

A decorative graphic on the left side of the slide consisting of a network of thin, light blue lines. These lines form a complex, branching pattern that resembles a circuit board or a neural network. Some lines end in small circles, while others are open. The lines vary in thickness and are arranged in a way that creates a sense of depth and connectivity.

CSC 462: Machine Learning

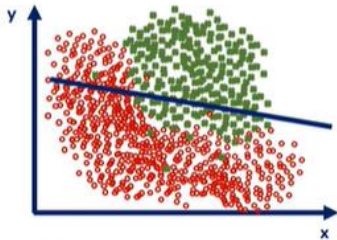
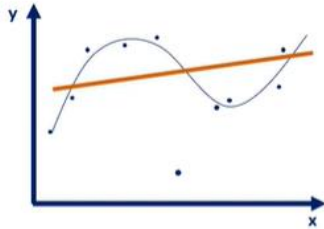
5.4 Underfitting and Overfitting

5.5 Regularization

Dr. Sultan Alfarhood

Underfitting and Overfitting

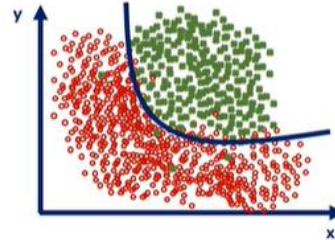
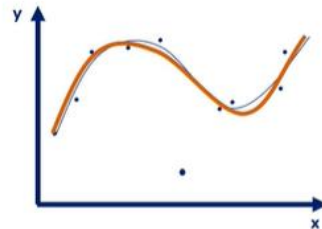
An **underfitted** model



Doesn't capture any logic

- High loss
- Low accuracy

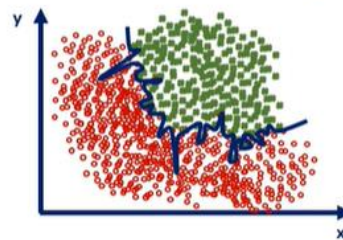
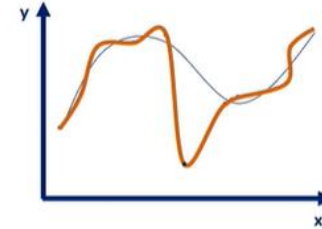
A **good** model



Captures the underlying logic of the dataset

- Low loss
- High accuracy

An **overfitted** model

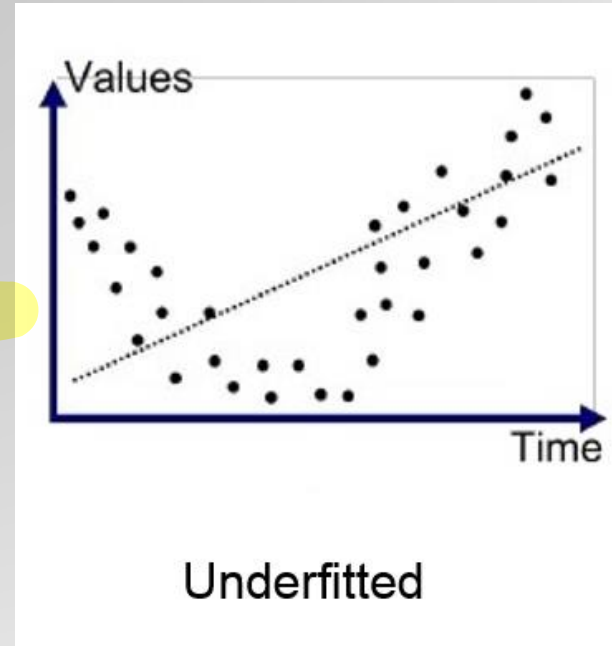


Captures all the noise, thus "misses the point"

- Low loss
- Low accuracy

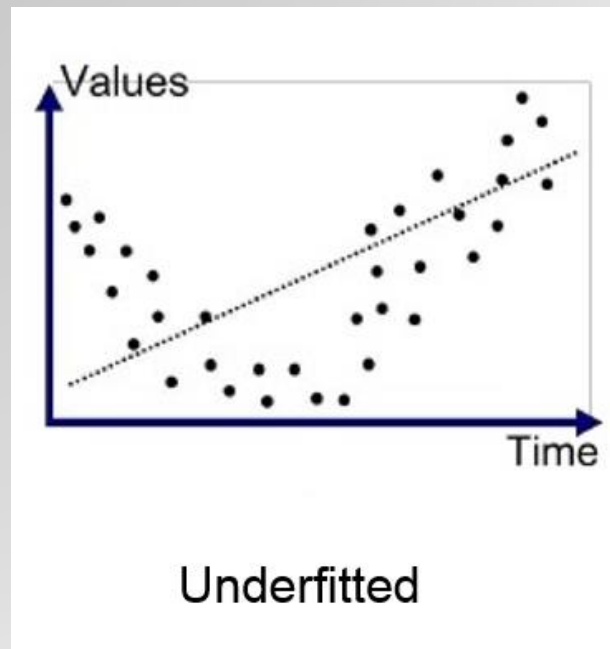
Underfitting

- Underfitting is the inability of the model to predict well the labels of the data it was trained on.



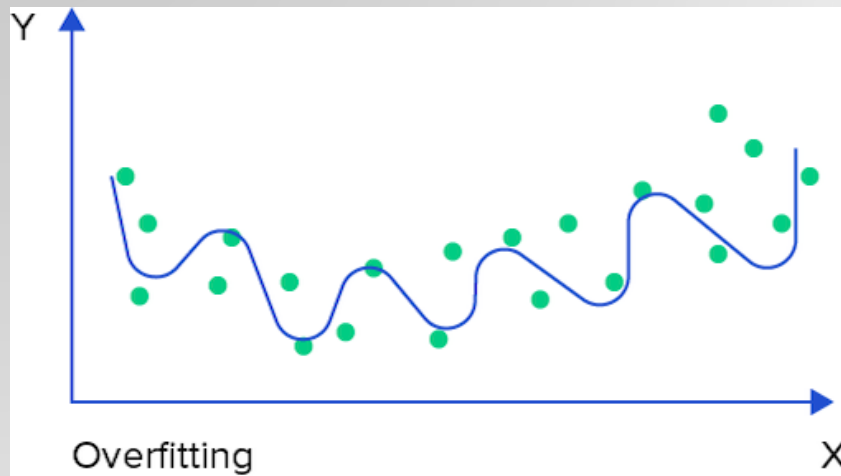
Underfitting

- There could be several reasons for underfitting, the most important of which are:
 - The **model is too simple** for the data
 - For example, a linear model can often underfit
 - The **features** you engineered are **not informative** enough
- The solution of underfitting is to try a more **complex model** or to engineer features with **higher predictive power**.



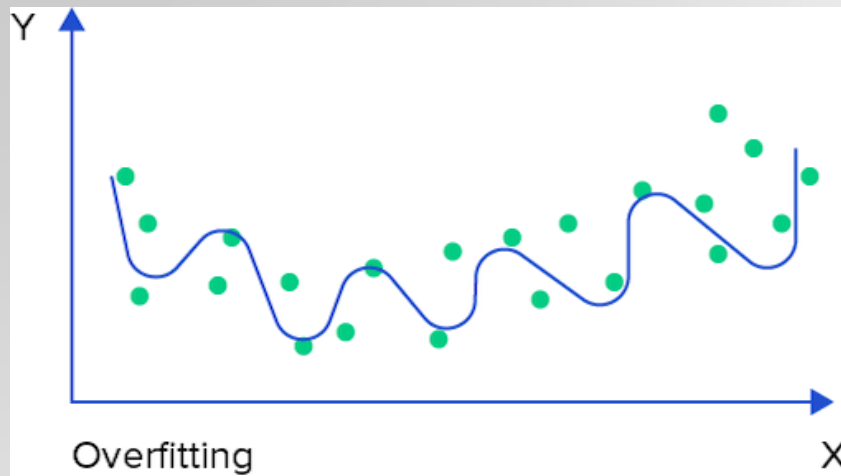
Overfitting

- The model that **overfits** predicts very well the training data but poorly the data from at least one of the two hold-out sets.
- Also referred to as the **problem of high variance**.



