



### Physics 2: Electricity, Optics and Quanta

#### Week 2 – Electrostatics

2023.9

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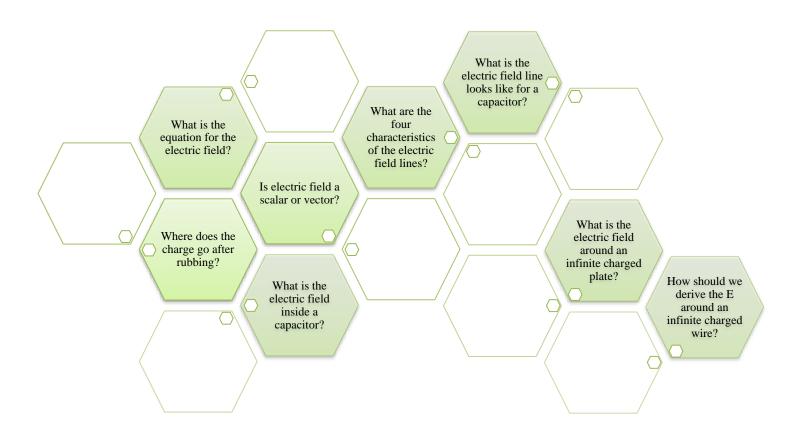
What have we learned LAST WEEK?

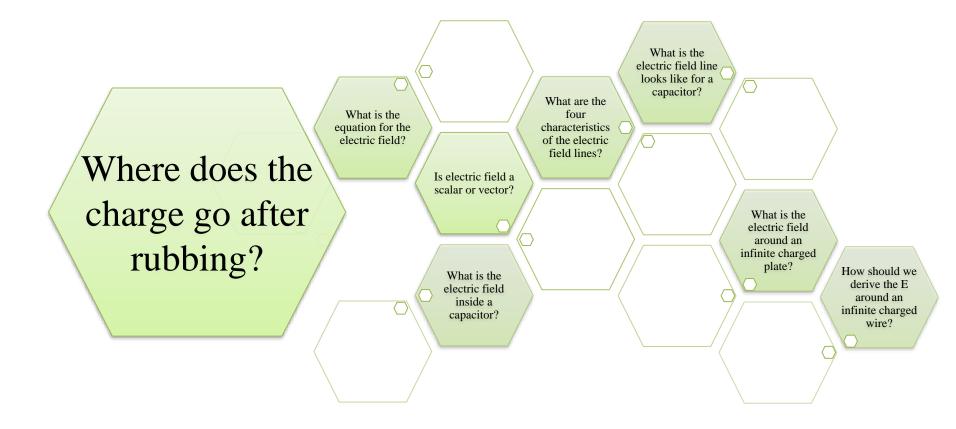
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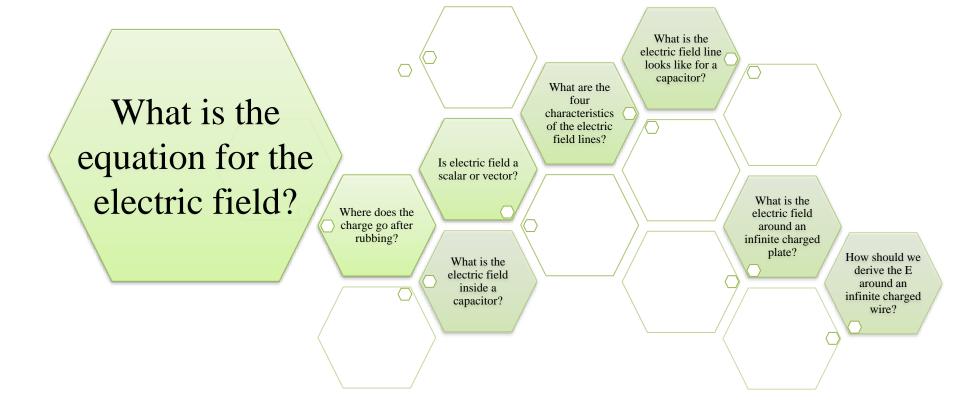
Is there anything that we still need to spend more time to get understood?

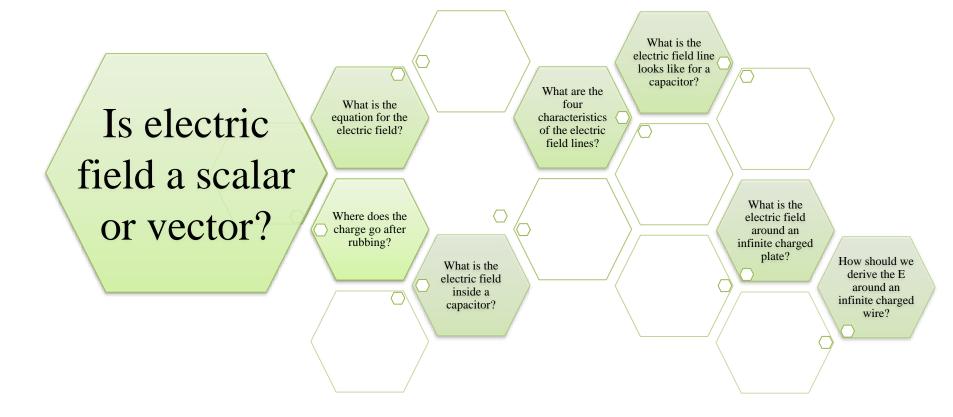
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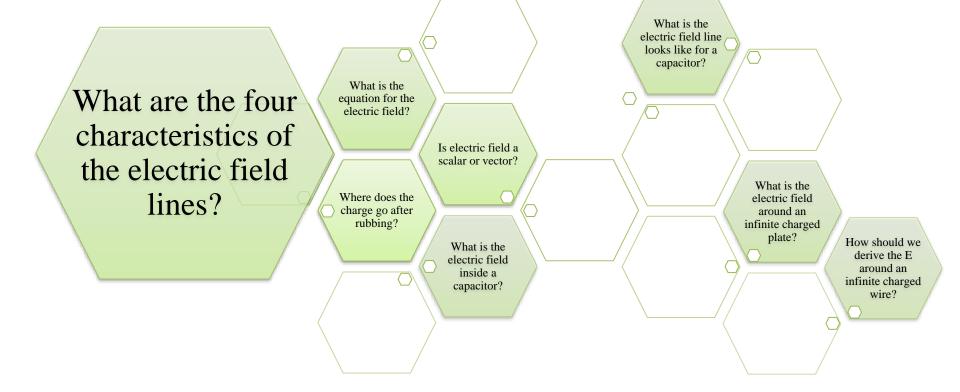
What are we going to do after the lecture?

