



Visual Computing Digital Images

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CHAPTER 11

Image Editing - Dot Operators

Image Editing - Dot Operators

Histograms Point operations

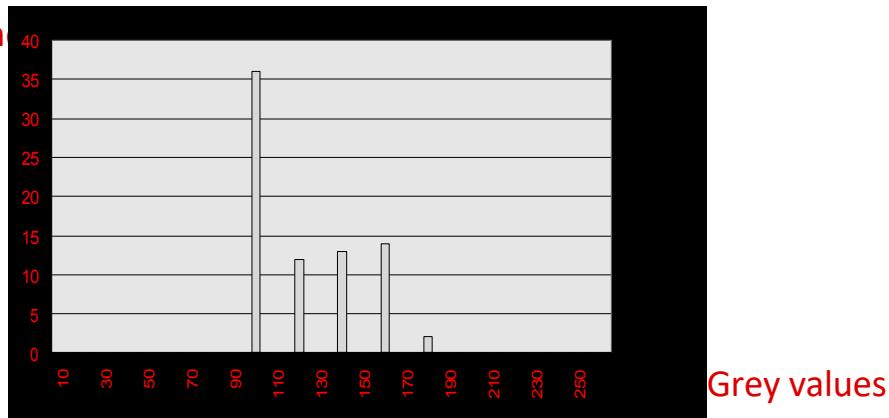
- Linear change of the grey values:
 - Changing the picture brightness
 - Invert the image
 - Changing the contrast
 - Binarisation through thresholding
- Non-linear change in grey values:
 - Gamma correction
- Colour Transformations (Color Transformation)

11. digital images

Image Editing - Dot Operators

Histograms: A graphical representation of the frequency distribution of grey values in images.

Frequency of the
values



Grey values

	0	1	2	3	4	5	6	7	8	9	10
0	100	100	100	120	160	160	120	100	100	100	137
1	100	100	100	120	160	160	120	100	100	100	137
2	100	100	100	120	160	160	120	100	100	100	137
3	100	100	100	120	160	160	140	140	140	140	178
4	100	100	100	120	160	160	140	140	140	140	177
5	100	100	100	120	160	160	120	100	100	100	136
6	100	100	100	120	160	160	120	100	100	100	136

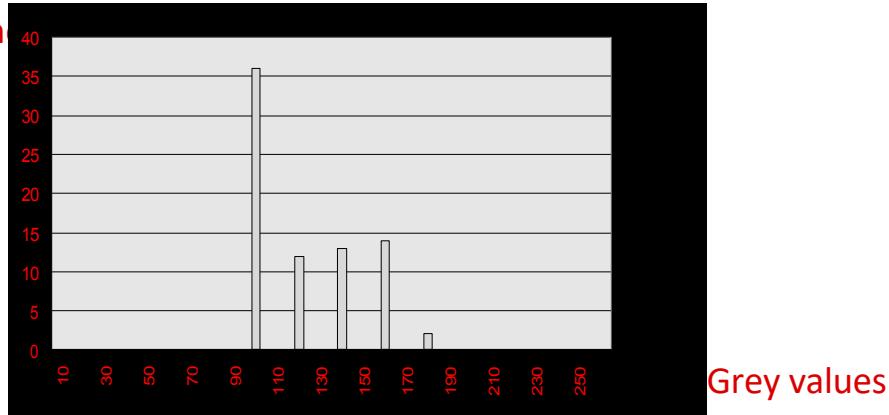
Underlying grey tone image in the form of an image matrix in which the individual grey values are represented by numerical values.

11. digital images

Image Editing - Dot Operators

Histograms: A graphical representation of the frequency distribution of grey values in images.

Frequency of the
values



Absolute and relative frequencies:

A distinction is made between the absolute frequency distribution, as shown in the figure on the right, and the relative frequency distribution. In the relative distribution, frequency values are normalised, i.e. transformed into an interval between 0 and 1.

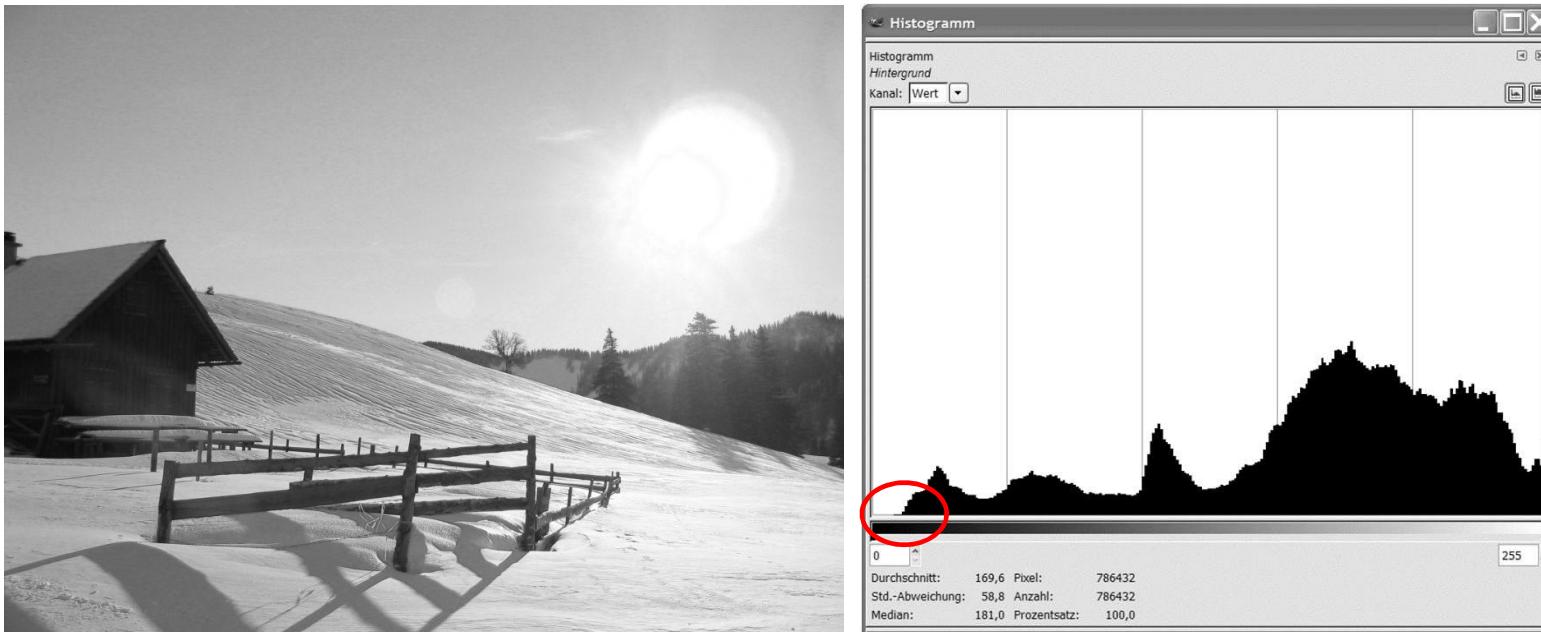
	0	1	2	3	4	5	6	7	8	9	10
0	100	100	100	120	160	160	120	100	100	100	137
1	100	100	100	120	160	160	120	100	100	100	137
2	100	100	100	120	160	160	120	100	100	100	137
3	100	100	100	120	160	160	140	140	140	140	178
4	100	100	100	120	160	160	140	140	140	140	177
5	100	100	100	120	160	160	120	100	100	100	136
6	100	100	100	120	160	160	120	100	100	100	136

Underlying grey tone image in the form of an image matrix in which the individual grey values are represented by numerical values.

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Image Editing - Dot Operators

Histograms: A measure used to assess image quality.



The histogram of the brightness channel of an image can be used to decide whether an image is overexposed or underexposed. The picture is overexposed because the dark grey tones are missing (see red mark in the histogram).

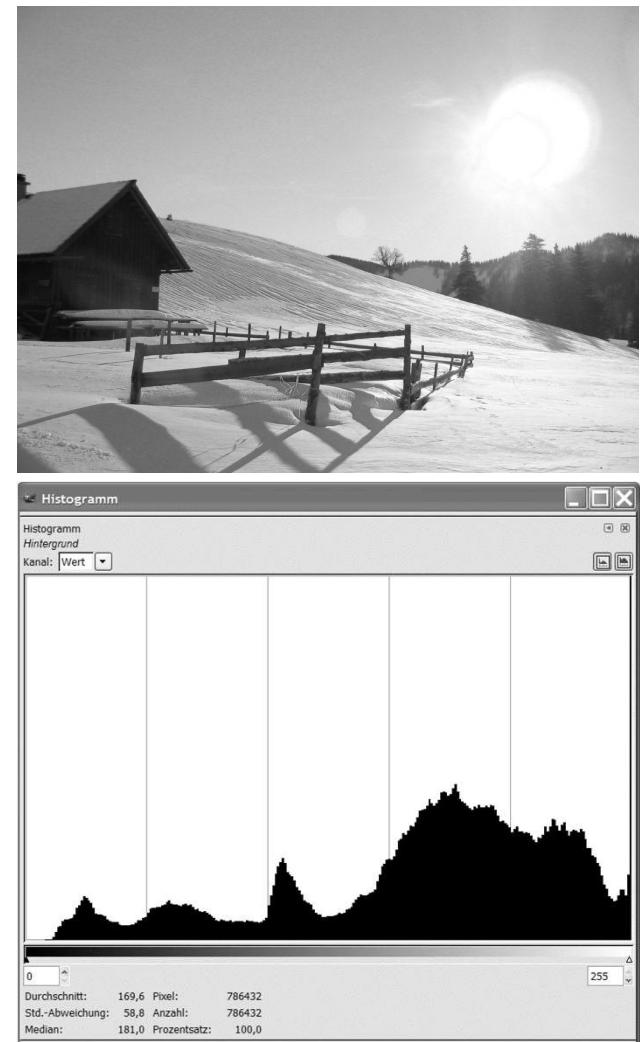
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Image Editing - Dot Operators

Histograms: A measure used to assess image quality.

Exposure error*)

One end of the grey value scale remains unused while at the other end of the scale there are clusters. On the left of the histogram are the dark grey values (grey value 0 = black), on the right the light grey values (maximum grey value = white).



*) