

#### TAD<Hash Table>

Hash table={size,table,hashFunction,keyEqualityFunction}

Inv=  $\{\forall k_1 \forall k_2 \ (k_1 \in \text{table}(\text{Keys}) \ y \ k2 \notin \text{table}(\text{keys}) \ y \ k_1 \neq k2 \ y \ \text{hashFuction}(k_1) \neq k_1 \ y \ \text{hashFuction}(k_2) \neq k2 \ y \ \text{hashFuction}(k_1) \neq \text{hashFuction}(k_2) \}$ 

#### **Main operations**

**Builder**  $\rightarrow$  **CreationHashTable**(size): size  $\rightarrow$  HashTable

**Modifier**  $\rightarrow$  **Insert**(key, Element): HashTable x key x Element  $\rightarrow$  HashTable

**Modifier**  $\rightarrow$ **Remove**(**key**): HashTable x key x Element  $\rightarrow$ HashTable

Analyzer  $\rightarrow$  Search(): HashTable x Key  $\rightarrow$  Element Analyzer  $\rightarrow$  Contains(): HashTable x key  $\rightarrow$  boolean Builder  $\rightarrow$  clone(): HashTable 1 $\rightarrow$ HashTable 2

#### TAD <Stack>

Stack= {push,pop, peek}

Inv = {Comparator(a,b)=( $S=\{E1,E2,E3...En\}\ S.pop=En$ )  $\land$  True }

#### **Main operations**

**Builder**  $\rightarrow$  **CreateStack**():  $\rightarrow$  Stack

**Modifier**  $\rightarrow$  **Push**(Element): Stack x Element  $\rightarrow$  Stack

**Analyzer**  $\rightarrow$  **Top():** Stack  $\rightarrow$  Element

**Modifier**  $\rightarrow$  **Pop**(): Stack  $\rightarrow$  Element y Stack **Analyzer**  $\rightarrow$ **isEmpty**(): Stack  $\rightarrow$  Element

Analyzer  $\rightarrow$ size():  $\rightarrow$  Integer Builder  $\rightarrow$  clone(): Stack1 $\rightarrow$ Stack2

#### TAD < Oueue>

Queue={offer,poll,front}

Inv={ Comparator(a,b) =  $(Q=\{E1, E2,E3,E4...En\} \land Q.poll=E1) \land True \}$ 

#### **Main Operations:**

**Builder** → **CreateQueue** : → Queue

**Analyzer**  $\rightarrow$  **front():** Queue x Element  $\rightarrow$  Element

**Modifier**  $\rightarrow$  Offer(Enqueue): Queue x Element  $\rightarrow$  Queue **Modifier**  $\rightarrow$  Poll(Dequeue): Queue  $\rightarrow$  Element  $\land$  Queue

**Analyzer**  $\rightarrow$  IsEmpty(): Queue $\rightarrow$  Boolean

Analyzer  $\rightarrow$ size():  $\rightarrow$  n (size)

**Builder**  $\rightarrow$  **clone():** Queue1 $\rightarrow$ Queue2



#### **TAD <Max Priority Queue>**

Priority Queue={size, comparator}

Inv: {comparator(a,b)= True}

### **Main Operations:**

Builder → CreatePriorityQueue(): Element → PriorityQueue Modifier → Offer(Enqueue)(): Element → PriorityQueue Analyzer → Peek(Front)(): PriorityQueue → Element Modifier → Poll(Dequeue)(): PriorityQueue → Element

Analyzer  $\rightarrow$  Size():  $\rightarrow$  Integer

#### TAD <Heap>

 $Heap = \{size, comparator\}$ 

Inv:  $\{\text{heap}[L(i/2)J] >= \text{heap}[i] \land \text{parent} > \text{left } \land \text{ parent} > \text{right } \}$  (assuming it is zero-indexed)

## **Main Operations:**

**Builder**  $\rightarrow$  **CreateHeap():**  $\rightarrow$  heap **Modifier**  $\rightarrow$  **Heapify():** array  $\rightarrow$  heap

**Modifier**  $\rightarrow$  **Insert**(): element, heap  $\rightarrow$  heap **Modifier**  $\rightarrow$  **Extract**(): heap  $\rightarrow$  Element **Analyzer**  $\rightarrow$  **IsEmpty**(): heap  $\rightarrow$  Boolean

Builder  $\rightarrow$  clone(): Heap1 $\rightarrow$ Heap2 Analyzer  $\rightarrow$ size():  $\rightarrow$  Integer (size)

