



COLLEGE OF  
**ENGINEERING, ARCHITECTURE  
AND TECHNOLOGY**



**西南交通大学**  
Southwest Jiaotong University

# INTRODUCTION TO ENGINEERING (ENGR 1111)

Joint Bachelors Degree Program of Oklahoma State University & Southwest Jiaotong University

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## Fundamental Dimensions and Units







# Fundamental Dimensions and Units

## Dimensions

Basketball player

- Q: “How **tall** are you?”
- A: “I’m 1.8 **meters** tall”.
- Dimension we consider is length (height)
- Unit used to describe the dimension **‘length’** is **meters**.
- **Dimension** describes the measurement of interest, which in the above case is *length*.
- No other “dimension to height” necessary.
- Multiple different units can be used (i.e. *feet, inch etc*)

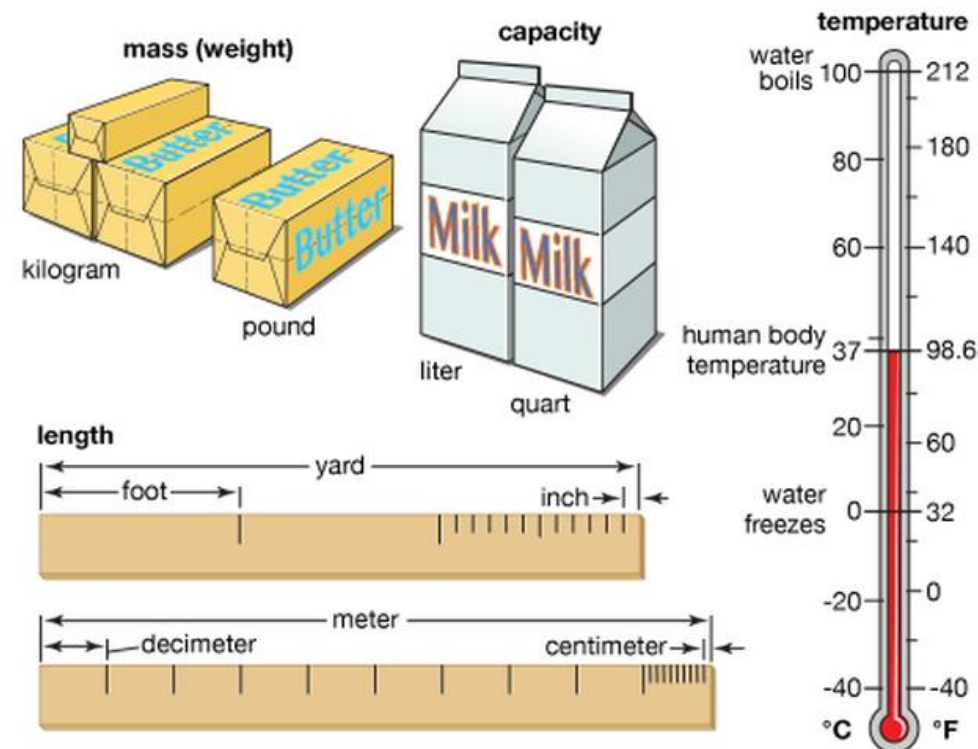


# Fundamental Dimensions and Units

## Primary Units (Base Units)

- The Primary Units are used to measure each of the fundamental dimensions.
- Two primary unit systems are predominantly used in engineering applications throughout the world:
  - International System of Units (SI units)
  - United States customary system (USCS or US System)

Customary and international system (SI) units



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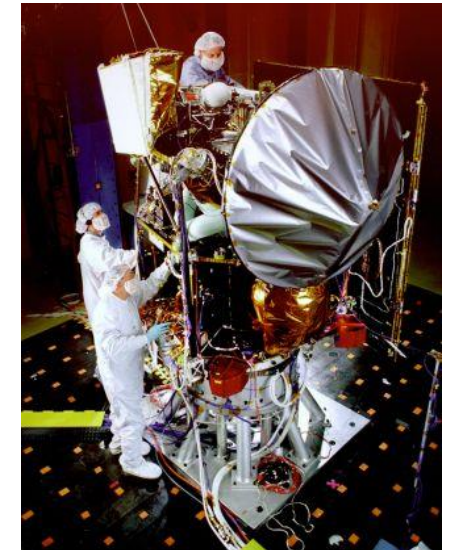
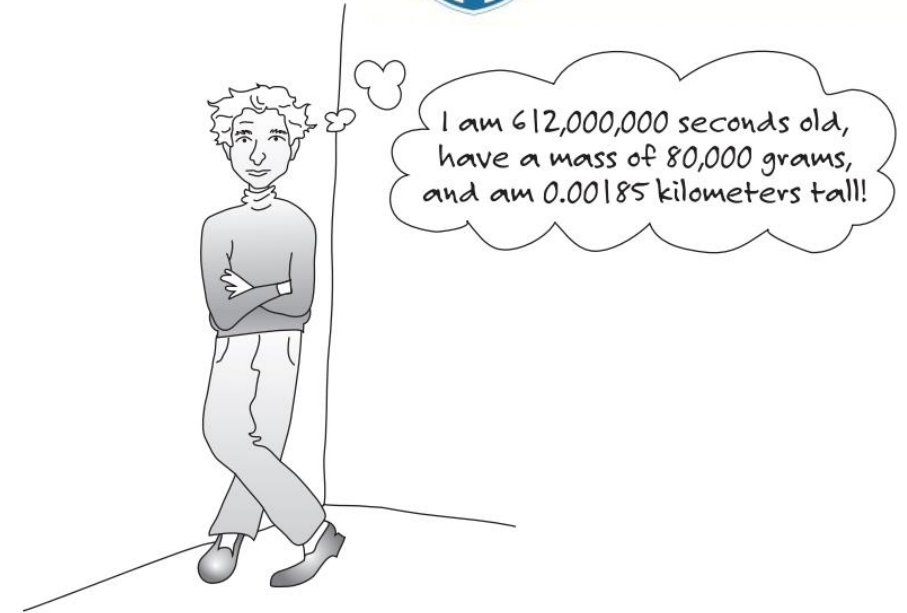
# Fundamental Dimensions and Units

## ■ Why are units important?

- A number without units has no meaning in engineering
- A number with improper units has a misleading meaning

