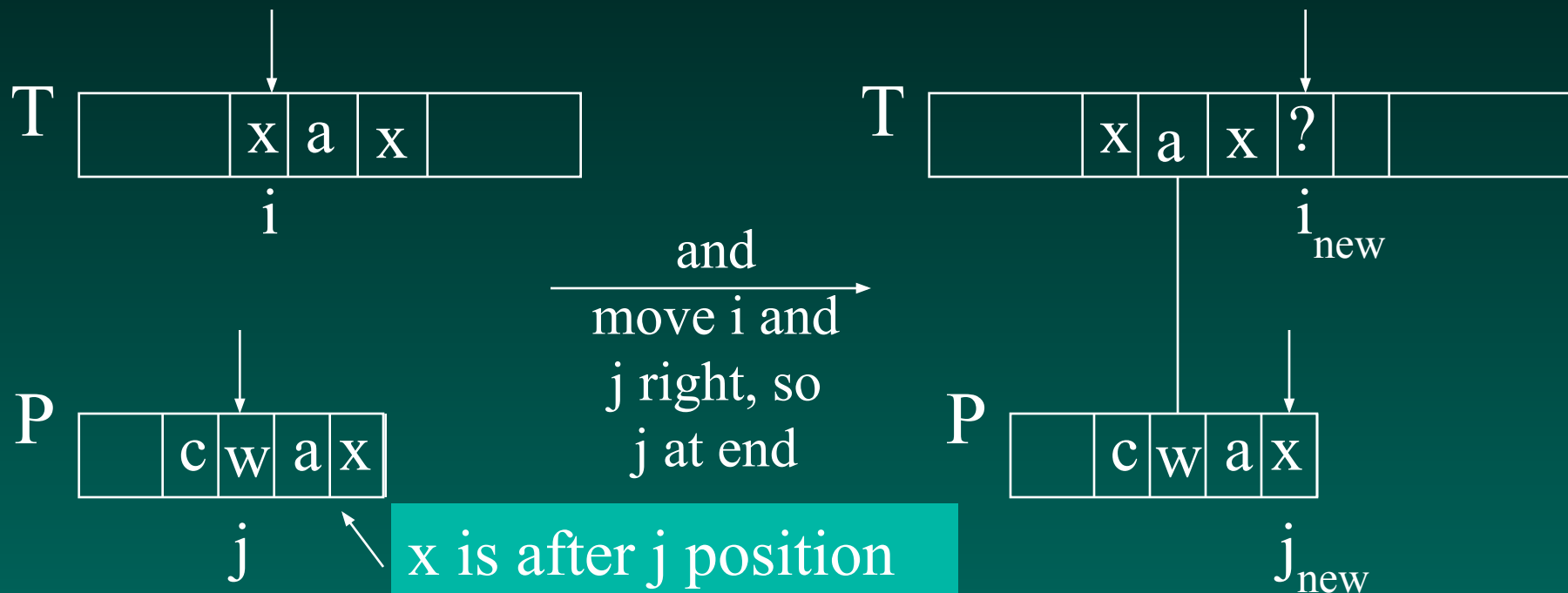
- If P contains x somewhere, then try to *shift P* right to align the last occurrence of x in P with $T[i]$.