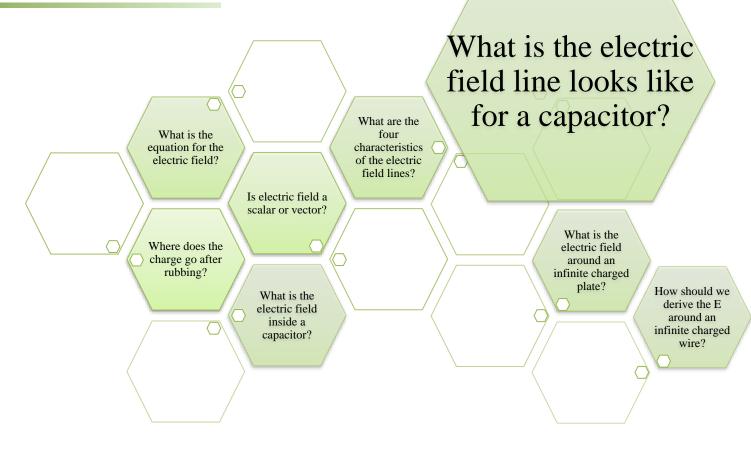


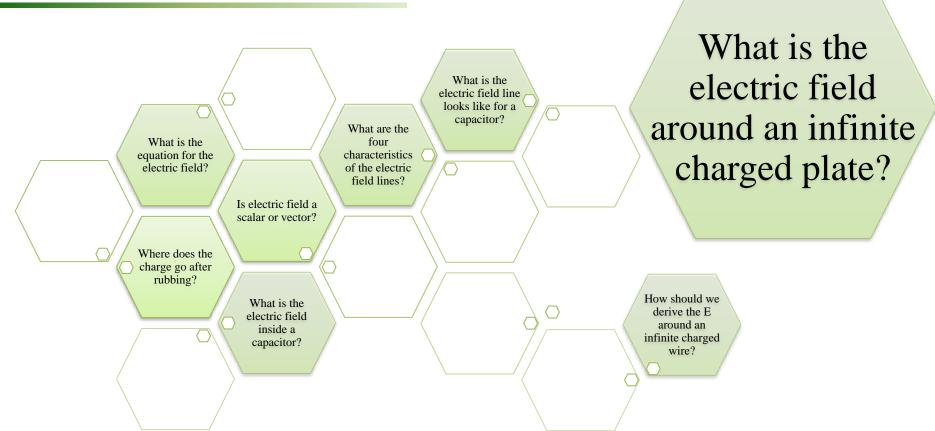


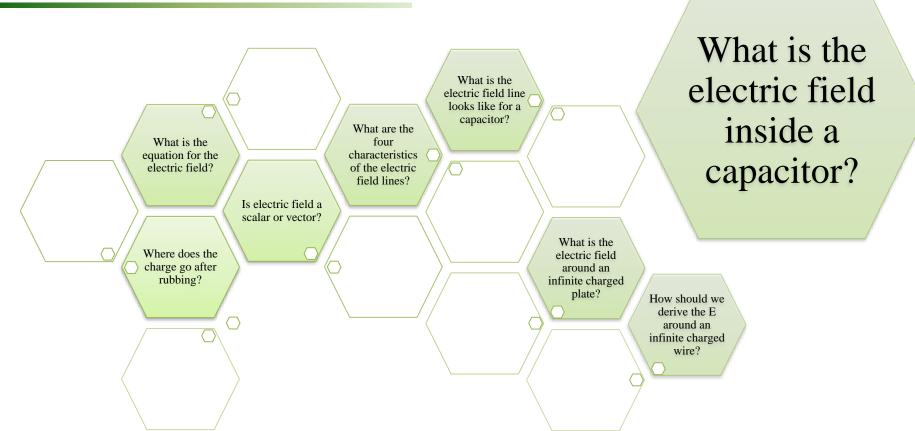


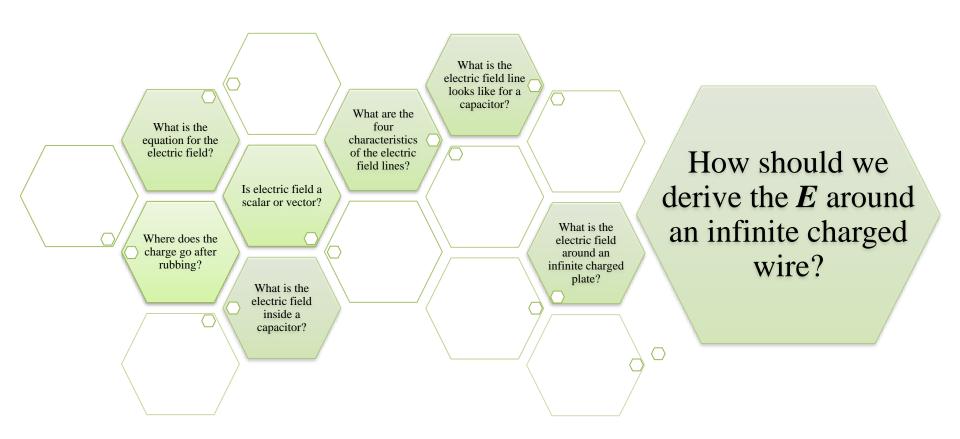


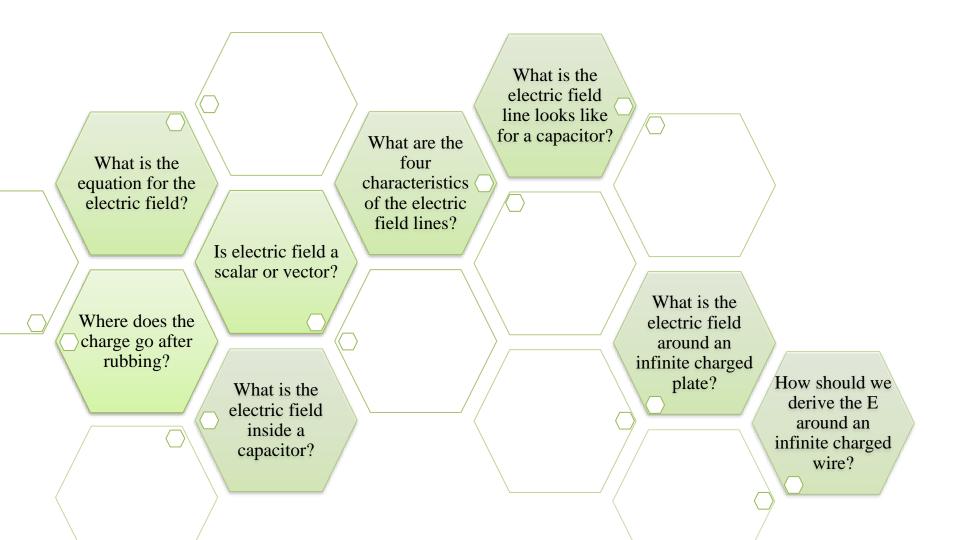




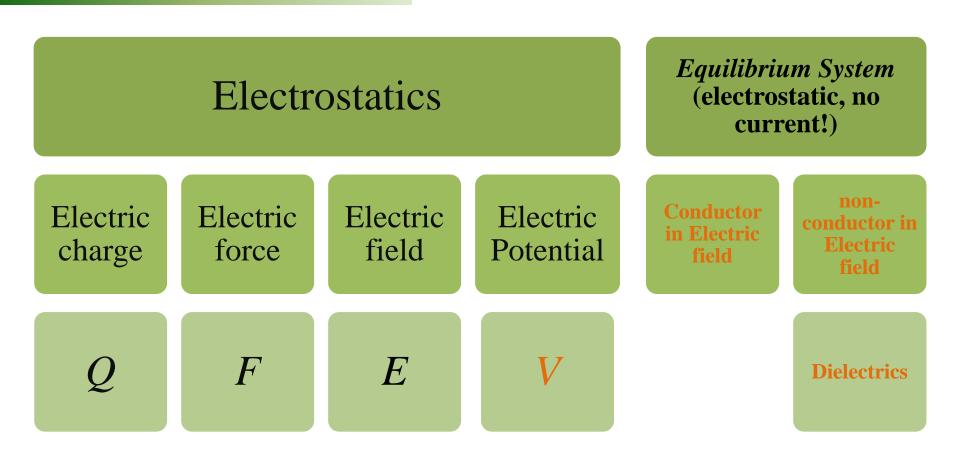




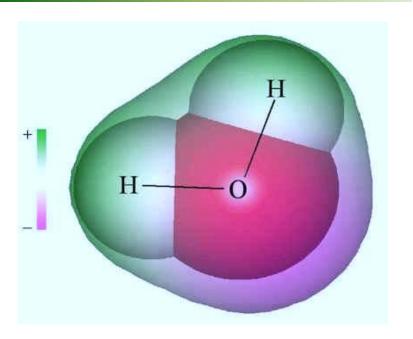




#### **OUTLINE**



### Static electricity



Polar – neutral, but charge is not distributed uniformly

#### Hold a net charge for long?

Hold their charge for a limited time and return to neutral state.

