Package 'cdmTools'

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Type Package

Title Useful Tools for Cognitive Diagnosis Modeling

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Description Provides useful tools for cognitive diagnosis modeling (CDM). The package includes functions for empirical Q-matrix estimation and validation, such as the Hull method (Nájera, Sorrel, de la Torre, & Abad, 2021, <doi:10.1111/bmsp.12228>) and the discrete factor loading method (Wang, Song, & Ding, 2018, <doi:10.1007/978-3-319-77249-3_29>). It also contains dimensionality assessment procedures for CDM, including parallel analysis and automated fit comparison as explored in Nájera, Abad, and Sorrel (2021, <doi:10.3389/fpsyg.2021.614470>). Other relevant methods and features for CDM applications, such as the general nonparametric classification method (Chiu et al., 2018; <doi:10.1007/s11336-017-9595-4>) and corrected estimation of the classification accuracy via multiple imputation (Kreitchmann et al., 2022) are also available. Lastly, the package provides some useful functions for CDM simulation studies, such as random Q-matrix generation and detection of complete/identified Q-matrices.

License GPL-3

LazyData FALSE

Depends R (>= 3.6.0)

Imports GDINA (>= 2.8.0), NPCD (>= 1.0-11), ggplot2 (>= 3.3.0), psych (>= 1.9.12), parallel (>= 3.6.3), stats (>= 3.6.3), GPArotation (>= 2014.11-1), combinat (>= 0.0-8), foreach, doSNOW

URL https://github.com/pablo-najera/cdmTools

BugReports https://github.com/pablo-najera/cdmTools/issues

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CA.MI

R topics documented:

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Description

This function calculates the test-, pattern-, and attribute-level classification accuracy indices based on integrated posterior probabilities from multiple imputed item parameters (Kreitchmann et al., 2022). The classification accuracy indices are the ones developed by Iaconangelo (2017) and Wang et al. (2015). It is only applicable to dichotomous attributes. The function is built upon the CA function from the GDINA package (Ma & de la Torre, 2020).

Usage

```
CA.MI(fit, what = "EAP", R = 500, n.cores = 1, verbose = TRUE, seed = NULL)
```

Arguments

fit	A G-DINA model fit object from the GDINA package (Ma & de la Torre, 2020).
what	What attribute estimates are used? The default is "EAP".
R	Number of bootstrap samples and imputations. The default is 500.
n.cores	Number of processors to use to speed up multiple imputation. The default is 2.
verbose	Show progress. The default is TRUE.
seed	A seed for obtaining consistent results. If NULL, no seed is used. The default is NULL.

Value

CA.MI returns an object of class CA, with a list of elements:

tau Estimated test-level classification accuracy, see Iaconangelo (2017, Eq 2.2) (vector). tau_1 Estimated pattern-level classification accuracy, see Iaconangelo (2017, p. 13) (vector).

 $tau_k \ \ Estimated \ attribute-level \ classification \ accuracy, see \ Wang, \ et \ al \ (2015, p. \ 461 \ Eq \ 6) \ (vector).$

CCM Conditional classification matrix, see Iaconangelo (2017, p. 13) (matrix).

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Author(s)

Rodrigo S. Kreitchmann, Universidad Autónoma de Madrid

References

Iaconangelo, C.(2017). Uses of classification error probabilities in the three-step approach to estimating cognitive diagnosis models. (Unpublished doctoral dissertation). New Brunswick, NJ: Rutgers University.

Kreitchmann, R. S., de la Torre, J., Sorrel, M. A., Nájera, P., & Abad, F. J. (2022). Improving reliability estimation in cognitive diagnosis modeling. [Manuscript submitted for publication].

Ma, W., & de la Torre, J. (2020). GDINA: An R package for cognitive diagnosis modeling. *Journal of Statistical Software*, 93(14). https://doi.org/10.18637/jss.v093.i14

Wang, W., Song, L., Chen, P., Meng, Y., & Ding, S. (2015). Attribute-level and pattern-level classification consistency and accuracy indices for cognitive diagnostic assessment. *Journal of Educational Measurement*, emph52, 457-476.

