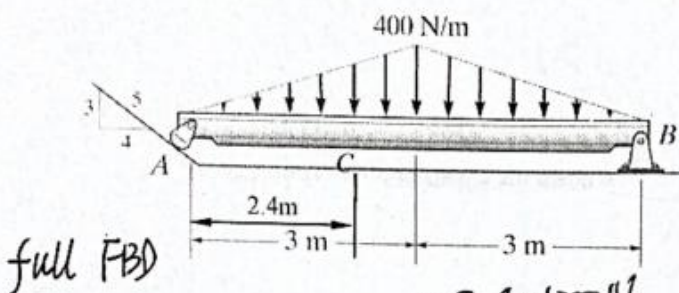


Chinese Name: \_\_\_\_\_ English Name: \_\_\_\_\_  
ID#: \_\_\_\_\_

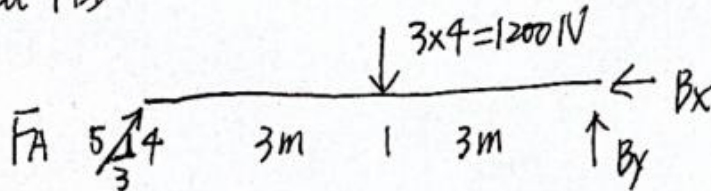
### ENSC 2113 – Fall 2023 – Sample EXAM #3

EACH PROBLEM IS WORTH THE POINTS INDICATED. BOX YOUR ANSWERS AND PROVIDE PROPER UNITS, WHERE APPLICABLE. CALCULATIONS AND FREE BODY DIAGRAMS MUST BE SHOWN THAT SUPPORT THE ANSWER TO RECEIVE CREDIT.

1. Determine the internal shear, moment, and axial force at point C. Point A is a rocker and point B is a pin. Draw all pertinent free-body diagrams. 25 POINTS



对于内力, 结果只  
标明正负, 无需  
指明方向, 因为它们  
是成对的。

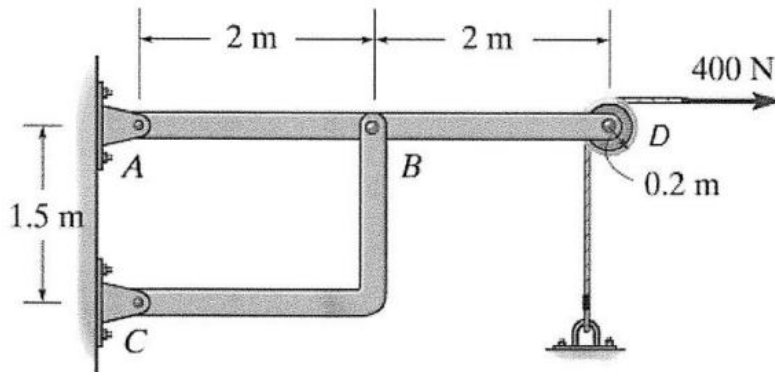


$$\begin{aligned} \sum M_A(\vec{F}) = 0 &= -1200 \times 3 + B_y \cdot 6 = 0 & B_y &= 600 \text{ N} (\uparrow) \\ +\uparrow \sum F_y = 0 &= \frac{4}{5} F_A + B_y - 1200 & F_A &= 750 \text{ N} (\uparrow) \\ \pm \rightarrow \sum F_x = 0 &= \frac{3}{5} F_A - B_x = 0 & B_x &= 450 \text{ N} (\leftarrow) \end{aligned}$$

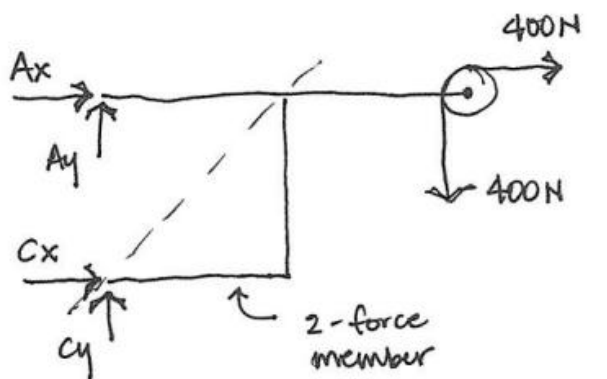
The Cut FBD  $q(x) = 400 \times \frac{2.4}{3} = 320 \text{ N/m}$

$$\begin{aligned} F' &= \frac{1}{2} \times 320 \times 2.4 = 384 \text{ N} \\ \pm \rightarrow \sum F_x = 0 & N_c + \frac{3}{5} F_A = 0 \quad \boxed{N_c = -450 \text{ N}} \\ +\uparrow \sum F_y = 0 & \frac{4}{5} F_A - F' - V_c = 0 \quad \boxed{V_c = 216 \text{ N}} \\ (+\curvearrowright \sum M_c(\vec{F}) = 0 & M_c + 384 \cdot 0.8 - \frac{4}{5} F_A \cdot 2.4 = 0 \\ & \boxed{M_c = 1132.8 \text{ N}\cdot\text{m}} \end{aligned}$$

2. The frame below consists of two members, AB and CB. Determine the external support reactions at the pins A and C. Indicate direction in your answer with directional arrows and draw any pertinent free-body diagrams. 25 POINTS



OVERALL FBD:



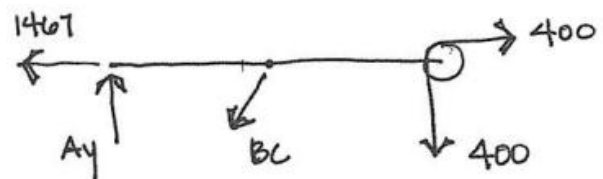
$$+\circlearrowleft \sum M_A = 0 = -400(0.2) - 400(3.8) + C_x(1.5)$$

$$\boxed{C_x = 1067 \text{ N} \rightarrow}$$

$$+\rightarrow \sum F_x = 0 = A_x + 1067 + 400$$

$$\boxed{A_x = 1467 \text{ N} \leftarrow}$$

FBD ABD:



$$+\circlearrowleft \sum M_B = 0 = -A_y(2) - 400(0.2) - 400(1.8)$$

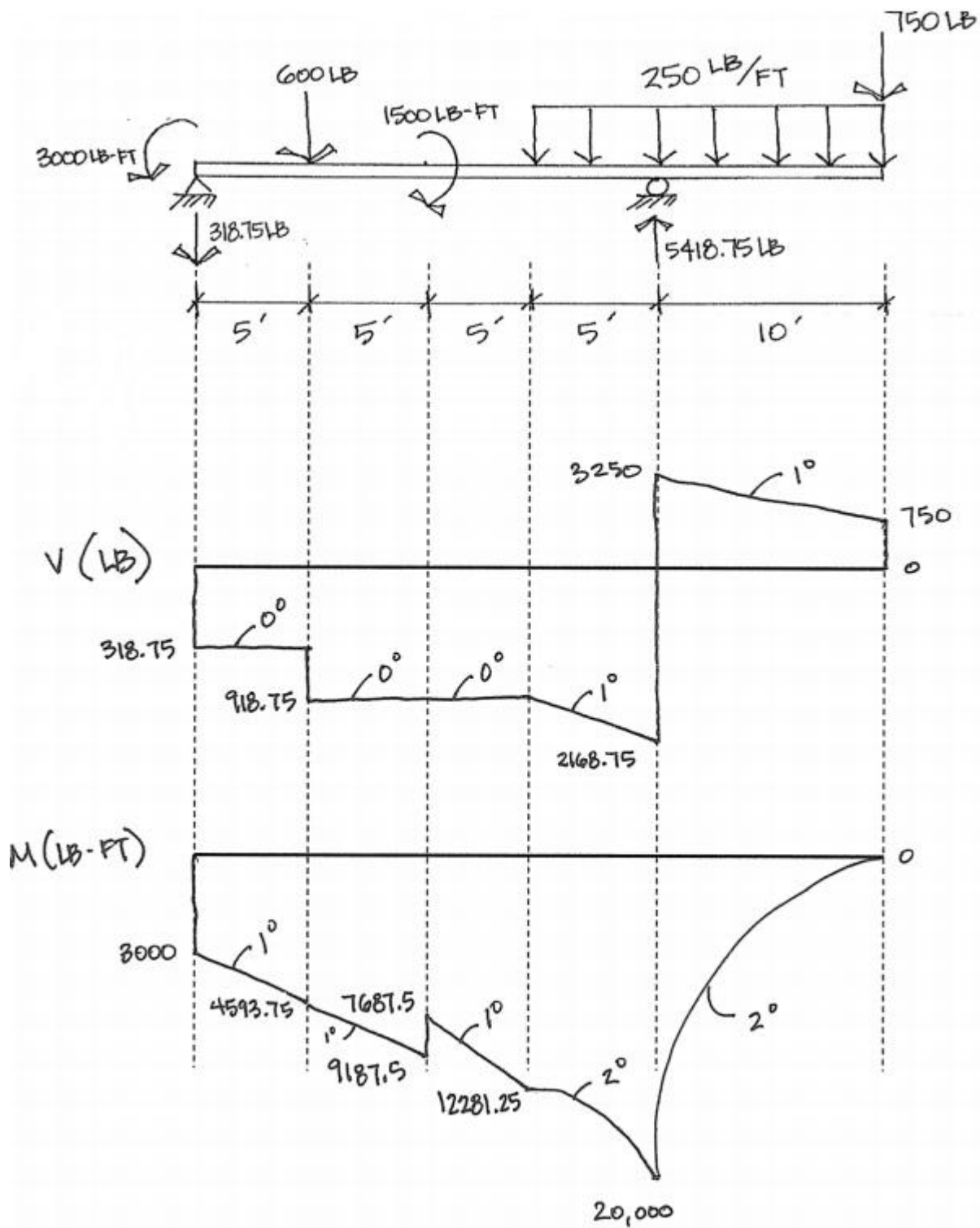
$$\boxed{A_y = 400 \text{ N} \downarrow}$$

FROM OVERALL:

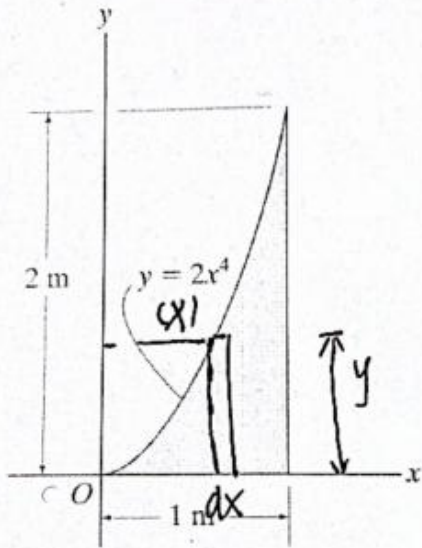
$$\uparrow \sum F_y = 0 = -400 - 400 + C_y$$

$$\boxed{C_y = 800 \text{ N} \uparrow}$$

3. Draw the shear and bending moment diagrams for the loading condition below. Label all diagrams appropriately. 30 POINTS



4. Determine the moment of inertia of the shaded area about the y-axis by integration. State which method of integration is used and label the diagram accordingly. 20 POINTS



$$dA = y dx = 2x^4 dx$$

$$I_y = \int_A x^2 dA = \int_0^1 x^2 \cdot 2x^4 dx$$

$$= \int_0^1 2x^6 dx$$

$$= \frac{2}{7} x^7 \Big|_0^1 = \frac{2}{7} m^4$$

This is integration by definition.