#### Where does the charge go?

Excess charge "leaks off" on to water molecules in the air.

### Electrostatic Force – Coulomb's law

2 **point** charges  $q_1$  and  $q_2$ :

Vector! 
$$\mathbf{F}_{21} = k \frac{q_1 q_2}{r_{21}^2} \hat{\mathbf{r}}_{21} = \frac{q_1 q_2}{4\pi \varepsilon_0 r_{21}^2} \hat{\mathbf{r}}_{21}$$
 unit vector (to show the direction)

$$q_1$$
 on  $q_2$ ?

$$q_2$$
 on  $q_1$ ?

$$k = 9 \times 10^9 \, Nm^2 C^{-2}$$

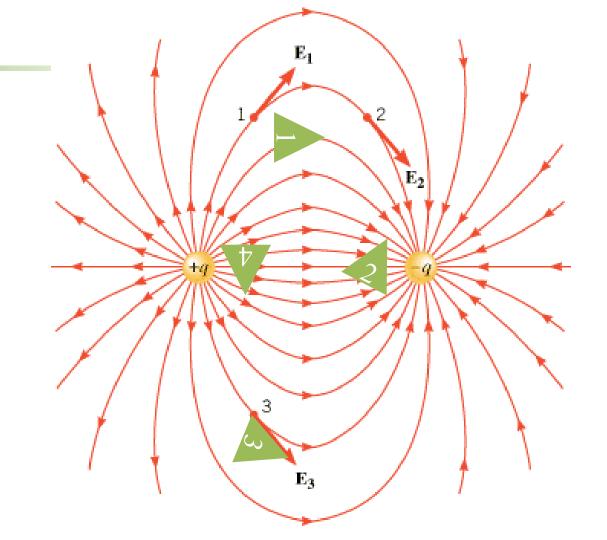
$$\varepsilon_0 = 8.85 * 10^{-12} \,\mathrm{C}^2 / (\mathrm{N \, m}^2)$$