Examples

```
library(GDINA)
dat <- sim10GDINA$simdat[1:100,]
Q <- sim10GDINA$simQ
fit <- GDINA(dat = dat, Q = Q, model = "GDINA")
ca.mi <- CA.MI(fit, R = 100) # R > 500 is recommended
ca.mi
```

estQ

Empirical Q-matrix estimation

Description

Empirical Q-matrix estimation based on the *discrete factor loading* method (Wang, Song, & Ding, 2018) as used in Nájera, Abad, and Sorrel (2021). Apart from the conventional dichotomization criteria, the procedure based on loading differences described in Garcia-Garzon, Abad, and Garrido (2018) is also available. Furthermore, the bagging bootstrap implementation (Xu & Shang, 2018) can be applied; it is recommended when working with small sample sizes. The psych package (Revelle, 2020) is used for estimating the required exploratory factor analysis (EFA).

Usage

```
estQ(
    r,
    K,
    n.obs = NULL,
    criterion = "row",
    boot = FALSE,
    efa.args = list(cor = "tet", rotation = "oblimin", fm = "uls"),
    boot.args = list(N = 0.8, R = 100, verbose = TRUE, seed = NULL)
)
```

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Arguments

r

A correlation matrix or raw data (matrix or data.frame). If a correlation matrix is used, it must have dimensions J items $\times J$ items. Please note that tetrachoric or polychoric correlations should be used when working with dichotomous or polytomous items, respectively. If raw data is used, it must have dimensions N individuals $\times J$ items. Missing values need to be coded as NA.

K

Number of attributes to use.

n.obs

Number of individuals if r is a correlation matrix. If n.obs is provided, r will be treated as a correlation matrix. Use NULL if r is raw data. The default is NULL.

criterion

Dichotomization criterion to transform the factor loading matrix into the Q-matrix. The possible options include "row" (for row means), "col" (for column means), "loaddiff" (for the procedure based on loading differences), or a value between 0 and 1 (for a specific threshold). The default is "row".

boot

Apply the bagging bootstrap implementation? Only available if r is raw data. If FALSE, the EFA will be applied once using the whole sample size. If TRUE, several EFAs will be applied with different subsamples; the estimated Q-matrix will be dichotomized from the bootstrapped Q-matrix, but the EFA fit indices, factor loadings, and communalities will be computed from the EFA with the whole sample size. The default is FALSE.

efa.args

A list of arguments for the EFA estimation:

cor Type of correlations to use. It includes "cor" (for Pearson correlations) and "tet" (for tetrachoric/polychoric correlations), among others. See fa function from the psych R package for additional details. The default is "tet".

rotation Rotation procedure to use. It includes "oblimin", "varimax", and "promax", among others. An oblique rotation procedure is usually recommended. See fa function from the psych R package for additional details. The default is "oblimin".

fm Factoring method to use. It includes "uls" (for unweighted least squares), "ml" (for maximum likelihood), and "wls" (for weighted least squares), among others. See fa function from the psych R package for additional details. The default is "uls".

boot.args

A list of arguments for the bagging bootstrap implementation (ignored if boot = FALSE):

N Sample size (or proportion of the total sample size, if lower than 1) to use in each bootstrap replication. The default is .8.

R Number of bootstrap replications. The default is 100.

verbose Show progress? The default is TRUE.

seed A seed for obtaining consistent results. If NULL, no seed is used. The default is NULL.

Value

estQ returns an object of class estQ.
est.Q Estimated Q-matrix (matrix).

efa.loads Factor loading matrix (matrix).

efa.comm EFA communalities (vector).

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```
efa.fit EFA model fit indices (vector).
```

boot.Q Bagging bootstrap Q-matrix before dichotomization. Only if boot = TRUE (matrix).

is.Qid Is the generated Q-matrix identifiable under the DINA/DINO models or others CDMs? (vector).

specifications Function call specifications (list).

Author(s)

Pablo Nájera, Universidad Autónoma de Madrid

References

Garcia-Garzon, E., Abad, F. J., & Garrido, L. E. (2018). Improving bi-factor exploratory modelling: Empirical target rotation based on loading differences. *Methodology*, *15*, 45–55. https://doi.org/10.1027/1614-2241/a000163

Nájera, P., Abad, F. J., & Sorrel, M. A. (2021). Determining the number of attributes in cognitive diagnosis modeling. *Frontiers in Psychology*, *12*:614470. https://doi.org/10.3389/fpsyg.2021.614470

Revelle, W. (2019). *psych: Procedures for Psychological, Psychometric, and Personality Research*. R package version 1.9.12. https://CRAN.R-project.org/package=psych.

Wang, W., Song, L., & Ding, S. (2018). An exploratory discrete factor loading method for Q-matrix specification in cognitive diagnosis models. In: M. Wilberg, S. Culpepper, R. Janssen, J. Gonzalez, & D. Molenaar (Eds.), *Quantitative Psychology. IMPS 2017. Springer Proceedings in Mathematics & Statistics* (Vol. 233, pp. 351–362). Springer.

Xu, G., & Shang, Z. (2018). Identifying latent structures in restricted latent class models. *Journal of the American Statistical Association*, 113, 1284–1295. https://doi.org/10.1080/01621459.2017.1340889

6 genQ

genQ	Generate Q-matrix
0 (~

Description

Generates a Q-matrix. The criteria from Chen, Liu, Xu, & Ying (2015) and Xu & Shang (2018) can be used to generate identifiable Q-matrices. Only binary Q-matrix are supported so far. Useful for simulation studies.

Usage

```
genQ(J, K, Kj, I = 2, min.JK = 3, max.Kcor = 1, Qid = "none", seed = NULL)
```

Arguments

J	Number of items.
K	Number of attributes.
Kj	A vector specifying the number (or proportion, if summing up to 1) of items measuring 1, 2, 3,, attributes. The first element of the vector determines the number (or proportion) of items measuring 1 attribute, and so on. See Examples.
I	Number of identity matrices to include in the Q-matrix (up to column permutation). The default is 2 .
min.JK	Minimum number of items measuring each attribute. It can be overwritten by I, if I is higher than min. JK. The default is 3.
max.Kcor	Maximum allowed tetrachoric correlation among the columns to avoid overlapping (Nájera, Sorrel, de la Torre, & Abad, 2020). The default is 1.
Qid	Assure that the generated Q-matrix is identifiable. It includes "none" (for no identifiability assurance), "DINA", "DINO", or "others" (for other CDMs identifiability). The default is "none".
seed	A seed for obtaining consistent results. If NULL, no seed is used. The default is NULL.

Value

```
genQ returns an object of class genQ.
```

gen.Q The generated Q-matrix (matrix).

JK Number of items measuring each attribute (vector).

Kcor Tetrachoric correlations among the columns (matrix).

is.Qid Is the generated Q-matrix identifiable under the DINA/DINO models or others CDMs? (vector).

specifications Function call specifications (list).

Author(s)

Pablo Nájera, Universidad Autónoma de Madrid

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References

Chen, Y., Liu, J., Xu, G., & Ying, Z. (2015). Statistical analysis of Q-matrix based diagnostic classification models. *Journal of the American Statistical Association*, *110*, 850-866. https://doi.org/10.1080/01621459.2014.9

Nájera, P., Sorrel, M. A., de la Torre, J., & Abad, F. J. (2020). Balancing fit and parsimony to improve Q-matrix validation. *British Journal of Mathematical and Statistical Psychology*. https://doi.org/10.1111/bmsp.122

Xu, G., & Shang, Z. (2018). Identifying latent structures in restricted latent class models. *Journal of the American Statistical Association*, 113, 1284-1295. https://doi.org/10.1080/01621459.2017.1340889

Examples

```
Kj <- c(15, 10, 0, 5) \# 15 one-att, 10 2-atts, 0 3-atts, and 5 four-atts items Q <- genQ(J = 30, K = 4, Kj = Kj, Qid = "others", seed = 123)
```

GNPC

General nonparametric classification method

Description

Attribute profile estimation using the *general nonparametric classification method* (GNPC; Chiu, Sun, & Bian, 2018). The GNPC can be considered as a robust alternative to the parametric G-DINA model with low sample sizes. The AlphaNP function from the NPCD package (Zheng & Chiu, 2019; Chiu, Sun, & Bian, 2018) using weighted Hamming distances is used to initiate the procedure.

Usage

```
GNPC(
  dat,
  Q,
  initiate = "AND",
  min.change = 0.001,
  maxitr = 1000,
  verbose = TRUE
)
```

Arguments

dat	A N individuals x J items (matrix or data.frame). Missing values need to be coded as NA. Caution is advised if missing data are present.
Q	A J items x K attributes Q-matrix (matrix or data.frame).
initiate	Should the conjunctive ("AND") or disjunctive ("OR") NPC be used to initiate the procedure? Default is "AND".
min.change	Minimum proportion of modified attribute profiles to use as a stopping criterion. Default is $.001$.
maxitr	Maximum number of iterations. Default is 1000.
verbose	Print information after each iteration. Default is TRUE.

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Value

