

Task 1: Non-dominated sorting and hypervolume (20%)

- Describe how the following population will be sorted when using the non-dominated sorting algorithm as in NSGA II. What will be the layers of equal rank. What are the crowding distances* in the first ranked layer?

Rank 1 is $y_2, y_1, y_{11}, y_9, y_{12}$

Rank 2 is y_6, y_7, y_3, y_8

Rank 4 is y_5

Rank 5 is y_4

Crowding distance:

y_2 infinity, $y_1: 5+2=7$, $y_{11}=5$

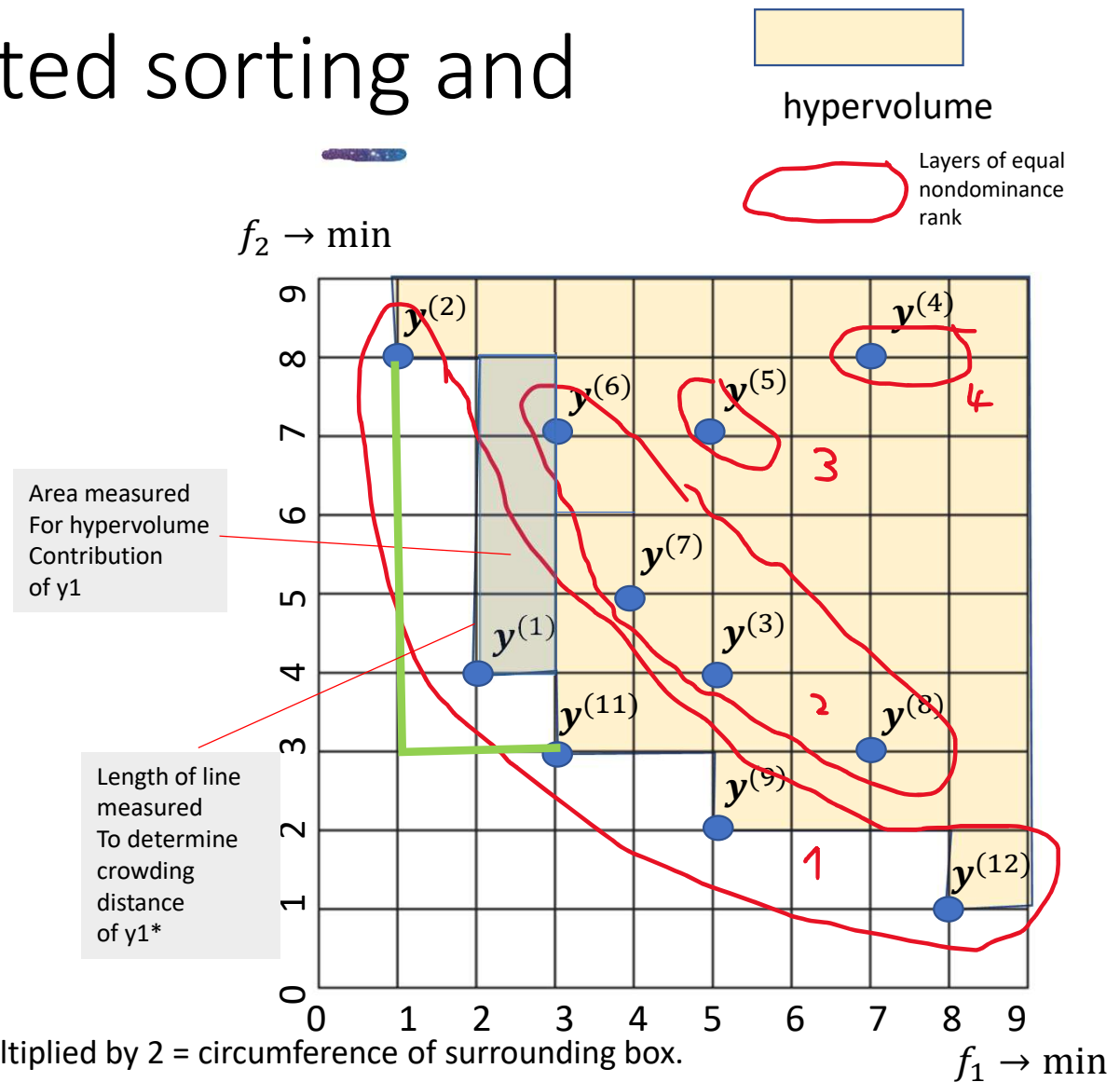
y_9 $5+2=7$ y_{12} : infinity

- What is the hypervolume indicator of this population when the reference point is (9,9)

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- What are the hypervolume contributions of the points in the best ranked layer (only consider points in that layer).

y_2 : 1 y_1 : 4 y_{11} : 2 y_9 : 3 y_{12} : 1



*Remark: in some literature the crowding distance is multiplied by 2 = circumference of surrounding box.

It is also correct.