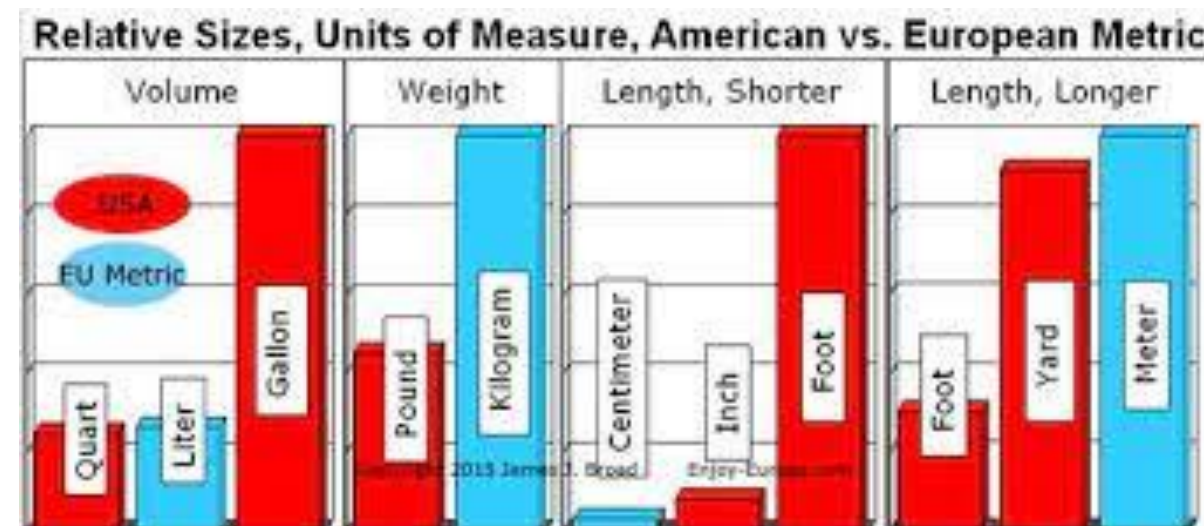
## ■ Example:

- 1999 Mars Climate Orbiter
  - Launched in December 1998, communication lost in September 1999
  - Measurement mismatch failure
  - NASA used metric while the manufacturer used US customary units



# Fundamental Dimensions and Units

- Dimensions – used to describe the measurable aspects of an object
- Units – increments necessary to quantify dimensions
- Common dimensions:
  - Length
  - Mass
  - Time
  - Temperature
- Derived units:
  - Volume
  - Density
  - concentration





# Fundamental Dimensions and Units

## Primary Units (Base Units)

### ***International System of Units (SI units)***

- Most commonly used system of measurement, except USA, Liberia, & Myanmar.
- Modern form of the metric system, built on seven base units, which correspond to the seven fundamental dimensions.
- Standard units used in medicine, science, engineering, & military



# Fundamental Dimensions and Units

## Primary Units (Base Units)

### ***United States customary system (USCS or US System)***

- The system evolved from the British Imperial unit system
- Used for measurement in commercial activities, consumer products, construction, & manufacturing



# Fundamental Dimensions and Units



## U.S. Customary Units

- In the US, most engineers still use U.S. Customary system of units

**TABLE 6.5** Examples of U.S. Customary Units in Everyday Use

Examples of U.S. Customary Unit Usage	U.S. Customary Units Used
Fuel tank capacity	20 gallons or $2.67 \text{ ft}^3$ ( $1 \text{ ft}^3 = 7.48 \text{ gallons}$ )
Sports (length of a football field)	100 yd or 300 ft
Power capacity of an automobile	150 hp or $82500 \text{ lb} \cdot \text{ft/s}$ ( $1 \text{ hp} = 550 \text{ lb} \cdot \text{ft/s}$ )
Distance between two cities	100 miles ( $1 \text{ mile} = 5280 \text{ ft}$ )



# Fundamental Dimensions and Units

## British Gravitational (BG) System

$$1\text{lb} = (1\text{slug})(1\text{ft}/\text{s}^2)$$

Primary Units	SI	BG
Mass $M$	kg	slug=32.2lbm
Length $L$	m	ft
Time $t$	s	s
Temperature $T$	°C (°K)	°F (°R)

In the BG system, the unit of temperature is expressed in °F or in terms of absolute temperature degree Rankine (°R).

$$^{\circ}\text{R} = ^{\circ}\text{F} + 459.67$$

$$T(^{\circ}\text{F}) = \frac{9}{5} T(^{\circ}\text{C}) + 32$$

$$T(^{\circ}\text{R}) = \frac{9}{5} T(\text{K})$$



# Fundamental Dimensions and Units



TABLE 6.6 Systems of Units and Conversion Factors

Dimension	System of Units			Conversion Factors
	SI	BG	U.S. Customary	
Length	Meter (m)	Foot (ft)	Foot (ft)	1 ft = 0.3048 m 1 m = 3.2808 ft
Time	Second (s)	Second (s)	Second (s)	
Mass	Kilogram (kg)	Slugs*	Pound mass (lb <sub>m</sub> )	1 lb <sub>m</sub> = 0.4536 kg 1 kg = 2.2046 lb <sub>m</sub> 1 slug = 32.2 lb <sub>m</sub>
Force	Newton (N)	$1 \text{ lb}_f^{**} = (1 \text{ slug}) \left( 1 \frac{\text{ft}}{\text{s}^2} \right)$	One pound mass***	1 N = 224.809E-3 lb <sub>f</sub>
	$1 \text{ N} = (1 \text{ kg}) \left( 1 \frac{\text{m}}{\text{s}^2} \right)$		weighs one pound force at sea level	1 lb <sub>f</sub> = 4.448 N
Temperature	Degree Celsius (°C) or Kelvin (K)**** K = °C + 273.15	Degree Fahrenheit (°F) or degree Rankine (°R) °R = °F + 459.67	Degree Fahrenheit (°F) or degree Rankine (°R) °R = °F + 459.67	°C = $\frac{5}{9} [°F - 32]$ °F = $\frac{9}{5} °C + 32$ K = $\frac{5}{9} °R$ °R = $\frac{9}{5} K$
Work, Energy	Joule (J) = (1N)(1m)	lb <sub>f</sub> ·ft = (1 lb <sub>f</sub> )(1 ft) Commonly written as ft · lb <sub>f</sub>	lb <sub>f</sub> ·ft = (1 lb <sub>f</sub> )(1 ft)	1 J = 0.7375 ft · lb <sub>f</sub> 1 ft · lb <sub>f</sub> = 1.3558 J 1 Btu = 778.17 ft · lb <sub>f</sub>
Power	Watt(W) = $\frac{1 \text{ Joule}}{1 \text{ second}}$  kW = 1000 W	$\frac{\text{lb}_f \cdot \text{ft}}{\text{second}} = \frac{(1 \text{ lb}_f)(1 \text{ ft})}{1 \text{ second}}$	$\frac{\text{lb}_f \cdot \text{ft}}{\text{second}} = \frac{(1 \text{ lb}_f)(1 \text{ ft})}{1 \text{ second}}$	1 W = $0.7375 \frac{\text{ft} \cdot \text{lb}_f}{\text{s}}$  1 hp = $550 \frac{\text{ft} \cdot \text{lb}_f}{\text{s}}$  1 hp = 0.7457 kW

