



Problem Solving

Math for CP

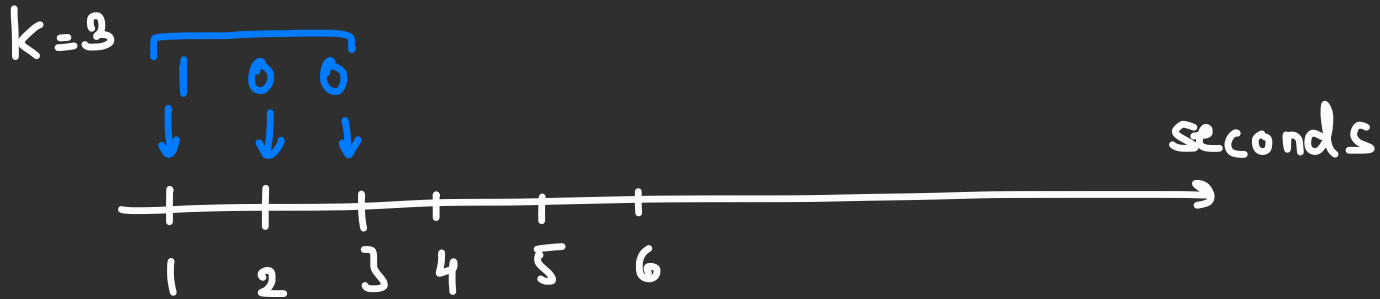
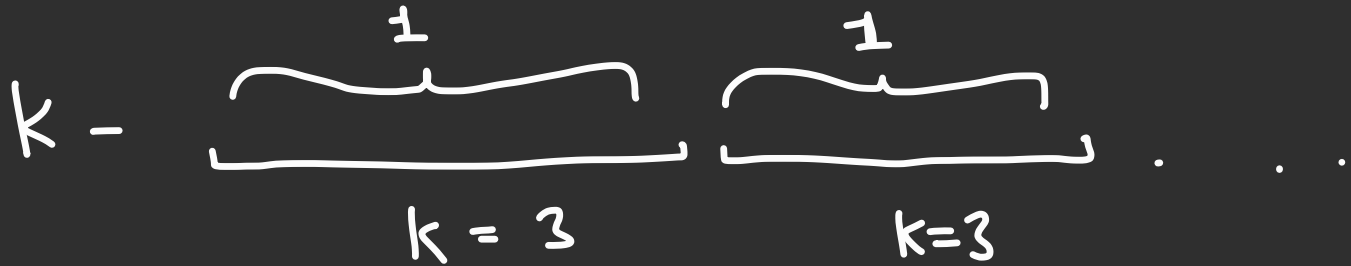
- Viraj Chandra

