Universidad de Alcalá Escuela Politécnica Superior

Grado en Ingeniería Informática

Trabajo Fin de Grado

On the Data Quality Characteristics of Software Engineering

Defect Prediction Datasets

ESCUELA POLITECNICA

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UNIVERSIDAD DE ALCALÁ

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	Vocal 2º:	Name of the second vocal
	Calificación:	

Fecha:



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Sin entrenamiento, no existe el conocimiento. Sin conocimiento, no existe la confianza. Sin confianza, la victoria no existe.

Julio César

Tras muchas horas de esfuerzo, querer tirarme de los pelos, dar cabezazos contra la pared o querer gritar...simplemente han pasado 4 años, sin darme cuenta. Siempre he tenido junto a mí el apoyo de mi familia o amigos; también he conocido a quienes los considero como a mis hermanos; hay quienes han venido, han dejado su marca, y han venido casi sin despedirse - pero todo ello me ha hecho convencerme de un solo dogma: no podría haber hecho esto solo.

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 memoria hasta que esta empiece a fallar.

Resumen

Este documento ha sido generado con una plantilla para memorias de trabajos fin de carrera, fin de máster, fin de grado y tesis doctorales. Está especialmente pensado para su uso en la Universidad de Alcalá, pero debería ser fácilmente extensible y adaptable a otros casos de uso. En su contenido se incluyen las instrucciones generales para usarlo, así como algunos ejemplos de elementos que pueden ser de utilidad. Si tenéis problemas, sugerencias o comentarios sobre el mismo, dirigidlas por favor a Pablo Acereda García pablo.acereda@edu.uah.es>.

Palabras clave: Plantillas de trabajos fin de carrera/máster/grado y tesis doctorales, IATEX, soporte de español e inglés, generación automática.

Abstract

This document has been generated with a template for Bsc and Msc Thesis (trabajos fin de carrera, fin de máster, fin de grado) and PhD. Thesis, specially thought for its use in Universidad de Alcalá, although it should be easily extended and adapted for other use cases. In its content we include general instructions of use, and some example of elements than can be useful. If you have problemas, suggestions or comments on the template, please forward them to Pablo Acereda García pablo.acereda@edu.uah.es>.

Keywords: Data Mining, Imbalanced Data, Complexity Metrics, Under Sampling, Over Sampling.

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Chapter 1

Introduction

1.1. Introduction to Machine Learning

Through time, humans wanted to keep all memories or thoughts precious to them for posterity. Thanks to some technological advancements, larges amounts of information can be stored for a relatively cheap price - videos, photographs, drawings, weather measures, financial information, academic data, etc. It can all be digitalized and kept *forever*. These new possibilities also brought new challenges. What to do with all that information? Data scientists try to manage and make some sense out of the overwhelming new information that is being continuously created.

The figure of a data scientist is the one who uses scientific methods, processes, algorithms and systems to extract knowledge from structured and unstructured data. The algorithms used in data science, are sequences of statistical processing steps. Then, there is Machine Learning which uses computer algorithms that improve through experience - it is also a subset of Artificial Intelligence (AI). In this case, the algorithms are *trained* to filter and discover patterns and features with massive amounts of data.

The training and learning processes allow us to make predictions and decisions for new data, being advantageous for almost any field: commercial purposes, fraud detection, fault prediction, health, environment (climate), network traffic, and so on.

The number of machine learning tools/techniques applied in this project is quite large and those are further explained in the *Background* (Section 2). As a brief introduction to the techniques and material in this paper, it has been used ECol R package to obtain the complexity metrics of several datasets; the Python's scikit-learn package for learning algorithms and some performance metrics for the classification algorithms (used through the experiments); as well as the imbalanced-learn Python package to deal with imbalanced datasets. The resulting scripts allow us the visualization between different tables and plots for comparing results.

1.2. Aim and Objectives

Here we analyse the complexity metrics proposed by Ho and Basu [4] in a number of software defect datasets, that have been previously implemented in ECol R package.

The aim of this work is to explore complexity metrics on software defect datasets. Also, to analyse how classification algorithms are affected by techniques that mitigate imbalance and how that affects the complexity metrics previously analysed. To do so, we explore several objectives:

- RQ1 How complexity metrics are correlated to the outcome of supervised algorithms?
- RQ2 How complexity metrics and imbalance are related?
- RQ3 Do complexity metrics tell us something about the quality of the datasets?

The purpose of this dissertation is to conduct a study of complexity metrics and imbalanced datasets. A comparison between the raw data and that data after performing some changes that should affect the results: K-folding Cross Validation (CV), imbalanced techniques, etc.

Chapter 2

Background

2.1. Data Complexity Metrics

There are many complexity metrics that could be used for the scope of this project, but it has been chosen the ones that are explained below; following the metrics obtained from [4], and surveys by Lorena et al [2,5] (see also [6]). They are also implemented in the Extended Complexity Metrics Library (ECoL) for R.

These are a set of measures that help characterizing the complexity of classification and regression problems. The measures that are going to be computed for this project are:

- Overlapping Evaluate how informative the available features are to separate the classes. See 2.1.1 for more details.
- **Neighborhood** Characterize the presence and density of classes in local neighborhoods. See 2.1.2 for more details.
- **Linearity** Quantify, if it is possible, whether classes are linear separable by a hyperplane or linear function. See 2.1.3 for more details.
- **Dimensionality** Indicative of data sparsity, how smoothly samples are distributed within attributes. See ?? for more details.
- Balance Capture the difference in the number of examples per class in the dataset. See 2.1.5 for more details
- **Network** Represents the dataset as a graph and extracts structural information out of it. See 2.1.6 for more details.
- Correlation Relationship between the feature values and the outputs. See 2.1.7 for more details.
- **Smoothness** In regression problems, the smoother the function to be fitted to the data, the simpler it shall be. See 2.1.8 for more details.

These complexity measures are going to be computed for certain datasets and comparisons between results are going to be made.

2.1.1. Measures of Overlap of Individual Feature Values

An overlapped dataset is defined as a multi-class dataset where the data is interlaced. The meaning of this statement is explained as follows: having a dataset whose geometrical expression have the domain, D_n^1 , a second class will have a domain, D'_n , intersecting that of the first class.

2.1.1.1. Fisher's Discriminant Ratio (F1)

This metric is specific to one feature dimension. Even if the given problem is multidimensional, not necessarily all features have to contribute to class discrimination, only one of the features needs to be the discriminant. Fulfilling this statement would ease the complexity of the problem.

The measure uses the following mathematical expression:

$$f = \frac{(\mu_1 - \mu_2)^2}{\sigma_1^2 + \sigma_2^2}$$

Where $\mu_1, \mu_2, \sigma_1^2, \sigma_2^2$ are the means and variances, respectively, of the two classes².

2.1.1.2. Directional Vector Fishers Discriminant Ratio (F1v)

Complemented F1 (see Section 2.1.1.1). It does so by searching for a vector capable of separating two classes after the training samples have been projected into it.

2.1.1.3. Volume of Overlap Region (F2)

Another way to measure the complexity is by using the tails of the overlap of the classes. This is accomplished by taking the maximum and minimum values of each class. Afterwards, the length of overlap is calculated, normalized by range of the classes. This is done by:

$$f = \prod_{i} \frac{MIN(max(f_i, c_1), max(f_i, c_2)) - MAX(min(f_i, c_1), min(f_i, c_2))}{MAX(max(f_i, c_1), max(f_i, c_2)) - MIN(min(f_i, c_1), min(f_i, c_2))}$$

Where f_i indicates the feature; c_n indicates the class; and i indicates the dimensionality of the problem.

2.1.1.4. Feature Efficiency (F3)

In this measure, in high-dimensional problems, each feature is evaluated separately on how much it contributes to the separation of the classes. If there exists overlap within the range of each class for a certain feature, the class is considered to be ambiguous for that dimension in the specific region where the overlap takes place.

Therefore a problem will be more feasible if the exists at least one feature where the ranges for each class do not overlap. Thus, the *maximum feature efficiency* will be used as a measure. This measure is obtained with the entire training set, by obtaining the remaining points being separable by the feature.

 $^{^{1}}$ Being n the number of attributes for that class

²It has been used two classes for the definition of the metric, but more classes could be added to the problem.

2.1.1.5. Collective Feature Efficiency (F4)

It gives an overview on how different features may work together in data separation. The most discriminant feature (see F3 - 2.1.1.4) is selected and then all samples separable by this feature are removed from the dataset. This process is repeated with all the features until no samples are left. The resulting value of this metric comes from the ratio of samples that have been discriminated.

2.1.2. Measures of Neighborhood

For a certain set of target classes in a dataset, the neighborhood measures try to analyze the neighbor data items of every data point and try to capture class overlapping and the shape of the decision boundary. The work is done over a distance matrix which stores distances between all pairs of data points in the dataset.

2.1.2.1. Mixture Identifiability (N1, N2, N3)

The measure is defined as the mean Euclidean distance from each point in the dataset, to its nearest neighbors, not minding the class they are in [7]. The valuable rates that can be taken are the means for interclass neighbors and intraclass neighbors.

2.1.2.2. Non-linearity of the Nearest Neighbor Classifier (N4)

It builds a new dataset by interpolating pairs of training samples of the same class and the induce a 1NN classifier on the original data and measure the error rate in the new data points.

2.1.2.3. Fraction of Hyper-spheres Covering Data (T1)

It creates a hyper-sphere centered at each one of the training samples. Their radios are then growth until one hyper-sphere reaches a sample of other class. Then, smaller hyper-spheres contained in larger hyper-spheres are eliminated. This measure is the ratio between the number of remaining hyper-spheres and the total number of samples in the dataset.

2.1.2.4. Local Set Average Cardinality (LSC)

It is a set of points from the dataset whose distance of each sample is smaller than the distance from the samples of the different classes.

2.1.3. Measures of Separability of Classes

Given two, or more classes, inside a certain dataset, they can be called linear separable if a straight line between those classes can be drawn. As the previous statement suggests, the classes must be isolated clusters after the linear function is delimited.

2.1.3.1. Linear Separability (L1, L2, L3)

As a way to adapt to separable and non-separable problems, it is used the formulation proposed by Smith [8], which minimizes an error function:

$$\label{eq:subject_to_Z} \begin{aligned} & \text{minimize } a^t t \\ & \text{subject to } Z^t w + t \geq b \\ & t > 0 \end{aligned}$$

Implying that a and b are vectors; w is the weight vector; t is the error vector and Z is a matrix obtained by adding one dimension, with value one, to the input vector \mathbf{x} .

2.1.4. Measures of Dimensionality

For any dataset, the dimensionality measures will indicate data sparsity. These measures capture how sparse a dataset tends to have regions of low density. These regions have been proven to be harder for the extraction of good classification and regression models.

2.1.4.1. Average Number of samples per dimension (T2)

It represents the average number of points per dimension. It is calculated with the ratio between the number of examples and dimensionality of the dataset.

2.1.4.2. Average intrinsic dimensionality per number of samples (T3)

Another way to measure the dimensionality of a dataset, is by computing the average of number of points per PCA. It is a similar measure to T2, which uses the number of PCA components needed to represent 95 variability as the base of a data sparsity assessment.

2.1.4.3. Intrinsic dimensionality proportion (T4)

It represents a ratio of PCA Dimensions to the original. It returns an estimate of the proportion of relevant and original dimensions of the dataset.

2.1.5. Measures of Class Balance

Given a dataset, *balance measures* capture the differences in the number of samples per class for that dataset. When the imbalance ratio is too severe, problems related to generalization of classification techniques can happen.

2.1.5.1. Entropy of class proportions (C1)

This measure captures the imbalance of a dataset using proportions of samples per class.

2.1.5.2. Multi-class imbalance ratio (C2)

The ratio at hand represents an index calculated to measure a class balance. It is not only suited for binary class classification problems, but also is suited for multi-class classification problems.

2.1.6. Measures of Network

These measures create a graph representation of the dataset to extract structural information from it. The transformation between raw data and the graph representation is based on the epsilon-NN ($\varepsilon-NN$) algorithm. Afterwards, a post-processing step is applied to the graph, pruning edges between samples of opposite classes.

2.1.6.1. Average density of of network (Density)

It is a representation of the count of edges in the graph, divided by the maximum number of edges between pairs of data points.

2.1.6.2. Clustering Coefficient (ClsCoef)

Computes the average of the clustering tendency of the vertices by the ratio of existent edges between neighbors and the total number of edges that could possibly exist between them.

2.1.6.3. Average hub score (Hubs)

Is given by the number of connections to other nodes, weighted by the amount of connections the neighbors have.

2.1.7. Measures of Feature Correlation

A regression task that calculate the correlation of the values of the features to the outputs. In case one feature is highly correlated to the output, it is understandable that simpler functions can be fitted to the data.

2.1.7.1. Maximum/Average feature correlation to the output (C1, C2)

Representation of the maximum/average value of the Spearman correlations for each feature and the output.

2.1.7.2. Individual feature efficiency (C3)

Returns the number of samples to be removed from the dataset to reach a high Spearman correlation value to the output.

2.1.7.3. Collective feature efficiency (C4)

Gives the ratio of samples removed from the dataset based on an iterative process of linear fitting between the features and the target attribute.

2.1.8. Measures of Smoothness

It is a regression task, used for regression problems. In those problems, the smoother the function to be fitted, the simpler the task it becomes. Large variations in input/output are an indication of the existence of more intricate relationships between them.

2.1.8.1. Output distribution (S1)

Checks if the samples joined in then MST have similar output values. The lower the value, the simpler the problem - where outputs of similar samples in the input space are also next to each other.

2.1.8.2. Input distribution (S2)

Monitors the similarity in the input space of data items with similar outputs based on distance.

2.1.8.3. Error of a nearest neighbor regressor (S3)

Stands for the mean squared error of a 1-nearest neighbor regressor using leave-one-out.

2.1.8.4. Non-linearity of nearest neighbor regressor (S4)

Computes the mean squared error of a 1-NN regressor to the new randomly interpolated points.

CategoryA cronymMinMaxAsymptotic Cost NameMaximum Fisher's discriminant ratio F1 ≈ 0 1 $O(m \cdot n)$ Directional vector maximum Fisher's discriminant ratio F1v ≈ 0 1 $O(m \cdot n \cdot n_c + m^3)$ Feature-based Volume of overlapping region F20 $O(m \cdot n \cdot n_c)$ Maximum individual feature efficiency F3 0 1 $O(m \cdot n \cdot n_c)$ $O(m^2 \cdot n \cdot n_c)$ Collective feature efficiency F4 0 1 Faction of borderline points $O(m \cdot n^2)$ N1 0 1 Ratio of intra/extra class NN distance $\overline{\mathrm{N2}}$ $O(m \cdot n^2)$ 0 $O(m \cdot n^2)$ Error rate of NN classifier N30 Neighborhood $O(m \cdot n^2 + m \cdot l \cdot n)$ Non linearity of NN classifier N4 0 $O(m \cdot n^2)$ Fraction of hyper-spheres covering data T1 0 1 Local set average cardinality LSC 0 $O(m \cdot n^2)$ Sum of the error distance by linear programming L10 $O(n^2)$ $O(n^2)$ Linearity L_2 Error rate of linear classifier 0 $O(n^2 + m \cdot n \cdot n_c)$ Non linearity of linear classifier 0 Average number of features per dimension T2 ≈ 0 O(m+n)Average number of PCA dimensions per points Т3 $O(m^2 \cdot n + m^3)$ Dimensionality ≈ 0 m $O(m^2 \cdot n + m^3)$ Ratio of the PCA dimension to the original dimension T40 Entropy of classes proportions C1 0 $\overline{O(n)}$ 1 Class Imbalance Imbalance ratio C2O(n)Density Density 0 1 $O(m \cdot n^2)$ Network Clustering Coefficient ClsCoef 0 $O(m \cdot n^2)$ 1 0 $O(m \cdot n^2)$ Hubs Hubs Maximum Feature Correlation to the Output C10 $O(n \cdot m \cdot logm)$ Average Feature Correlation to the Output 0 $O(n \cdot m \cdot log m)$ Correlation Individual Feature Efficiency C30 1 $O(n \cdot m^2)$ C40 $O(n \cdot (d + n \cdot log n))$ Collective Feature Efficiency 1 Output Distribution S10 $O(n^2)$ $O(m \cdot (n + log m))$ Smoothness Input Distribution S2Error of a nearest neighbor regressor $O(n^2)$ S30

Table 2.1: Complexity Metrics from [2,3]

2.2. Supervised Methods

There are mainly two achine Learning has different methods or styles available:

Supervised classification trains a model using completely labeled dataset.

Unsupervised classification ingests unlabeled data to either create groups (clustering) or associate variables (e.g., association rules).

Semi-supervised Uses smaller labeled dataset to set up a guide and large amounts of unlabeled data for feature extraction

In this work, we focus only on the first one, supervised classification, i.e., a machine learning model is built on data that all instances have labeled information on how to determine and classify new incoming data.

In supervised learning, an optimal scenario is considered when the model is able to label correctly unseen data.

For this project, supervised learning is used more as a mean rather than as a final goal, in the sense that it aims at exploring how some data quality characteristics affect the performance of supervised classification rather than trying to improve the performance itself.

2.3. Imbalance

On any dataset obtained from a real world environment, there will be a class within the target outputs that will be more predominant than the rest of the classes. When the difference between the predominant class and the rest of the classes is not "remarkable" the dataset is called balanced. On the other hand, the classes are imbalanced if the number of samples from one class vastly outnumbers the number of samples from the rest of the classes, this is called imbalance problem. This means, that not enough data from the minority classes is available to train the algorithm.

Even though it might seem as a trivial matter, having an overwhelming amount of samples of just one of the classes means that usually algorithm will be biased towards the majority class, failing to classify properly the rest of the classes.

Most canonical classification algorithms (e.g. SVM, decision tree and neural networks) suffer from the *majority class bias* - they perform nicely on balanced datasets, but very few of them does under an imbalanced scenario. Since most of these learning processes are oriented to global accuracy, the resulting classifiers tend to have majority class bias. This is translated to an apparent good performance, that acts poorly on terms of accuracy in the minority class.

re-weighting through the learning process.