Overfitting

- Several reasons can lead to overfitting, the most important of which are:
 - The model is **too complex** for the data
 - For example, a very tall decision tree or a very deep or wide neural network often overfit
 - Too many features but with a small number of training examples



Overfitting

- Several solutions to the problem of overfitting are possible:

1. Try a **simpler** model

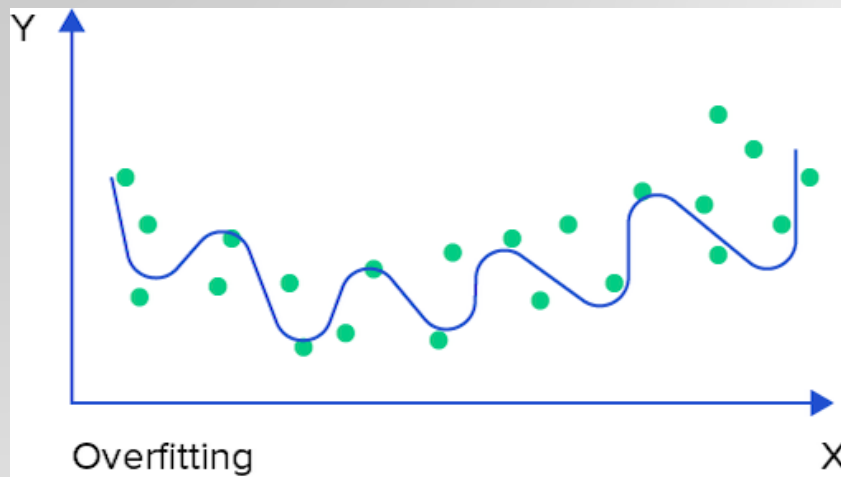
- Linear instead of polynomial regression
- SVM with a linear kernel instead of RBF
- A neural network with fewer layers/units

2. **Reduce the dimensionality** of examples in the dataset

- For example, by using one of the dimensionality reduction techniques discussed in Chapter 9

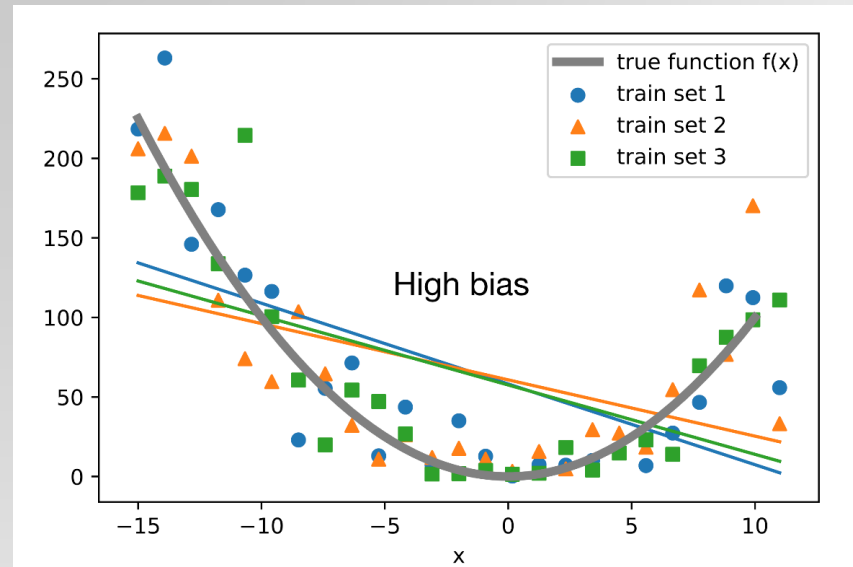
3. Add **more** training **data**, if possible