3. The Boyer-Moore Algorithm

Case 2

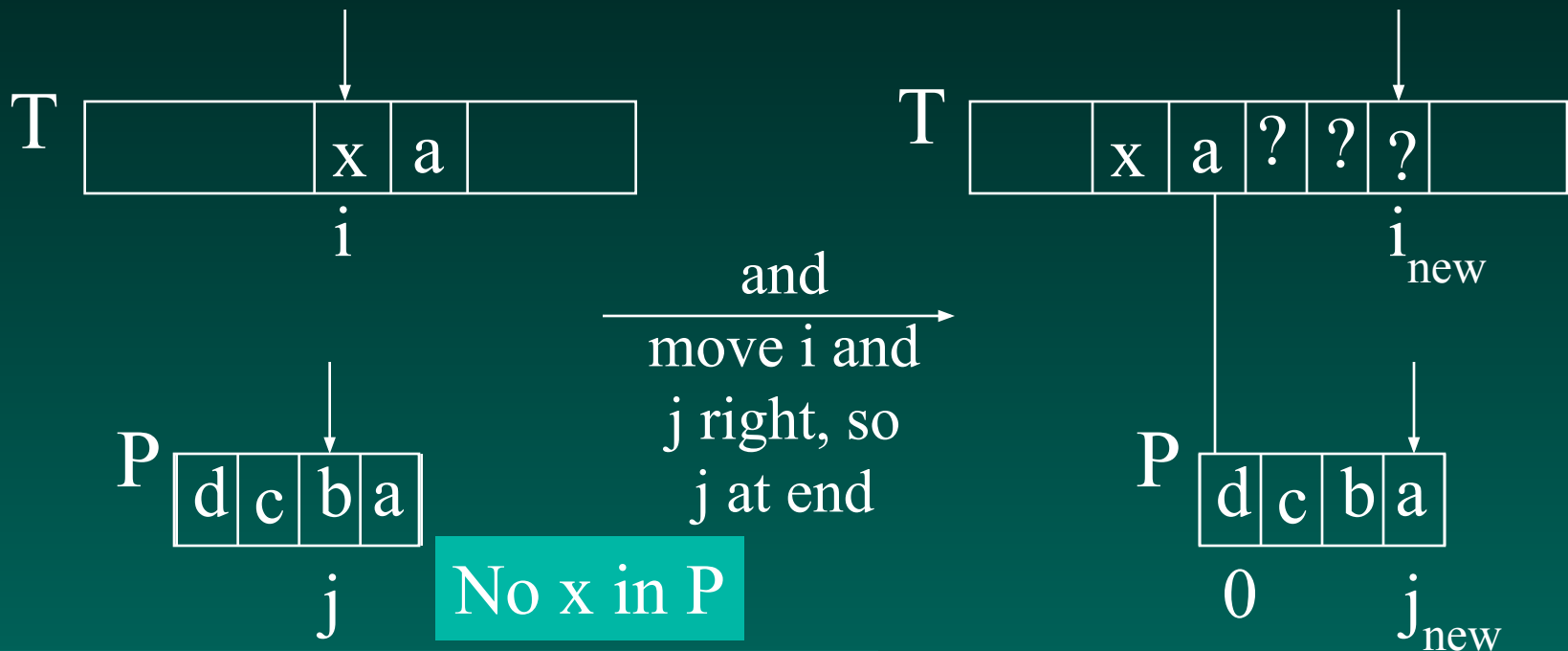
- If P contains x somewhere, but a shift right to the last occurrence is *not* possible, then *shift P* right by 1 character to $T[i+1]$.



3. The Boyer-Moore Algorithm

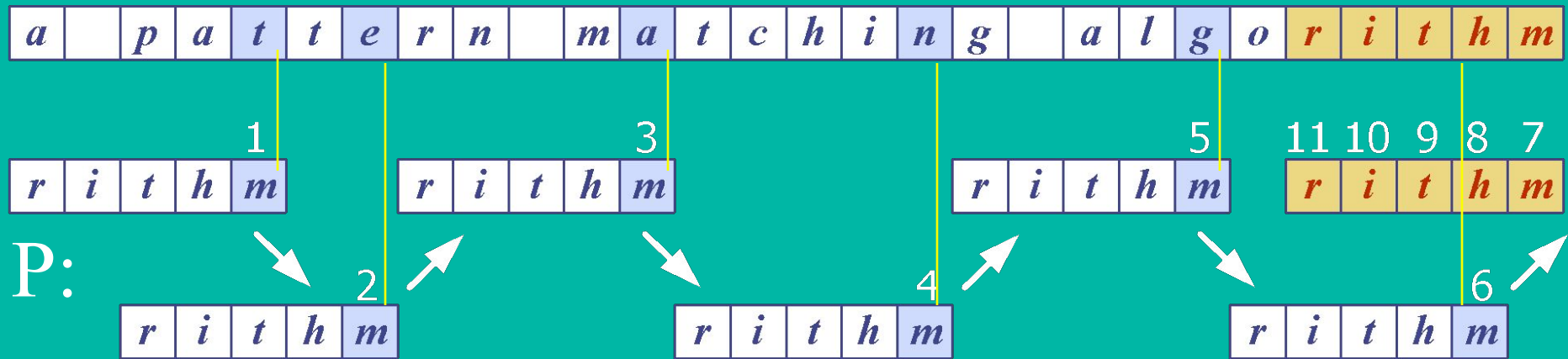
Case 3

- If cases 1 and 2 do not apply, then *shift* P to align P[0] with T[i+1].