(Permittivity of free space)

#### Electric field line

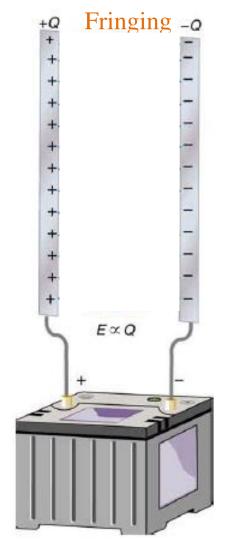
#### Characteristics:

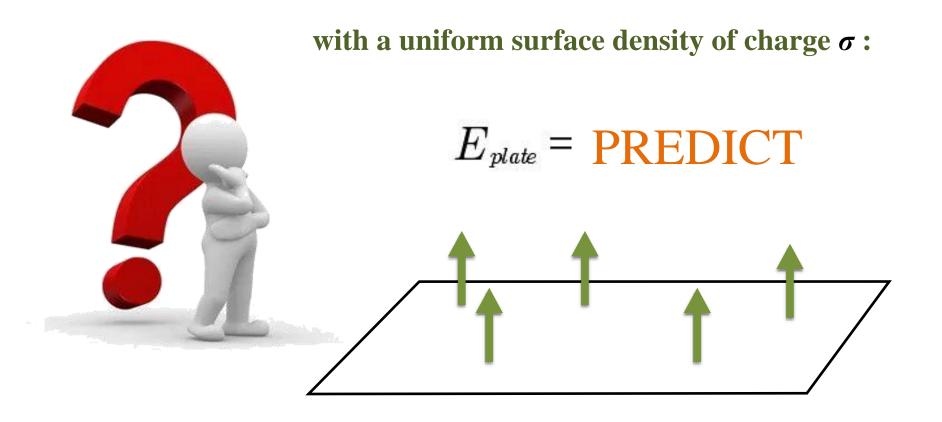
- 1. Direction
- 2. Magnitude
- 3. Direction of *E*
- 4. Never cross

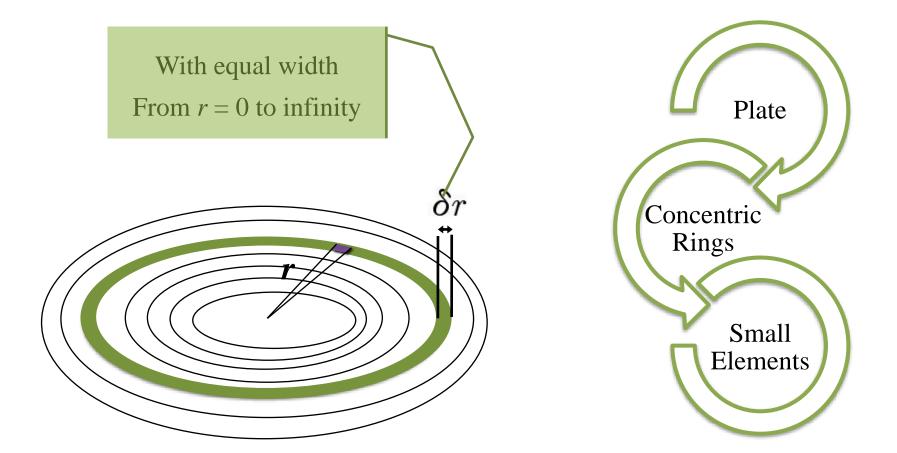


# Electric field line

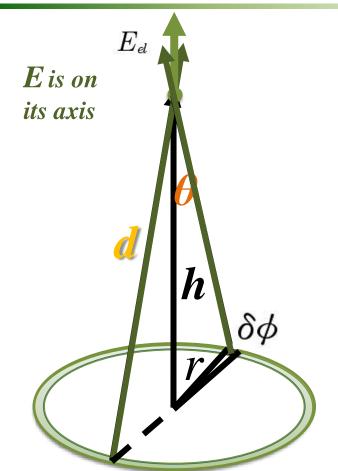
Nearly uniform field between parallel plates







### Electric field from a uniformly charged ring

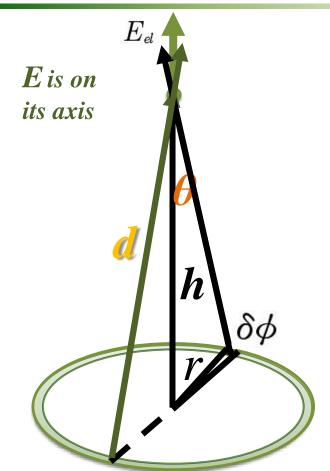


### Surface charge density $\sigma = Q/A$

- divide the circle into small elements
- Direction of electric field of the small elements?

• Direction of total E?

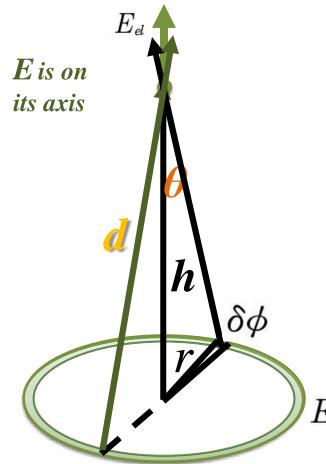
### Electric field from a uniformly charged ring



### Surface charge density $\sigma = Q/A$

- divide the circle into small elements
- the *horizontal* components from elements on opposite sides of the circle cancel out
- all the small elements give a same amount of electric field in the *vertical* direction

## Electric field from a uniformly charged ring



- area of each element:  $A_{el} = r\delta\phi \delta r$
- charge of each element:  $Q_{el} = \sigma r \delta \phi \ \delta r$
- number of elements in a circle:  $\frac{2\pi r}{r\delta\phi} = \frac{2\pi}{\delta\phi}$ 
  - field from one element:

$$E_{el} = \frac{Q_{el}}{4\pi\varepsilon_0 d^2} \cos\theta = \frac{\sigma r \delta \phi \, \delta r \cos\theta}{4\pi\varepsilon_0 d^2}$$

total field from the circle

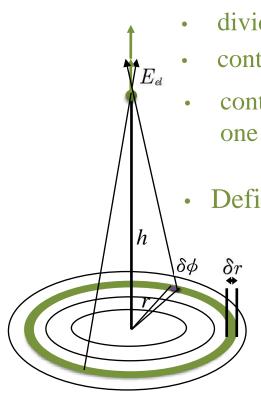
$$E_{tot}(r) = rac{2\pi}{\delta\phi} rac{\sigma r \delta\phi}{4\pi oldsymbol{arepsilon}_0 d^2} \cos heta = rac{\sigma r \, h \, \delta r}{2oldsymbol{arepsilon}_0 (r^2 + h^2)^{3/2}}$$

- divide the plane into concentric rings with equal width
- contributions from rings, from r=0 to infinity
  contribution from one ring (r):  $E_{tot}(r) = \frac{2\pi}{\delta\phi} \frac{\sigma r \delta\phi}{4\pi\varepsilon_0 d^2} \cos\theta = \frac{\sigma r h \delta r}{2\varepsilon_0 (r^2 + h^2)^{3/2}}$ 
  - Define a new variable x:  $x = \frac{r}{h}$   $\delta x = \frac{\delta r}{h}$

$$E_{tot}(r) = rac{\sigma(rac{r}{h})\!ig(rac{\delta r}{h}ig)}{2oldsymbol{arepsilon}_0ig(ig(rac{r}{h}ig)^{\!\!2}+1ig)^{\!\!3/2}}$$

• Field from charges at radius r = hx

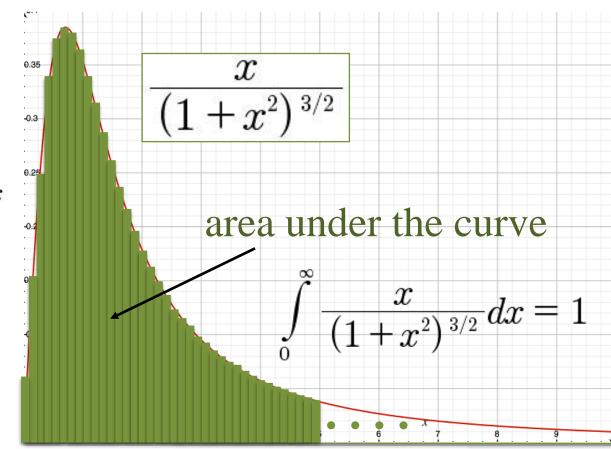
$$E_{tot}(x) = \frac{\sigma x \delta x}{2\varepsilon_0 (x^2 + 1)^{3/2}}$$



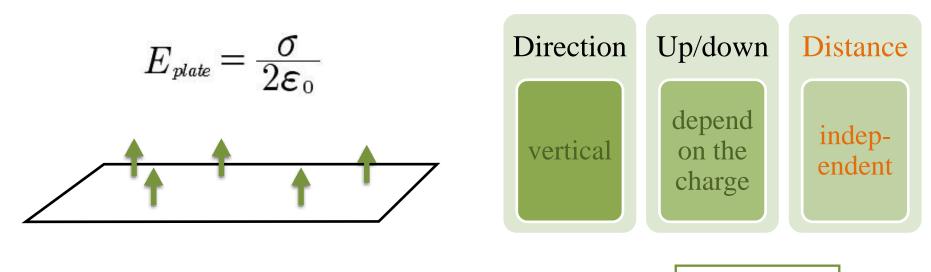
Add all Fields from x = 0 to  $x = \infty$ 

$${E}_{ extit{plate}} = rac{\sigma}{2oldsymbol{arepsilon}_0}\int\limits_0^\infty rac{x}{(1+x^2)^{3/2}}dx$$

$$E_{\it plate} = rac{\sigma}{2 oldsymbol{arepsilon}_0}$$



#### with a uniform surface density of charge $\sigma$ :

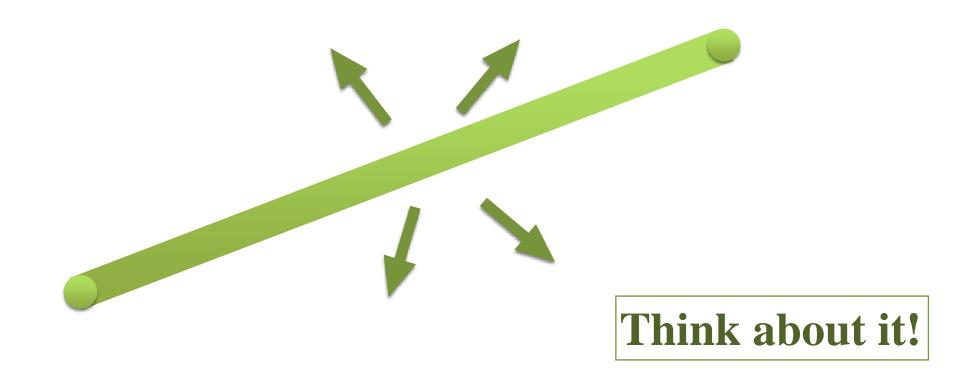


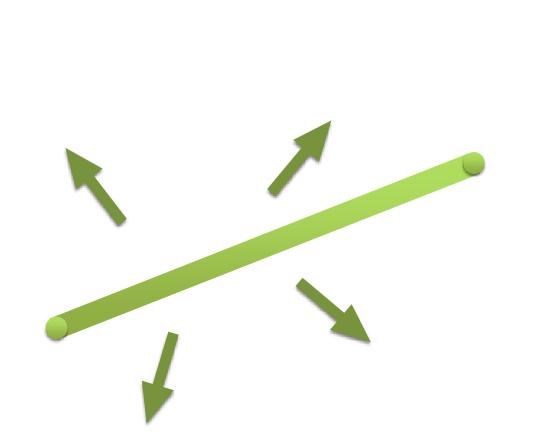
- But of course, no plate can be infinite
- This is only an approximation



Plate is large

Close to the plate





Related to the distance?