```
\ensuremath{\mathsf{GNPC}} returns an object of class \ensuremath{\mathsf{GNPC}}.
```

alpha.est Estimated attribute profiles (matrix).

loss.matrix The distances between the weighted ideal responses from each latent class (rows) and examinees' observed responses (columns) (matrix).

eta.w The weighted ideal responses for each latent class (rows) on each item (columns) (matrix).

w The estimated weights, used to compute the weighted ideal responses (matrix).

n.ite Number of iterations required to achieve convergence (double).

hist.change Proportion of modified attribute profiles in each iteration (vector).

specifications Function call specifications (list).

Author(s)

Pablo Nájera, Universidad Autónoma de Madrid

References

Chiu, C.-Y., & Douglas, J. (2013). A nonparametric approach to cognitive diagnosis by proximity to ideal response patterns. *Journal of Classification*, *30*, 225-250. DOI: 10.1007/s00357-013-9132-9

Chiu, C.-Y., Sun, Y., & Bian, Y. (2018). Cognitive diagnosis for small education programs: The general nonparametric classification method. *Psychometrika*, 83, 355-375. DOI: 10.1007/s11336-017-9595-4

Zheng, Y., & Chiu, C.-Y. (2019). *NPCD: Nonparametric methods for cognitive diagnosis*. R package version 1.0-11. https://cran.r-project.org/web/packages/NPCD/.

Examples

```
library(GDINA)
Q <- sim30GDINA$simQ # Q-matrix
K <- ncol(Q)
J <- nrow(Q)
set.seed(123)
GS <- data.frame(guessing = rep(0.1, J), slip = rep(0.1, J))
sim <- simGDINA(200, Q, GS)
simdat <- sim$dat # Simulated data
simatt <- sim$attribute # Generating attributes
fit.GNPC <- GNPC(simdat, Q) # Apply the GNPC method
ClassRate(fit.GNPC$alpha.est, simatt) # Check classification accuracy</pre>
```

is.Qid

Check whether a Q-matrix is identifiable

Description

Checks whether a Q-matrix is complete (Köhn & Chiu, 2017, 2018) and identifiable according to the criteria from Chen, Liu, Xu, & Ying (2015) and Xu & Shang (2018).

is.Qid

Usage

```
is.Qid(Q, model = "others", verbose = TRUE)
```

Arguments

Q A *J* items x *K* attributes Q-matrix (matrix or data.frame).

model CDM to be considered. It includes "DINA", "DINO", or "others" (for other

CDMs; e.g., G-DINA, A-CDM). The default is "others".

verbose Should a message about the identifiability of the Q-matrix be printed? The de-

fault is TRUE.

Value

is.Qid returns an object of class is.Qid.

id.Q Is the Q-matrix identifiable? (logical).

comp.Q Is the Q-matrix complete? (logical).

criteria.Qid Identifiability criteria and whether they are fulfilled or not (vector).

message A message about the identifiability of the Q-matrix and references (string).

specifications Function call specifications (list).

Author(s)

Pablo Nájera, Universidad Autónoma de Madrid Miguel A. Sorrel, Universidad Autónoma de Madrid

References

Chen, Y., Liu, J., Xu, G., & Ying, Z. (2015). Statistical analysis of Q-matrix based diagnostic classification models. *Journal of the American Statistical Association*, 110, 850-866. https://doi.org/10.1080/01621459.2014.9

Köhn, H.-F., & Chiu, C.-Y. (2017). A procedure for assessing the completeness of the Q-matrices of cognitively diagnostic tests. *Psychometrika*, 82, 112-132. https://doi.org/10.1007/s11336-016-9536-7

Köhn, H.-F., & Chiu, C.-Y. (2018). How to build a complete Q-matrix for a cognitively diagnostic test. *Journal of Classification*, *35*, 273-299. https://doi.org/10.1007/s00357-018-9255-0

Xu, G., & Shang, Z. (2018). Identifying latent structures in restricted latent class models. *Journal of the American Statistical Association*, 113, 1284-1295. https://doi.org/10.1080/01621459.2017.1340889

```
Kj \leftarrow c(15, 10, 0, 5)
Q \leftarrow genQ(J = 30, K = 4, Kj = Kj, Qid = "others", seed = 123)$gen.QidQ <math>\leftarrow is.Qid(Q)
```

10 missQ

missQ	Introduce random	misspecifications in	Q-matrix

Description

Introduces random misspecifications in a Q-matrix. Only binary Q-matrix are supported so far. Useful for simulation studies.

Usage