\*Derived or secondary dimension

\*\*Fundamental dimension

\*\*\*Note unlike SI and BG systems, the relationship between pound force and pound mass is not defined using Newton's second law

\*\*\*\*Note a Temperature value expressed in K reads Kelvin not degree Kelvin

# Fundamental Dimensions and Units



Dimension	Symbol	SI unit	AES (USCS)
Mass	[M]	Kilogram (Kg)	Pound – mass (lbm)
Length	[L]	Meter (m)	Foot (ft)
Time	[T]	Second (s)	Second (s)
Amount of Substance	[n]	Mole (mol)	Pound-mole (lbmol)
Light intensity	[J]	Candela (cd)	Candela (cd)
Electric intensity	[I]	Ampere (A)	Ampere (A)
Temperature	[ $\theta$ ]	Kelvin (K)	Rankine ( $^{\circ}\text{R}$ )

AES: American Engineering System

USCS: United States Customary System

[ ] means “dimensions of”.











# Fundamental Dimensions and Units

Table 2.2 Commonly Used SI Unit Prefixes

Prefix name	Symbol	Factor
tera	T	$10^{12}$
giga	G	$10^9$
mega	M	$10^6$
kilo	k	$10^3$
deka	da	10
deci	d	$10^{-1}$
centi	c	$10^{-2}$
milli	m	$10^{-3}$
micro	$\mu$	$10^{-6}$
nano	n	$10^{-9}$
pico	p	$10^{-12}$

# Fundamental Dimensions and Units

## International System (SI) of Units

Physical Quantity		Name of SI Base Unit	SI Symbol
Length	 1.6 m–2.0 m Range of height for most adults	Meter	m
Mass	 50 kg–120 kg Range of mass for most adults	Kilogram	kg
Time	 Fastest person can run 100 meters in approximately 10 seconds	Second	s
Thermodynamic temperature	 Ice water: 273 kelvin Comfortable room temperature: 295 kelvin	Kelvin	K
Electric current	 120 volts 150 watts 1.25 amps	Ampere	A
Amount of substance	Uranium      238 ← One of the Gold          197      heaviest Silver        108      atoms known Copper        64 Calcium       40 Aluminum     27 Carbon        12 ← Common Carbon is Helium        4      used as a standard Hydrogen     1 ← Lightest atom	Mole	mol
Luminous intensity	 A candle has luminous intensity of approximately 1 candela	Candela	cd

*Table: A List of SI Base (Fundamental) Units*






# Fundamental Dimensions and Units


## Secondary Units (Derived Units)

Energy [=] joule [J]




$1 \text{ J} = (1 \text{ N}) (1 \text{ m})$

Power [=] watt [W]



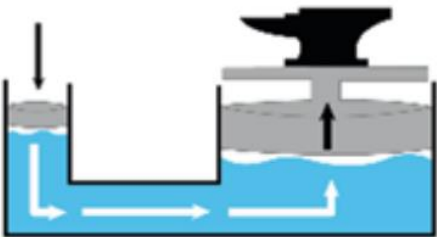
$1 \text{ W} = 1 \text{ J} / \text{s}$

Force [=] newton [N]




$1 \text{ N} = (\text{kg}) \left( 1 \frac{\text{m}}{\text{s}^2} \right)$

Pressure [=] pascal [Pa]



$1 \text{ Pa} = \frac{1 \text{ N}}{1 \text{ m}^2}$

Voltage [=] volt [V]



$1 \text{ V} = \frac{1 \text{ W}}{1 \text{ A}}$

Special names for certain derived SI units



# Fundamental Dimensions and Units

TABLE: Examples of **Derived Units** in Engineering

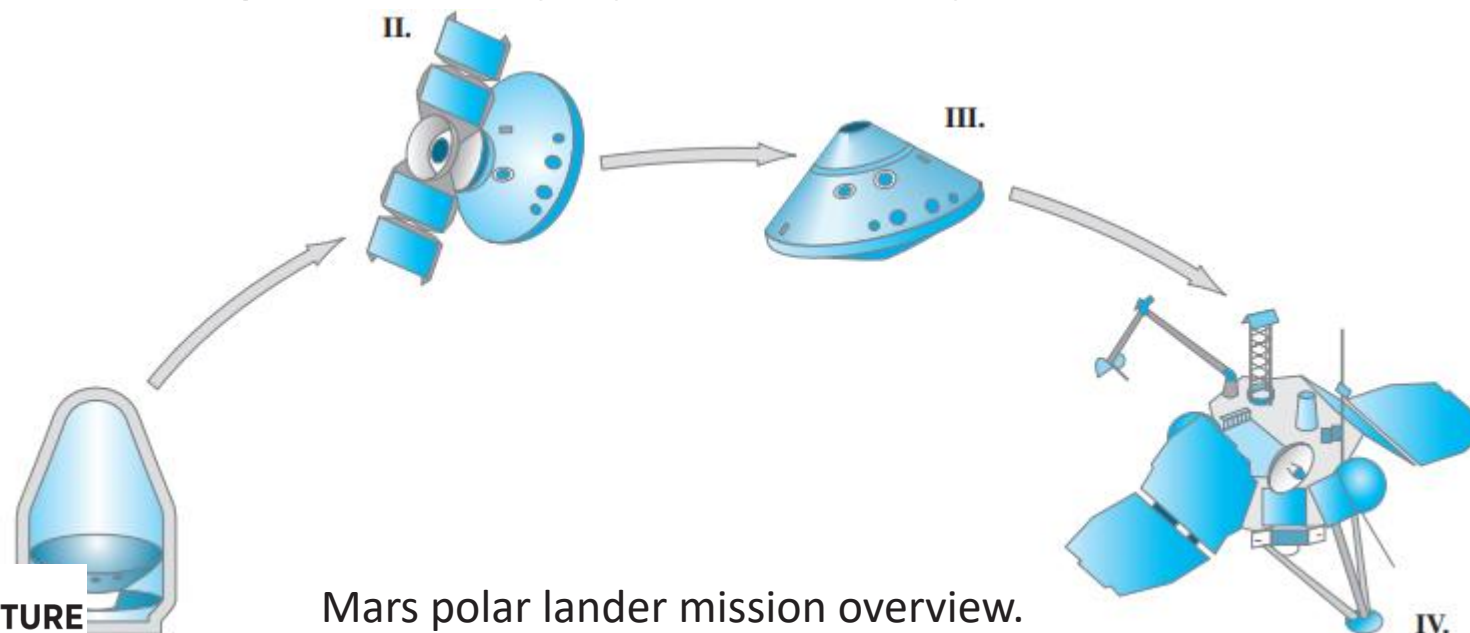
Physical Quantity	Name of SI Unit	Symbol for SI Unit	Expression in Terms of Base Units
Acceleration	Radian	rad	$\text{m/s}^2$
Angle			
Angular acceleration			$\text{rad/s}^2$
Angular velocity			$\text{rad/s}$
Area	Joule	J	$\text{m}^2$
Density			$\text{kg/m}^3$
Energy, work, heat			$\text{N}\cdot\text{m}$ or $\text{kg}\cdot\text{m}^2/\text{s}^2$
Force			$\text{kg}\cdot\text{m}/\text{s}^2$
Frequency	Hertz	Hz	$\text{s}^{-1}$
Impulse	Watt	W	$\text{N}\cdot\text{s}$ or $\text{kg}\cdot\text{m}/\text{s}$
Moment or torque			$\text{N}\cdot\text{m}$ or $\text{kg}\cdot\text{m}^2/\text{s}^2$
Momentum			$\text{kg}\cdot\text{m}/\text{s}$
Power			$\text{J/s}$ or $\text{N}\cdot\text{m}/\text{s}$ or $\text{kg}\cdot\text{m}^2/\text{s}^3$
Pressure, stress	Pascal	Pa	$\text{N}/\text{m}^2$ or $\text{kg}/\text{m}\cdot\text{s}^2$
Velocity	Coulomb	C	$\text{m/s}$
Volume			$\text{m}^3$
Electric charge			$\text{A}\cdot\text{s}$
Electric potential			$\text{J/C}$ or $\text{m}^2\cdot\text{kg}/(\text{s}^3\cdot\text{A}^2)$
Electric resistance	Ohm	$\Omega$	$\text{V/A}$ or $\text{m}^2\cdot\text{kg}/(\text{s}^3\cdot\text{A}^2)$
Electric conductance	Siemens	S	$1/\Omega$ or $\text{s}^3\cdot\text{A}^2/(\text{m}^2\cdot\text{kg})$
Electric capacitance	Farad	F	$\text{C/V}$ or $\text{s}^4\cdot\text{A}^2/(\text{m}^2\cdot\text{kg})$
Magnetic flux density	Tesla	T	$\text{V}\cdot\text{s}/\text{m}^2$ or $\text{kg}/(\text{s}^2\cdot\text{A})$
Magnetic flux	Weber	Wb	$\text{V}\cdot\text{s}$ or $\text{m}^2\cdot\text{kg}/(\text{s}^2\cdot\text{A})$
Inductance	Henry	H	$\text{V}\cdot\text{s}/\text{A}$
Radioactivity	Gray	Gy	$\text{J/kg}$ or $\text{m}^2/\text{s}^2$