How?

Think about it!

#### Gravitational field



Definition: Force per unit mass

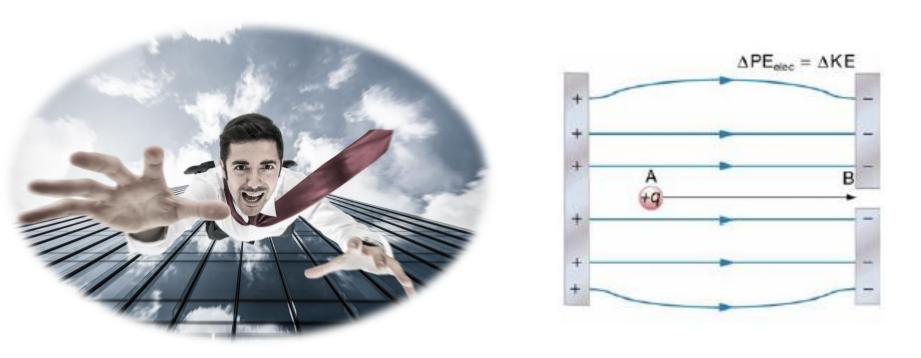
Magnitude above Earth surface:

 $GM_E/r^2$ 

At the earth surface, magnitude

$$g = GM_E/r^2$$

### Charge accelerated in an electric field

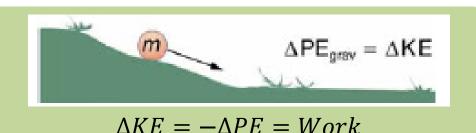


Potential Energy U

### Charge accelerated in an electric field

In a gravitational field.

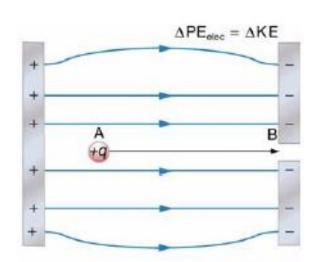
Potential Energy



The electrostatic force is a conservative force



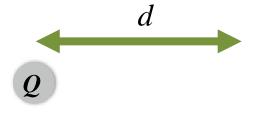
Corresponding potential energy



## Potential energy of a charge

## Zero potential - infinitely far away



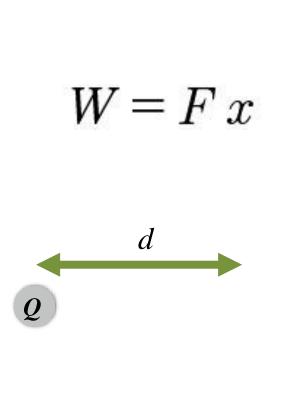


$$v = 0$$

Change in potential energy = - work done

$$W = Fx = -\Delta U$$

# Potential energy of a charge



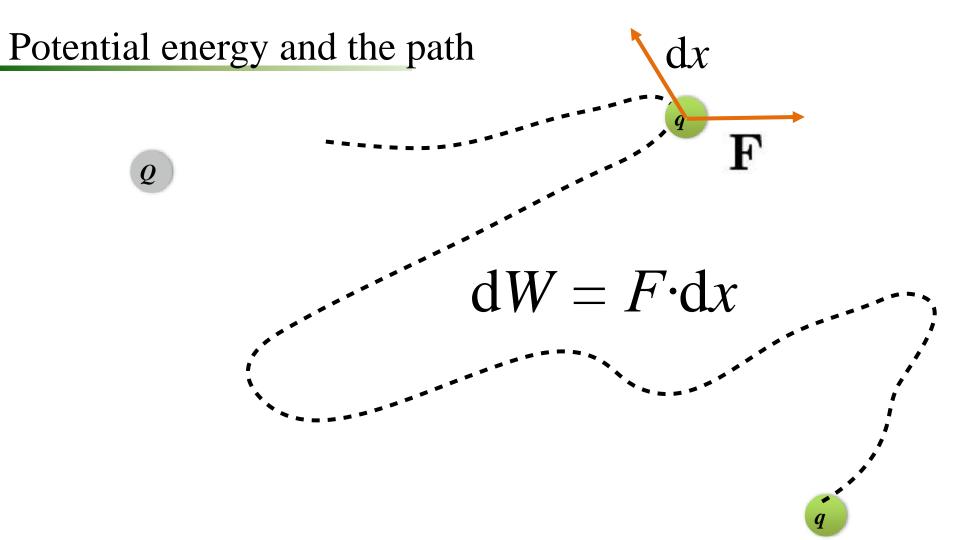


## Potential energy of a charge



$$W = F x$$

F depends on x



# Potential energy and the path

 $W = \int F \cdot dr$ 

W only depends on movement in

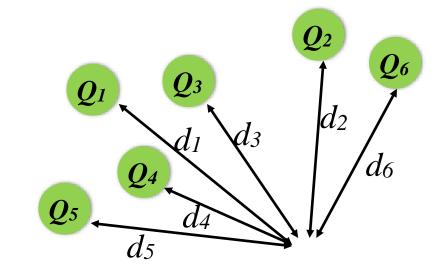
the radial direction

So the work does not depend on the path!