```
missQ(Q, qjk, retainJ = 0, Qid = "none", seed = NULL)
```

Arguments

Q	A J items x K attributes Q-matrix (matrix or data.frame).
qjk	Number (or proportion, if lower than 1) of q-entries to modify in the Q-matrix.
retainJ	Number of items to retain (i.e., not modify) in the Q-matrix. It will retain the first retainJ items. It is useful for assuring the completeness of the misspecified Q-matrix if the first items conform one or more identity matrices. The default is 0.
Qid	Assure that the generated Q-matrix is identifiable. It includes "none" (for no identifiability assurance), "DINA", "DINO", or "others" (for other CDMs identifiability). The default is "none".
seed	A seed for obtaining consistent results. If NULL, no seed is used. The default is NULL.

Value

missQ returns an object of class missQ.

miss.Q The misspecified Q-matrix (matrix).

Q The input (true) Q-matrix (matrix).

JK Number of items measuring each attribute (vector).

Kcor Tetrachoric correlations among the columns (matrix).

is.Qid Is the generated Q-matrix identifiable under the DINA/DINO models or others CDMs? (vector).

specifications Function call specifications (list).

Author(s)

Pablo Nájera, Universidad Autónoma de Madrid

References

Xu, G., & Shang, Z. (2018). Identifying latent structures in restricted latent class models. *Journal of the American Statistical Association*, 113, 1284-1295. https://doi.org/10.1080/01621459.2017.1340889

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Examples

```
Kj <- c(15, 10, 0, 5) \# 15 \text{ one-att}, 10 2-atts, 0 3-atts, and 5 four-atts items Q <- genQ(J = 30, K = 4, Kj = Kj, Qid = "others", seed = 123) miss.Q <- missQ(Q = Q$gen.Q, qjk = .20, retainJ = 4, seed = 123)
```

modelcompK

CDM fit comparison - dimensionality assessment method

Description

A procedure for determining the number of attributes underlying CDM using model fit comparison. For each number of attributes under exploration, a Q-matrix is estimated from the data using the *discrete factor loading* method (Wang, Song, & Ding, 2018), which can be further validated using the *Hull* method (Nájera, Sorrel, de la Torre, & Abad, 2020). Then, a CDM is fitted to the data using the resulting Q-matrix, and several fit indices are computed. After the desired range of number of attributes has been explored, the fit indices are compared. A suggested number of attributes is given for each fit index. The AIC index should be preferred among the other fit indices. For further details, see Nájera, Abad, & Sorrel (2021). This function can be also used by directly providing different Q-matrices (instead of estimating them from the data) in order to compare their fit and select the most appropriate Q-matrix. Note that, if Q-matrices are provided, this function will no longer serve as a dimensionality assessment method, but just as an automated model comparison procedure.

Usage