All the aforementioned metrics about datasets (and some recommended for imbalanced datasets) do not say how to mitigate its effects on classification algorithms. The different approaches to achieve this goal - deal with imbalanced data - are sampling techniques, cost-sensitive, ensemble approaches or hybrid approaches. They are going to be briefly described in the incoming sections.

2.3.1. Sampling Techniques

Techniques that are classified as *Sampling Techniques* are oversampling and undersampling (or upsampling and downsmapling). These methods are based on the addition or removal of instances of a given training dataset. The process of replicating or creating instances from a minority class towards a more balanced distribution (number of samples of majority and minority class are more or less similar) is called Random OverSampling (ROS); whereas Random Under-Sampling (RUS) is the procedure of removing instances from the majority class to reduce the difference between the amount of samples of each class.

Rather than using this early proposals, there can be found more sophisticated approaches generating new artificial samples, rather than the replication of already existing instances. Some of these proposals are going to be explained in the following sections.

2.3.1.1. Undersampling

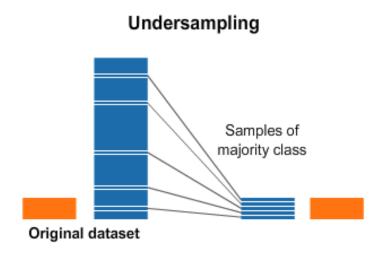


Figure 2.1: Undersampling Technique [1]

It involves removing samples from the dataset until the data is balanced. The reasons to use undersampling are usually related to practical reasons, such as resource costs. The techniques presented are:

Undersampling involves deleting samples from the majority class, with or without replacement. It is one of the early proposals to deal with imbalanced datasets. Although it may alleviate the imbalance in the dataset, it may also increase the variance of the classifier or discard meaningful samples from the majority class.

Cluster Centroid replaces a cluster of samples by the cluster centroid of a *K-means* algorithm. The number of clusters is set by the level of undersampling.

Near Miss refers to a collection of undersampling methods that select samples based on the distance of the majority class samples to the minority class samples [9]. There are three versions of this algorithm:

 NearMiss-1 selects majority class samples with minimum average distance to three closest minority class samples; 2.3 Imbalance

2. NearMiss-2 selects majority class examples with minimum average distance to the three furthest minority class examples;

3. NearMiss-3 selects majority class examples with minimum distance to each minority class example.

Among all the available techniques, *Near Miss* has been the on used for this research. Other techniques that remove instances intelligently include the Edited Nearest Neighbor (ENN) and Wilson's Editing that remove instances in which close neighbors belong to a different class [10].

2.3.1.2. Oversampling

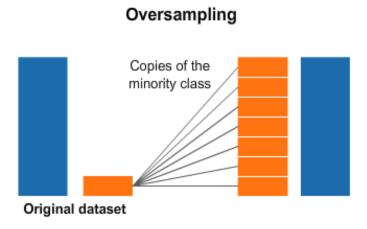


Figure 2.2: Oversampling Technique [1]

It involves replicating or creating new data points from the already existing data. The techniques analyzed are:

Oversampling involves copying supplementary data from the minority classes. It can be done more than once (actually, as many times as the developers sees fit). One of the early proposals regarding imbalanced datasets. It is robust, as it may randomly replace some of the samples from the minority class.

SMOTE (Synthetic Minority Oversampling Technique [11]) is one of the most popular oversampling techniques. It works by selecting samples close in the feature space. That means, that a line is drawn between the samples in the feature space and the a new sample at a point along that line. It is effective because the samples from the minority class created are plausible - relatively close in feature space to existing samples from minority class. A downside of this technique is that samples are created without looking at the majority class, meaning a possible overlapping of classes.

ADASYN (ADaptative SYNthetic) sampling algorithm was developed using the SMOTE approach shifting the importance of the classification boundary to those minority classes which are difficult. It weights the most difficult to learn classes so that those have more importance when creating new data. In other words, ADASYN generates more synthetic data in the minority class samples that are harder to learn.

The technique selected for this article is the SMOTE method, implemented by the *imbalance-learn* ³ Python package.

2.3.2. Cost-Sensitive Classifiers

Also known as CSC. These are adapted classifiers that handle imbalanced datasets by either:

- 1. Adding weights to instances⁴.
- 2. Resampling the training data according to the costs assigned to each class in a predefined cost matrix.
- 3. Or generating a model that minimizes the expected cost⁵. The idea behind this methodology is to penalize differently each type of error in the specific case of binary classification, the false positives (FP) and false negatives (FN).

The problem with CSC is defining the cost matrix as there is no systematic approach to do so. However, it is common practice to set the cost to equalize the class distribution.

2.3.3. Ensembles

Also known as meta-learners are a combination of multiple models with the objective of obtaining better predictions. They are typically classified as *Bagging*, *Boosting* and Stacking - Stacked generalization.

Bagging [12] (also known as Bootstrap aggregating) is a ensemble technique that involves a base learner applied to multiple equal size datasets. These datasets are created from the original data using bootstraping. Predictions are made on voting of the individual predictions.

An advantage of this technique is that it does not require to modify any aspect of the learning algorithm, taking advantage of the instability of the base classifier to create diversity among individual ensembles - so that individual members of the ensemble perform well in different regions of the data. However, if the output is robust to perturbation of the data (like is the case with nearest-neighbor -NN-classifiers) the performance drops and should not be used with those base classifiers.

Boosting techniques generate multiple models that complement each other. The final objective is to induce models that improve certain regions of the data, where previous induced models had low performance. This can be achieved by increasing the weights of instances that have been wrongly classified. That way, new learners focus on those regions.

Classification is based on a weighted voted among all members of the ensemble. One of the most popular boosting algorithms is AdaBoost.M1 [13] for classification. The set of training examples is assigned an equal weight at the beginning and the weight of instances can be increased or decreased depending on the classification of the learner. The next iterations focus on those instances with higher weights. AdaBoost.M1 can be applied to any base learner.

Models from ensembles are difficult to interpret (black-box behavior), comparing them to decision trees or rules providing explanation of their decision making process.

 $^{^3}$ https://imbalanced-learn.readthedocs.io/en/stable/

 $^{^4\}mathrm{Can}$ only be used if the base classifier algorithm allows it

 $^{^{5}}$ It can be obtained by multiplying the predicted probability distribution with the misclassification costs

2.3 Imbalance 13

2.3.4. Hybrid Approaches

There are other hybrid approaches that can be used. Like that ones that are going to be explained in the following section.

SMOTEBoost tries to reduce the bias from the learning procedure due to the class imbalance, and increase the sampling weight for the minority class. SMOTE [14] is introduced in each round of boosting, which enables each learner to be able to sample more of the minority class cases, and learn better and broader decision regions for the minority class.

It also brings the benefit of enhancing the probability of selection for the difficult minority class cases that are dominated by the majority class points [15]. The variation of boosting procedure of the SMOTEBoost process is a variant of the AdaBoost.M2 procedure [16].

RUSBoost [17] uses the AdaBoost.M2. The difference with SMOTEBoost is that RUSBoost applies Random Under Sampling instead of SMOTE. The application of SMOTE at this point has two drawbacks that RUSBoost is designed to overcome:

- It increases the complexity of the algorithm. SMOTE finds the k nearest neighbors of the minority class samples, and then extrapolates them to make new synthetic samples. RUS, on the other hand, simply deletes the majority class examples randomly.
- RUS produces less training data (as it is an undersampling technique, not like SMOTE, which is an oversampling technique). This can be translated into shorter model training times [17].

MetaCost [18] is a combination of bagging with cost-sensitive classification. The bagging part of the technique is used to relabel training data so that each training example is assigned a prediction that minimizes the expected cost for that instance. Based on the modified training data, MetaCost induces a new classifier which provides information about how a decision was reached.

2.3.5. Defect Prediction

Regarding the problem of software defect prediction, many techniques have been proposed in the literature - statistical methods (regression [19], and Support Vector Machines [20], etc.), machine learning (classification trees [21]), neural networks [22]), probabilistic models (Naïve Bayes [23] and Bayesian networks), ensembles of different techniques and meta-heuristics (ant colonies [24], etc). Despite this fact, some discrepancies are found:

- No classifier is consistently better than others.
- There is no optimum metric that allows the evaluation and comparison of classifiers ([23,25,26]).
- Data is also affected by quality issues class imbalance, overlapping, outliers, etc.).

Some authors highlight the problem of imbalanced datasets when dealing with the project at hand, defect prediction (Seiffert et al. [27] and in Khoshgoftaar et al. [28]).

As it has been mentioned before, there is no classifier that behaves consistently better. No technique is able to give a an outstanding performance when evaluating classifiers. Some authors have compared performance of several measures (e.g., Peng [29], Peng et al. [30], this paper actually propose performance metrics to evaluate merit of classification algorithms and ranked classification algorithms, respectively).

Further analysis on the subject comes from the hand of Lessman et al. [31]. This paper compared several classifiers, discussing performance metrics such like TP_r and FP_r . But finally advocated to use the AUC^6 as a good indicator for classifiers comparison. This results is known as sub-optimal for highly imbalanced datasets.

Arisholm et al. [?] compared different classification algorithms (tree algorithm (C4.5), coverage rule algorithm (PART), logistic regression, back-propagation neural networks and Support Vector Machines) over 13 different Java developed systems. They used three metrics to compare results:

- Object-oriented metrics.
- Churn (δ) metrics between successive releases.
- Process management metrics from a configuration management system.

The conclusion was that large differences can be achieved depending on the comparison criteria of the data. To solve this problem, the paper proposed a new AUC based, cost-effectiveness metric. Same approach has been evaluated and explored in Mende and Koschke [32].

 $^{^6\}mathrm{Further}$ explained in Section 3.3.7, Area Under the ROC Curve

Chapter 3

Empirical Work

In this chapter, we cover the experimental work carried out. Firstly, we describe the datasets used for the experimentation; then, the supervised classifiers evaluated; the evaluation metrics chosen; and finally, present and discuss the results.

3.1. Datasets

In this work, publicly available datasets in the domain of Software defect prediction were used, were used, the Jureczko and Madeyski dataset ¹ [33, 34], the Apache dataset ([35]) and the Harman Search Base dataset [36].

From the first cluster of datasets, 15 open source projects are the ones chosen (a total of 8 are used for this project). The number of defects found in each class collected from the Software Management System (SCM) using a regular expression. The datasets are publicly available (can be found in the PROMISE repository [37]). These datasets have been used in previous researches, [38–40], which allows comparing and analyzing the obtained results.

A sample can be considered as *defective* when the number of defects inside the class is more than 0. Similarly, if the number of defects is 0, then the class is *non-defective*. This allows a binary classification, making easier handling results, operations and comparisons.

Table 3.1: Defect Metrics Dataset Variables

Metric	Description
WMC	Weighted methods per class [41]
DIT	Depth of Inheritance Tree [41]
NOC	Number of Children [41]
CBO	Coupling between object classes [41]
RFC	Response for a Class [41]
LCOM	Lack of cohesion in methods [41]
Ca	Afferent couplings [42]
Ce	Efferent couplings [42]
NPM	Number of Public Methods [43]

Continued on next page

¹http://snow.iiar.pwr.wroc.pl:8080/MetricsRepo/

Metric	Description			
LCOM3	Lack of cohesion in methods [44]			
LOC	Lines of Code [43]			
DAM	Data Access Metric [43]			
MOA	Measure of Aggregation [43]			
MFA	Measure of Functional Abstraction [43]			
CAM	Cohesion Among Methods of Class [43]			
IC	Inheritance Coupling [45]			
CBM	Coupling Between Methods [45]			
AMC	Average Method Complexity [45]			
MAX_CC	Maximum McCabe's cyclomatic complexity [46]			
AVG_CC	Average McCabe's cyclomatic complexity [46]			

Table 3.1 – Continued from previous page

There is another sole dataset obtained from the same source as the previous collection of datasets, with a very similar structure of data, the *Apache* dataset. It has the same origin and objective as its predecessors.

On the second cluster of datasets, the data comes from a total of 8 different Hadoop versions. Their original purpose is to train a search based fault prediction system.

Similarly to Jureczko and Madeyski dataset [33,34], it uses: (1) WMC, (2) DIT, (3), NOC, (4) CBO, (5) RFC, (6) LCOM, (7) NOM, and (8) LOC; metrics to define each dataset.

Regarding more information on the content of the datasets the next table (see Table 3.2) summarizes the number of samples on each dataset and further valuable information, such as the absolute and relative number of defects for those datasets.

Project	Version	#instances	$\#Non ext{-}Defective$	#Defective	%Defective
	1.3	125	105	20	16.00
	1.4	178	138	40	22.47
ant	1.5	293	261	32	10.92
	1.6	351	259	92	26.21
	1.7	745	579	166	22.28
apache	-	191	107	84	43.98
	1.0	339	326	13	3.83
1	1.2	608	392	216	35.52
camel	1.4	872	727	145	16.62
	1.6	965	777	188	19.48
	0.1	141	91	50	35.60
	0.2	191	149	42	21.99
	0.3	211	158	53	25.12
badaan	0.4	201	159	42	20.90
hadoop	0.5	217	180	37	17.05

Table 3.2: Description of the Datasets

Continued on next page

Project	Version	#instances	$\#Non ext{-}Def$	#Def	%Def
	0.6	234	203	31	13.25
	0.7	250	202	48	19.20
	0.8	240	224	16	6.67
i	1.4	241	225	16	6.63
ivy	2.0	352	312	40	11.36
	3.2	272	182	90	33.08
	4.0	306	231	75	24.50
jedit	4.1	312	233	79	25.32
	4.2	367	319	48	13.07
	4.3	492	481	11	2.23
	1.0	135	101	34	25.18
log4j	1.1	109	72	37	33.94
	1.2	205	16	189	92.19
	1.0	157	141	16	10.19
synapse	1.1	222	162	60	27.02
	1.2	256	170	86	33.59
	2.4	723	613	110	15.21
xalan	2.5	803	416	387	48.19
Xalali	2.6	885	474	411	46.44
	2.7	909	11	898	98.78
	1.2	440	369	71	16.13
xerces	1.3	453	384	69	15.23
	1.4	588	151	437	74.31

Table 3.2 – Continued from previous page

The experiments of this paper use the latest version of the datasets ant, apache, camel, hadoop, ivy, jedit, log4j, xalan and xerces; alongide all the available versions of the hadoop dataset.

3.2. Supervised Classifiers

This work makes use of several supervised learning algorithms. The experiments carried out use the following algorithms:

Naive Bayes (NB) [47] is a classifier that works on conditional probabilities, uses the Bayes theorem to predict the class for each data input. Calculates the probability of a certain event, given prior knowledge. This classifier assigns a set of attributes a_1, \ldots, a_n to a given class C so that the probability of the class description value of the attributes instances is maximal: $P(C|a_1, \ldots, a_n)$. The probability of the hypothesis, given that the evidence is true, is the probability of the evidence, given the hypothesis is true, multiplied by the probability of the hypothesis; in relation to the probability of the evidence. See Eq. 3.1.

$$P(H|E) = \frac{(E|H) * P(H)}{P(E)}$$
(3.1)

For this project it has been selected the Gaussian Naive Bayes from scikit-learn ² to perform the experimentation. Being *Gaussian* means that the likelihood of the features is assumed to be Gaussian. The formula is given by Eq. 3.2.

$$P(x_i|y) = \left(\frac{1}{\sqrt{2\pi\sigma_y^2}}\right) \exp\left(-\frac{(x_i - \mu_y)^2}{2\sigma_y^2}\right)$$
(3.2)

Decision Trees can be seen as rules with a root node, branches are conditions and leaves correspond to classes. There are many decision trees algorithm such as CART (Classification And Regression Trees) [48] is a non-parametric decision tree, similar to **C4.5** [49].

CART constructs a two branch bifurcation of the most discriminating attribute, based on the Gini index. It can generate either classification or regression trees - depends on the variable (categorical or numeric, respectively). The implementation available in scikit-learn [50] ³ is an optimised version of this algorithm, although it does not support categorical variables.

Nearest Centroid classifier[51], Nearest Prototype classifier, or Rocchio classifier for its similarity to an algorithm with the same name (see Eq.3.3).

$$\overrightarrow{Q_m} = (a \cdot \overrightarrow{Q_o}) + (b \cdot \frac{1}{|D_r|} \cdot \sum_{\overrightarrow{D_j} \in D_r} \overrightarrow{D_j}) - (c \cdot \frac{1}{|D_{nr}|} \cdot \sum_{\overrightarrow{D_k} \in D_{nr}} \overrightarrow{D_k})$$
(3.3)

The labels of a given sample are assigned by evaluating the classes of training samples whose mean is closest to the evaluated point. The training procedure, given a labeled training set $(\overrightarrow{x_1}, y_1), \ldots, (\overrightarrow{x_n}, y_n)$ with class labels $y_i \in Y$, compute the per-class centroid with Eq. 3.4.

$$\overrightarrow{\mu_l} = \frac{1}{|C_l|} \sum_{i \in C_l} \overrightarrow{x_i} \tag{3.4}$$

where C_l is the set of indices of samples belonging to class $l \in Y$. The prediction functions, takes the class assigned to an observation \overrightarrow{x} is Eq. 3.5.

$$\overrightarrow{y} = argmin_{l \in Y} ||\overrightarrow{\mu_l} - \overrightarrow{x}||$$
(3.5)

3.3. Evaluation Metrics

Part of the process of applying a classification algorithm is to measure the success and the results of the training. In order to do it, some metrics can be calculated out of the testing to the trained classifier. Here is where the Confusion Matrix comes at hand. The Confusion Matrix (see Table 3.3) allows us to summarize the performance of a given classification algorithm, it is also the foundation of many of the performance metrics used in classification by:

True Positive (TP) - Data is correctly classified as positive.

True Negative (TN) - Data is correctly classified as negative.

False Positive (FP) - Data being negative classified as positive.