- Unit for force is the *Newton* (N)
- Newton is derived from Newton's second law of motion.
- 1N is a magnitude of a force that when applied to 1 kg of mass, will accelerate the mass at a rate of  $1 \text{ m/s}^2$
- **$1\text{N} = (1\text{kg})(1\text{m/s}^2)$**

# Fundamental Dimensions and Units

## Unit Conversion

- NASA lost a spacecraft called Mars Climate Orbiter because two groups of engineers working on the project neglected to communicate correctly their calculations with appropriate units.
- One team used U.S. Customary units (e.g., ft and lb) while other used SI units (e.g., m and kg) for a key spacecraft operation.



Mars polar lander mission overview.



CONVERSION FACTORS		
Quantity	SI → U.S. Customary	U.S. Customary → SI
<b>Length</b>	$1 \text{ mm} = 0.03937 \text{ in.}$ $1 \text{ mm} = 0.00328 \text{ ft}$  $1 \text{ cm} = 0.39370 \text{ in.}$ $1 \text{ cm} = 0.0328 \text{ ft}$  $1 \text{ m} = 39.3700 \text{ in.}$ $1 \text{ m} = 3.28 \text{ ft}$	$1 \text{ in.} = 25.4 \text{ mm}$ $1 \text{ ft} = 304.8 \text{ mm}$  $1 \text{ in.} = 2.54 \text{ cm}$ $1 \text{ ft} = 30.48 \text{ cm}$  $1 \text{ in.} = 0.0254 \text{ m}$ $1 \text{ ft} = 0.3048 \text{ m}$
<b>Area</b>	$1 \text{ mm}^2 = 1.55\text{E-}3 \text{ in}^2$ $1 \text{ mm}^2 = 1.0764\text{E-}5 \text{ ft}^2$  $1 \text{ cm}^2 = 0.155 \text{ in}^2$ $1 \text{ cm}^2 = 1.07\text{E-}3 \text{ ft}^2$  $1 \text{ m}^2 = 1550 \text{ in}^2$ $1 \text{ m}^2 = 10.76 \text{ ft}^2$	$1 \text{ in}^2 = 645.16 \text{ mm}^2$ $1 \text{ ft}^2 = 92,903 \text{ mm}^2$  $1 \text{ in}^2 = 6.4516 \text{ cm}^2$ $1 \text{ ft}^2 = 929.03 \text{ cm}^2$  $1 \text{ in}^2 = 6.4516\text{E-}4 \text{ m}^2$ $1 \text{ ft}^2 = 0.0929 \text{ m}^2$
<b>Volume</b>	$1 \text{ mm}^3 = 6.1024\text{E-}4 \text{ in}^3$ $1 \text{ mm}^3 = 3.5315\text{E-}8 \text{ ft}^3$  $1 \text{ cm}^3 = 0.061024 \text{ in}^3$ $1 \text{ cm}^3 = 3.5315\text{E-}5 \text{ ft}^3$  $1 \text{ m}^3 = 61024 \text{ in}^3$ $1 \text{ m}^3 = 35.315 \text{ ft}^3$	$1 \text{ in}^3 = 16387 \text{ mm}^3$ $1 \text{ ft}^3 = 28.317\text{E}6 \text{ mm}^3$  $1 \text{ in}^3 = 16.387 \text{ cm}^3$ $1 \text{ ft}^3 = 28317 \text{ cm}^3$  $1 \text{ in}^3 = 1.6387\text{E-}5 \text{ m}^3$ $1 \text{ ft}^3 = 0.028317 \text{ m}^3$
<b>Second Moment of Area (length)<sup>4</sup></b>	$1 \text{ mm}^4 = 2.402\text{E-}6 \text{ in}^4$ $1 \text{ mm}^4 = 115.861\text{E-}12 \text{ ft}^4$  $1 \text{ cm}^4 = 24.025\text{E-}3 \text{ in}^4$ $1 \text{ cm}^4 = 1.1586\text{E-}6 \text{ ft}^4$  $1 \text{ m}^4 = 2.40251\text{E}6 \text{ in}^4$ $1 \text{ m}^4 = 115.86 \text{ ft}^4$	$1 \text{ in}^4 = 416.231\text{E}3 \text{ mm}^4$ $1 \text{ ft}^4 = 8.63097\text{E}9 \text{ mm}^4$  $1 \text{ in}^4 = 41.623 \text{ cm}^4$ $1 \text{ ft}^4 = 863110 \text{ cm}^4$  $1 \text{ in}^4 = 416.231\text{E-}9 \text{ m}^4$ $1 \text{ ft}^4 = 8.631\text{E-}3 \text{ m}^4$





CONVERSION FACTORS (Continued)

Quantity	SI → U.S. Customary	U.S. Customary → SI
Mass	1 kg = 68.521E-3 slug 1 kg = 2.2046 lb <sub>m</sub>	1 slug = 14.593 kg 1 lb <sub>m</sub> = 0.4536 kg
Density	1 kg/m <sup>3</sup> = 0.001938 slug/ft <sup>3</sup> 1 kg/m <sup>3</sup> = 0.06248 lb <sub>m</sub> /ft <sup>3</sup>	1 slug/ft <sup>3</sup> = 515.7 kg/m <sup>3</sup> 1 lb <sub>m</sub> /ft <sup>3</sup> = 16.018 kg/m <sup>3</sup>
Force	1 N = 224.809E-3 lb <sub>f</sub>	1 lb <sub>f</sub> = 4.448 N
Moment	1 N·m = 8.851 in·lb 1 N·m = 0.7376 ft·lb	1 in·lb = 0.113 N·m 1 ft·lb = 1.356 N·m
Pressure, Stress, Modulus of Elasticity, Modulus of Rigidity	1 Pa = 145.0377E-6 lb/in <sup>2</sup> 1 Pa = 20.885E-3 lb/ft <sup>2</sup> 1 kPa = 145.0377E-6 ksi	1 lb/in <sup>2</sup> = 6.8947E3 Pa 1 lb/ft <sup>2</sup> = 47.880 Pa 1 ksi = 6.8947E3 kPa
Work, Energy	1 J = 0.7375 ft·lb 1 kWh = 3.41214E3 Btu	1 ft·lb = 1.3558 J 1 Btu = 293.071E-6 kWh
Power	1 W = 0.7375 ft·lb/s 1 kW = 3.41214E3 Btu/h 1 kW = 1.341 hp	1 ft·lb/s = 1.3558 W 1 Btu/h = 293.07E-6 kW 1 hp = 0.7457 kW
Temperature	°C = $\frac{5}{9}$ (°F - 32)	°F = $\frac{9}{5}$ °C + 32

# Fundamental Dimensions and Units



## ■ Significant Figures

- Measurements are uncertain, therefore only meaningful numbers are used.
- Three rules in determining significant figures:
  - Non-zero digits are always significant.
  - Any zeros between two significant digits are significant.
  - A final zero or trailing zeros in the decimal portion ONLY are significant.

## Significant Figures Rules

Significant Figures can be done using a set of around 5 rules, With a lot of complications for how to deal with zeroes.

Not significant:

zero for  
“cosmetic”  
purpose

Not significant:

zeros used only  
to locate the  
decimal point

Significant:

all zeros between  
nonzero numbers

Significant:

all nonzero  
integers

Significant:

zeros at the end of  
a number to the right  
of decimal point

0 . 0 0 4 0 0 4 5 0 0



# Fundamental Dimensions and Units

## ■ Significant Figures

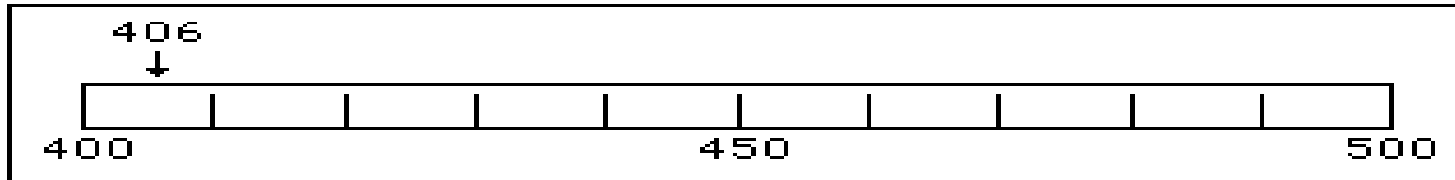
- Non-zero digits are always significant.
  - How many significant figures are in the following?
    - 25.74
      - 4 sig figs
    - 66.4
      - 3 sig figs
    - 7.3
      - 2 sig figs
    - 12.5
      - 3 sig figs



# Fundamental Dimensions and Units

## ■ Significant Figures

- Any zeros between two significant digits are significant.
- Given the number 406, how many numbers are significant?







# Fundamental Dimensions and Units

## ■ Significant Figures

- A final zero or trailing zeros in the decimal portion ONLY are significant.
  - How many significant figures are in the following?
    - 0.00600 – 3 sig figs
    - 0.03040
      - 4 sig figs
    - $2.50 \times 10^{-5}$ 
      - 3 sig figs
    - $4.300 \times 10^{14}$ 
      - 4 sig figs



# Fundamental Dimensions and Units

## ■ Significant Figures

### ■ Addition and Subtraction

- Count the number of significant figures in the decimal portion of each number in the problem.
- Add or subtract in the normal fashion.
- Round the answer to the LEAST number of places in the decimal portion of any number in the problem

$$\begin{array}{r} 101.25 \\ + 3536.2 \\ + 123.448 \\ \hline 3760.898 \end{array}$$

least precise number, only one digit after decimal

digits to be dropped

last digit retained

answer round to one digit after the decimal

**3760.9**

$$\begin{array}{r} 85.6 \\ 7.25 \\ 95.7 \\ + 0.5 \\ \hline 189.05 = 189.1 \end{array}$$

3 sig figs

3 sig figs

3 sig figs

1 sig fig

**4 sig figs**

# Fundamental Dimensions and Units

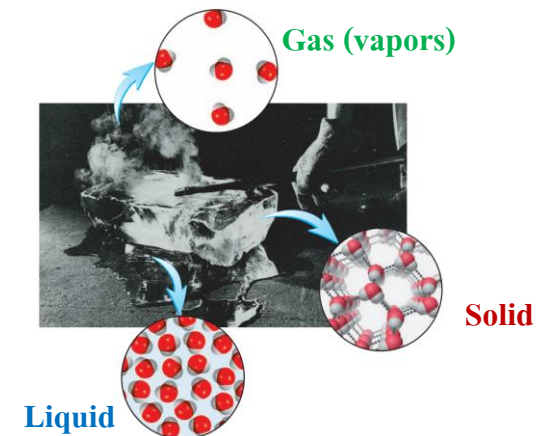
- **Density** – the ratio of mass to a unit volume

$$\rho = \frac{m}{V}$$

- Where,

- $\rho$  = density, kg/m<sup>3</sup>
- $m$  = mass, kg
- $V$  = volume, m<sup>3</sup>