3. The Boyer-Moore Algorithm

T:



3. The Boyer-Moore Algorithm

Last Occurrence Function

- Boyer-Moore's algorithm preprocesses the pattern P and the alphabet A to build a last occurrence function $L()$
 - $L()$ maps all the letters in A to integers
- $L(x)$ is defined as: // x is a letter in A
 - the largest index i such that $P[i] == x$, or
 - -1 if no such index exists

3. The Boyer-Moore Algorithm

L() Example

- $A = \{a, b, c, d\}$
- P : "abacab"

P

a	b	a	c	a	b
0	1	2	3	4	5



x	a	b	c	d
$L(x)$	4	5	3	-1

$L()$ stores indexes into $P[]$

3. The Boyer-Moore Algorithm



- In Boyer-Moore code, $L()$ is calculated when the pattern P is read in.
- Usually $L()$ is stored as an array
 - something like the table

3. The Boyer-Moore Algorithm

Example (2)

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
													3				7	8	

T:

a	b	a	c	a	a	b	a	d	c	a	b	a	c	a	b	a	a	b	b
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

P:

a	b	a	c	a	b
---	---	---	---	---	---

4 3 2

a	b	a	c	a	b
---	---	---	---	---	---

13 12 11 10 9 8

a	b	a	c	a	b
---	---	---	---	---	---

5

a	b	a	c	a	b
---	---	---	---	---	---

7

a	b	a	c	a	b
---	---	---	---	---	---

6

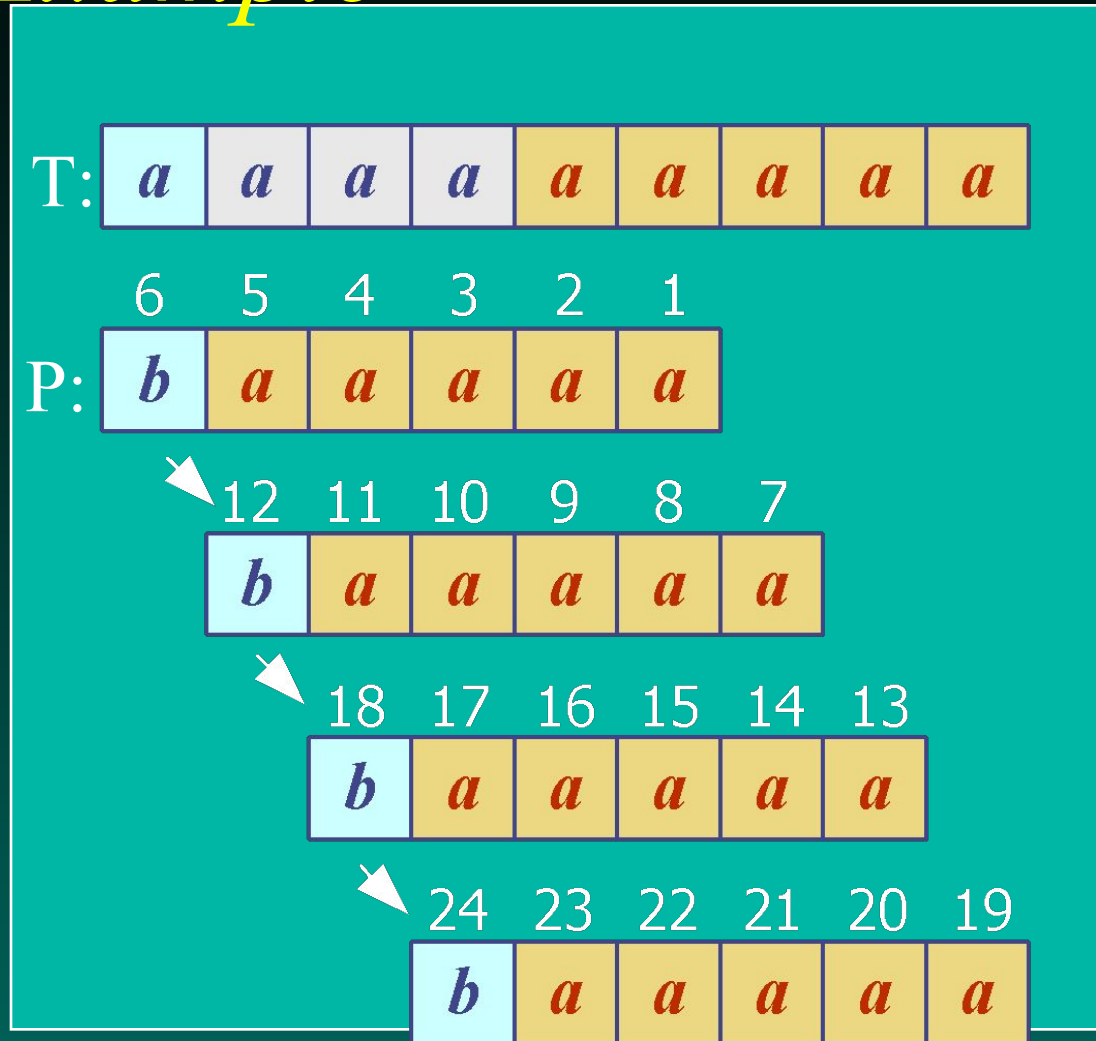
a	b	a	c	a	b
---	---	---	---	---	---

x	a	b	c	d
$L(x)$	4	5	3	-1

3. The Boyer-Moore Algorithm

Worst Case Example

- T: "aaaaa...a"
- P: "baaaaa"

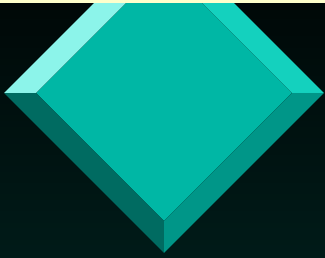