 $^{^2 \\ \}text{https://scikit-learn.org/stable/modules/generated/sklearn.naive_bayes.GaussianNB.html} \\ ^3 \\ \text{https://scikit-learn.org/stable/modules/tree.html}$

3.3 Evaluation Metrics 19

Table 3.3:	Confusion	Matrix	for	Binary	Classification
------------	-----------	--------	-----	--------	----------------

		Actual	l Class
		Positive	Negative
	Positive	True Positive	False Positive
Predicted Class		(TP)	(FP)
1 realcied Class	Negative	False Negative	True Negative
		(FN)	(TN)

False Negative (FN) - Data being positive classified as negative.

These specifications indicate that the input data should have a binary target: one value that can be classified as *positive* and a second value that can be classified as negative. From this statistical classification ⁴, many performance measures can be calculated. Some of the most widely used metrics, and the ones used in this paper are explained next.

3.3.1. Precision

Also know as Positive Predictive Value (PPV). It is the relation between the *true positives* calculated and the overall positives detected by the classification algorithm (see Eq. 3.6).

$$PPV = \frac{TP}{TP + FP} = 1 - FDR \tag{3.6}$$

3.3.2. Recall

Also known as sensitivity, hit rate, or True Positive Rate (TPR). It stands for the relation between the *true positives* calculated and the real number of positives (see Eq. 3.7).

$$TPR = \frac{TP}{P} = \frac{TP}{TP + FN} = 1 - FNR \tag{3.7}$$

3.3.3. Fall-out

Also called False Positive Rate (FPR). It is the probability of rejecting (falsely) the null hypothesis⁵ for a particular test (see Eq. 3.8).

$$FPR = \frac{FP}{N} = \frac{FP}{FP + TN} = 1 - TNR \tag{3.8}$$

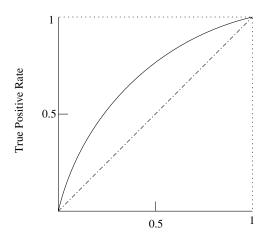
3.3.4. Balance Accuracy

It goes by the acronym BA. It is a metric generally used to evaluate how good is a (binary) classifier. It is a measure that comes in specially handy for imbalanced datasets. Its formula is represented by the mean of *sensitivity* and *specificity* (see Eq. 3.9).

$$BA = \frac{TPR + TNR}{2} \tag{3.9}$$

⁴Also know as error matrix.

 $^{^5}$ General statement or default position that there is no relationship between two measured phenomena or no association among groups.



False Positive Rate

Figure 3.1: ROC Curve

3.3.5. F-Measure

Also known as F_1 , or Sørensen-Dice coefficient (independently developed by Sørensen [52] and Dice [53]) is the harmonic mean of precision and sensitivity, the two previous measures, which measures accuracy (see Eq. 3.10). It is twice the relation of the multiplication between recall and precision and their addition. It is commonly used in highly imbalanced datasets but there are also some criticisms as it does not take into account the True Negative (TN) cases.

$$F_1 = 2 \cdot \frac{PPV \cdot TPR}{PPV + TPR} = \frac{2 \cdot TP}{2 \cdot TP + FP + FN}$$

$$(3.10)$$

3.3.6. MCC

The Matthews Correlation Coefficient (MCC) [54] or phi coefficient measures the quality of a binary classification robust to the imbalance problem (Eq. 3.11). Its range values are between -1 and +1, where -1 represents complete inconsistency (disagreement), 0 indicates that the prediction is no better than a random prediction; and +1 would be a perfect prediction.

$$MCC = \frac{TP \cdot TN - FP \cdot FN}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}}$$
(3.11)

3.3.7. Receiver Operating Characteristic Curve

The Receiver Operating Characteristic (ROC)[55] Curve represents graphically the True Positive Rate (TPR) versus the False Positive Rate (FPR) as shown in Figure 3.1.

Once the curve is plotted, the more the curve gets similar to a slope of TPR = FPR the more imbalance that can be found in the dataset. It provides graphical visualization of the results.

The Area Under the ROC Curve (AUC) is a quality measure between positive and negative rates with a single value. This metric allows to compare models.

An approximation to the function can be calculated with Eq 3.12.

$$AUC = \frac{1 + TP_r - FP_r}{2} \tag{3.12}$$

Typically, three unbiased metrics, i.e., AUC, F-score ([52, 53]), Matthews Correlation Coefficient (MCC - [54]), are used to evaluate the performance on imbalanced datasets. Other measures cannot be used when data is highly imbalanced, like *accuracy* (Acc) (defined by Eq. 3.13), as it does not take into account the number of labels of different classes.

$$Acc = \frac{TP + TN}{TP + TN + FP + FN} \tag{3.13}$$

3.4. Results and discussion

3.4.1. Methodology

To answer the research questions stated in Section 1.2, we run several experiments. First, we analyse the complexity metrics (see Section 2.1) from all selected datasets (see Section 3.1). Then, we retrieve some analytical metrics (see Section 3.3), applying K-fold Cross Validation to those datasets. Finally, we repeat the process applying some under/oversampling techniques with K-CV (see Sections 2.3.1.1 and 2.3.1.2, respectively).

As the final aim is to see how complexity metrics affect classification and therefore the analytical metrics, a final section is going to summarize the results obtained and the conclusions drawn out of those measures and answer the research questions.

3.4.2. Data Complexity Metrics Analysis

As it has been mentioned in *Data Complexity Metrics* (see Section 2.1), the software package to calculate them is available in R, ECol⁶. Therefore, it was necessary to call it from the Python environment. In order to do so, the package RServe, a client server implementation for R workspace to execute functions from other environments like Python, was used. In other words, this is a connector that allow us to execute the ECol complexity metrics functions. The source code regarding this connector can be found in the Appendix B, Section B.1.

The rest of the experimental work was implemented in a Python script. The structure of the script tries to find and compare the complexity metrics obtained from different datasets to see if there is a certain relation between metrics. To do so, a script was developed (see Algorithm 1) to connect Python to the ECoL library in R and returns the complexity metrics of a certain dataset (see its full implementation in Appendix B, Section B.4).

Algorithm 1 Datasets Complexity Metrics Comparison

```
Require: D dataset

Ensure: C complexity metrics

1: con ← connectEcol()

2: for all set in D do

3: inputs, targets ← getDataset(set)

4: metrics ← con.getMetrics(inputs, targets)

5: C.add(metrics)

6: end for

7: plotComparison(C)
```

⁶https://github.com/lpfgarcia/ECoL/

The results are also stored in CSV files, which are represented as Tables C.1 and C.2.

The experiment has been repeated for two independents sets of datasets (see Section 3.1 for more details regarding the datasets and their content). The first experiment results are summarized in Table C.1, whereas the second experiment, regarding the Hadoop datasets is shown in Table C.2.

The obtained results are also showed in the following Figures: (3.2) balance, (3.3) correlation, (3.4) dimensionality, (3.5) linearity, (3.6) neighborhood, (3.7) network, (3.8) overlap, and (3.9) smoothness.

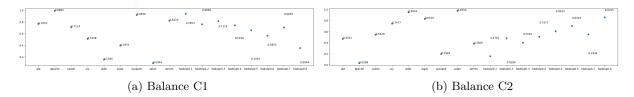


Figure 3.2: Balance Measures

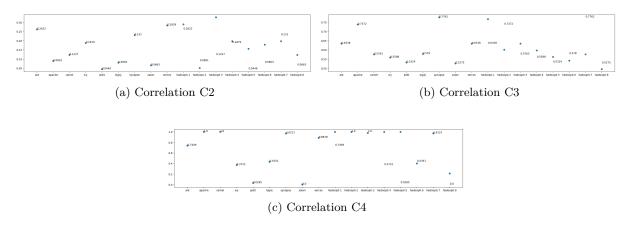


Figure 3.3: Correlation Measures

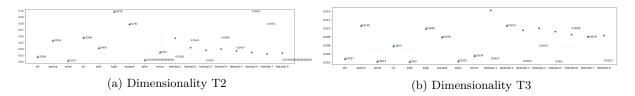


Figure 3.4: Dimensionality Measures

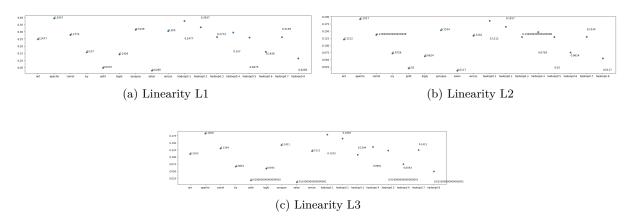


Figure 3.5: Linearity Measures



Figure 3.8: Overlap Measures

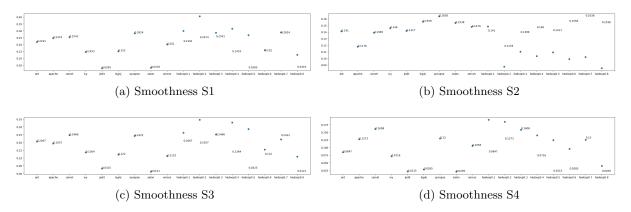


Figure 3.9: Smoothness Measures

This way it is easier to compare results through datasets and metrics. To see the whole extent of the numerical values, see the tables at Appendix C. The data is summarized in tables C.1 and C.2. To see the images in more detail (bigger) go to Appendix D, Section D.1.

Further results are compared and discussed in Section 3.4.5.

3.4.3. Cross Validation Analysis

This experiment tries to find the impact of applying the K-fold Cross-Validation. It is a widely extended technique in data science that brings a solution to the problem of performing testing to a data set with no separate training data - the same instances in a given dataset should not be used for both training and testing a classifier at the same time, instead data can be divided so a portion is used for training and another separate portion for testing/validation. Cross validation allows us to estimate the performance of the model trained by the whole dataset dividing it into k folds as follows:

- Training set which is known data by the classifier, and used to train it. It represents k-1/k parts of the original set.
- Testing set, also known as validation set which corresponds to unseen data for trained classifier used to test its performance. It usually is 1/k of the original dataset.

Then, the average of carrying out k iterations, same as the number of folds (parts/divisions) of the dataset, is calculated. On each iteration, the *testing set* is rotated to another unused fold⁷ of the datanotesting set is repeated, which means that each fold is used only once for *testing* purposes.

The most common values for k (folds) used in data science are 5 and 10. For this experiment, k has been selected as k = 5, as a common value of k was needed for all experiments and some of the datasets did not have enough samples for a larger value of k.

The algorithm that analyses the performance of each fold and the calculates the mean performance can be simplified as the one explained in the Algorithm 2.

Algorithm 2 Metrics Analysis on K-fold

Require: \mathcal{D} dataset

- 1: inputs, targets $\leftarrow \mathcal{D}$
- 2: k ← 5
- 3: $kf \leftarrow kfold(k)$

⁷The data in the different folds does not change throughout the cross validation process.

```
4: splits \leftarrow kf.split(inputs)
5: for all train_i, test_i in splits do
6: x_{train}, x_{test} \leftarrow inputs.get(train_i), inputs.get(test_i)
7: y_{train}, y_{test} \leftarrow targets.get(train_i), targets.get(test_i)
8: clf \leftarrow trainNetwork(x_{train}, y_{train})
9: confusionMatrix(x_{test}, x_{test}, clf)
10: end for
11: calculateMeanPerformance(clf)
```

The Python script used for this experiment can be found in Appendix B, Section B.4. It basically separates a dataset into folds and calculates the performance metrics for each fold, to later on compute the mean value of those metrics for the entire dataset.

With the *confusion matrix* other metrics are calculated such as *recall*, *MCC*, etc. Those metrics are then compared in Tables 3.4 and 3.5, for each specific dataset (to see the full extent of the comparison we refer to Section 3.4.5. For the sake of simplicity, only two tables of the aforementioned resulting datasets. Table 3.4 shows the results obtained from Apache dataset.

Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MCC	AUC
	Naive Bayes	0.4286	0.1579	0.200	0.4789	0.2308	-0.0548	0.4789
1	Decision Tree	0.8235	0.7368	0.1500	0.7934	0.7778	0.5915	0.7934
_	Nearest Centroid	0.3333	0.3158	0.6000	0.3579	0.3243	-0.2850	0.3579
	Naive Bayes	0.5000	0.0800	0.1538	0.4631	0.3243	-0.1142	0.4631
	v							
2	Decision Tree	0.8095	0.6800	0.3077	0.6862	0.7391	0.3552	0.6862
	Nearest Centroid	0.5000	0.1600	0.3077	0.4262	0.2424	-0.1719	0.4262
	Naive Bayes	0.5000	0.0909	0.1250	0.4830	0.1538	-0.0548	0.4830
3	Decision Tree	0.8462	0.5000	0.1250	0.6875	0.6286	0.3903	0.6875
	Nearest Centroid	0.4000	0.1818	0.3750	0.4034	0.2500	-0.2166	0.4034
	Naive Bayes	0.3333	0.8182	0.6667	0.5758	0.4737	0.1515	0.5758
4	Decision Tree	0.5833	0.6364	0.1852	0.7256	0.6087	0.4402	0.7256
	Nearest Centroid	0.8000	0.7273	0.0741	0.8266	0.7619	0.6727	0.8266
	Naive Bayes	0.3043	1.0000	0.5161	0.7419	0.4667	0.3838	0.7419
5	Decision Tree	0.5000	1.0000	0.2258	0.8871	0.6667	0.6222	0.8871
	Nearest Centroid	0.4545	0.7143	0.1935	0.7604	0.5556	0.4451	0.7604
	Naive Bayes	0.4132	0.4294	0.3323	0.5485	0.2926	0.0623	0.5485
Mean	Decision Tree	0.7125	0.7106	0.1987	0.7560	0.6842	0.4799	0.7560
	Nearest Centroid	0.4976	0.4198	0.3101	0.5549	0.4268	0.0889	0.5549

Table 3.4: Cross-Validation Results — Apache Dataset

The second example shown in Table 3.5 was obtained on the experiment performed over the Hadoop (v0.8) dataset.

Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MCC	AUC
	Naive Bayes	1.0000	0.1250	0.0000	0.5625	0.2222	0.3262	0.5625
1	Decision Tree	0.0000	0.0000	0.0250	0.4875	0.0000	-0.0652	0.4875
	Nearest Centroid	0.1667	1.0000	1.0000	0.5000	0.2857	0.0000	0.5000
	Naive Bayes	0.0000	0.0000	0.1064	0.4468	0.0000	-0.0497	0.4468
2	Decision Tree	0.0000	0.0000	0.1064	0.4468	0.0000	-0.0497	0.4468
	Nearest Centroid	0.0208	1.0000	1.0000	0.5000	0.0408	0.0000	0.5000
	Naive Bayes	0.0000	0.0000	0.0851	0.4574	0.0000	-0.0440	0.4574
3	Decision Tree	0.0000	0.0000	0.0851	0.4574	0.0000	-0.0440	0.4574
	Nearest Centroid	0.0208	1.0000	1.0000	0.5000	0.0408	0.0000	0.5000
	Naive Bayes	0.3333	0.2500	0.0455	0.6023	0.2857	0.2335	0.6023
4	Decision Tree	0.0000	0.0000	0.0426	0.4787	0.0000	-0.0304	0.4787
	Nearest Centroid	0.0000	0.0000	0.0227	0.4886	0.0000	-0.0440	0.4886
	Naive Bayes	0.0000	0.0000	0.0000	0.5000	0.0000	0.0000	0.5000
5	Decision Tree	0.0000	0.0000	0.0000	0.5000	0.0000	0.0000	0.5000
	Nearest Centroid	0.0000	0.0000	0.0000	0.5000	0.0000	0.0000	0.5000
	Naive Bayes	0.26667	0.0750	0.0474	0.5138	0.1016	0.0932	0.5138
Mean	Decision Tree	0.0000	0.0000	0.0484	0.4758	0.0000	-0.0446	0.4758
	Nearest Centroid	0.0417	0.6000	0.6045	0.4977	0.0735	-0.0088	0.4977

Table 3.5: Cross-Validation Results — Hadoop 0.8 Dataset

The inner results of each fold are not evaluated when analyzing the results of the experiments, but that data could be used to understand how data metrics (including imbalance) affect classification. The objective evaluated in this paper is to see if the metrics obtained for each dataset have any relation with the performance of the classifiers.

3.4.4. Imbalance Experimental Work

After experimenting with cross-validation, we now focus on if filters applied to the dataset have any effect on the quality of the trained classifier. In this case, it is carried out by applying imbalance filters to the folds in the datasets (see Section 2.3 for more information on imbalance filters). Here, the following techniques were used in the experiments:

Undersampling Removing samples from majority class.

Oversampling Creating new samples in the minority class.

3.4.4.1. Undersampling with Cross Validation

For this experiment, one undersampling algorithm is applied (2.3.1.1) to see how folds are affected by removing majority class samples, and therefore, looking at how it impacts the classification algorithm.

The undersampling technique is not done on the whole dataset in advance, only the training folds are the ones that the undersampling algorithm is applied.

The k value chosen for cross validation is k = 5. A simplification of the procedure followed by this experiment can be found in the Algorithm 3.

Algorithm 3 Undersampling with Cross-Validation

```
Require: \mathcal{D} dataset
 1: inputs, targets \leftarrow \mathcal{D}
 2: k \leftarrow 5
 3: kf \leftarrow kfold(k)
 4: splits \leftarrow kf.split(inputs)
 5: samplingStrategy \leftarrow 0:50, 1:50
                                                     ▷ Binary class with a post undersampling distribution of 50-50
 6: randomState \leftarrow 42
 7: for all train_i, test_i in splits do
         x_{train}, x_{test} \leftarrow \text{inputs.get}(train_i), \text{inputs.get}(test_i)
         y_{train}, y_{test} \leftarrow \text{targets.get}(train_i), \text{targets.get}(test_i)
 9:
         X, Y = makeImbalance(
10:
11:
            x_{train}, y_{train},
            samplingStrategy,
12:
            randomState
13:
14:
         clf \leftarrow classifier(NearMiss(2), GaussianNB())
15:
         clf \leftarrow trainNetwork(X, Y)
16:
         confusionMatrix(x_{test}, y_{test}, clf)
17:
18: end for
19: calculateMeanPerformance(clf)
```

Similarly to the previous experiment, the following classification algorithms were used to measure performance of the alterations done on the dataset, i.e., (1) Naive Bayes (Gaussian), (2) Decision Tree and (3) kNN Nearest Centroid.

