TAD<Hash Table>

Hash table={size,table,hashFunction,keyEqualityFunction}

Inv= $\{\forall k_1 \forall k_2 \ (k_1 \in \text{table}(\text{Keys}) \ y \ k2 \notin \text{table}(\text{keys}) \ y \ k_1 \neq k2 \ y \ \text{hashFuction}(k_1) \neq k_1 \ y \ \text{hashFuction}(k_2) \neq k2 \ y \ \text{hashFuction}(k_1) \neq \text{hashFuction}(k_2) \}$

Main operations

Builder → **CreationHashTable**(size): size → HashTable

Modifier \rightarrow **Insert**(key, Element): HashTable x key x Element \rightarrow HashTable

Modifier \rightarrow **Remove**(**key**): HashTable x key x Element \rightarrow HashTable

Analyzer \rightarrow Search(): HashTable x Key \rightarrow Element Analyzer \rightarrow Contains(): HashTable x key \rightarrow boolean Builder \rightarrow clone(): HashTable_1 \rightarrow HashTable_2

TAD <Stack>

Stack= {push,pop, peek}

Inv = {Comparator(a,b)=($S=\{E1,E2,E3...En\}\ S.pop=En\} \land True \}$

Main operations

Builder \rightarrow **CreateStack**(): \rightarrow Stack

Modifier \rightarrow **Push**(Element): Stack x Element \rightarrow Stack

Analyzer \rightarrow **Top():** Stack \rightarrow Element

Modifier \rightarrow **Pop**(): Stack \rightarrow Element y Stack **Analyzer** \rightarrow **isEmpty**(): Stack \rightarrow Element

Analyzer \rightarrow size(): \rightarrow Integer Builder \rightarrow clone(): Stack1 \rightarrow Stack2

TAD <Queue>

Queue={offer,poll,front}

Inv={ Comparator(a,b) = $(Q=\{E1, E2,E3,E4...En\} \land Q.poll=E1) \land True \}$

Main Operations:

Builder → **CreateQueue** : → Queue

Analyzer \rightarrow **front**(): Queue x Element \rightarrow Element

Modifier \rightarrow Offer(Enqueue): Queue x Element \rightarrow Queue **Modifier** \rightarrow Poll(Dequeue): Queue \rightarrow Element \land Queue

Analyzer → IsEmpty(): Queue→ Boolean

Analyzer \rightarrow size(): \rightarrow n (size) Builder \rightarrow clone(): Queue1 \rightarrow Queue2

TAD <Max Priority Queue>

Priority Queue={size, comparator}

Inv: {comparator(a,b)= True}

Main Operations:

Builder → CreatePriorityQueue(): Element → PriorityQueue

Modifier → Offer(Enqueue)(): Element → PriorityQueue

Analyzer → Peek(Front)(): PriorityQueue → Element

Modifier → Poll(Dequeue)(): PriorityQueue → Element

Analyzer \rightarrow **Size**(): \rightarrow Integer

TAD <Heap>

 $Heap = \{size, comparator\}$

Inv: $\{\text{heap}[L(i/2)J] >= \text{heap}[i] \land \text{parent} > \text{left } \land \text{ parent} > \text{right } \}$ (assuming it is zero-indexed)

Main Operations:

Builder \rightarrow **CreateHeap():** \rightarrow heap **Modifier** \rightarrow **Heapify():** array \rightarrow heap **Modifier** \rightarrow **Insert():** element, heap \rightarrow heap **Modifier** \rightarrow **Extract():** heap \rightarrow Element **Analyzer** \rightarrow **IsEmpty():** heap \rightarrow Boolean **Builder** \rightarrow **clone():** Heap1 \rightarrow Heap2 **Analyzer** \rightarrow **size():** \rightarrow Integer (size)

HashTable

CreateHashTable(size)

"Creates a new hashTable"

pre: size > 0

{ post: HashTable }

Insert(key,Element)

"places value in a key"

```
pre: HashTable \neq Nil \land key \neq Nil \land Inv=True} post( HashTable={(,E1), (k2,E2)...(kn-1,En-1)), (key,Elemento)})
```

Remove(key)

"removes value from key"

pre: HashTable \neq Nil \land key \neq Nill \land Inv=true

{post: HashTable={(,E1), (k2,E2)...(kn-1,En-1))}

Search(key)

"gets value from key"

pre: HashTable \neq Nil \land key \neq Nill \land inv=true}

{post: Element }

Constains(key)

"finds if it has a key"

pre: HashTable \neq Nil \land key \neq Nill \land inv=true}

{post: True (if TasTable has this key)}

Size()

"return the amount of elements in the heap"

pre: HashTable ≠ Nil

{post: size }

Clone(HashTable1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: HashTable1 \neq Nil

{post: hashtable2}

Stack

CreateStack():

"Creates a new Stack"

pre: True

{post: Stack}

Push(Element)

"adds a element to the Stack, in the first position"

pre: Element≠nil ∧ Stack≠nil

 $\{post=Stack=\{E1,E2,E3...En+1\}\}$

Top()

"takes the first element of the Stack"

pre=Stack≠nil

{post: En}

Pop()

"takes and remove the first element of the Stack"

pre=Stack≠nil

{post= En \land Stack={E1,E2,E3....En-1}}

isEmpty()

"If the Stack is Empty"

```
pre=Stack≠nil
{post= True if(Stack=Ø) }
```

Size()

"find and return the Stack size"

pre: Stack≠ Nil

{post: size}

Clone(Stack1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: Stack1 ≠ Nil

{post: Stack2}

Queue

CreateQueue()

"Creates a new queue"

pre=True

{post=Queue}

Front(Queue)

"Take the first element of the Queue"

pre: (Queue \neq nill) \land !Queue.isEmpty()

{post=E1}

Offer(Element)

"Add the element in the Queue in the last position"

pre: Queue≠nil ∧ Element≠nil ∧ Queue={E1, E2...En}

```
{post= Queue=(E1, E2...En-1,Element) }
```

Poll()

"Take and remove the first element of the Queue"

pre: (Queue ≠ nill V Queue={E1, E2,E3,E4...En}) ∧ !Q.isEmpty()

{post= E1 \land Queue={E2,E3,E4...En}}

IsEmpty()

"If the QueueisEmpty"

pre: Queue ≠nill

{post=True if(Queue=Ø)}

Size()

"find and return the Queue size"

pre: Queue≠ Nil

{post: size}

Clone(Queue1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: Queue1 ≠ Nil

{post: Queue2}

PriorityQueue

Create Priority Queue (size):

"Creates a new priority queue"

{pre: Size ∧ True }

{post: PriorityQueue}

Offer(Element):

"Adds Element to queque"

{pre: Element}

{pos: print PriorityQueque Elements with enquque Element }

Peek()

"print queque"

{pre: PriorityQueue≠ null}

{pos: prints queque}

Poll()

"Removes Element from queque"

{pre: PriorityQueue≠ null}

{pos: print PriorityQueque Elements with dequeque Element }

size():

Size()

"find and return the PrioriyQueue size"

pre: PriorityQueue≠ null

{post: size}

Heap

CreateHeap(size)

"creates a new heap"

pre: size>0

{post: heap

Heapify(array)

"it receives an array and turns it into a heap"

pre: True

{post: array.isHeap() = true}

Insert(Element)

"it receives an element and adds it to the heap maintaining the its property"

pre: heap.isHeap()

{post: heap.isHeap() = true}

Extract(heap)

"return and eliminates the first element in the heap"

pre: heap.isHeap()

{post: heap.isHeap() = true \land heap.size = heap.size-1}

IsHeap(array)

"return true if the array is a heap, false if it is not"

pre: True

{post: true if it is a heap, false if not}

IsEmpty(heap)

"return true if the heap is empty, false if it is not"

pre: True

{post: true if it is empty, false if not}

Size(heap)

"return the amount of elements in the heap"

pre: True

{post: heap.size}

Clone(Heap1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: Heap1 ≠ Nil

{post: Heap2}