3. The Boyer-Moore Algorithm

Analysis

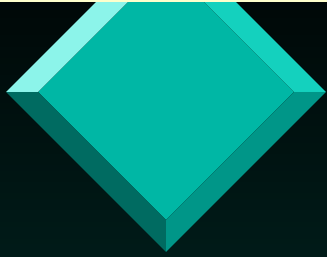
- Boyer-Moore is fast when the alphabet (A) is large, slow when the alphabet is small.
 - e.g. good for English text, poor for binary
- Boyer-Moore is *significantly faster than brute force* for searching English text.

Algorithm for searching the pattern P in text T using Boyer Moore



```
Algorithm Boyer – Moore (char T[], char P[], int n, int m)
{
    call BuildLast(P,m,L);
    int i=j = m-1;
    do {
        if (P[j] == T[i])
        {
            if (j == 0) return i; // match
            else { // looking-glass technique
                i--; j--;
            }
        }
        else { // character jump technique
            int lo = L[T[i]]; //last occurrence
            i = i + m - min(j, 1+lo);
            j = m - 1;
        }
    } while (i <= n-1);
    return -1; // no match
} // end of Boyer More
```

Algorithm for Building the Last Array Values



```
Algorithm BuildLast(char P[], int m,L)
{ // Return array storing index of last
  // occurrence of each char in pattern.
  int L[26]
  char C[26] = {a,b,c,d,e,f,g,h,i,,k,l,m,n,o,p,q,r,s,t,u,v,x,y,z}

  for(int i=0; i < 26; i++)

    L[i] = -1; // initialize array

  for (int i = 0; i< m; i++)
  { A=p[i]
    for(int j=0;j<26;j++)
      if (A==C[j]) exit;
      L[j]= i;
    }
  return(L);
} // end of BuildLast()
```