Problem 1 - Upload More RAM

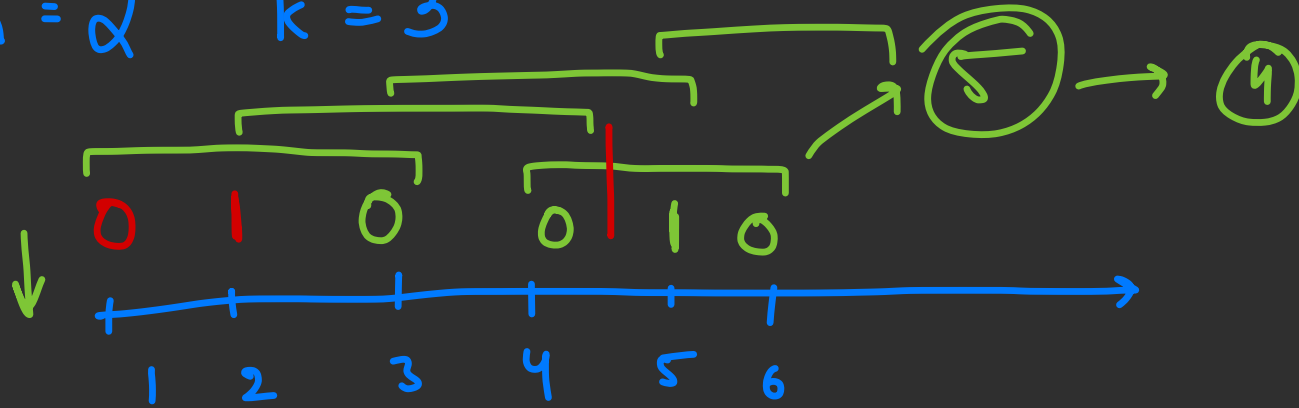


$$n = 8$$

1 sec - 0, 1 RAM



$n = 2$ $k = 3$

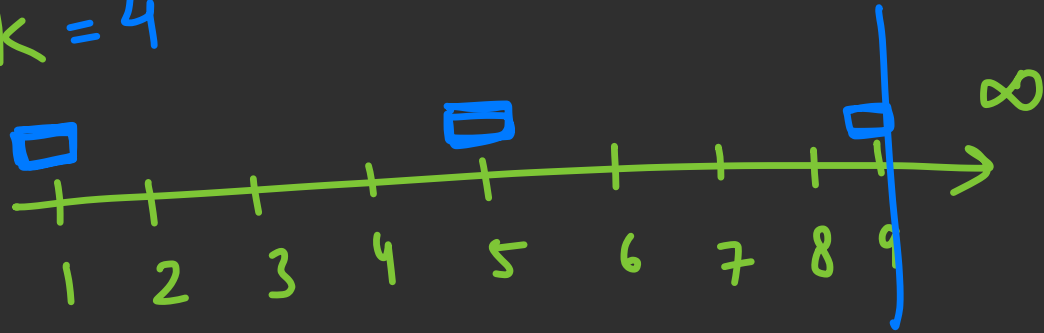


$O(N^2) \rightarrow O(N) \rightarrow O(1)$

↑

$$N=3 \quad k=4$$

\Rightarrow ✓



$$N \approx 10^9$$

$$O(\log N)$$

$$O(1)$$

$$AP = 1 \quad k+1 \quad 2k+1 \quad 3k+1 \quad \dots$$

N

$$\Rightarrow T_n = a + (N-1)d$$

$$= 1 + (N-1)k \quad \checkmark \quad O(1)$$

Problem 2 - Maximum Multiple Sum



N $N = 17$

$$2 \leq X \leq N$$

$$X=2 \dots \underline{X=4} \quad X=5 \quad X=6 \quad X=7 \dots X=N$$

$$\underline{4 + 8 + 12 + 16} = \text{Sum}$$

$$O(N^2)$$

↓

$$X$$

$$\rightarrow O(1)$$

for ($2^i \dots n$)

{ $sum = 0$
 for ($i \dots i + 1$)
 { $m \leq n$
 $sum += m$
 }
 $sum \Rightarrow max$

$$2 \leq x \leq N$$

$$N = 7$$

$$N = 13$$

$$x = 2 \rightarrow 2 + 4 + 6 = 12$$

$$x = 3 \rightarrow 3 + 6 = 9$$

$$x = 4 \rightarrow 4$$

$$x = 5 \rightarrow 5$$

$$x = 6 \rightarrow 6$$

$$7$$

$$kx \leq n$$

$$k \leq \frac{n}{x}$$

$$2$$

$$AP \text{ sum} = \frac{n}{x} \cdot 2 \left(\overset{\downarrow}{x} + \left(\frac{n}{x} - 1 \right) d \right)$$

Hence
Proved

k = terms

$$\Rightarrow n + \frac{n^2}{x^2} (x-1) d$$

Problem 3 - Large Addition



1 3 3 7

5, 6, 7, 8, 9 ↓

$5 \leq d \leq 9$

large {

$a = \dots 9 \overset{!}{9} \overset{!}{9} / . \overset{!}{5} \overset{!}{5} \overset{!}{5}$

$b = \dots 9 \overset{!}{9} \overset{!}{9} \dots \overset{!}{5} \overset{!}{5} \overset{!}{5}$

1 9 9 8 1 1 1 0

119

"No"

$X = \text{---} X \overset{!}{1} \rightarrow \text{"No"}$

$X = \text{---} > 8 \rightarrow \text{"No"}$

108
"No"



$X = \text{not last not first} \rightarrow 1 \leq d \leq 9$

$a = \underline{59}$ ✓✓

$b = \underline{59}$

08



Problem Links -

1. <https://codeforces.com/problemset/problem/1987/A>
2. <https://codeforces.com/problemset/problem/1984/B>
3. <https://codeforces.com/problemset/problem/1985/B>
4. <https://codeforces.com/problemset/problem/1987/B>