The experiment creates the same tables obtained in experiment 3.4.3, that is why sharing all the resulting tables of this experiment would be unnecessary - the results evaluated here can be found in Section 3.4.5. That is why only two of them have been included into this dissertation. The Apache dataset experiment (see Table 3.6).

	Table 3.6: Cross-	validation wi	ith Under	sampling R	esults — A _l	pache dat	aset
Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MC
	Naire Davies	0 5556	0.0004	0 = 4 = =	0.6694	0.6010	0.26

Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MCC	AUC
	Naive Bayes	0.5556	0.8824	0.5455	0.6684	0.6818	0.3620	0.6684
1	Decision Tree	0.7000	0.8235	0.2727	0.7754	0.7568	0.5464	0.7754
	Nearest Centroid	0.4167	0.2941	0.3182	0.4880	0.3448	-0.0259	0.4880
	Naive Bayes	0.5500	0.7333	0.3913	0.6710	0.6286	0.3348	0.6710
2	Decision Tree	0.5500	0.7333	0.3913	0.6710	0.6286	0.3348	0.6710
	Nearest Centroid	0.3571	0.3333	0.3913	0.4710	0.3448	-0.0587	0.4710
	Naive Bayes	0.7586	0.8800	0.5385	0.6708	0.8148	0.3811	0.6708
3	Decision Tree	0.8421	0.6400	0.2308	0.7046	0.7273	0.3883	0.7046
	Nearest Centroid	0.7000	0.2800	0.2308	0.5246	0.4000	0.0530	0.5246
	Naive Bayes	0.6667	0.7273	0.1481	0.7896	0.6957	0.5650	0.7896
4	Decision Tree	0.6667	0.7273	0.1481	0.7896	0.6957	0.5650	0.7896
	Nearest Centroid	0.3077	0.3636	0.3333	0.5152	0.3333	0.0290	0.5152

Continued on next page

	,	Table 3.6 –	Continue a	d from previ	$ious\ page$			
Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MCC	AUC
	Naive Bayes	0.5000	0.5625	0.4091	0.5767	0.5294	0.1517	0.5767
5	Decision Tree	0.6316	0.7500	0.3182	0.7159	0.6857	0.4264	0.7159
	Nearest Centroid	0.5556	0.3125	0.1818	0.5653	0.4000	0.1518	0.5653
	Naive Bayes	0.5928	0.6662	0.3917	0.6372	0.6059	0.2992	0.6372
Mean	Decision Tree	0.6781	0.7348	0.2722	0.7313	0.6988	0.4522	0.7313
	Nearest Centroid	0.4674	0.3167	0.2911	0.5128	0.3646	0.0298	0.5128

And the result obtained on the same experiment for the Hadoop (v0.8) experiment (see Table 3.7).

Table 3.7: Cross-validation with Undersampling Results — Hadoop 0.8

Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MCC	AUC
	Naive Bayes	0.1429	0.5000	0.1304	0.6848	0.2222	0.2092	0.6848
1	Decision Tree	0.1053	1.0000	0.3696	0.8152	0.1905	0.2576	0.8152
	Nearest Centroid	0.0345	0.5000	0.6087	0.4457	0.0645	-0.0444	0.4457
	Naive Bayes	0.0000	0.0000	0.2667	0.3667	0.0000	-0.1491	0.3667
2	Decision Tree	0.0833	0.3333	0.2444	0.5444	0.1333	0.0497	0.5444
	Nearest Centroid	0.0952	0.6667	0.4222	0.6222	0.1667	0.1193	0.6222
	Naive Bayes	0.0833	0.5000	0.2391	0.6304	0.1429	0.1204	0.6304
3	Decision Tree	0.0000	0.0000	0.3261	0.3370	0.0000	-0.1406	0.3370
	Nearest Centroid	0.0000	0.0000	0.4348	0.2826	0.0000	-0.1762	0.2826
	Naive Bayes	0.1333	0.3333	0.3095	0.5119	0.1905	0.0170	0.5119
4	Decision Tree	0.1765	0.5000	0.3333	0.5833	0.2609	0.1153	0.5833
	Nearest Centroid	0.0625	0.1667	0.3571	0.4048	0.0909	-0.1336	0.4048
	Naive Bayes	0.0000	0.0000	0.1556	0.4222	0.0000	-0.1067	0.4222
5	Decision Tree	0.2000	0.6667	0.1778	0.7444	0.3077	0.2914	0.7444
	Nearest Centroid	0.0000	0.0000	0.2444	0.3778	0.0000	-0.1408	0.3778
	Naive Bayes	0.0719	0.2667	0.2203	0.5232	0.1111	0.0182	0.5232
Mean	Decision Tree	0.1130	0.5000	0.2902	0.6049	0.1785	0.1147	0.6049
	Nearest Centroid	0.0384	0.2667	0.4134	0.4266	0.0644	-0.0751	0.4266

As it has been mentioned in Section 2.3.1.1, there are several versions of Near Miss algorithm. For this experiment it was used version 2. This undersampling algorithm selects the majority class samples with the least average distance to the 3 farthest minority class samples.

The analysis of the metrics obtained are discussed in Section 3.4.5.

3.4.4.2. Oversampling with Cross Validation

In this experiment, similarly to Section 3.4.4.1, an imbalance filter is used. In this case, the oversampling technique is implemented and is later on compared to other experiment results (see Section 3.4.5). The technique has been applied to the different folds of the dataset, not to the entire data. Once again, the dataset is divided into k = 5 folds.

The logic of the Python code experiment is summarized in Algorithm 4. The difference with the undersampling Algorithm 3 is that uses the SMOTE technique (see Section 2.3.1.2) instead of *Near Miss* undersampling technique.

Algorithm 4 Oversampling and K-fold on classification performance

```
Require: \mathcal{D} dataset
 1: inputs, targets \leftarrow \mathcal{D}
 2:\ k \leftarrow 5
 3: kf \leftarrow kfold(k)
 4: splits \leftarrow kf.split(inputs)
 5: for all train_i, test_i in splits do
         x_{train}, x_{test} \leftarrow \text{inputs.get}(train_i), \text{inputs.get}(test_i)
         y_{train},\,y_{test} \leftarrow \text{targets.get}(train_i),\,\text{targets.get}(test_i)
 7:
 8:
         clf \leftarrow classifier(SMOTE(), GaussianNB())
         clf \leftarrow trainNetwork(x_{train}, \, y_{train})
10:
         confusionMatrix(x_{test}, y_{test}, clf)
11: end for
12: calculateMeanPerformance(clf)
```

The classifiers used for this experiment are - (1) Naive Bayes (Gaussian); (2) Decision Tree; and (3) kNN Nearest Centroid.

Next we show two of the results obtained, fhe first one is the result on the Apache dataset (see Table 3.8).

Table 3.8: Over sampling with Cross Validation Results — A pache dataset

Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MCC	AUC
	Naive Bayes	0.4286	0.1579	0.2000	0.4789	0.2308	-0.0548	0.4789
1	Decision Tree	0.7222	0.6842	0.2500	0.7171	0.7027	0.4354	0.7171
	Nearest Centroid	0.3333	0.3158	0.6000	0.3579	0.3243	-0.2850	0.3579
	Naive Bayes	0.5000	0.0800	0.1538	0.4631	0.1379	-0.1142	0.4631
2	Decision Tree	0.8889	0.6400	0.1538	0.7431	0.7442	0.4619	0.7431
	Nearest Centroid	0.5000	0.1600	0.3077	0.4262	0.2424	-0.1719	0.4262
	Naive Bayes	0.5000	0.0909	0.1250	0.4830	0.1538	-0.0548	0.4830
3	Decision Tree	0.8000	0.5455	0.1875	0.6790	0.6486	0.3616	0.6790
	Nearest Centroid	0.4286	0.1364	0.2500	0.4432	0.2069	-0.1447	0.4432
	Naive Bayes	0.3333	0.8182	0.6667	0.5758	0.4737	0.1515	0.5758
4	Decision Tree	0.5385	0.6364	0.2222	0.7071	0.5833	0.3959	0.7071
	Nearest Centroid	0.6000	0.5455	0.1481	0.6987	0.5714	0.4092	0.6987
	Naive Bayes	0.3182	1.0000	0.4839	0.7581	0.4828	0.4052	0.7581
5	Decision Tree	0.5000	1.0000	0.2258	0.8871	0.6667	0.6222	0.8871
	Nearest Centroid	0.4545	0.7143	0.1935	0.7604	0.5556	0.4451	0.7604
	Naive Bayes	0.4160	0.4294	0.3259	0.5518	0.2958	0.0666	0.5518
Mean	Decision Tree	0.6899	0.7012	0.2079	0.7467	0.6691	0.4554	0.7467
	Nearest Centroid	0.4633	0.3744	0.2999	0.5373	0.3801	0.0505	0.5373

The second example is the one from the Hadoop (v0.8) experiment (see Table 3.9).

Fold	Function	Precision	Recall	Fall Out	Balanced	F1	MCC	AUC
	Naive Bayes	0.1176	0.2500	0.3750	0.4375	0.1600	-0.0974	0.4375
1	Decision Tree	0.2500	0.1250	0.0750	0.5250	0.1667	0.0674	0.5250
	Nearest Centroid	0.1667	1.0000	1.0000	0.5000	0.2857	0.0000	0.5000
	Naive Bayes	0.1000	1.0000	0.1915	0.9043	0.1818	0.2843	0.9043
2	Decision Tree	0.0000	0.0000	0.4468	0.2766	0.0000	-0.1286	0.2766
	Nearest Centroid	0.0208	1.0000	1.0000	0.5000	0.0408	0.0000	0.5000
	Naive Bayes	0.0000	0.0000	0.1915	0.4043	0.0000	-0.0701	0.4043
3	Decision Tree	0.0000	0.0000	0.1064	0.4468	0.0000	-0.0497	0.4468
	Nearest Centroid	0.0208	1.0000	1.0000	0.5000	0.0408	0.0000	0.5000
	Naive Bayes	0.0667	0.5000	0.6364	0.4318	0.1176	-0.0778	0.4318
4	Decision Tree	0.2500	0.2500	0.0682	0.5909	0.2500	0.1818	0.5909
	Nearest Centroid	0.0000	0.0000	0.0000	0.5000	0.0000	0.0000	0.5000
	Naive Bayes	0.0000	0.0000	0.0000	0.5000	0.0000	0.0000	0.5000
5	Decision Tree	0.0000	0.0000	0.0435	0.4783	0.0000	-0.0435	0.4783
	Nearest Centroid	0.0000	0.0000	0.0000	0.5000	0.0000	0.0000	0.5000
	Naive Bayes	0.0569	0.3500	0.2789	0.5356	0.0919	0.0078	0.5356
Mean	Decision Tree	0.1000	0.0750	0.1480	0.4635	0.0833	0.0055	0.4635
	Nearest Centroid	0.0417	0.6000	0.6000	0.5000	0.0735	0.0000	0.5000

Table 3.9: Oversampling with Cross-Validation Results — Hadoop 0.8 dataset

The analysis of the metrics obtained are in Section 3.4.5.

3.4.5. Comparison of the Results and Discussion

In this section, we analyze the results from the previous experiments. These are shown in Tables 3.10, 3.11 and 3.12. The RQ were as follows:

- RQ1 How complexity metrics are correlated to the outcome of supervised algorithms?
- RQ2 How complexity metrics and imbalance are related?
- RQ3 Do complexity metrics tell us something about the quality of the datasets?

To answer the RQ1 (see Section 3.4.5) we need to observe, for example, the values from *overlapping*. We assume that there is a certain correlation between overlapping and the classifiers' performance. For most cases in our experimentation, the higher the overlapping rate, the less efficient the classifier becomes. In this work, this assumption is not backed up by any statistical test, but just looking at the results.

For example, looking at the *overlapping* measures, when *overlapping* F1 is higher than 0.90, almost none of the classifiers is able to surpass 0.5 in *precision* score, something similar happens with the *recall* and *fall-out* scores (all three measures indicate on a relative value how many input samples are

correctly predicted). It makes sense once to assume that the more interlaced the samples are (the more overlapping), the harder for a classifier to correctly predict its class.

In a similar way, it *linearity* measures are also directly related to the performance of the classification algorithms. Having high *overlapping* measures means that the *linearity* should be smaller (it is harder to separate data using a linear function if data is interlaced). Therefore, the higher the *linearity* measures obtained, the higher the performance should be. as all the selected datasets seem to have high *overlapping* values.

A third complexity metric that should be taken into account, regarding classifiers performance, is balance - (RQ1 and RQ2, 3.4.5 and 3.4.5, respectively). Its measures try to approximate the level of imbalance of a certain class. Therefore, the higher the measures' values, the greater should be the gap between the number of samples from the majority and minority class (all the datasets work with binary classes).

It can be observed that with large values of imbalance, not only the results have poor performance (less than 0.7 of *precision*, and similarly with *recall* and *fall-out* measures), but it also means that the different classifiers have very different results on the same dataset. This can be translated as, the performance on certain classifiers might depend on the imbalance of a certain dataset (RQ2 - see 3.4.5).

Taking a look at *Balanced Accuracy* measure (useful for imbalanced datasets, it can be observed that most of the classifiers do not behave as they should in either the positive or negative prediction. In example, all of the Hadoop datasets, where the imbalance ratio (*balance* measures) is not ideal, and the overlapping is too high.

Therefore, MCC, as a measure to see the quality of a binary classifier should also be low - just like in the Hadoop datasets. As for this last observation, it could be assumed that filters that would reduce imbalance, should also be able to increase the performance of the classifiers.

After some experimentation regarding this matter, no clear improvements have been noticed in any of the analytical measures. Furthermore, undersampling seems not to be a good technique when the number of samples is too low, as the number of samples in the resulting training dataset is not enough to obtain a good classifier. In some cases, it even reduces the performance.

After using SMOTE oversampling technique, the Balanced Accuracy metric seems to indicate that the classifier identified slightly better some of the testing data samples, but the resulting classifier still does not meet the desired quality (MCC).

In general, it seems that the techniques applied do not seem to fix perfectly the problems arose from either imbalance or overlapped datasets. This topic is going to be further discussed in Section 4, as well as some other remarks about the selected classifiers and possible further experimentation on this topic.

On trying to answer the final RQ3, Do complexity metrics tell us something about the quality of the dataset? We can assume (just looking at the results) that they do. A dataset with bad quality could be considered one that has high overlapping, imbalanced classes, etc. As the results seem to indicate a relation between those values and the performance of the obtained classifier - as the analytical metrics tell us. This should tell us that we need to explore ways to improve the data (feature engineering, collect further attributes, etc.).