4. **Regularize** the model



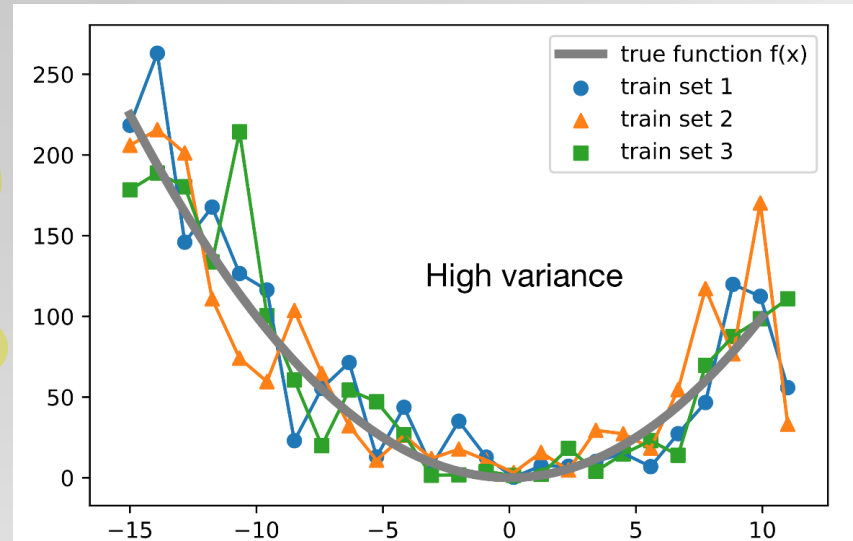
Bias

- **Bias** is the difference between the average prediction of our model and the correct value which we are trying to predict
 - If the model makes many mistakes on the training data, we say that the model has a **high bias** or that the model **underfits**
 - A model has a **low bias** if it predicts well the labels of the training data.

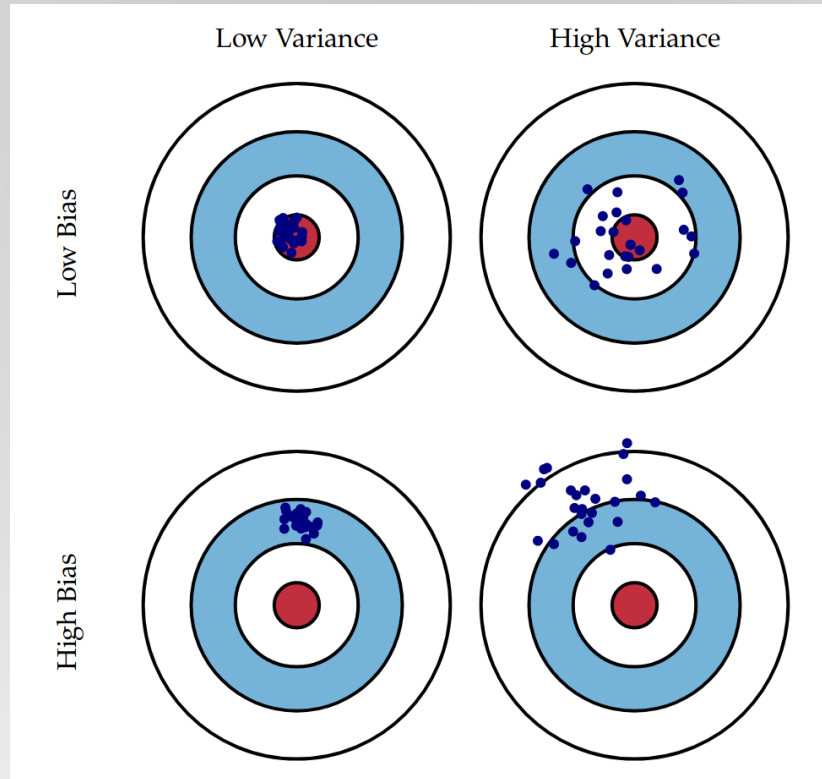


Variance

- The **variance** is an error of the model due to its sensitivity to small fluctuations in the training set
- Variance describes how much a model changes when trained using different portions of a data set.