#### U and multiple charges

Total U is the sum of potential energy due to all charges

$$U = \sum_{i=1}^{6} \frac{Q_i q}{4\pi \varepsilon_0 d_i}$$



- > Potential energy is always proportional to q
- > Define:  $V = \frac{U}{q} = \sum_{i=1}^{6} \frac{Q_i}{4\pi\varepsilon_0 d_i}$

V is the "potential"

# Electric potential

$$V = \frac{U}{q}$$

V is the 'electric potential', or just 'potential'

Change in potential between points A and B is:

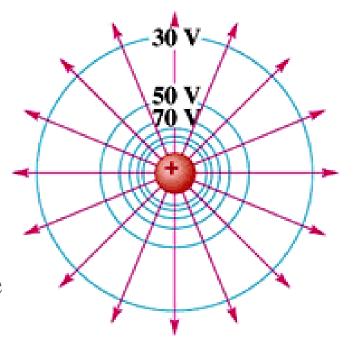
$$\Delta V = V_B - V_A = \frac{\Delta U_{BA}}{q}$$
 (Joules/Coulomb = Volt) also called "Voltage"

$$Q \leftarrow \frac{5 \text{ cm}}{} \qquad V = ? \qquad Q = -3 \text{ nC}$$

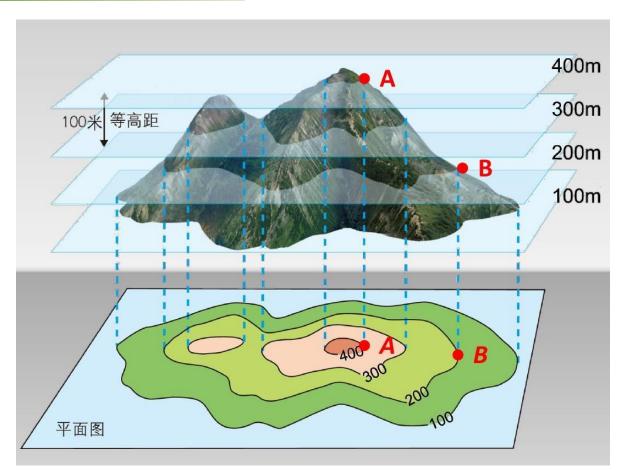
$$V = \frac{kQ}{r}$$

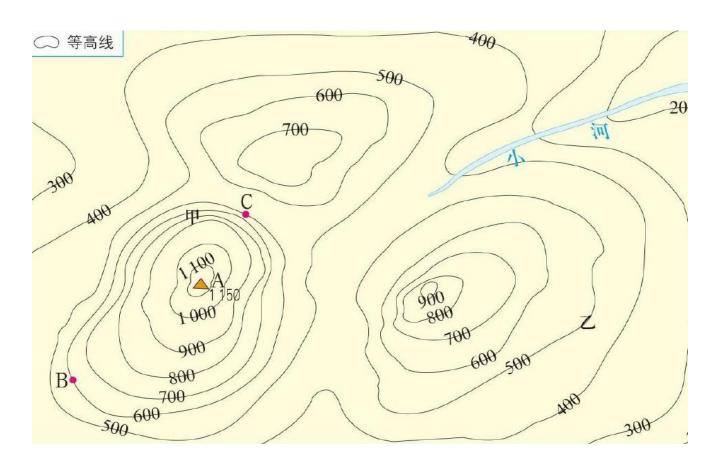
Potential at distance 'r' from a point charge is the same

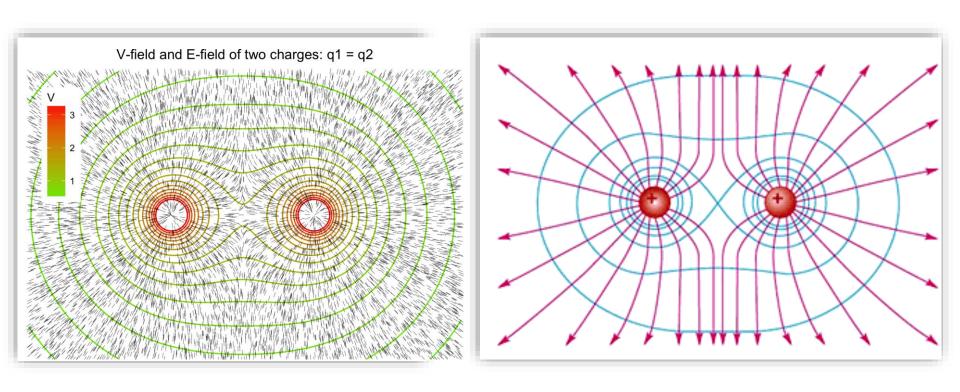
We can draw "equipotential lines" where potential is the same

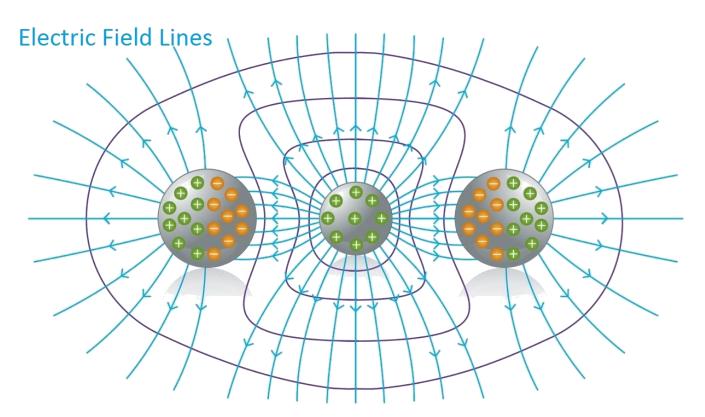


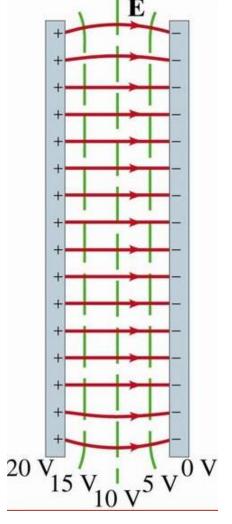
Equipotential lines/surfaces are perpendicular to Electric Field lines











