

I. Stokes' theorem example

```
1 #showybox(  
2   title: "Stokes' theorem",  
3   frame: (  
4     border-color: blue,  
5     title-color: blue.lighten(30%),  
6     body-color: blue.lighten(95%),  
7     footer-color: blue.lighten(80%)  
8   ),  
9   footer: "Information extracted from a well-known public encyclopedia"  
10 ) [  
11   Let  $\Sigma$  be a smooth oriented surface in  $\mathbb{R}^3$  with boundary  $\partial\Sigma \equiv \Gamma$ . If a vector field  $\mathbf{F}(x,y,z) = (F_x(x,y,z), F_y(x,y,z), F_z(x,y,z))$  is defined and has continuous first order partial derivatives in a region containing  $\Sigma$ , then  
12  
13   
$$\iint_{\Sigma} (\nabla \times \mathbf{F}) \cdot \mathbf{n} \, dA = \oint_{\Gamma} \mathbf{F} \cdot d\mathbf{r}$$
  
14 ]
```

Stokes' theorem

Let Σ be a smooth oriented surface in \mathbb{R}^3 with boundary $\partial\Sigma \equiv \Gamma$. If a vector field $\mathbf{F}(x, y, z) = (F_x(x, y, z), F_y(x, y, z), F_z(x, y, z))$ is defined and has continuous first order partial derivatives in a region containing Σ , then

$$\iint_{\Sigma} (\nabla \times \mathbf{F}) \cdot \mathbf{n} \, dA = \oint_{\Gamma} \mathbf{F} \cdot d\mathbf{r}$$

Information extracted from a well-known public encyclopedia

II. Gauss's Law example

```
1 #showybox(  
2   frame: (  
3     border-color: red.darken(30%),  
4     title-color: red.darken(30%),  
5     radius: 0pt,  
6     thickness: 2pt,  
7     body-inset: 2em,  
8     dash: "densely-dash-dotted"  
9   ),  
10  title: "Gauss's Law"  
11 ) [  
12   The net electric flux through any hypothetical closed surface is equal  
13   to  $\frac{1}{\epsilon_0}$  times the net electric charge enclosed within that  
14   closed surface. The closed surface is also referred to as Gaussian  
15   surface. In its integral form:  
16  
17   
$$\Phi_E = \oiint \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$
  
18 ]
```

Gauss's Law

The net electric flux through any hypothetical closed surface is equal to $\frac{1}{\epsilon_0}$ times the net electric charge enclosed within that closed surface. The closed surface is also referred to as Gaussian surface. In its integral form:

$$\Phi_E = \oiint_S \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

III. Carnot's cycle efficiency example

```
1 #showybox(  
2   title-style: (  
3     weight: 900,  
4     color: red.darken(40%),  
5     sep-thickness: 0pt,  
6     align: center  
7   ),  
8   frame: (  
9     title-color: red.lighten(80%),  
10    border-color: red.darken(40%),  
11    thickness: (left: 1pt),  
12    radius: 0pt  
13  ),  
14  title: "Carnot cycle's efficiency"  
15 ) [  
16   Inside a Carnot cycle, the efficiency  $\eta$  is defined to be:  
17  
18    $\eta = W/Q_H = \frac{Q_H + Q_C}{Q_H} = 1 - T_C/T_H$   
19 ]
```

Carnot cycle's efficiency

Inside a Carnot cycle, the efficiency η is defined to be:

$$\eta = \frac{W}{Q_H} = \frac{Q_H + Q_C}{Q_H} = 1 - \frac{T_C}{T_H}$$

IV. Clairaut's theorem example

```
1 #showybox(  
2   title-style: (  
3     boxed-style: (  
4       anchor: (  
5         x: center,  
6         y: horizon  
7       ),  
8       radius: (top-left: 10pt, bottom-right: 10pt, rest: 0pt),
```

```

9      )
10     ),
11     frame: (
12         title-color: green.darken(40%),
13         body-color: green.lighten(80%),
14         footer-color: green.lighten(60%),
15         border-color: green.darken(60%),
16         radius: (top-left: 10pt, bottom-right: 10pt, rest: 0pt)
17     ),
18     title: "Clairaut's theorem",
19     footer: text(size: 10pt, weight: 600, emph("This will be useful every
20 time you want to interchange partial derivatives in the future.))
21 )[
22     Let  $f: A \rightarrow \mathbb{R}$  with  $A \subset \mathbb{R}^n$  an open set such that its
23 cross derivatives of any order exist and are continuous in  $A$ . Then for
24 any point  $(a_1, a_2, \dots, a_n)$  in  $A$  it is true that
25
26 
$$\frac{\partial^n f}{\partial x_i \dots \partial x_j}(a_1, a_2, \dots, a_n) =$$

27 
$$\frac{\partial^n f}{\partial x_j \dots \partial x_i}(a_1, a_2, \dots, a_n)$$

28 ]

```

Clairaut's theorem

Let $f: A \rightarrow \mathbb{R}$ with $A \subset \mathbb{R}^n$ an open set such that its cross derivatives of any order exist and are continuous in A . Then for any point $(a_1, a_2, \dots, a_n) \in A$ it is true that

$$\frac{\partial^n f}{\partial x_i \dots \partial x_j}(a_1, a_2, \dots, a_n) = \frac{\partial^n f}{\partial x_j \dots \partial x_i}(a_1, a_2, \dots, a_n)$$

This will be useful every time you want to interchange partial derivatives in the future.