```
modelcompK(
  dat,
  exploreK = 1:7,
  Qs = NULL,
  stop = "none",
  val.Q = TRUE,
  estQ.args = list(criterion = "row", cor = "tet", rotation = "oblimin", fm = "uls"),
  valQ.args = list(index = "PVAF", iterative = "test.att", maxitr = 5, CDMconv = 0.01),
  verbose = TRUE
)
```

Arguments

dat

A N individuals x J items (matrix or data. frame). Missing values need to be coded as NA.

exploreK

Number of attributes to explore. The default is from 1 to 7 attributes.

Qs

A list of Q-matrices to compare in terms of fit. If Qs is used, exploreK is ignored.

stop

A fit index to use for stopping the procedure if a model leads to worse fit than a simpler one. This can be useful for saving time without exploring the whole exploreK when it is probable that the correct dimensionality has been already visited. It includes "AIC", "BIC", "CAIC", "SABIC", "M2", "SRMSR", "RMSEA2", or "sig.item.pairs". The latter represents the number of items that show bad fit with at least another item based on the transformed correlations (see itemfit function in the GDINA package; Ma & de la Torre, 2020). It can be also "none", which means that the whole exploreK will be examined. The default is "none".

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val.Q Validate the estimated Q-matrices using the *Hull* method? Note that validating the Q-matrix is expected to increase its quality, but the computation time will increase. The default is TRUE.

A list of arguments for the discrete factor loading empirical Q-matrix estimation estQ.args method (see the estQ function):

- criterion Dichotomization criterion to transform the factor loading matrix into the Q-matrix. The possible options include "row" (for row means), "col" (for column means), "loaddiff" (for the procedure based on loading differences), or a value between 0 and 1 (for a specific threshold). The default is "row".
- cor Type of correlations to use. It includes "cor" (for Pearson correlations) and "tet" (for tetrachoric/polychoric correlations), among others. See fa function from the psych R package for additional details. The default is "tet".
- rotation Rotation procedure to use. It includes "oblimin", "varimax", and "promax", among others. An oblique rotation procedure is usually recommended. See fa function from the psych R package for additional details. The default is "oblimin".
- fm Factoring method to use. It includes "uls" (for unweighted least squares), "ml" (for maximum likelihood), and "wls" (for weighted least squares), among others. See fa function from the psych R package for additional details. The default is "uls".

valQ.args A list of arguments for the Hull empirical Q-matrix validation method. Only applicable if valQ = TRUE (see the valQ function):

index What index to use. It includes "PVAF" or "R2". The default is "PVAF".

- iterative (Iterative) implementation procedure. It includes "none" (for noniterative), "test" (for test-level iterations), "test.att" (for test-level iterations modifying the least possible amount of q-entries in each iteration), and "item" (for item-level iterations). The default is "test.att".
- maxitr Maximum number of iterations if an iterative procedure has been selected. The default is 5.
- CDMconv Convergence criteria for the CDM estimations between iterations (only if an iterative procedure has been selected). The default is 0.01.

verbose Show progress? The default is TRUE.

Value

modelcompK returns an object of class modelcompK.

- sug.K The suggested number of attributes for each fit index (vector). Only if Qs = NULL.
- sel.Q The suggested Q-matrix for each fit index (vector).
- fit The fit indices for each fitted model (matrix).
- exp.exploreK Explored dimensionality (vector). It can be different from exploreK if stop has been used.
- usedQ Q-matrices used to fit each model (list). They will be the estimated (and validated) Qmatrices if Qs = NULL. Otherwise, they will be Qs.

specifications Function call specifications (list).

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Author(s)

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References

Ma, W., & de la Torre, J. (2020). GDINA: An R package for cognitive diagnosis modeling. *Journal of Statistical Software*, 93(14). https://doi.org/10.18637/jss.v093.i14

Nájera, P., Abad, F. J., & Sorrel, M. A. (2021). Determining the number of attributes in cognitive diagnosis modeling. *Frontiers in Psychology*, *12*:614470. https://doi.org/10.3389/fpsyg.2021.614470

Nájera, P., Sorrel, M. A., de la Torre, J., & Abad, F. J. (2020). Balancing fit and parsimony to improve Q-matrix validation. *British Journal of Mathematical and Statistical Psychology*. https://doi.org/10.1111/bmsp.122

Wang, W., Song, L., & Ding, S. (2018). An exploratory discrete factor loading method for Q-matrix specification in cognitive diagnosis models. In: M. Wilberg, S. Culpepper, R. Janssen, J. González, & D. Molenaar (Eds.), *Quantitative Psychology. IMPS 2017. Springer Proceedings in Mathematics & Statistics* (Vol. 233, pp. 351-362). Springer.

```
library(GDINA)
dat <- sim30GDINA$simdat</pre>
Q <- sim30GDINA$simQ
# Assess dimensionality from CDM data
#-----
mcK <- modelcompK(dat = dat, exploreK = 4:7, stop = "AIC", val.Q = TRUE, verbose = TRUE)</pre>
mcKsug.K # Check suggested number of attributes by each fit index
mcK$fit # Check fit indices for each K explored
sug.Q \leftarrow mcK sug.K["AIC"])]] # Suggested Q-matrix by AIC Suggested Q-matrix B-matrix 
sug.Q <- orderQ(sug.Q, Q)$order.Q # Reorder Q-matrix attributes</pre>
mean(sug.Q == Q) # Check similarity with the generating Q-matrix
#-----
# Automatic fit comparison of competing Q-matrices
trueQ <- Q
missQ1 \leftarrow missQ(Q, .10, seed = 123)$miss.Q
missQ2 \leftarrow missQ(Q, .20, seed = 456)$miss.Q
missQ3 \leftarrow missQ(Q, .30, seed = 789)$miss.Q
Qs <- list(trueQ, missQ1, missQ2, missQ3)
mc <- modelcompK(dat = dat, Qs = Qs, verbose = TRUE)</pre>
mc$sel.Q # Best-fitting Q-matrix for each fit index
mc$fit # Check fit indices for each Q explored
```

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orderQ

Reorder Q-matrix columns

Description

Reorders Q-matrix columns according to a target matrix (e.g., another Q-matrix). Specifically, it provides a reordered Q-matrix which columns show the lowest possible average Tucker index congruent coefficient with the target columns. Reordering a Q-matrix is alike relabeling the attributes and it does not change the model. Useful for simulation studies (e.g., comparing a validated Q-matrix with the generating Q-matrix).

Usage