- Density is independent of sample size but varies with temperature or the concentration of impurities
- Example: saltwater vs fresh water





# Fundamental Dimensions and Units

## Density

Table 2.4 Densities of Common Substances

Substance	Density (g/cm <sup>3</sup> )
Air @ STP	0.001293
Southern pine	0.65
Gasoline	0.72
Ethanol	0.802
Ice @ 0°C	0.92
Water @ 4°C	1.00
Rubber	1.5
Glass	2.6
Aluminum	2.7
Wrought iron	7.6
Uranium	18.7



# Fundamental Dimensions and Units



## Density

### ■ Example 1:

- A 2 L graduated cylinder initially contains 500 ml of water. An irregularly shaped object having a mass of 105 g is submerged into the water. The final volume of the water in the cylinder is 1025 ml. Determine the density of the object.

### Solution:

V1 H<sub>2</sub>O: 500 mL

V2 H<sub>2</sub>O: 1025 mL

Volume of the object = V1 – V2 = 1025 mL – 500 mL = 525 mL

Mass of the object: 105 g

$$\rho = m/V = 105 \text{ g}/525 \text{ mL} = \mathbf{0.20 \text{ g/mL}}$$



## Density

### ■ Example 2:

During an environmental assessment of a natural wetland in the Everglades, it was determined that 1.5 cubic meters of the dry native soil had a mass of 420 kg.

Determine the mass of a cubic foot of that same soil.

### Solution:

Volume of soil: 1.5 cubic meters ( $\text{m}^3$ )

Mass of soil: 420 kg

$$\rho = m/V = 420 \text{ kg}/1.5 \text{ m}^3 = 280 \text{ kg}/\text{m}^3$$

$$\text{Density (kg}/\text{ft}^3) = \frac{280 \text{ kg}/\text{m}^3}{35.3147 \text{ ft}^3/\text{m}^3} = 7.92 \text{ kg}/\text{ft}^3$$

$$1\text{m}^3 = 35.3147 \text{ ft}^3$$

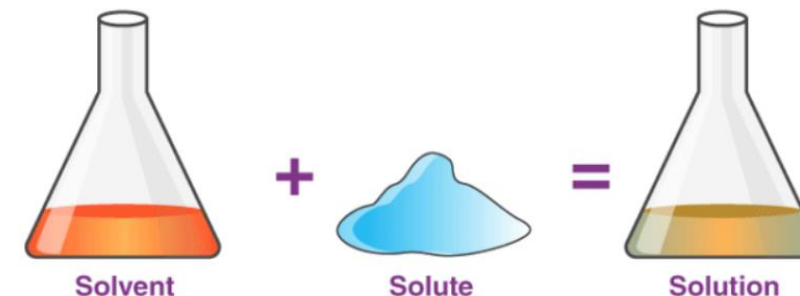
# Fundamental Dimensions and Units

## ■ Concentration –

- The amount of a substance in a defined space.
- The ratio of solute in a solution to either solvent or total solution.
- Concentration is often described on a mass-per-unit-volume basis

$$C = \frac{m}{V}$$

- Where,
  - $C$  = concentration of dissolved substance,  $mg/L$
  - $m$  = mass of solute or dissolved substance,  $mg$
  - $V$  = total volume,  $L$



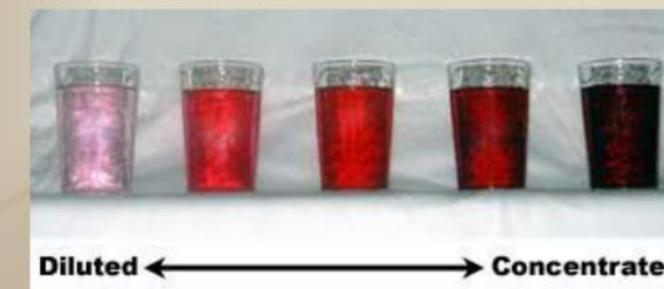
## Solution Concentration

Solution Concentration is the measure of how much solute is dissolved in a specific amount of solvent.

Solutions can be described qualitatively using words **concentrated** and **dilute**.

-A **concentrated** solution would have a lot of solute compared to the amount of solvent.

-A **dilute** solution would have very little solute compared to the amount of solvent.





# Fundamental Dimensions and Units

## Concentration –

### CALCULATING CONCENTRATION OF SOLUTIONS

1. Mass Percent = (mass of solute/mass of solution)100
2. Parts per million = (mass of solute/mass of solution)10<sup>6</sup>
3. Mass/volume percent = (mass of solute/mL solution)100
4. Volume percent = (mL solute / mL solution)100
5. Molarity = moles solute / L solution

- A 350 mL sample of drinking water was analyzed and found to contain 0.0046 g of sulfate salts. Calculate the concentration of sulfate salts in this water sample?
- $\text{Mass}_{\text{water}} = \text{density}_{\text{water}} (\text{Volume}_{\text{water}})$   
 $= 1.00 \text{ g/mL} (350 \text{ mL})$   
 $= 350 \text{ g solution}$   
 $\text{ppm} = (\text{mass}_{\text{solute}} / \text{mass}_{\text{solution}}) 10^6$   
 $\text{ppm} = (0.0046 \text{ g} / 350 \text{ g}) 10^6$   
 $\text{ppm} = 13 \text{ ppm}$





# Fundamental Dimensions and Units

## ■ Mass-per-unit-mass basis

- The most common mass-based units are parts per million (ppm) and parts per billion (ppb).
- For perspective, the maximum contaminant level goal (MCLG) of mercury in drinking water allowed by the Environmental Protection Agency (EPA) is 0.002 ppm. This means that there can be no more than 0.002 grams of mercury in every million grams of drinking water purified and distributed by your local municipality.
- Assuming the density of water is 1.0 g/ml, this is equivalent to allowing only 2 grams of mercury in approximately 264,000 gallons of drinking water.



## Mass-per-unit-mass basis

### ■ Example 3:

- In many environmental aqueous systems, it is appropriate to make the simplifying assumption that 1 mg/L is equal to 1 ppm, provided that the fluid in question is primarily water, so that the density of the solution is essentially 1 g/ml. Show that 1 mg/L = 1 ppm.