Table 3.10: All Metrics

3,6	Martin		1			- Transco			1			,			17777			1001	
M easure	Metr.		ant			apacue			camer	1		rey 0 1 1 0 0			Jeant 0			0.0043	
Balance	3 8		0.7653			0.9890			0.7114			0.5108			0.1545			0.3953	
	000		0.000			0.0200			0.0429	1		0.1411			0.50.0			0.0019	
	C2		0.2622			0.0891			0.1227			0.1879			0.0448			0.0804	
Correlation	S 23		0.6338			0.7372			0.5763			0.5588			0.5324			0.5780	
	T.8		0.0268			0.0524			0.0207			0.0568			0.0407			0.0976	
Dimension.	T_3		0.0027			0.0105			0.3000			0.0057			0.0020			0.0098	
	L1		0.2477			0.3937			0.2774	İ		0.1570			0.0475			0.1426	
Linearity	Γ 2	_	0.1212			0.1917			0.1370			0.0726			0.0200			0.0624	
,	F7		0.1103			0.1828			0.1304			0.0661			0.0180			0.0593	-
	N1		0.3208			0.3822			0.3565			0.2159			0.0447			0.2195	
	N2		0.3588			0.3232			0.3629			0.3285			0.2543			0.3588	
Modelhow	N3		0.2067			0.1937			0.2435			0.1364			0.0325			0.1220	
Neignoor.	N4		0.0913			0.1728			0.1358			0.0739			0.0122			0.0293	
	TI	_	0.0025			0.0135			0.0021			0.0082			0.0184			0.0161	
	LSC		0.9860			0.9659			0.9923			0.9533			0.8870			0.9476	
	Density		0.8658			0.8801			0.8627			0.8293			0.8170			0.8260	
Network	ClsCoef		0.3377			0.2232			0.3131			0.3564			0.3314			0.4158	
	Hubs		0.7665			0.9236			0.7608			0.7628			0.8789			0.8487	
	FI		0.9192			0.9776			0.9825			0.9432			0.9874			0.9922	
	F1v		0.2882			0.4659			0.5203			0.2083			0.2048			0.3223	
Overlap	F2		0.0000			0.0061			0.0004			0.0005			0.000.0			0.0000	
	F3		0.9074			0.9476			0.9513			0.7102			0.5915			0.6585	
	F4		0.8295			0.8325			0.8487			0.3977			0.0671			0.1659	
	$_{ m S1}$		0.2191			0.2474			0.2541			0.1453			0.0285			0.1520	
Smooth.	88		0.1410			0.1178			0.1389			0.1460			0.1417			0.1556	
	83		0.2067			0.1937			0.2466			0.1364			0.0325			0.1220	
	84		0.0847			0.1273		ŀ	0.1608			0.0716			0.0215			0.0285	
		NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DT	NC
:	-	0.5600	0.4598	0.6263	0.4132	0.7125	0.4976	0.4478	0.3275	0.3304	0.2687	0.2533	0.3401	0.0645	0.1000	0.0496	0.9734	0.9350	0.9093
Frecision	تن 10	0.5095	0.4200	0.6166	0.4160	0.6899	0.4633	0.4372	0.2891	0.3243	0.2422	0.2478	0.3220	0.0427	0.0402	0.0491	0.9734	0.9530	0.9149
	1	0.5497	0.4677	0.5105	0.4294	0.7106	0.4198	0.2600	0.3732	0.2550	0.3122	0.2389	0.4372	0.1300	0.0500	0.1900	0.4912	0.9151	0.3216
Recall	<i>01</i>	8909.0	0.6416	0.4788	0.6662	0.7348	0.3167	0.2990	0.6038	0.2850	0.5508	0.6765	0.5000	0.3667	0.8500	0.4167	0.4786	0.5498	0.2804
	3	0.5913	0.5115	0.5164	0.4294	0.7012	0.3744	0.3212	0.3528	0.3203	0.4011	0.3122	0.4372	0.1800	0.3800	0.1900	0.5017	0.9261	0.3430
	-	0.1231	0.1552	0.0866	0.3323	0.1987	0.3101	0.0763	0.1838	0.1266	0.1104	0.0734	0.1008	0.1027	0.0226	0.1136	0.2167	0.7333	0.4000
Fall Out	o) (0.1703	0.3126	0.0790	0.3917	0.2722	0.2911	0.1171	0.4313	0.1399	0.1603	0.3546	0.0996	0.3132	0.4359	0.0624	0.3200	0.2133	0.3533
	٠,	0.1609	0.2051	0.0919	0.3259	0.2079	0.2999	0.0995	0.2072	0.1600	0.1520	0.1248	0.1101	0.2876	0.0643	0.1300	0.2167	0.5333	0.4000
Balanced	- 0	0.7183	0.6545	0.7170	0.5465	0.7313	0.0049	0.5919	0.5862	0.5726	_	0.5827	0.0002	0.5267	0.6097	0.6341	0.6573	0.5909	0.4600
	\$ 00	0.7152	0.6532	0.7122	0.5518	0.7467	0.5373	0.6109	0.5728	0.5801	0.6245	0.5937	0.6635	0.5098	0.7508	0.6229	0.6425	0.6964	0.4715
	1	0.5547	0.4598	0.5610	0.2926	0.6842	0.4268	0.3285	0.3453	0.2850	0.2844	0.2428	0.3795	0.0796	7990.0	0.0656	0.6448	0.9248	0.4713
FI	95	0.5445	0.4672	0.5423	0.6059	0.6988	0.3646	0.3333	0.3573	0.2845	0.3703	0.2812	0.3956	0.0334	0.0754	0.1664	0.6301	0.6914	0.4216
	3	0.5489	0.4606	0.5605	0.2958	0.6691	0.3801	0.3679	0.3158	0.3203	0.3009	0.2719	0.3703	0.0619	0.2033	0.0649	0.6548	0.9372	0.4946
	1	0.4295	9608.0	0.4577	0.0623	0.4799	0.0889	0.2285	0.1789	0.1425	0.1929	0.1647	0.3027	0.0481	0.0576	0.0497	0.1564	0.1543	-0.0402
MCC	ং	0.4117	0.2809	0.4446	0.2992	0.4522	0.0298	0.2050	0.1376	0.1454	0.2943	0.2032	0.3449	0.0036	0.1113	0.1781	0.1162	0.1648	-0.0409
	3	0.4114	0.2872	0.4538	0.0666	0.4554	0.0505	0.2497	0.1342	0.1601	0.2056	0.1726	0.2886	0.0122	0.2086	0.0464	0.1612	0.4101	-0.0274
	-	0.7133	0.6563	0.7120	0.5485	0.7560	0.5549	0.5919	0.5947	0.5642	0.6009	0.5827	0.6682	0.5285	0.5222	0.5653	0.6373	0.5909	0.4608
AUC	જા -	0.7182	0.6645	0.6998	0.6372	0.7313	0.5128	0.5909	0.5862	0.5726	0.6952	0.6609	0.7002	0.5267	0.7071	0.6771	0.5793	0.6682	0.4635
	3	0.7152	0.6532	0.7122	0.5518	0.7467	0.5373	0.6109	0.5728	0.5801	0.6245	0.5937	0.6635	0.4782*	0.7062*	0.5463*	0.6425	0.6964	0.4715

Table 3.11: All Metrics

Measure	Metr.		synapse			xalan			xerces			hadoop 0.1			hadoop 0.2			hadoop 0.3	
	CI		0.9209			0.0944			0.8219			0.9381			0.7600			0.8132	
Balance	C2		0.1944			0.9755			0.3826			0.1559			0.4777			0.3970	
	C2		0.2310			0.0663			0.2839			0.2868			0.0520			0.3171	
Correlation	C3		0.7762			0.5275			0.6338			0.7741			9009.0			0.6330	
	C4		0.9727			0.0000			0.8878			1.0000			1.0000			0.9810	
Dimension.	T2		0.0781			0.0220			0.0340			0.0496			0.0366			0.0332	
	T3		0.0078			0.0022			0.0034			0.0142			0.0052			0.0095	
	LI		0.3139			0.0285			0.3050			0.3770			0.3327			0.2658	
Linearity	L2		0.1534			0.0117			0.1342			0.1870			0.1664			0.1305	
	L3		0.1421			0.0110			0.1211			0.1832			0.1644			0.1055	
	NI		0.4023			0.0396			0.2789			0.4965			0.4712			0.4028	
	NS NS		0.3780			0.1615			0.2667			0.3474			0.4611			0.3151	
Neighbor.	N3		0.2422			0.0121			0.1173			0.2553			0.3037			0.2417	
	N4		0.0859			0.0308			0.0833			0.2411			0.2408			0.1374	
	TI		0.0072			0.0294			0.0057			0.0127			0.0079			0.0118	
	$_{LSC}$		0.9797			0.8329			0.9601			0.9755			0.9838			0.9686	
	Density		0.8805			0.8165			0.8530			0.8678			0.8610			0.8478	
Network	ClsCoef		0.3143			0.3460			0.3429			0.3965			0.4411			0.4281	
	Hubs		0.9300			0.8564			0.8499			0.8595			0.9252			0.9305	
	F1		0.9438			0.9973			0.9496			0.9129			0.9958			0.8365	
	F1v		0.3313			0.3274			0.3118			0.5101			0.8483			0.3019	
Overlap	F2		0.0065			0.0000			0.000			0.1818			0.0508			0.0135	
	F3		0.9141			0.3399			0.8129			0.8865			0.9791			0.9479	
	F4		0.7227			0.0055			0.6990			0.6879			0.9215			0.8294	
	S1		0.2824			0.0319			0.2010			0.3643			0.3421			0.2952	
Smooth.	88		0.1638			0.1538			0.1479			0.1465			0.0908			0.1134	
	833		0.2422			0.0121			0.1122			0.2411			0.3246			0.2417	
	54		0.1300			0.0209			0.1056			0.2003			0.1863			0.1552	
		NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DT	NC
:		0.6317	0.5581	0.6431	0.9963	0.9944	0.9971	0.9339	0.9374	0.9283	0.6933	0.4782	0.5091	0.1357	0.0286	0.1097	0.6467	0.3671	0.5821
Frecision	20 00	0.5499	0.4750	0.6444	0.9942	0.9973	0.0000	0.9200	0.9395	0.9583	0.6033	0.5028	0.5955	0.1334	0.1998	0.1403	0.6384	0.3965	0.6738
	0 -	0.0320	0.5641	0.04450	0.8791	0.0000	0.3930	0.5768	0.93%	0.3007	0.3086	0.6969	0.3976	0.1736	0.1000	0.3305	0.0138	0.3000	0.0138
Recall	। <i>ত</i> ং	0.5353	0.5741	0.5309	0.9511	0.7158	0.4923	0.6346	0.8836	0.2577	0.4814	0.6905	0.4447	0.2634	0.3915	0.4613	0.5322	0.8189	0.4900
	8	0.5618	0.6636	0.5342	0.9032	0.9933	0.4019	0.5931	0.9218	0.3007	0.3276	0.7795	0.3276	0.2471	0.1638	0.3442	0.7133	0.8457	0.7391
	1	0.1613	0.2309	0.1467	0.2167	0.3667	0.0500	0.1200	0.1832	6990.0	0.0835	0.3650	0.1437	0.2528	0.3141	0.5494	0.0464	0.1936	0.0820
Fall Out	જા અ	0.2225	0.3016	0.1399	0.3867	0.0800	0.0000	0.1576	0.1607	0.0498	0.1468	0.3506	0.1628	0.3558	0.4480	0.5418	0.0996	0.4086	0.1129
	3	0.1767	0.2634	0.1579	0.3167	0.2667	0.0500	0.1271	0.1880	0.0669	0.0835	0.3553	0.1437	0.5278	0.3680	0.5611	0.0566	0.1841	0.0872
	-	0.6657		0.6742	0.8277	0.8122	0.6715	0.7284	0.8710	0.6169	0.6126	0.6656	0.5920	0.4604	0.3929	0.3906	0.7739	0.7642	0.7619
Balanced	ા	0.6564		0.6955	0.7822	0.8179	0.7461	0.7385	0.8614	0.6039	0.6673	0.6699	0.6410	0.4538	0.4717	0.4598	0.7163	0.7051	0.6885
	3	0.6926	0.7001	0.6881	0.7933	0.8633	0.6759	0.7330	0.8669	0.6169	0.6221	0.7121	0.5920	0.3597	0.3979	0.3916	0.7784	0.7737	0.7688
	-	0.5450	0.5495	0.5506	0.9295	0.9927	0.5623	0.7126	0.9311	0.4534	0.4071	0.5033	0.3942	0.0702	0.0444	0.0969	0.6307	0.3834	0.5626
FI	o≀ '	0.5286	0.5124	0.5754	0.9717	0.8268	0.6487	0.7500	0.9103	0.3993	0.5389	0.5776	0.5015	0.1642	0.2637	0.2389	0.5738	0.5184	0.5567
	3	0.5823	0.5955	0.5721	0.9467	0.9944	0.5712	0.7244	0.9282	0.4534	0.4235	0.5523	0.3942	0.0805	0.0812	0.1134	0.6092	0.3915	0.5657
	н (0.3601	0.3322	0.3780	0.1999	0.4730	0.0693	0.3998	0.7314	0.2375	0.2969	0.2480	0.2093	-0.0751	-0.1679	-0.1940	0.4862	0.2945	0.4438
MCC	৯২ ০	0.3131	0.2548	0.4089	0.3450	0.1551	0.0962	0.4167	0.6855	0.2254	0.3677	0.3349	0.3051	-0.0992	-0.0367	-0.0672	0.4569	0.3571	0.4334
	oo .	0.3971	0.3855	0.3983	0.1871	0.6163	0.0708	0.4073	0.7251	0.2375	0.3108	0.3369	0.2093	-0.2479	-0.1659	-0.1773	0.4592	0.2994	0.4363
		0.6657	0.6666	0.6742	0.8277	0.8122	0.6715	0.7284	0.8710	0.6169	0.6126	0.6656	0.5920	0.4604	0.3929	0.3906	0.8543*	0.8540*	0.8571*
AUC	o) (0.6564	0.6362	0.6955	0.7822	0.8179	0.7461	0.7385	0.8614	0.6039	0.6673	0.6699	0.6410	0.4538	0.4717	0.4598	0.7163	0.7051	0.6885
	3	0.6926	0.7001	0.6881	0.7933	0.8633	0.6759	0.7330	0.8669	0.6169	0.6221	0.7121	0.5920	0.3597	0.3979	0.3916	0.8480*	0.8599*	0.8538*

Table 3.12: All Metrics

Measure	Metr.		hadoop 0.4			hadoop 0.5			hadoop 0.6			hadoop 0.7			hadoop 0.8	
- L	CI		0.7395			0.6589			0.5642			0.7056			0.3534	
Batance	C2		0.5062			0.6056			0.7015			0.5501			0.8579	
	CS		0.1899			0.1601			0.1705			0.1997			0.1241	
Correlation	S C3		0.5956			0.5589			0.5397			0.5737			0.4917	
	7.9		0.0348			0.0322			0.0299			0.0280			0.0292	
Dimensional.	7.3		0.0050			0.0046			0.0042			0.0040			0.0042	
	L1		0.2950			0.2620			0.1996			0.2654			0.1134	
Linearity	L2		0.1473			0.1310			0.0981			0.1327			0.0550	
	LO		0.1400			#121.0			0.0010			#07T-0			0.0409	
	N1 N2		0.4378			0.4009			0.3333			0.3840			0.1708	
	N3		0.3234			0.2857			0.1838			0.2200			0.1208	
Neighborh.	N_4		0.1990			0.1429			0.1282			0.0960			0.0417	
	TI		0.0101			0.0096			0.0100			0.0087			0.0143	
	Demeir		0.9700			0.9720			0.9090	1		0.9786			0.9420	
Netmork	ClsCoef		0.4453			0.4398			0.4383			0.4435			0.8030	
	Hubs		0.9121			0.9152			0.8929			0.9074			0.8912	
	F1		0.9641			0.9643			0.9519			0.9370			0.9711	
	FIv		0.5797			0.6427			0.4057			0.4816			0.3269	
Overlap	F2		0.1107			0.3023			0.0257			0.0552			0.0329	
	F3		0.9900			0.9032			0.9530			0.9600			0.8750	
	F4		0.9453			0.8479			0.2446			0.9000			0.6875	
	1 05		0.3100			0.1108			0.2440			0.2731			0.0961	
Smooth.	83		0.3284			0.2857			0.1709			0.2080			0.1208	
	84		0.1516			0.1646			0.1175			0.1631			0.0625	
		NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DT	NC	NB	DL	NC
	1	0.4150	0.4632	0.3438	0.3619	0.1294	0.2726	0.3700	0.1600	0.0000	0.3149	0.3302	0.2639	0.2667	0.000.0	0.0417
Precision	०३ ०	0.4267	0.2003	0.3316	0.2332	0.1710	0.2274	0.3267	0.2323	0.5909	0.3433	0.2340	0.3688	0.0719	0.1130	0.0384
		0.2478	0.4868	0.3240	0.2174	0.1687	0.3062	0.2192	0.0500	0.0000	0.2554	0.5484	0.3218	0.0750	0.0000	0.6000
Recall	≈ ≀	0.4165	0.4451	0.3321	0.2713	0.5327	0.2982	0.5695	0.7195	0.4889	0.3500	0.5833	0.3643	0.2667	0.5000	0.2667
	З	0.3164	0.4344	0.3565	0.1841	0.2228	0.3723	0.2067	0.1525	0.0000	0.2954	0.5537	0.4270	0.3500	0.0750	0.6000
		0.0990	0.1244	0.1629	0.0885	0.2025	0.1959	0.0683	0.0524	0.0000	0.0928	0.1716	0.1774	0.0474	0.0272	0.6045
ratt Out	N 60	0.1522	0.1915	0.1757	0.1387	0.2685	0.3335	0.0820	0.3742	0.0000	0.1181	0.2058	0.1740	0.2789	0.1480	0.6000
	1	0.5744	0.6812	0.5805	0.5645	0.4831	0.5551	0.5754	0.4988	0.5000	0.6753	0.7644	0.6602	0.5138	0.4864	0.4977
Balanced	82	0.6334	0.4777	0.5842	0.5284	0.5173	0.5528	0.6965	0.6726	0.7048	0.5958	0.5756	0.5951	0.5232	0.6049	0.4266
	3	0.5821	0.6214	0.5904	0.5227	0.4772	0.5194	0.5623	0.5159	0.5000	0.6827	0.7519	0.7021	0.5356	0.4635	0.5000
	1	0.2896	0.4405	0.3090	0.2507	0.1397	0.2680	0.1813	0.0762	0.0000	0.2347	0.2974	0.2314	0.1016	0.0000	0.0735
FI	o) o	0.3952	0.2738	0.3268	0.2268	0.2554	0.2453	0.4051	0.3372	0.4850	0.3403	0.3224	0.3525	0.1111	0.1785	0.0644
	0 -	0.3103	0.3033	0.3324	1,007	0.1189	0.2019	0.1400	0.0130	0.0000	0.2024	0.2104	0.2002	6.600	0.0033	0.000
JJW	-1 0	0.1832	0.3324	0.1645	0.1589	-0.0435	0.1108	0.1595	0.0220	0.0000	0.1572	0.2647	0.1267	0.0932	-0.0347	-0.0088
	\$ e2	0.1767	0.2116	0.1781	0.0489	-0.0172	0.0347	0.1053	0.0395	0.0000	0.1599	0.2277	0.1595	0.0078	0.0055	0.0000
		0.5744	0.6812	0.5805	0.5645	0.4831	0.5551	0.5754	0.4988	0.5000	*16091	0.7656*	0.6052*	0.5138	0.4864	0.4977
AUC	જ ર	0.6334	0.4777	0.5842	0.5284	0.5173	0.5528	0.6965	0.6726	0.7048	0.5958	0.5756	0.5951	0.5232	0.6049	0.4266
	8	0.5821	0.6214	0.5904	0.5227	0.4772	0.5194	0.5623	0.5159	0.5000	0.6173*	0.7449*	0.6576*	0.5356	0.4635	0.5000

Chapter 4

Conclusions and Future Work

4.1. Conclusions

In this work, we analysed data complexity metrics, as well as analytical metrics obtained from the confusion matrix and some basic classifiers. To recapitulate, the following work was conduced through this dissertation:

- 1. An introduction to *data complexity metrics*, class imbalance and techniques to mitigate its effects, datasets used for the experimentation, and analytical metrics (see Chapter 2, Sections 3.1 and 3.3).
- 2. Python implementation of the experimentation (connecting to R's ECol to obtain the complexity metrics) see Section ??:
 - Obtain the complexity metrics of the datasets.
 - Calculate the analytical metrics of the datasets using K-fold.
 - Compute the analytical metrics of the datasets after applying Under/Oversampling to each fold.
- 3. Analysis of the obtained results (see Section 3.4.5).

The experiments carried out showed that the datasets selected have many *problems* including *imbal-anced classes*, and data *overlapping* are some of them. This could be one of the reasons why the classifiers do not achieve the expected results.

It has also been tried out a few way to improve the classification in those datasets, such as K-folding Cross Validation combined with Undersampling and Oversampling techniques. The result of those experiments led to the intuition that either the applied techniques are not fit for the datasets (do not manage to increase the performance); or that the classification algorithms selected do not perform as well as they were expected. To solve this, in addition to further research, better datasets should be generated, trying to reduce the value of metrics such as overlapping, and therefore maximize linearity; reduce the class imbalance, etc. We also need to explore other balancing techniques than the ones used for this paper.

