

Figure 1. Schematic of the proposed HEAVEN method in a reciprocal form.  $B_s$  and  $B_d$  are respectively the static and dynamic prior error covariance matrices. Steps 1 through 6 indicate the procedure for one assimilation cycle. k, K, N, i show time step in each assimilation window, assimilation window size, ensemble size, and particle index respectively. B,  $R_k$ ,  $Q_k$  specify prior, observation, and model error covariance matrices respectively. Initial deterministic guess for state variables and parameters are also respectively represented by  $x_{0,b}$  and  $\Theta$ .