Topological Superconductivity

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The present review will focus on the basic properties of topological insulators with time-reversal symmetry.

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