In summary, we observed that the nature of the data might affect the results and this needs further explored in several path as stated next.

4.2. Future Work

There are several paths that can follow this work. First we need to run all experiments with more datasets - trying to have a wider variety of the values obtained in the complexity metrics - and classification algorithms, that could lead to better results than the ones used. Other way would be to apply other imbalance techniques could be applied to the datasets.

The final objective is to try minimize/maximize the aforementioned complexity metrics, which should lead to better classification results.

There are also other paths to follow, for example, analyze the data/quality in the context of feature selection. There is also another path to to do so with interpretable machine learning [56].

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Appendix A

Prerequisites

Some relevant code sections have been included. The whole project is publicly available on GitHub: https://github.com/PabloAceG/ComputingProject.

To be able to execute the experiments within the repository, Python3 is needed. Anaconda or the official Python located in the official repositories can be used as long as version 3 or posterior is used. Trying to replicate the experiments on some operative systems might terminate in error. If this is the case, python can be changed (*Linux*) with:

```
sudo update-alternatives --config python
```

R (programming language) is needed before trying to execute the project. Also, the following packages are mandatory in order to replicate the experiments:

- ECoL Dataset Complexity Metrics Package.
 - https://github.com/lpfgarcia/ECoL
 - https://cran.r-project.org/web/packages/ECoL/
- Rserve server, responds requests made to R: https://rforge.net/Rserve/doc.html.

Once the previous requisites are fulfilled, the R server can be started by executing the following commands:

```
library(Rserve) # import the library
run.Rserve() # start the server. Or simply Rserve()
```

Now, it is time to download the project to install the remaining Python packages. The project can be downloaded from https://github.com/PabloAceG/ComputingProject/.

Same as before, some Python packages are mandatory to execute the project. These packages are available in requirements.txt ¹ file. To automatically install those packages, run²:

```
pip install -r .\code\requirements.txt
```

It might happen that pip install -r might not install all packages. To solve this, the failing packages must be installed manually:

```
pip install <package_name>
```

 $^{^{1} \}verb|https://github.com/PabloAceG/ComputingProject/blob/master/code/requirements.txt|$

 $^{^2}$ All commands are executed from the parent folder of the repository.

Now, the experiments should be replicable. The experiment's code is under the folder https://github.com/PabloAceG/ComputingProject/tree/master/code To run them, execute:

```
python code/metrics_comparison.py
python code/metrics_kfold.py
python code/metrics_kfold_undersampling.py
python code/metrics_kfold_oversampling.py
```

Each of the previous commands execute one experiment.

As final remarks, the class r_connect.py 3 is the client connection the server in R (Rserve). It makes the requests to the Ecol package to obtain the complexity metrics.

The class data.py ⁴ standardizes the datasets input (parsing data) and some other metrics from the package sklearn ⁵.

 $^{^3 \}verb|https://github.com/PabloAceG/ComputingProject/blob/master/code/r_connect.py|$

⁴https://github.com/PabloAceG/ComputingProject/blob/master/code/data.py

⁵https://scikit-learn.org/stable/index.html

Appendix B

Python Relevant Code

B.1. Rserve Python Client

The class r_connect.py is a client for R package Rserve. Makes requests to ECoL R package and parses data.

The import statements have been made redundant in this snippet and the rest of the snippets in this appendix.

```
class r_connect:
      __metrics = None
      def __init__ (self):
           self.__connection = self.__connect()
      def __connect (self):
           return pyRserve.connect()
      def get_metrics (self, X=None, Y=None):
           if X is None and Y is None :
              if self.__metrics is not None:
13
                   return self.__metrics
14
               else :
                   # No data and no parameters: finish execution
                   error_message = '...'
                   raise Exception(error_message)
18
                   sys.exit (400)
19
          else :
20
               # Stores connection to R's RPC.
21
               connect = self.__connection
23
               # Sends the input matrix and the output vector to R.
               connect.r.X = X
               connect.r.y = Y
27
               # Library to use in R.
28
               connect.r('df_X <- as.data.frame(X)')</pre>
29
               connect.r('df_y <- as.data.frame(y)')</pre>
               connect.r('library("ECoL")')
32
               ## Metrics, uses a dictionary to provide a faster access to its
```

```
# contents.
34
              metrics = {}
               # Balance: C1, C2
              balance = self.safe_connect('balance(df_X, df_y)')
38
              balance_dic_entry = { 'balance' : balance }
39
              metrics.update (balance_dic_entry)
40
41
               # Correlation: C1, C2, C3, C4
42
              correlation = self.safe_connect('correlation(df_X, df_y, summary=c("mean"))')
43
               correlation_dic_entry = { 'correlation' : correlation }
              metrics.update (correlation_dic_entry)
               # Dimensionality: T2, T3, T4
47
              dimensionality = self.safe_connect('dimensionality(df_X, df_y, summary=c("mean"))'
48
      )
              dimensionality_dic_entry = { 'dimensionality' : dimensionality }
49
              metrics.update (dimensionality_dic_entry)
               # Linearity: L1, L2, L3
              linearity = self.safe_connect('linearity(df_X, df_y, summary=c("mean"))')
               linearity_dic_entry = { 'linearity' : linearity }
              metrics.update (linearity_dic_entry)
56
               # Neighborhood: N1, N2, N3, N4, T1, LSC
57
              neighborhood = self.safe_connect('neighborhood(df_X, df_y, summary=c("mean"))')
58
              neighborhood_dic_entry = { 'neighborhood' : neighborhood }
              metrics.update (neighborhood_dic_entry)
60
61
               # Network: Density, ClsCoef, Hubs
              network = self.safe_connect('network(df_X, df_y, summary=c("mean"))')
               network_dic_entry = { 'network' : network }
64
              metrics.update (network_dic_entry)
65
66
               # Overlap: F1, F1v, F2, F3, F4
67
              overlap = self.safe_connect('overlapping(df_X, df_y, summary=c("mean"))')
              overlap_dic_entry = { 'overlap' : overlap }
69
              metrics.update (overlap_dic_entry)
               # Smoothness: S1, S2, S3, S4
               smoothness = self.safe_connect('smoothness(df_X, df_y, summary=c("mean"))')
               smoothness_dic_entry = { 'smoothness' : smoothness }
74
              metrics.update (smoothness_dic_entry)
75
76
               self.__metrics = metrics
78
              return metrics
79
80
      def print_metrics (self, metrics=None) :
           print ('\n\n=== Printing metrics ===', end='\n\n')
83
84
           . . .
85
           . . .
86
      def get_print_metrics(self, X, Y):
87
          self.get_metrics (X, Y)
88
          self.print_metrics (self.__metrics)
89
90
        return self.__metrics
```

Listing B.1: Connection code to requests R ECoL functions

B.2. Datasets and Operations on Data

The following code contains the logic to read and parse datasets requested through the function getDataset(...). The datasets can be shuffled if specified through parameter, but in this situation no experiments used that option (as the results should be replicated, the input that should always be the same).

The class also uses *sklearn* library to calculate some metrics. The functions in this code simply parse the results so that they are easier to read afterwards (no need to have more than 4 digits of precision in float numbers).

Not all the code has been copied, as some parts repeat.

```
. . .
3
  def __load_arff(path):
           Loads the dataset content of an .arff file into the workspace.
               - path: Location of the file.
           Output:
9
               - dataset: Data from the file.
12
      dataset = []
14
15
       with open(path, 'r') as data:
           dataset = arff.load(data)['data']
16
17
       return dataset
18
19
      __load_csv(path):
20
21
           Loads the data content of an .csv file into the workspace.
22
           Input:
23
24
             - path: Location of the file.
           Output:
               - dataset: Data from the file.
26
27
28
29
       dataset = []
30
       with open (path, 'r') as csv_file:
31
           dataset = pd.read_csv(
33
               csv_file,
34
               sep=','
35
           )
36
```

```
return dataset
37
38
  def __parte_dataset(dataset, input_select, target_select):
          Takes a dataset and parses it to only take what is necessary.
41
          Inputs:
42
               - dataset: Input raw data as a Pandas Data Framework.
43
               - start: Where columns start to be useful.
44
45
               - input: Input arrays of the dataset.
46
               - target: Target column of the dataset.
47
      num_rows = len(dataset)
      last_column = target_select if (target_select < 0) else None</pre>
51
52
53
      # Input
      input_columns = dataset.columns[input_select:last_column]
54
55
      input = dataset[input_columns].head(num_rows).astype(float).to_numpy()
      # Target
57
      target_column = dataset.columns[target_select]
      target = dataset[target_column].head(num_rows)
59
60
      # Parse output
61
62
      sample = target[0]
      if not isinstance(sample, str):
63
          target = numpy.where(target > 0, 1, 0)
64
      else:
65
          has_faults = target == 'yes'
          target = numpy.where(has_faults , 1, 0)
      return input, target
69
70
71 def __data_preparation(path, input_select, target_select, type='arff', shuffle=False):
72
          Loads an .arff/.csv file and parses its content to input/output valid
73
          for a Machine Learning application.
74
          Input:
               - path: Location of the file.
                - start: Where columns start to be useful (string columns are not
                  necessary).
78
79
               - type: It can be:
80
                   - arff
                   - csv
          Output:
82
               - input: Input arrays of the dataset.
83
               - target: Target column of the dataset.
84
      # Load data
87
      dataset = []
88
      if type == 'arff':
89
          dataset = __load_arff(path)
90
      elif type == 'csv':
91
          dataset = __load_csv(path)
92
93
          raise Exception('Not a valid file type. Try with arff or csv!')
94
          sys.exit(404)
```

```
dataset = pd.DataFrame(dataset)
96
97
       if shuffle:
98
           dataset = dataset.sample(frac=1)
100
       # Parse data
       data = (dataset, input_select, target_select)
103
       input, target = __parte_dataset(*data)
104
       return input, target
106
107
   def __data_preparation_iris_dataset(path):
108
       # Load data
109
       dataset = __load_csv(path)
      dataset = pd.DataFrame(dataset)
111
112
      # Parse data
113
      start = 0
      last = -1
114
       num_rows = len(dataset)
116
       # Input
       input_columns = dataset.columns[start : last]
118
       input = dataset[input_columns].head(num_rows).astype(float).to_numpy()
119
120
121
       # Target
       target_column = dataset.columns[last]
       target = dataset[target_column].head(num_rows)
124
125
       # Parse target
127
       values = {'setosa': 1, 'versicolor': 2, 'virginica': 3}
       target = numpy.array( [
128
           values[type] for type in target
129
130
       ] )
131
       return input, target
132
def get_dataset(name, shuffle=False):
135
           Retrieves the data of a given dataset, separated into input information
           and target output - .arff or .csv files only.
138
           Input:
139
               - name: Dataset name.
140
                   - ant
                   - apache
141
                   - camel
142
                   - iris
143
                    - ivy
144
                    - jedit
146
                    - log4j
                    - poi
147
                    - synapse
148
149
                    - xalan
                    - xerces
150
               - input: Input arrays of the dataset.
152
               - target: Target column of the dataset.
153
```

```
= '' # Location of file
156
       path
       start = 0
                           # From which columns to use
157
       output_col = -2  # Position of output column
158
       type = 'arff' # Type of file to be read. Default .arff
159
160
       if name == 'ant':
161
          # Retrieve data
           path = './dataset/ant-1.7.arff'
163
           start = 3
164
       elif name == 'apache':
166
167
           # Retrieve data
           path = './dataset/Apache.csv'
168
           start = 3
169
          output_col = -1
170
171
          type = 'csv'
172
      elif name == 'camel':
           # Retrieve data
174
           path = './dataset/camel-1.6.arff'
175
           start = 3
177
       elif name == 'iris': # Special case. Non-binary output. Needs different
178
179
                             # treatment.
180
           # Retrieve data
           path = './dataset/iris.csv'
181
           input, target = __data_preparation_iris_dataset(path, shuffle)
182
183
           return input, target
184
186
       elif name == 'ivy':
           # Retrieve data
187
           path = './dataset/ivy-2.0.arff'
188
           start = 3
189
191
       . . .
192
       elif name == 'xerces':
193
           # Retrieve data
194
           path = './dataset/xerces-1.4.arff'
           start = 3
196
197
      elif name == 'hadoop-1':
198
           # Retrieve data
           path = './dataset/hadoop-proc-0.1.csv'
200
           start = 2
201
           output_col = 1
202
           type = 'csv'
203
205
       . . .
206
       elif name == 'hadoop-8':
207
208
          # Retrieve data
          path = './dataset/hadoop-proc-0.8.csv'
209
          start = 2
210
           output_col = 1
211
           type = 'csv'
212
```

```
214
       else:
215
           raise Exception ('The given dataset name is not valid.')
           sys.exit(404)
218
       # Return results
219
       input, target = __data_preparation(path, start, output_col, type, shuffle)
221
222
       return input, target
223
   def confusion_matrix(x_test: list, y_test: list, classifier):
224
225
           Obtains the confusion matrix for a given testing dataset, with binary
           output.
227
           Input:
228
               - x_test: paremeters for testing dataset.
229
230
               - y_test: target/desired output for testing dataset.
               - classifier: trained classifier.
           Output:
232
233
                   true_positive: successfully predicted positives
234
                   true_negative: successfully predicted negatives
                   false_positive: unsuccessfully predicted positives
                   false_negative: unsuccessfully predicted positives
237
238
239
       # Confusion Matrix Cells
       true_positive:float = 0
241
       true_negative:float = 0
242
       false_positive:float = 0
243
244
       false_negative:float = 0
       # Calculate number of repetitions of each classification.
246
       for (input, target) in zip(x_test, y_test):
247
248
           prediction:int = classifier.predict([input])[0]
249
           if prediction == target: # Success
250
               if prediction: true_positive += 1
251
                           true_negative += 1
               else:
252
                                       # Wrong
253
               if prediction: false_positive += 1
                              false_negative += 1
255
256
257
       # Transform absolute to relative values
       num\_samples = len(y\_test)
258
       true_positive = true_positive / num_samples
259
       true_negative = true_negative / num_samples
260
       false_positive = false_positive / num_samples
261
       false_negative = false_negative / num_samples
262
263
264
       return (true_positive, true_negative, false_positive, false_negative)
265
266 def recall(targets, predictions) -> float:
267
           Sensitivity, recall, hit rate or True Positive Rate (RPR)
           https://scikit-learn.org/stable/modules/generated/sklearn.metrics.recall_score.html
269
                 TP
                          TP
270
           TPR = ----
                         ----- = 1 - FNR
271
                     TP + FN
```

```
111
273
       return round(metrics.recall_score(targets, predictions), 4)
274
275
   def fall_out(targets, predictions) -> float:
277
           Fallout, or False Positive Rate (FPR)
278
                 FP FP
           FPR = ---- = ----- = 1 - TNR
                 N
                       FP + TN
281
       ,,,
282
       \ensuremath{\text{\#}} Calculate TN and FP rates
283
       num_items:int = len(targets)
284
285
       false_positive:float = 0
      true_negative: float = 0
286
       # Count
287
      for (t, o) in zip(targets, predictions):
288
289
          if (o == t and o == 0):
              true_negative += 1
          if (o != t and o == 1):
291
               false_positive += 1
292
293
      try:
           # Rates
           true_negative /= num_items
295
          false_positive /= num_items
296
297
298
           # False Positive Rate
           fdr:float = false_positive / (false_positive + true_negative)
           return round(fdr, 4)
300
       except:
301
          return 0
302
304
   def precision(targets, predictions) -> float:
305
           Precision or positive predictive value (PPV).
306
307
           https://scikit-learn.org/stable/modules/generated/sklearn.metrics.precision_score.html
                  TP
           PPV = ----- = 1 - FDR
309
                 TP + FP
310
311
312
       return round (metrics.precision_score(targets, predictions), 4)
314 def balanced(targets, predictions) -> float:
315
316
          Balanced Accuracy (BA)
          https://scikit-learn.org/stable/modules/generated/sklearn.metrics.
       balanced_accuracy_score.html#sklearn.metrics.balanced_accuracy_score
                TPR + TNR
318
           BA = -----
319
                    2
320
321
322
       return round(metrics.balanced_accuracy_score(targets, predictions), 4)
323
324
325 def f1(targets, predictions) -> float:
326
           F1 Score. Is the harmonic mean of precision and sensitivity.
327
           https://scikit-learn.org/stable/modules/generated/sklearn.metrics.f1_score.html
328
                  PPV x TPR 2 TP
329
           F1 = 2 -----
```

```
PPV + TPR 2 TP + FP + FN
331
332
333
       return round (metrics.fl_score (targets, predictions), 4)
334
   def mcc(targets, predictions) -> float:
335
336
           Matthews Correlation Coefficient (MCC).
337
           https://scikit-learn.org/stable/modules/generated/sklearn.metrics.matthews_corrcoef.
                             TP x TN - FP x FN
339
340
                  sqrt((TP + FP)(TP + FN)(TN + FP)(TN + FN))
341
       return round(metrics.matthews_corrcoef(targets, predictions), 4)
343
344
   def auc(targets, predictions) -> float:
345
346
           Area Under Receiver Operating Characteristic Curve,
347
           Area Under ROC Curve or AUC.
348
           https://scikit-learn.org/stable/modules/generated/sklearn.metrics.roc_curve.html
349
           https://scikit-learn.org/stable/modules/generated/sklearn.metrics.auc.html
350
                  1 + TPR - FPR
352
353
       ,,,
354
355
       fpr, tpr, thresholds = metrics.roc_curve(targets, predictions)
       return round(metrics.auc(fpr, tpr), 4)
357
358
   def store_results(filename:str, metrics:list):
359
       with open('./code/results/' + filename + '.csv', mode='a', newline='') as csvfile:
361
           writer = csv.writer(csvfile, delimiter=',', quoting=csv.QUOTE_MINIMAL)
           writer.writerow(metrics)
362
363
def calculate_results(targets:list, predictions:list) -> list:
       # Metrics
       ppv:float = precision(targets, predictions)
366
       tpr:float = recall (targets, predictions)
367
       fpr:float = fall_out (targets, predictions)
368
       ba :float = balanced (targets, predictions)
       fm :float = f1
                             (targets, predictions)
       m :float = mcc
                             (targets, predictions)
371
372
       a :float = auc
                             (targets, predictions)
373
       metrics:list = [ppv, tpr, fpr, ba, fm, m, a]
374
       return metrics
375
   def train_predict(clf, input_train, target_train, test):
378
       clf.fit(input_train, target_train)
       # Test
380
   return clf.predict(test)
381
```

Listing B.2: Load datasets, calculate metrics, export results to CSV files, etc.