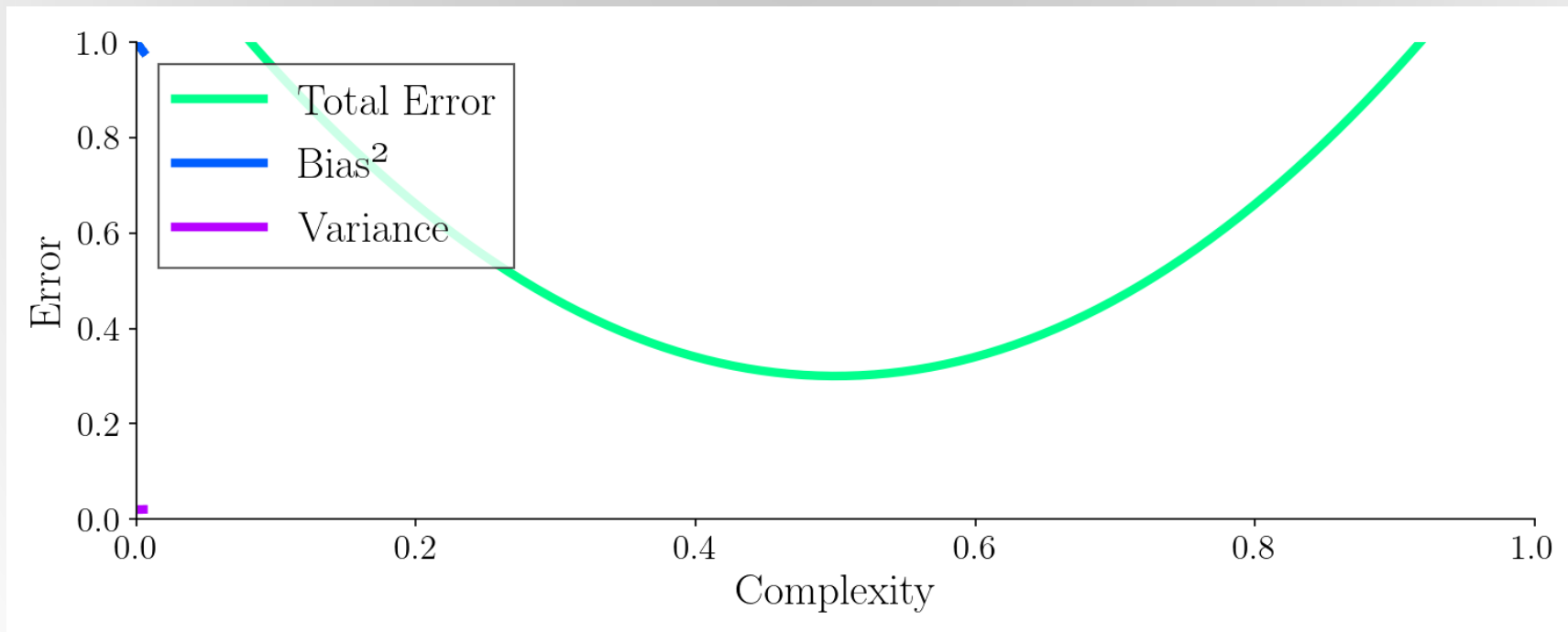
Bias & Variance



Regularization

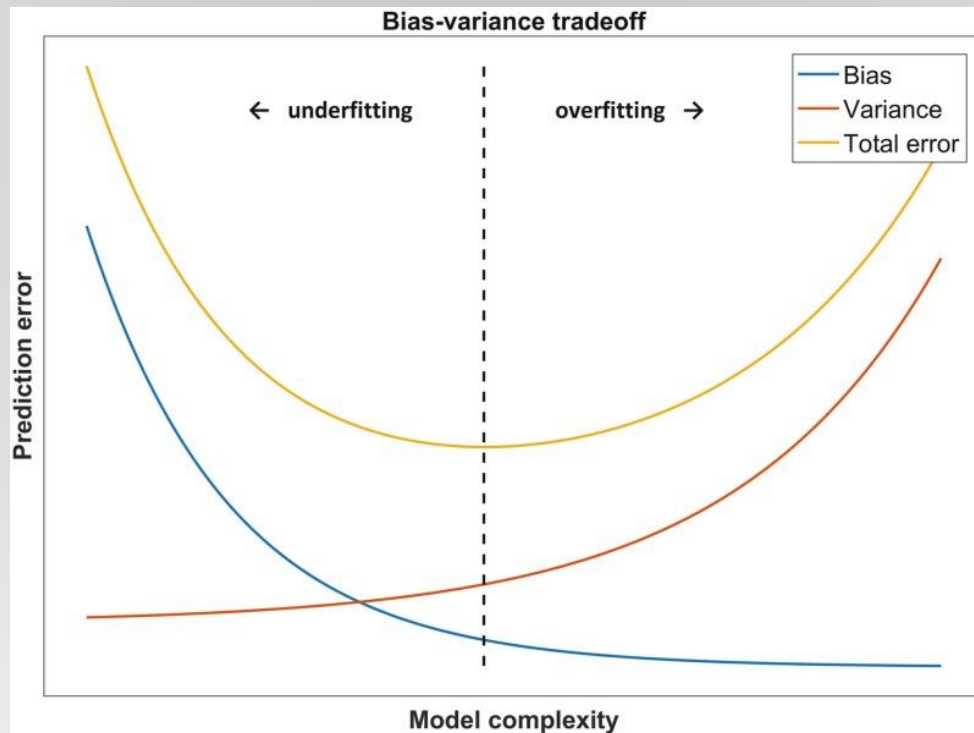
- **Regularization** is a general term that includes methods that **force the learning algorithm to build a less complex model**
 - A penalty is imposed on models, which are very complex
- In practice, that often leads to slightly higher bias but significantly reduces the variance.
 - This problem is known in the literature as the **bias-variance tradeoff**

