## Problem Set 10

- 1. Given NBA  $A_1, A_2$ , construct an NBA  $A_3$  such that  $L(A_3) = L(A_1) \cap L(A_2)$ .
- 2. Consider an  $\omega$ -automaton  $(Q, \Sigma, \delta, q_0, Acc)$ , and let  $\mathcal{G} \subseteq 2^Q$  be a set of good states. An  $\omega$ -word  $\alpha$  is said to be accepted iff there is a run  $\rho$  of  $\alpha$  such that  $Inf(\rho) \in \mathcal{G}$ .  $\delta: Q \times \Sigma \to 2^Q$  is the transition function.
  - Construct a deterministic  $\omega$ -automata with this acceptance condition that captures the language "Finitely many b's".
  - Show that  $\omega$ -automata with this acceptance condition captures  $\omega$ -regular languages.
  - How do you complement a deterministic  $\omega$ -automata with this acceptance condition?
- 3. Prove or disprove : A finite set of infinite words is  $\omega$ -regular.
- 4. Give an example of a language accepted by an NBA, but which cannot be written in LTL.