B.3. Experiment 1. Complexity Metrics Comparison

The objective is to see if there is any dependency between some complexity metrics (balance, dimensionality, overlapping, etc.).

This programs obtains the complexity metrics (more in section 2.1) from different datasets, and stores the results on a CSV file for their comparison. The dataset is loaded, metrics are retrieved for every dataset and those metrics are plotted and stored.

```
2 ...
3 from r_connect import r_connect
4 import data as DATASETS
  def add_metrics(storage, dataset_metrics):
          Includes a new set of calculated metrics into a variable.
          It creates an array for each metric's measure.
          Input:
               - storage(dict) : Data structure to store the list of measures from
                  the metrics of datasets.
12
               - dataset_metrics (dict): Metrics computed from a dataset.
13
          Output:
14
               - storage (dict): Metrics added to the already stored ones.
       # Iterate through the metrics
17
      for m in storage:
18
           # Metric might not have been calculated for dataset
19
          if m in dataset_metrics:
              metric = dataset_metrics[m]
21
22
               # Iterate through the measures of the metric
23
               for measure in storage[m]:
                       # Measure might not have been calculated for dataset
26
                       if measure in storage[m]:
27
28
                           storage[m] [measure].append(float(metric[measure]))
                   except Exception:
29
                       pass
          else:
31
               print('Something went wrong')
33
       return storage
35
  def plot_metrics_comparison(metrics):
36
37
38
          Input:
             - metrics:
          Output:
40
      ,,,
41
      i = 0
42
43
      j = 0
       for metric in metrics:
44
45
          cols = int (math.ceil(len(metrics[metric]) / rows))
46
          fig, axs = plt.subplots(rows, cols)
47
          for measure in metrics[metric]:
               DATASETS.store_results('metrics-hadoop', [metric, measure] + [round(i, 4) for i in
       metrics[metric][measure]])
```

```
if cols == 1:
50
                    if metrics[metric][measure]:
51
                        axs[i].bar(datasets, metrics[metric][measure])
54
                        axs[i].text(0.5, 0.5, 'No data')
55
56
                    title = metric + ': ' + measure
57
58
                    axs[i].set_title(title)
               else:
59
                    if metrics[metric][measure]:
60
                       axs[i, j].bar(datasets, metrics[metric][measure])
61
63
                   else:
                        axs[i, j].text(0.5, 0.5, 'No data')
64
65
                    title = metric + ': ' + measure
67
                    axs[i, j].set_title(title)
68
               if j == cols - 1:
69
                   i += 1
70
                    j = 0
               else:
72
                   j += 1
73
74
           i = 0
75
76
          j = 0
           plt.show()
77
78
79
   if __name__ == '__main__':
81
          Main code - to be executed
82
83
84
      # Datasets to analyze
       111
86
       datasets = [
87
          'ant',
88
           'apache',
           'camel',
           'ivy',
91
           'jedit',
92
           'log4j',
93
94
           'synapse',
           'xalan',
95
           'xerces'
96
      ]
97
       ,,,
98
       datasets = [
          'hadoop-1',
100
           'hadoop-2',
           'hadoop-3',
102
           'hadoop-4',
103
           'hadoop-5',
           'hadoop-6',
           'hadoop-7',
106
           'hadoop-8',
107
```

```
109
110
        # Store metrics computed from datasets (datatype: dict)
111
       results = {
112
           'balance': {
                'C1': [],
114
                'C2': []
115
116
           },
117
           'correlation': {
               'C1': [],
118
               'C2': [],
119
                'C3': [],
120
                'C4': []
121
122
           },
            'dimensionality': {
                'T1': [],
124
                'T2': [],
125
                'T3': []
126
            },
            'linearity': {
128
                'L1': [],
129
                'L2': [],
                'L3': []
131
           },
            'neighborhood': {
133
134
                'N1': [],
135
                'N2': [],
                'N3': [],
136
                'N4': [],
                'T1': [],
138
                'LSC': [],
140
            },
            'network': {
141
                'Density': [],
142
                'ClsCoef': [],
143
                'Hubs': []
144
145
           },
            'overlap': {
146
                'F1': [],
147
                'F1v': [],
148
                'F2': [],
149
                'F3': [],
                'F4': []
152
           },
153
           'smoothness': {
               'S1': [],
154
                'S2': [],
                's3': [],
156
                'S4': []
157
158
            }
159
       }
160
       # Connect to R
161
162
       connector = r_connect()
163
       # Get Metrics
164
       for set in datasets:
165
            print(set)
166
           inputs, targets = DATASETS.get_dataset(set)
```

```
metrics = connector.get_metrics(inputs, targets)

results = add_metrics(results, metrics)

results = add_metrics(results, metrics)

# Print Metrics

print(results)

plot_metrics_comparison(results)
```

Listing B.3: Compare complexity metrics of different datasets

B.4. Experiment 2. Compare Metrics on K-fold Cross Validation

The function calls to the data (referenced as DATASETS in the code) object are unfolded in the snippet B.2.

The objective is to look for a relation between confusion matrix metrics (recall, fallout, etc.) between the folds generated out of a K-fold Cross Validation. See if there is a certain linearity between folds and what might cause certain behaviors.

In order do create this experiment, a dataset is loaded, and then it is folded into k-equally-sized parts. For each part, three different classification algorithms are trained and tested to compare the aforementioned metrics (more about the metrics in 3.3). This same process is repeated for every dataset.

```
2 ...
3 import data as DATASETS
  if __name__ == '__main__':
       # Data
6
       datasets = [
           'ant',
           'apache',
9
           'camel',
           'ivy',
           'jedit',
12
           'log4j',
13
           'poi',
14
           'synapse',
           'xalan',
           'xerces',
17
           'hadoop-1',
18
           'hadoop-2',
19
           'hadoop-3',
20
           'hadoop-4',
21
           'hadoop-5',
22
           'hadoop-6',
23
           'hadoop-7',
24
           'hadoop-8'
26
27
       for d in datasets:
28
           print('----' + d + '-----')
29
30
           inputs, target = DATASETS.get_dataset(d)
31
           # K-fold Parameters
```

```
k = 5
33
          kf = KFold(n_splits=k)
34
          splits = kf.split(inputs)
                              Precision Recall Fallout Balanced F1 MCC AUC
36
                                    0,
                                             0,
          mean_naive = np.array([0,
                                                         Ο,
                                                               0, 0,
37
                                         0,
                                                 0,
          mean_tree = np.array([0,
                                                         Ο,
                                                               0, 0, 0])
38
                                                0,
                                         0,
                                                        0.
                                                             0, 0, 0])
39
          mean_knn = np.array([0,
          # Get measurements using K-fold
41
          for train_index, test_index in splits:
42
              # Data partition
              x_train, x_test = inputs[train_index], inputs[test_index]
              y_train, y_test = target[train_index], target[test_index]
46
              filename = d + '-k' + str(k)
47
48
              # Train NN
49
              print('---> Naive Bayes')
              clf = GaussianNB()
              predictions = DATASETS.train_predict(clf, x_train, y_train, x_test)
52
              naive_metrics = DATASETS.calculate_results(y_test, predictions)
53
              mean_naive = np.add(mean_naive, naive_metrics)
              naive_metrics = ['Naive Bayes'] + naive_metrics
              DATASETS.store_results(filename, naive_metrics)
56
57
              print('---> Decision Tree')
58
              clf = DecisionTreeClassifier()
59
              predictions = DATASETS.train_predict(clf, x_train, y_train, x_test)
60
              tree_metrics = DATASETS.calculate_results(y_test, predictions)
61
              mean_tree = np.add(mean_tree, tree_metrics)
              tree_metrics = ['Decision Tree'] + tree_metrics
              DATASETS.store_results(filename, tree_metrics)
64
65
              print('---> Nearest Centroid')
66
              clf = NearestCentroid()
67
              predictions = DATASETS.train_predict(clf, x_train, y_train, x_test)
68
              knn_metrics = DATASETS.calculate_results(y_test, predictions)
69
              mean_knn = np.add(mean_knn, knn_metrics)
              knn_metrics = ['Nearest Centroid'] + knn_metrics
              DATASETS.store_results(filename, knn_metrics)
              print('----')
74
75
          # K-fold Mean
76
          mean_naive = [round(i, 4) for i in (mean_naive / k)]
77
          DATASETS.store_results(filename, ['Naive Bayes Mean'] + mean_naive)
78
          mean_tree = [round(i, 4) for i in (mean_tree / k)]
79
          DATASETS.store_results(filename, ['Decision Tree Mean'] + mean_tree)
          mean_knn = [round(i, 4) for i in (mean_knn / k)]
          DATASETS.store_results(filename, ['Nearest Centroid Mean'] + mean_knn)
83
         print([mean_naive, mean_tree, mean_knn])
84
```

Listing B.4: Calculate Metrics from Confusion Matrix to compare in-fold results

B.5. Experiment 3. Compare Metrics with Under-sampling and K-fold Cross Validation

The function calls to the *data* (referenced as *DATASETS* in the code) object, can be observed in the snippet B.2. Also, the experiment is the same as in B.4, although an under-sampling filter is applied to each fold of the dataset before using any classification algorithm.

This experiment has to be executed as many times as datasets want to be analyzed, as a bulk execution of all the datasets would probably end in error. The reason for this is that if the sampling strategy is too low, then there should not be enough data to properly train the classification. Also, it depends on the amount of samples of the minority class, that is why not a low enough value can be set for all datasets, and a single-dataset execution must be performed.

The values commented at the right of each dataset indicate the recommended sampling strategy for that dataset.

```
1 ...
3 import data as DATASETS
  if __name__ == '__main__':
      # Data
      # In this case a loop cannot be used to make all experiments, as the value
      # of the undersampling may vary on each dataset.
      dataset ='ant'
                           # 50
      #dataset = 'apache'
                          # 50
     #dataset = 'camel'
                           # 50
     #dataset = 'ivy'
                           # 30
12
     #dataset = 'jedit'
                           # 7
     #dataset = 'log4j'
                           # 11
14
      #dataset = 'synapse' # 50
      #dataset = 'xalan'
                            # 6
      #dataset = 'xerces'
17
      #dataset = 'hadoop-1'
18
      #dataset = 'hadoop-2' # 31
19
      #dataset = 'hadoop-3' # 35
20
      #dataset = 'hadoop-4' # 32
21
      #dataset = 'hadoop-5' # 26
22
      #dataset = 'hadoop-6' # 22
      #dataset = 'hadoop-7' # 34
      #dataset = 'hadoop-8' # 10
26
      inputs, target = DATASETS.get_dataset(dataset)
27
28
      # K-fold Parameters
29
      k = 5
      kf = KFold(n_splits=k, shuffle=True, random_state=1)
31
      splits = kf.split(inputs)
32
                        Precision Recall Fallout Balanced F1 MCC AUC
33
      mean_naive = np.array([0,
                                   0, 0,
                                                   0, 0, 0, 0])
                                                           0, 0, 0])
                                     Ο,
                                             Ο,
                                                     Ο,
      mean_tree = np.array([0,
35
                                    0,
                                            0,
      mean_knn = np.array([0,
                                                    0.
36
37
38
      RANDOM_STATE = 42
39
      # Get measurements using K-fold
40
      for train_index, test_index in splits:
41
```

```
# Data partition
42
          x_train, x_test = inputs[train_index], inputs[test_index]
43
          y_train, y_test = target[train_index], target[test_index]
          X, Y = make_imbalance(
46
              x_train, y_train,
47
              sampling_strategy={0:50, 1:50},
48
              random_state=RANDOM_STATE)
          filename = dataset + '-k' + str(k) + '-under'
          # Train NN
          print('---> Naive Bayes')
               = GaussianNB()
          pipeline = make_pipeline(
56
              NearMiss(version=2),
57
              clf)
58
          predictions = DATASETS.train_predict(pipeline, X, Y, x_test)
          naive_metrics = DATASETS.calculate_results(y_test, predictions)
60
          mean_naive = np.add(mean_naive, naive_metrics)
61
          naive_metrics = ['Naive Bayes'] + naive_metrics
62
          DATASETS.store_results(filename, naive_metrics)
64
          print('---> Decision Tree')
65
          clf = DecisionTreeClassifier()
66
          pipeline = make_pipeline(
67
              NearMiss(version=2),
68
              clf)
69
          predictions = DATASETS.train_predict(pipeline, X, Y, x_test)
          tree_metrics = DATASETS.calculate_results(y_test, predictions)
          mean_tree = np.add(mean_tree, tree_metrics)
          tree_metrics = ['Decision Tree'] + tree_metrics
73
          DATASETS.store_results(filename, tree_metrics)
74
          print('---> Nearest Centroid')
76
          clf = NearestCentroid()
77
          pipeline = make_pipeline(
78
              NearMiss(version=2),
79
              clf)
80
          predictions = DATASETS.train_predict(pipeline, X, Y, x_test)
          knn_metrics = DATASETS.calculate_results(y_test, predictions)
          mean_knn = np.add(mean_knn, knn_metrics)
83
          knn_metrics = ['Nearest Centroid'] + knn_metrics
84
85
          DATASETS.store_results(filename, knn_metrics)
          print('----')
87
88
      # K-fold Mean
89
      mean_naive = [round(i, 4) for i in (mean_naive / k)]
      DATASETS.store_results(filename, ['Naive Bayes Mean'] + mean_naive)
      mean_tree = [round(i, 4) for i in (mean_tree / k)]
92
      DATASETS.store_results(filename, ['Decision Tree Mean'] + mean_tree)
93
      mean_knn = [round(i, 4) for i in (mean_knn / k)]
94
      DATASETS.store_results(filename, ['Nearest Centroid Mean'] + mean_knn)
95
  print([mean_naive, mean_tree, mean_knn])
97
```

Listing B.5: Calculate Metrics from Confusion Matrix to compare in-fold results after applying under-sampling filter

B.6. Experiment 4. Compare Metrics with Over-sampling and K-fold Cross Validation

The function uses *data* (referenced as *DATASETS* in the code) object - which is unfolded in the snippet B.2. Also, the experiment is the same as in B.4 and B.5, but in this situation an over-sampling filter is applied to each fold of the dataset before starting the classification process.

Once again, a bulk execution with all the datasets is performed - unlike in Section B.5 there is minimum number to meet, so all the datasets can be treated generically.

The oversampling algorithm selected for this experiment has been SMOTE (see Section 2.3.1.2 for more information). Also, the same three classifiers used for the previous experiments are the ones used to compare results: (1) Naive Bayes - Gaussian; (2) Decision Tree; and (3) kNN Nearest Centroid.

```
2 . . .
3 import data as DATASETS
  if __name__ == '__main__':
      # Data
      datasets = [
          'ant',
          'apache',
          'camel',
          'ivy',
          'jedit',
12
          'log4j',
          'poi',
14
          'synapse',
15
          'xalan',
16
          'xerces',
17
          'hadoop-1',
          'hadoop-2',
          'hadoop-3',
20
          'hadoop-4',
21
          'hadoop-5',
23
          'hadoop-6',
          'hadoop-7',
24
          'hadoop-8'
25
      1
26
27
      for d in datasets:
          print('----' + d + '----')
29
          inputs, target = DATASETS.get_dataset(d)
30
31
          # K-fold Parameters
          k = 5
          kf = KFold(n_splits=k)
34
          splits = kf.split(inputs)
35
          #
                              Precision Recall Fallout Balanced F1 MCC AUC
36
                                                 0,
                                                         0, 0, 0, 0])
          mean_naive = np.array([0, 0,
          mean_tree = np.array([0,
                                           Ο,
                                                   Ο,
                                                           0,
                                                                  0, 0,
38
                                           0,
                                                  0,
                                                           Ο,
          mean_knn = np.array([0,
39
40
41
          \# Get measurements using K-fold
42
          for train_index, test_index in splits:
43
               # Data partition
              x_train, x_test = inputs[train_index], inputs[test_index]
```

```
y_train, y_test = target[train_index], target[test_index]
45
46
              filename = d + '-k' + str(k) + '-over'
              # Train NN
49
              # Pipeline to NN
50
              print('---> Naive Bayes')
51
              clf = make_pipeline(
                  SMOTE(),
53
                  GaussianNB())
54
              predictions = DATASETS.train_predict(clf, x_train, y_train, x_test)
              naive_metrics = DATASETS.calculate_results(y_test, predictions)
57
              mean_naive = np.add(mean_naive, naive_metrics)
              naive_metrics = ['Naive Bayes'] + naive_metrics
58
              DATASETS.store_results(filename, naive_metrics)
59
60
              print('---> Decision Tree')
61
              clf = make_pipeline(
62
                  SMOTE(),
63
                  DecisionTreeClassifier())
64
              predictions = DATASETS.train_predict(clf, x_train, y_train, x_test)
              tree_metrics = DATASETS.calculate_results(y_test, predictions)
              mean_tree = np.add(mean_tree, tree_metrics)
67
              tree_metrics = ['Decision Tree'] + tree_metrics
68
69
              DATASETS.store_results(filename, tree_metrics)
70
              print('---> Nearest Centroid')
71
              clf = make_pipeline(
                  SMOTE(),
                  NearestCentroid())
              predictions = DATASETS.train_predict(clf, x_train, y_train, x_test)
              knn_metrics = DATASETS.calculate_results(y_test, predictions)
76
              mean_knn = np.add(mean_knn, knn_metrics)
              knn_metrics = ['Nearest Centroid'] + knn_metrics
78
79
              DATASETS.store_results(filename, knn_metrics)
              print('----')
81
82
          # K-fold Mean
83
          mean_naive = [round(i, 4) for i in (mean_naive / k)]
          DATASETS.store_results(filename, ['Naive Bayes Mean'] + mean_naive)
          mean_tree = [round(i, 4) for i in (mean_tree / k)]
86
          DATASETS.store_results(filename, ['Decision Tree Mean'] + mean_tree)
87
          mean_knn = [round(i, 4) for i in (mean_knn / k)]
          DATASETS.store_results(filename, ['Nearest Centroid Mean'] + mean_knn)
90
          print([mean_naive, mean_tree, mean_knn])
91
```