```
orderQ(Q, target)
```

Arguments

Q A *J* items x *K* attributes Q-matrix (matrix or data.frame). This is the Q-matrix

that will be reordered.

target A J items x K attributes Q-matrix (matrix or data.frame). This could be the

"true", generating Q-matrix.

Value

orderQ returns an object of class orderQ.

```
order.Q The reordered Q-matrix (matrix).
```

configs Comparison information between the different column configurations of the Q-matrix and the target Q-matrix, including the average absolute difference and the average Tucker index of factor congruence (matrix). The function will not look for all possible specifications if a perfect match is found.

specifications Function call specifications (list).

Author(s)

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```
library(GDINA) dat <- sim30GDINA$simdat Q <- sim30GDINA$simQ sugQ1 <- estQ(r = dat, K = 5) # Estimate Q-matrix sugQ1$est.Q <- orderQ(sugQ1$est.Q, Q)$order.Q # Reorder Q-matrix attributes mean(sugQ1$est.Q == Q) # Check similarity with the generating Q-matrix
```

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paK Parallel analysis - dimensionality assessment method

Description

Parallel analysis with column permutation (i.e., resampling) as used in Nájera, Abad, & Sorrel (2021). It is recommended to use principal components, Pearson correlations, and mean criterion (Garrido, Abad, & Ponsoda, 2013; Nájera, Abad, & Sorrel, 2021). The parallel analysis based on principal axis factor analysis is conducted using the fa.parallel function of the psych R package (Revelle, 2020). The tetrachoric correlations are efficiently estimated using the sirt R package (Robitzsch, 2020). The graph is made with the ggplot2 package (Wickham et al., 2020).

Usage

```
paK(
    dat,
    R = 100,
    fa = "pc",
    cor = "both",
    cutoff = "mean",
    fm = "uls",
    plot = TRUE,
    verbose = TRUE,
    seed = NULL
)
```

Arguments

dat	A N individuals \mathbf{x} J items (matrix or data.frame). Missing values need to be coded as NA.
R	Number of resampled datasets (i.e., replications) to generate. The default is 100.
fa	Extraction method to use. It includes "pc" (for principal components analysis), "fa" (for principal axis factor analysis), and "both". The default is "pc".
cor	What type of correlations to use. It includes "cor" (for Pearson correlations), "tet" (for tetrachoric/polychoric correlations), and "both". The default is "both".
cutoff	What criterion to use as the cutoff. It can be "mean" (for the average generated eigenvalues) or a value between 0 and 100 (for a percentile). A vector with several criteria can be used. The default is "mean".
fm	Factoring method to use. It includes "uls" (for unweighted least squares), "ml" (for maximum likelihood), and "wls" (for weighted least squares), among others. The default is "uls".
plot	Print the parallel analysis plot? Note that the plot might be messy if many variants are requested. The default is TRUE.
verbose	progress. The default is TRUE.
seed	A seed for obtaining consistent results. If NULL, no seed is used. The default is NULL.

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Value

```
paK returns an object of class paK.
sug.K The suggested number of attributes for each variant (vector).
e.values The sample and reference eigenvalues (matrix).
plot The parallel analysis plot. Only if plot = TRUE (plot).
specifications Function call specifications (list).
```

Author(s)

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Revelle, W. (2019). *psych: Procedures for Psychological, Psychometric, and Personality Research*. R package version 1.9.12. https://CRAN.R-project.org/package=psych.

Robitzsch, A. (2020). *sirt: Supplementary Item Response Theory Models*. R package version 3.9-4. https://CRAN.R-project.org/package=sirt.

Wickham, H., et al. (2020). *ggplot2: Create Elegant Data Visualisations Using the Grammar of Graphics*. R package version 3.3.2. https://CRAN.R-project.org/package=ggplot2.