### Solution:

Converting mg/L to ppm

1 mg/L:

Mass of solute: 1 mg = 0.001 g

Volume of solution: 1 L = 1 kg (since the density of water is 1 mg/L)

$$\text{ppm} = \frac{\text{mass of solute (g)}}{\text{mass of solution (g)}} \times 10^6$$

$$\text{ppm} = \frac{0.001 \text{ g}}{1000 \text{ g}} \times 10^6 = 1$$

$$1 \text{ mg/L} = 1 \text{ ppm}$$



# Fundamental Dimensions and Units

- **Molarity** ( $M$  = moles per liter) – one mole per unit volume of substance
  - Avogadro's number defines a mole (mol)
    - $6.02 \times 10^{23}$  molecules of any material per mole
  - The atomic mass of an element or substance is equal to the mass of one mole of that substance



## Concentrations of Solutions

- **Molarity (M):** the number of moles of solute per liter of solution
- **Molarity =  $\frac{\text{moles of solute}}{\text{volume of solution in liters}}$**
- **6.0 M HCl**
  - 6.0 moles of HCl per liter of solution.
- **9.0 M HCl**
  - 9.0 moles of HCl per liter of solution.



# Fundamental Dimensions and Units

## ■ Mass Percent and Volume Percent

- Mass percent of species A:

$$\text{mass A (\%)} = \frac{M_A}{M_A + M_B} \times 100$$

- Where,

- $M_A$  = mass of compound A, lb<sub>m</sub> (g)

- $M_A + M_A$  = total mass of the solution, lb<sub>m</sub> (g)

## ■ Mass Percent and Volume Percent

- Volume percent of species A:

$$x_A = \frac{\text{moles A in solution}}{\text{total moles of solution}}$$





# Mass Percent and Volume Percent

## Mass Percent

- Parts of solute in every 100 parts solution.
  - ✓ If a solution is 0.9% by mass, then there are 0.9 grams of solute in every 100 grams of solution.
    - Or 10 kg solute in every 100 kg solution.
- Since masses are additive, the mass of the solution is the sum of the masses of solute and solvent.

$$\text{Mass Percent} = \frac{\text{Mass of Solute, g}}{\text{Mass of Solution, g}} \times 100\%$$

$$\text{Mass of Solute} + \text{Mass of Solvent} = \text{Mass of Solution}$$

## Percent by Volume

Percent volume is the solution concentration that is the volume of solute divided by volume of solution, multiplied by 100.

$$\text{vol\%} = \frac{\text{volume of solute}}{\text{volume of solution}} \times 100$$

Find the vol% of a solution of 5.0 ml HCl diluted to 100 ml with water.

$$\begin{aligned}\text{vol\%} &= 5.0 \text{ ml} / 100 \text{ ml} \times 100 \\ \text{vol\%} &= 5.0\%\end{aligned}$$

Percent volume is also called vol% or % v/v.





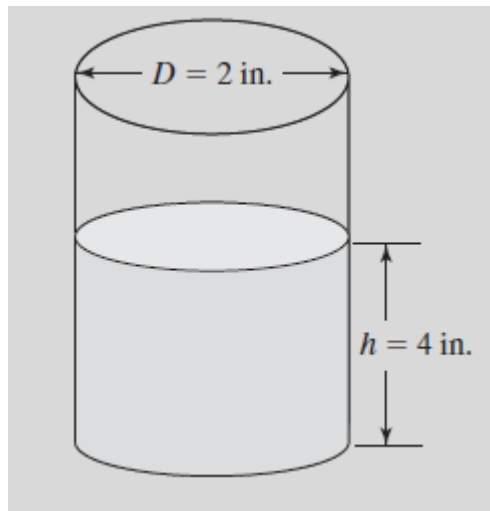


# Mass Percent and Volume Percent

## Example 4:

- A researcher has added 2.06 g of the salt sodium nitrate to a cylinder containing water. The cylinder diameter is 2 inches and the depth of the water in the cylinder is 4 inches. Determine the concentration of salt in solution, showing your answer in the units specified.

- a) mg/L
- b) mass %
- c) molarity



Mass of  $\text{NaNO}_3$ :  $2.06 \text{ g} = 2060 \text{ mg}$

Diameter of cylinder: 2 in

Water depth (h): 4 in

Radius (r) :  $2 \text{ in} / 2 = 1 \text{ in} = 2.54 \text{ cm}$

Water depth (h):  $4 \text{ in} = 4 * 2.54 = 10.16 \text{ cm}$

$$V = \pi r^2 h$$

$$\pi = 31.4$$

$$V = 206.23 \text{ cm}^3 = 206.23 \text{ mL} = 0.20623 \text{ L}$$

a) mg/L

$$\text{Concentration} = 2060 \text{ mg} / 0.20623 \text{ L}$$

$$= 9997.66 \text{ mg/L}$$

b) Mass

$$\text{Mass (\%)} = \text{Mass of solute} / \text{Mass of solution} * 100$$

$$\text{Mass of water} = 206.23 \text{ mL} * 1 \text{ g/mL} = 206.23 \text{ g}$$

$$\text{Mass of solution} = 206.23 \text{ g} + 2.06 \text{ g} = 208.29 \text{ g}$$