## HashTable

#### **CreateHashTable(size)**

"Creates a new hashTable"

pre: size > 0

{ post: HashTable }

#### **Insert**(key,**Element**)



"places value in a key"

pre: HashTable  $\neq$  Nil  $\land$  key  $\neq$  Nil  $\land$  Inv=True}

post( HashTable={(,E1), (k2,E2)...(kn-1,En-1)), (key,Elemento)})

## Remove(key)

"removes value from key"

pre: HashTable  $\neq$  Nil  $\land$  key  $\neq$  Nill  $\land$  Inv=true

{post:  $HashTable=\{(E1), (k2,E2)...(kn-1,En-1)\}$ 

# Search( key)

"gets value from key"

pre: HashTable  $\neq$  Nil  $\land$  key  $\neq$  Nill  $\land$  inv=true}

{post: Element }

## Constains( key)

"finds if it has a key"

pre: HashTable  $\neq$  Nil  $\land$  key  $\neq$  Nill  $\land$  inv=true}

{post: True (if TasTable has this key)}

## Size()

"return the amount of elements in the heap"

pre: HashTable ≠ Nil

{post: size }



### Clone(HashTable1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: HashTable1 ≠ Nil

{post: hashtable2}

#### Stack

## CreateStack():

"Creates a new Stack"

pre: True

{post: Stack}

## Push(Element)

"adds a element to the Stack, in the first position"

pre: Element≠nil ∧ Stack≠nil

 $\{post=Stack=\{E1,E2,E3...En+1\}\}$ 

## Top()

"takes the first element of the Stack"

pre=Stack≠nil

{post: En}

## Pop()

"takes and remove the first element of the Stack"

pre=Stack≠nil

{post= En  $\land$  Stack={E1,E2,E3...En-1}}



isEmpty()	
"If the Stack isEmpty"	
pre=Stack≠nil	

# Size()

"find and return the Stack size"

{post= True if(Stack=Ø) }

pre: Stack≠ Nil

{post: size}

# Clone(Stack1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: Stack1 ≠ Nil

{post: Stack2}

#### Queue

## **CreateQueue()**

"Creates a new queue"

pre=True

{post=Queue}

# Front(Queue)

"Take the first element of the Queue"

pre: (Queue  $\neq$  nill)  $\land$  !Queue.isEmpty()

{post=E1}



### Offer(Element)

"Add the element in the Queue in the last position"

pre: Queue≠nil ∧ Element≠nil ∧ Queue={E1, E2...En}

{post= Queue=(E1, E2...En-1,Element) }

# Poll()

"Take and remove the first element of the Queue"

pre: (Queue  $\neq$  nill V Queue={E1, E2,E3,E4...En})  $\land$  !Q.isEmpty()

 $\{post=E1 \land Queue=\{E2,E3,E4...En\}\}$ 

## IsEmpty()

"If the QueueisEmpty"

pre: Queue ≠nill

{post=True if(Queue=Ø)}

# Size()

"find and return the Queue size"

pre: Queue≠ Nil

{post: size}

#### Clone(Queue1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: Queue1 ≠ Nil

{post: Queue2}

## **PriorityQueue**

#### **CreatePriorityQueue(size):**



"Creates a new priority queue"	
{pre: Size ∧ True }	
{post: PriorityQueue}	

#### **Offer(Element):**

"Adds Element to queque"

{pre: Element}

{pos: print PriorityQueque Elements with enquque Element }

## Peek()

"print queque"

{pre: PriorityQueue≠ null}

{pos: prints queque}

# Poll()

"Removes Element from queque"

{pre: PriorityQueue≠ null}

{pos: print PriorityQueque Elements with dequeque Element }

## Size()

"find and return the PrioriyQueue size"

pre: PriorityQueue≠ null

{post: size}

### Heap

# CreateHeap(size)

"creates a new heap"

pre: size>0



{post: heap

## Heapify(array)

"it receives an array and turns it into a heap"

pre: True

{post: array.isHeap() = true}

## **Insert(Element)**

"it receives an element and adds it to the heap maintaining the its property"

pre: heap.isHeap()

{post: heap.isHeap() = true}

# Extract(heap)

"return and eliminates the first element in the heap"

pre: heap.isHeap()

{post: heap.isHeap() = true  $\land$  heap.size = heap.size-1}

# IsHeap(array)

"return true if the array is a heap, false if it is not"

pre: True

{post: true if it is a heap, false if not}

## IsEmpty(heap)

"return true if the heap is empty, false if it is not"

pre: True

{post: true if it is empty, false if not}

#### Size(heap)



"return the amount of elements in the heap"

pre: True

{post: heap.size}

# Clone(Heap1)

"Return a clone (an object identical to his "parent", but has different object reference and a different memory direction)"

pre: Heap1 ≠ Nil

{post: Heap2}