Examples

```
library(GDINA)
dat <- sim30GDINA$simdat
Q <- sim30GDINA$simQ
# In paK, R = 100 is recommended (R = 30 is here used for illustration purposes)
pa.K <- paK(dat = dat, R = 30, fa = "pc", cutoff = c("mean", 95), plot = TRUE, seed = 123)
pa.K$sug.K # Check suggested number of attributes by each parallel analysis variant
pa.K$e.values # Check eigenvalues
pa.K$plot # Show parallel analysis plot</pre>
```

valQ

Empirical Q-matrix validation

Description

Empirical Q-matrix validation using the *Hull* method (Nájera, Sorrel, de la Torre, & Abad, 2020a). The procedure can be used either with the PVAF (de la Torre & Chiu, 2016) or McFadden's pseudo R-squared (McFadden, 1974). The PVAF is recommended (Nájera, Sorrel, de la Torre, & Abad, 2020a). Note that the pseudo R-squared might not be computationally feasible for highly dimensional Q-matrices, say more than 10 attributes. Different iterative implementations are available, such as the test-level implementation (see Terzi & de la Torre, 2018), attribute-test-level implementation (Nájera, Sorrel, de la Torre, & Abad, 2020a), and item-level implementation (Nájera, Sorrel, de la Torre, & Abad, 2020b). If an iterative implementation is used, the GDINA R package (Ma & de la Torre, 2020) is used for the calibration of the CDMs.

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Usage

```
valQ(
  fit,
  index = "PVAF",
  iterative = "test.att",
  emptyatt = TRUE,
  maxitr = 100,
  CDMconv = 1e-04,
  verbose = TRUE
)
```

Arguments

fit A G-DINA model fit object from the GDINA package (Ma & de la Torre, 2020).

index What index to use. It includes "PVAF" or "R2". The default is "PVAF".

iterative (Iterative) implementation procedure. It includes "none" (for non-iterative),

"test" (for test-level iterations), "test.att" (for attribute-test-level), and "item"

(for item-level iterations). The default is "test.att".

emptyatt Is it possible for the suggested Q-matrix to have an empty attribute (i.e., an

attribute not measured by any item)? Although rarely, it is possible for iterative procedures to provide a suggested Q-matrix in which one or more attributes are empty. This might indicate that the original Q-matrix had more attributes than necessary. If FALSE, then at least one item (i.e., the one that is most likely) will

measure each attribute in the suggested Q-matrix. The default is TRUE.

maxitr Maximum number of iterations if an iterative procedure has been selected. The

default is 100.

CDMconv Convergence criteria for the CDM estimations between iterations (only if an

iterative procedure has been selected). The default is 0.0001.

verbose Print information after each iteration if an iterative procedure is used. The de-

fault is TRUE.

Value

valQ returns an object of class valQ.

sug.Q Suggested Q-matrix (matrix).

Q Original Q-matrix (matrix).

sugQ. fit Several fit indices from the model obtained with the suggested Q-matrix (vector).

index PVAF or pseudo R-squared (depending on which one was used) for each item (matrix).

iter.Q Q-matrices used in each iteration (list). Provided only if an iterative procedure has been used.

iter.index PVAF or pseudo R-squared (depending on which one was used) for each item in each iteration (list). Provided only if an iterative procedure has been used.

n.iter Number of iterations used (double). Provided only if an iterative procedure has been used.

convergence Convergence information (double). It can be 1 (convergence), 2 (lack of convergence: maximum number of iterations achieved), 3 (lack of convergence: empty attribute obtained), and 4 (lack of convergence: loop Q-matrices). Provided only if an iterative procedure has been used.

time Initial and finish time (vector).

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time.used Total computation time (difftime). specifications Function call specifications (list).

Author(s)

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Terzi, R., & de la Torre, J. (2018). An iterative method for empirically-based Q-matrix validation. *International Journal of Assessment Tools in Education*, *5*, 248-262. https://doi.org/10.21449/ijate.407193

```
library(GDINA)
dat <- sim30GDINA$simdat
Q <- sim30GDINA$simQ # Generating Q-matrix
miss.Q <- missQ(Q = Q, qjk = .30, retainJ = 5, seed = 123)$miss.Q # Misspecified Q-matrix
fit <- GDINA(dat, miss.Q) # GDINA object
sug.Q <- valQ(fit = fit, verbose = TRUE) # Hull method for Q-matrix validation
mean(sug.Q$sug.Q == Q) # Check similarity with the generating Q-matrix</pre>
```

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