Bias-variance Tradeoff (Animated)



- **Bias** is the difference between the average prediction of our model and the correct value which we are trying to predict
- **Variance** is an error of the model due to its sensitivity to small fluctuations in the training set

Bias-variance Tradeoff



- **Bias** is the difference between the average prediction of our model and the correct value which we are trying to predict
- **Variance** is an error of the model due to its sensitivity to small fluctuations in the training set

Regularization

$$MSE = \frac{1}{N} \sum_{i=1}^N (y_i - f_{w,b}(x_i))^2$$

- Regularization is the most widely used approach to prevent overfitting
- The two most widely used types of regularization are
 - L1 regularization (Lasso Regression)
 - L2 regularization (Ridge Regression)

$$\text{L1 objective} = \left(\frac{1}{N} \sum_{i=1}^N (y_i - f_{w,b}(x_i))^2 \right) + \left(\lambda \sum_{j=1}^D |w^j| \right)$$

$$\text{L2 objective} = \left(\frac{1}{N} \sum_{i=1}^N (y_i - f_{w,b}(x_i))^2 \right) + \left(\lambda \sum_{j=1}^D (w^j)^2 \right)$$

λ is the regularization coefficient which determines how much regularization we want.

L1 & L2 Regularization

- To create a regularized model, we modify the objective function by adding a **penalizing term** whose value is higher when the model is more complex.
- The **key difference** between these techniques is that L1 shrinks the less important feature's coefficient to zero thus, removing some feature altogether
 - So, this works well for **feature selection** in case we have a huge number of features

L1 regularization (Lasso Regression):

$$\text{L1 objective} = \left(\frac{1}{N} \sum_{i=1}^N (y_i - f_{w,b}(x_i))^2 \right) + \left(\lambda \sum_{j=1}^D |w^j| \right)$$

L2 regularization (Ridge Regression):

$$\text{L2 objective} = \left(\frac{1}{N} \sum_{i=1}^N (y_i - f_{w,b}(x_i))^2 \right) + \left(\lambda \sum_{j=1}^D (w^j)^2 \right)$$

λ is the regularization coefficient which determines how much regularization we want.

L1 & L2 Regularization

- In practice, L1 regularization produces a sparse model
 - A model that has most of its parameters equal to zero (provided the hyperparameter λ is large enough).
- L1 makes feature selection by deciding which features are essential for prediction and which are not.
 - That can be useful in case you want to increase model explainability
- However, if your only goal is to maximize the performance of the model on the hold-out data, then L2 usually gives better results.

L1 & L2 Regularization

<i>Comparison of L1 and L2 regularization</i>	
<i>L1 regularization</i>	<i>L2 regularization</i>
Sum of absolute value of weights	Sum of square of weights
Sparse solution	Non-sparse solution
Multiple solutions	One solution
Built-in feature selection	No feature selection
Robust to outliers	Not robust to outliers (due to the square term)

Regularization