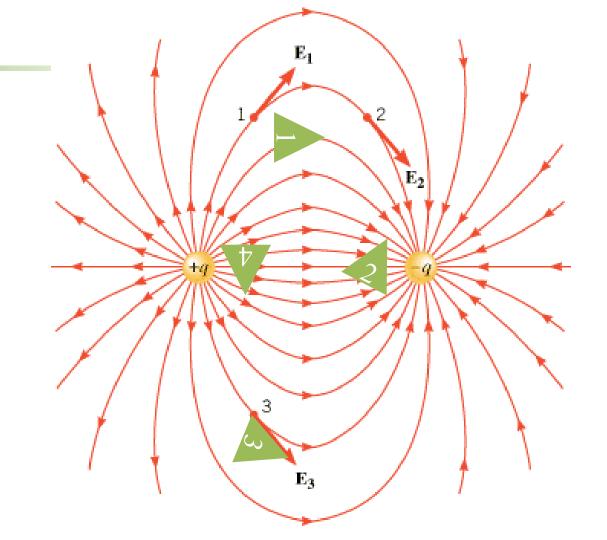
# Differences between

# Electric field line &

#### Electric field line

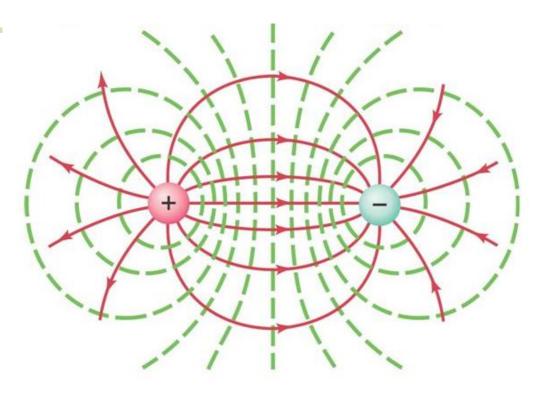
#### Characteristics:

- 1. Direction
- 2. Magnitude
- 3. Direction of *E*
- 4. Never cross

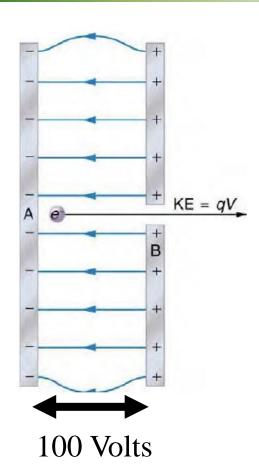


#### Characteristics:

- 1. Direction to E
- 2. Shape
- 3. Shortest way



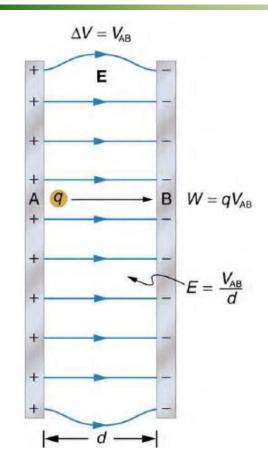
Similar in the Gravitational potential lines/Conservation of mechanical Energy



#### The speed of the electron?

$$\Delta E_p + \Delta E_k = 0$$

#### V and E



#### How to relate potential to electric field?

#### In a constant electric field

$$W = qV_{AB} = F_E d = qEd$$

$$E = \frac{V_{AB}}{d}$$

$$1 \text{ N/C} = 1 \text{ V/m}$$

#### In general

$$E = -\frac{dV}{dr}$$

or  $\vec{E} = -\nabla V$  gradient

Four identical point charges are arranged at the corners of a square [Hint: Draw a figure]. The electric field E and potential V at the center of the square are

- (a) E = 0, V = 0.
- (b)  $E = 0, V \neq 0.$
- (c)  $E \neq 0, V \neq 0$ .
- $(d) E \neq 0, V = 0.$
- (e) E = V regardless of the value.

Which of the following statements is valid?

- (a) If the potential at a particular point is zero, the field at that point must be zero.
- (b) If the field at a particular point is zero, the potential at that point must be zero.
- (c) If the field throughout a particular region is constant, the potential throughout that region must be zero.
- (d) If the potential throughout a particular region is constant, the field throughout that region must be zero.

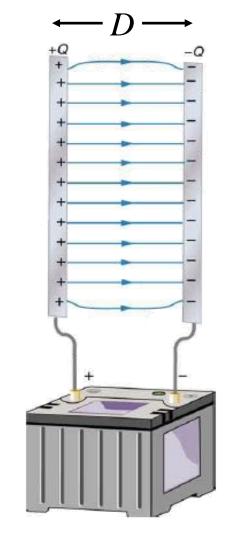
Parallel metal plates charged by a constant voltage source.

What is the charge on the plate(s)?

Voltage of the battery = potential difference

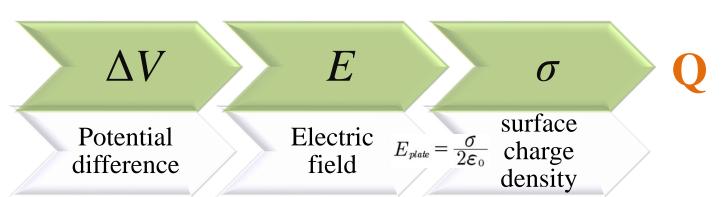
Distance between plates - D

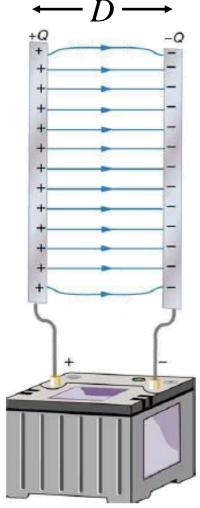
Surface area of plates - A



Parallel metal plates charged by a constant voltage source.

What is the charge on the plate(s)?





- **8.** Which of the following do not affect capacitance?
  - (a) Area of the plates.
  - (b) Separation of the plates.
  - (c) Material between the plates.
  - (d) Charge on the plates.
  - (e) Energy stored in the capacitor.

#### TRY TO RECALL

What have we learned this WEEK?

- 1.
- 2
- 3.

Is there anything that we still need to spend more time to get understood?

- 1.
- 2.

What are we going to do after the lecture?