$$\text{Mass \%} = 2.06 \text{ g} / 208.29 \text{ g} * 100 = 0.988\%$$

c) Molarity

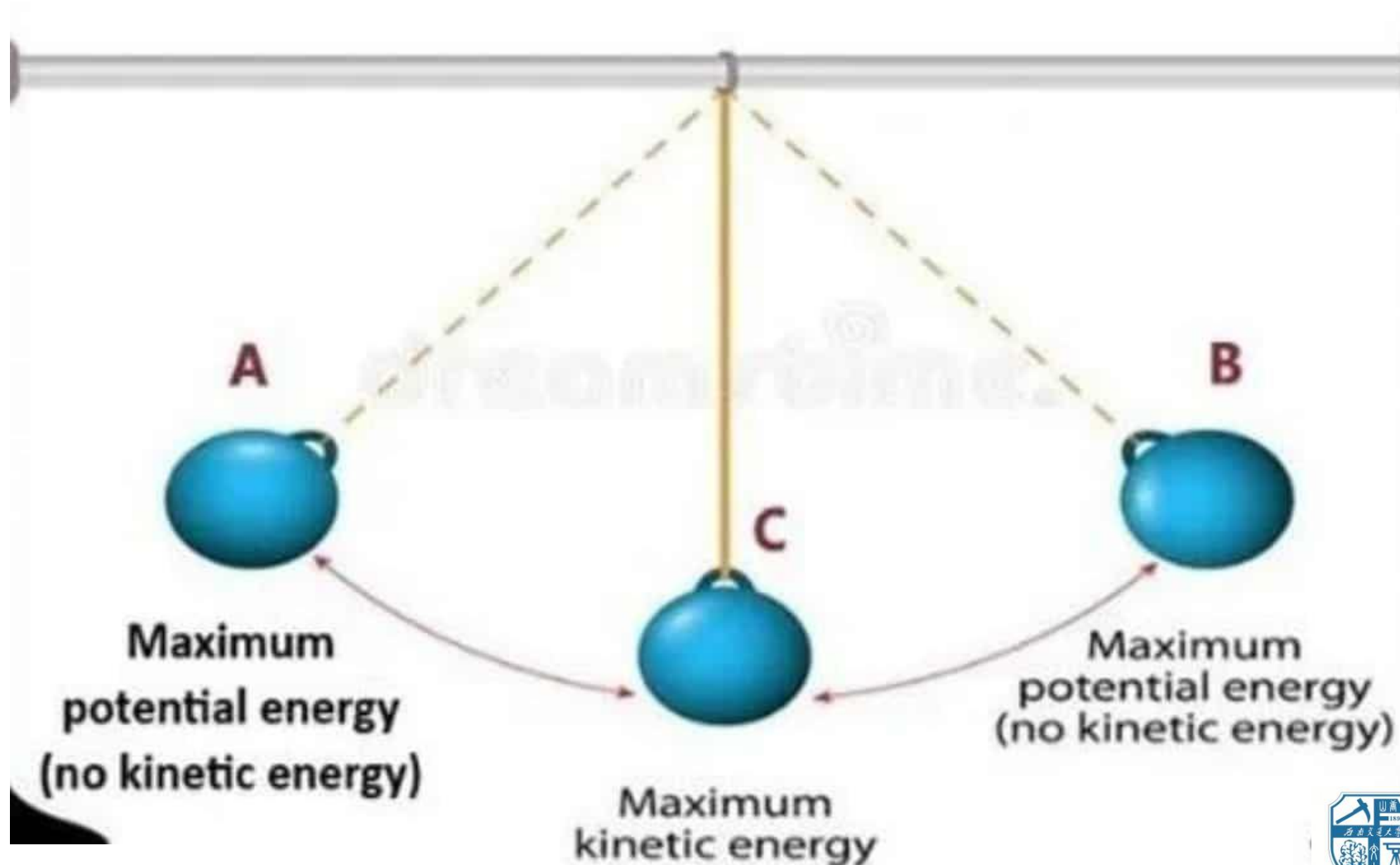
$$0.02424 \text{ mol} / 0.20623 \text{ L} = 0.1176 \text{ M}$$

# Physical Laws and Observations in Engineering

- Engineers apply physical and chemical laws and principles along with mathematics to design, develop, test, and mass-produce products and services that we use in our everyday lives.
- Physical laws are based on observations



# Conservation of energy

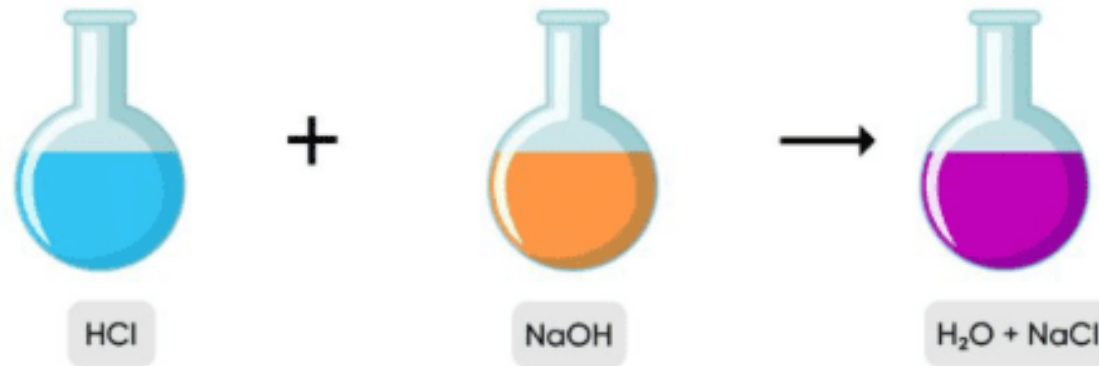




## Conservation of Mass



### LAW OF CONSERVATION OF MASS



#### The Law of Conservation of Mass

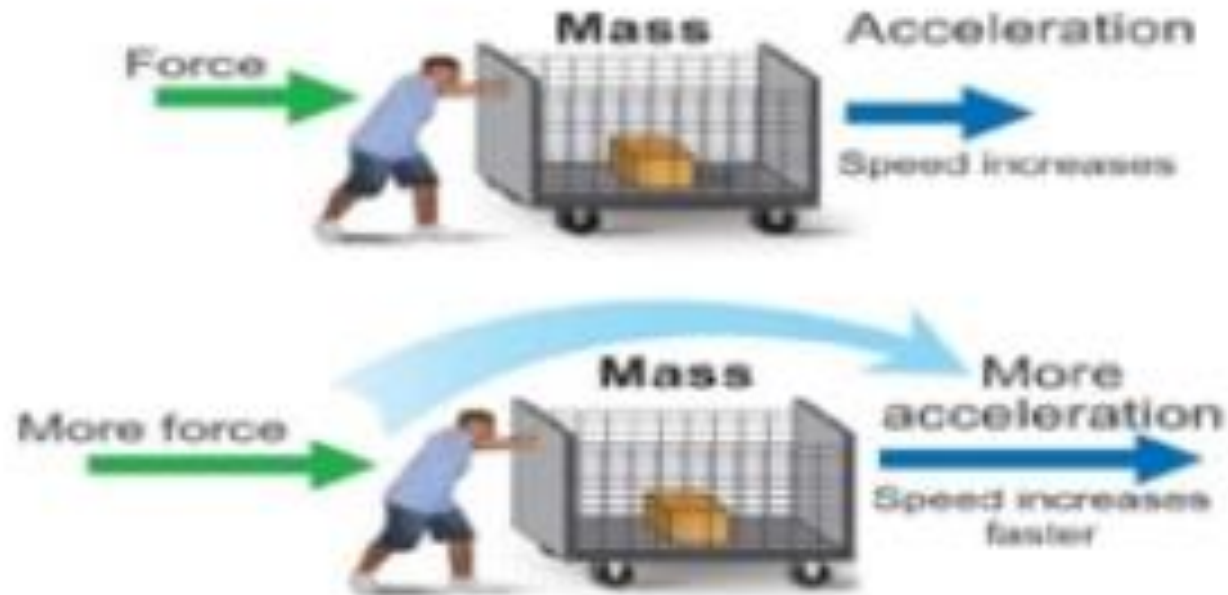
$$\text{mass}_{\text{reactants}} = \text{mass}_{\text{products}}$$

Mass is conserved in a chemical reaction; products have the same mass as reactants.

The law of conservation of mass states that mass is neither created nor destroyed during a chemical reaction—it is conserved.

# Newton's Second Law

- If you apply more force to an object, it accelerates at a higher rate.







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# Thank you