Listing B.6: Calculate Metrics from Confusion Matrix to compare in-fold results after applying over-sampling filter

Appendix C

Tables

C.1. Complexity Metrics OO datasets

Table C.1: Complexity Metrics Analysis

Measure	Metric	ant	apache	camel	ivy	jedit	log4j	synapse	xalan	xerces
D 1	C1	0.7653	0.9895	0.7114	0.5108	0.1545	0.3953	0.9209	0.0944	0.8219
Balance	C2	0.4701	0.0286	0.5429	0.7477	0.9543	0.8319	0.1944	0.9755	0.3826
	C2	0.2622	0.0891	0.1227	0.1879	0.0448	0.0804	0.2310	0.0663	0.2839
Correlation	C3	0.6338	0.7372	0.5763	0.5588	0.5324	0.5780	0.7762	0.5275	0.6338
	C4	0.7409	1.0000	1.0000	0.3722	0.0285	0.4341	0.9727	0.0000	0.8878
Dimensionality	T2	0.0268	0.0524	0.0207	0.0568	0.0407	0.0976	0.0781	0.0220	0.0340
Dimensionality	T3	0.0027	0.0105	0.3000	0.0057	0.0020	0.0098	0.0078	0.0022	0.0034
	L1	0.2477	0.3937	0.2774	0.1570	0.0475	0.1426	0.3139	0.0285	0.3050
Linearity	L2	0.1212	0.1917	0.1370	0.0726	0.0200	0.0624	0.1534	0.0117	0.1342
	L3	0.1103	0.1828	0.1304	0.0661	0.0180	0.0593	0.1421	0.0110	0.1211
	N1	0.3208	0.3822	0.3565	0.2159	0.0447	0.2195	0.4023	0.0396	0.2789
	N2	0.3588	0.3232	0.3629	0.3285	0.2543	0.3588	0.3780	0.1615	0.2667
Neighborhood	N3	0.2067	0.1937	0.2435	0.1364	0.0325	0.1220	0.2422	0.0121	0.1173
Neighoornood	N_4	0.0913	0.1728	0.1358	0.0739	0.0122	0.0293	0.0859	0.0308	0.0833
	T1	0.0025	0.0135	0.0021	0.0082	0.0184	0.0161	0.0072	0.0294	0.0057
	LSC	0.9860	0.9659	0.9923	0.9533	0.8870	0.9476	0.9797	0.8329	0.9601
	Density	0.8658	0.8801	0.8627	0.8293	0.8170	0.8260	0.8805	0.8165	0.8530
Network	ClsCoef	0.3377	0.2232	0.3131	0.3564	0.3314	0.4158	0.3143	0.3460	0.3429
	Hubs	0.7665	0.9236	0.7608	0.7628	0.8789	0.8487	0.9300	0.8564	0.8499
	F1	0.9192	0.9776	0.9825	0.9432	0.9874	0.9922	0.9438	0.9973	0.9496
	F1v	0.2882	0.4659	0.5203	0.2083	0.2048	0.3223	0.3313	0.3274	0.3118
Overlap	F2	0.0000	0.0061	0.0004	0.0005	0.0000	0.0000	0.0065	0.0000	0.0000
	F3	0.9074	0.9476	0.9513	0.7102	0.5915	0.6585	0.9141	0.3399	0.8129
	F4	0.8295	0.8325	0.8487	0.3977	0.0671	0.1659	0.7227	0.0055	0.6990
	S1	0.2191	0.2474	0.2541	0.1453	0.0285	0.1520	0.2824	0.0319	0.2010
Smoothness	S2	0.1410	0.1178	0.1389	0.1460	0.1417	0.1556	0.1638	0.1538	0.1479
	S3	0.2067	0.1937	0.2466	0.1364	0.0325	0.1220	0.2422	0.0121	0.1122

 $Continued\ on\ next\ page$

Table C.1 – Continued from previous page

Measure	Metric	ant	apache	camel	ivy	jedit	log4j	synapse	xalan	xerces
	S4	0.0847	0.1273	0.1608	0.0716	0.0215	0.0285	0.1300	0.0209	0.1056

C.2. Complexity Metrics Hadoop datasets

Table C.2: Complexity Metrics Analysis on Hadoop datasets

Measure	Metric	Hadoop 0.1	H 0.2	H 0.3	H 0.4	H 0.5	H 0.6	H 0.7	H 0.8
Balance	C1	0.9381	0.7600	0.8132	0.7395	0.6589	0.5642	0.7056	0.3534
Balance	C2	0.1559	0.4777	0.3970	0.5062	0.6056	0.7015	0.5501	0.8579
	C2	0.2868	0.0520	0.3171	0.1899	0.1601	0.1705	0.1997	0.1241
Correlation	C3	0.7741	0.6006	0.6330	0.5956	0.5589	0.5397	0.5737	0.4917
	C4	1.0000	1.0000	0.9810	1.0000	1.0000	0.7692	0.9720	0.2125
Dim on sion alita	<i>T2</i>	0.0496	0.0366	0.0332	0.0348	0.0322	0.0299	0.0280	0.0292
Dimensionality	T3	0.0142	0.0052	0.0095	0.0050	0.0046	0.0042	0.0040	0.0042
	L1	0.3770	0.3327	0.2658	0.2950	0.2620	0.1996	0.2654	0.1134
Linearity	L2	0.1870	0.1664	0.1305	0.1473	0.1310	0.0981	0.1327	0.0550
	L3	0.1832	0.1644	0.1055	0.1408	0.1274	0.0875	0.1254	0.0489
	N1	0.4965	0.4712	0.4028	0.4378	0.4009	0.3333	0.3840	0.1708
	N2	0.3474	0.4611	0.3151	0.4207	0.3960	0.3457	0.3682	0.3151
Neighborhood	N3	0.2553	0.3037	0.2417	0.3234	0.2857	0.1838	0.2200	0.1208
Neighoornood	N4	0.2411	0.2408	0.1374	0.1990	0.1429	0.1282	0.0960	0.0417
	T1	0.0127	0.0079	0.0118	0.0101	0.0096	0.0100	0.0087	0.0143
	LSC	0.9755	0.9838	0.9686	0.9708	0.9725	0.9686	0.9786	0.9428
	Density	0.8678	0.8610	0.8478	0.8433	0.8430	0.8232	0.8426	0.8030
Network	ClsCoef	0.3965	0.4411	0.4281	0.4453	0.4398	0.4383	0.4435	0.4465
	Hubs	0.8595	0.9252	0.9305	0.9121	0.9152	0.8929	0.9074	0.8912
	F1	0.9129	0.9958	0.8365	0.9641	0.9643	0.9519	0.9370	0.9711
	F1v	0.5101	0.8483	0.3019	0.5797	0.6427	0.4057	0.4816	0.3269
Overlap	F2	0.1818	0.0508	0.0135	0.1107	0.3023	0.0257	0.0552	0.0329
	F3	0.8865	0.9791	0.9479	0.9900	0.9032	0.9530	0.9600	0.8750
	F4	0.6879	0.9215	0.8294	0.9453	0.8479	0.8846	0.9000	0.6875
	S1	0.3643	0.3421	0.2952	0.3100	0.2778	0.2446	0.2731	0.1255
Smoothness	S2	0.1465	0.0908	0.1134	0.1075	0.1108	0.1122	0.1043	0.0961
Smoothness	S3	0.2411	0.3246	0.2417	0.3284	0.2857	0.1709	0.2080	0.1208
	S4	0.2003	0.1863	0.1552	0.1516	0.1646	0.1175	0.1631	0.0625

Appendix D

Figures

D.1. Complexity Metrics

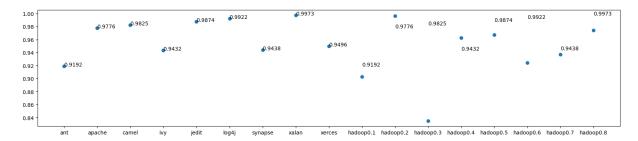


Figure D.1: Overlap F1

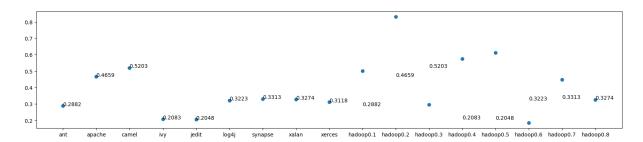


Figure D.2: Overlap F1v

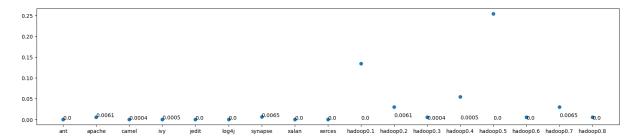


Figure D.3: Overlap F2

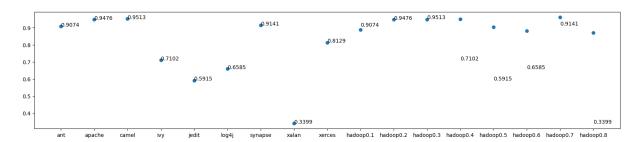


Figure D.4: Overlap F3

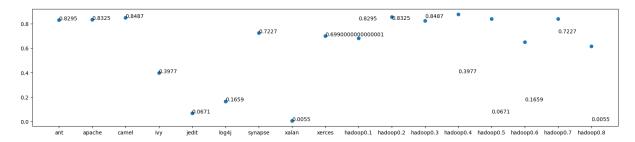


Figure D.5: Overlap F4

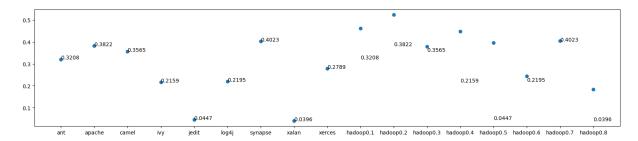


Figure D.6: Neighborhood N1

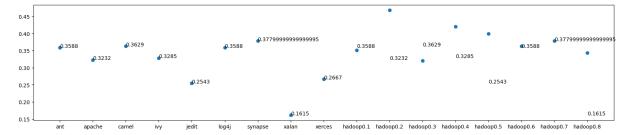


Figure D.7: Neighborhood N2 $\,$

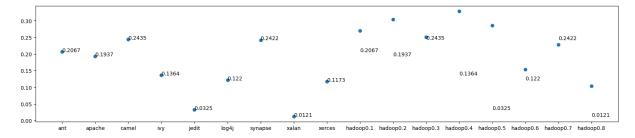


Figure D.8: Neighborhood N3

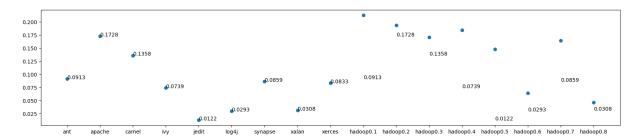


Figure D.9: Neighborhood N4

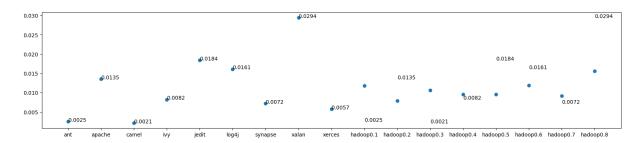


Figure D.10: Neighborhood T1

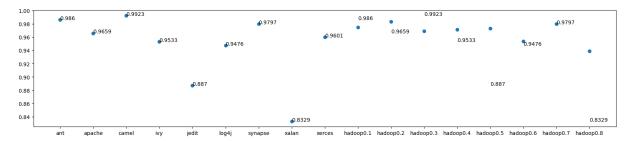


Figure D.11: Neighborhood LSC

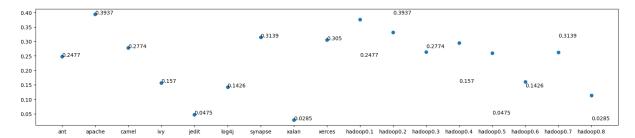


Figure D.12: Linearity L1

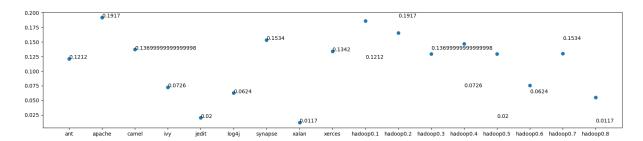


Figure D.13: Linearity L2 $\,$

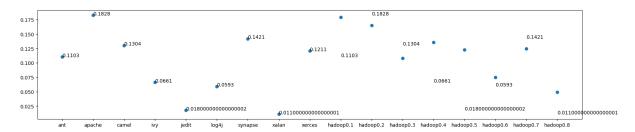


Figure D.14: Linearity L3

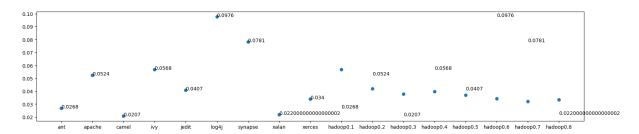


Figure D.15: Dimensionality T2

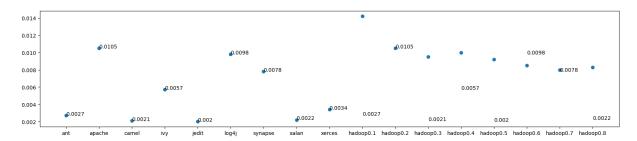


Figure D.16: Dimensionality T3

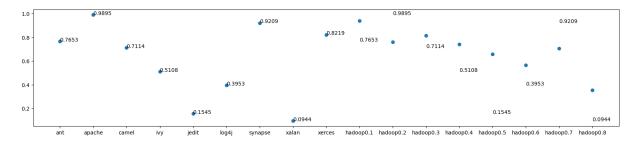


Figure D.17: Balance C1

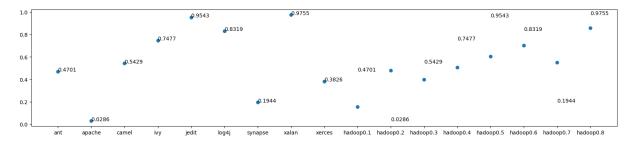


Figure D.18: Balance C2

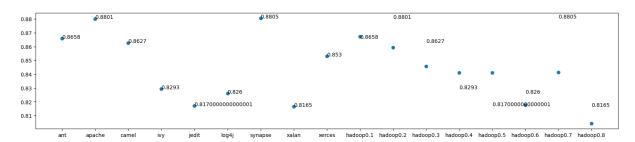


Figure D.19: Network Density

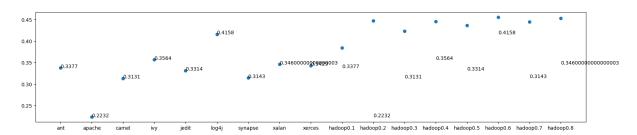


Figure D.20: Network ClsCoef

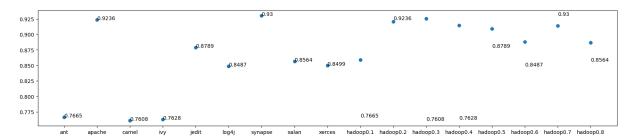


Figure D.21: Network Hubs

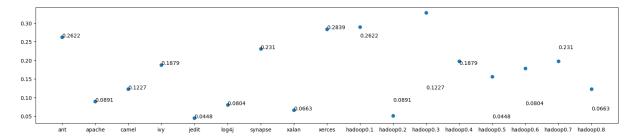


Figure D.22: Correlation C2

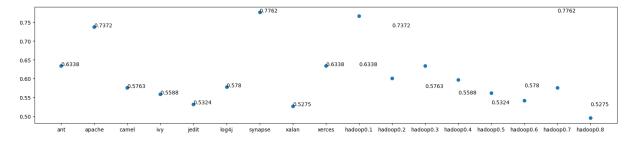


Figure D.23: Correlation C3

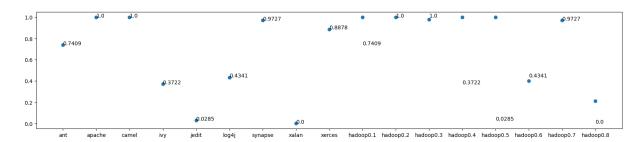


Figure D.24: Correlation C4

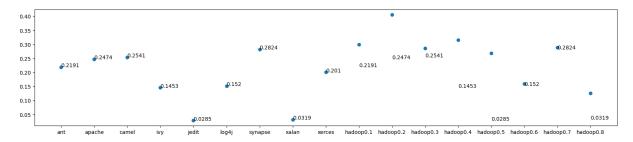


Figure D.25: Smoothness S1

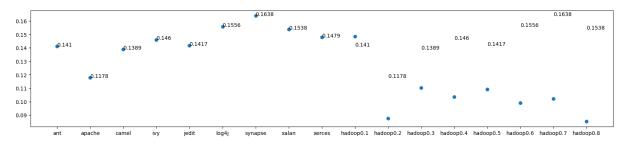


Figure D.26: Smoothness S2

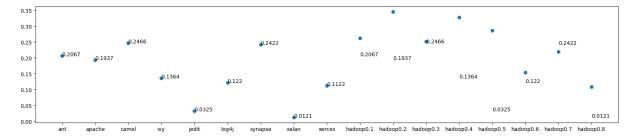


Figure D.27: Smoothness S3

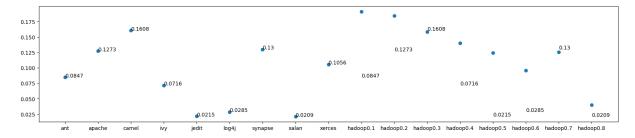


Figure D.28: Smoothness S4

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