V. Divergence theorem example

```

1  #showybox(
2      footer-style: (
3          sep-thickness: 0pt,
4          align: right,
5          color: black
6      ),
7      title: "Divergence theorem",
8      footer: [
9          In the case of  $n=3$ ,  $V$  represents a volume in three-dimensional
10 space, and  $\partial V = S$  its surface
11      ]
12 )[
13     Suppose  $V$  is a subset of  $\mathbb{R}^n$  which is compact and has a piecewise
14 smooth boundary  $S$  (also indicated with  $\partial V = S$ ). If  $\mathbf{F}$  is a
15 continuously differentiable vector field defined on a neighborhood of
16  $V$ , then:
17
18 ]

```

```

14     $ integral.triple_V (bold(nabla) dot bold(F)) dif V = integral.surf_S
    (bold(F) dot bold(hat(n))) dif S $
15 ]

```

Divergence theorem

Suppose V is a subset of \mathbb{R}^n which is compact and has a piecewise smooth boundary S (also indicated with $\partial V = S$). If \mathbf{F} is a continuously differentiable vector field defined on a neighborhood of V , then:

$$\iiint_V (\nabla \cdot \mathbf{F}) dV = \iint_S (\mathbf{F} \cdot \hat{\mathbf{n}}) dS$$

In the case of $n = 3$, V represents a volume in three-dimensional space, and $\partial V = S$ its surface

VI. Coulomb's law example

```

1  #showybox(
2    shadow: (
3      color: yellow.lighten(55%),
4      offset: 3pt
5    ),
6    frame: (
7      title-color: red.darken(30%),
8      border-color: red.darken(30%),
9      body-color: red.lighten(80%)
10   ),
11   title: "Coulomb's law"
12 ) [
13   Coulomb's law in vector form states that the electrostatic force
    $bold(F)$ experienced by a charge $q_1$ at position $bold(r)$ in the
14   vicinity of another charge $q_2$ at position $bold(r')$, in a vacuum is
    equal to
15
16   $ bold(F) = frac(q_1 q_2, 4 pi epsilon_0) frac(bold(r) - bold(r'),
    bar.v bold(r) - bold(r') bar.v^3) $

```

Coulomb's law

Coulomb's law in vector form states that the electrostatic force \mathbf{F} experienced by a charge q_1 at position \mathbf{r} in the vicinity of another charge q_2 at position \mathbf{r}' , in a vacuum is equal to

$$\mathbf{F} = \frac{q_1 q_2}{4\pi\epsilon_0} \frac{\mathbf{r} - \mathbf{r}'}{|\mathbf{r} - \mathbf{r}'|^3}$$

VII. Newton's second law example

```
1  #block(  
2    height: 4.5cm,  
3    inset: 1em,  
4    fill: luma(250),  
5    stroke: luma(200),  
6    breakable: false,  
7    columns(2)[  
8      #showybox(  
9        title-style: (  
10         boxed-style: (  
11           anchor: (x: center, y: horizon)  
12         )  
13       ),  
14       breakable: true,  
15       width: 90%,  
16       align: center,  
17       title: "Newton's second law"  
18     ) [  
19       If a body of mass  $m$  experiments an acceleration  $\mathbf{a}$  due to  
20       a net force  $\sum \mathbf{F}$ , this acceleration is related to the mass and  
21       force by the following equation:  
22       
$$\mathbf{a} = \frac{\sum \mathbf{F}}{m}$$
  
23     ]  
24   )
```

Newton's second law

If a body of mass m
experiments an acceleration \mathbf{a}
due to a net force $\sum \mathbf{F}$, this
acceleration is related to the

mass and force by the
following equation:

$$\mathbf{a} = \frac{\sum \mathbf{F}}{m}$$

VIII. Encapsulation example

```
1  #showybox(  
2    title: "Parent container",  
3    lorem(10),  
4    columns(2)[  
5      #showybox(  
6        title-style: (boxed-style: (:)),  
7        title: "Child 1",  
8        lorem(10)  
9      )  
10     #colbreak()  
11     #showybox(  
12       title-style: (boxed-style: (:)),
```

```
13     title: "Child 2",  
14     lorem(10)  
15   )  
16 ]  
17 )
```

Parent container

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do.

Child 1

Lorem ipsum dolor sit amet,
consectetur adipiscing elit, sed
do.

Child 2

Lorem ipsum dolor sit amet,
consectetur adipiscing elit, sed
do.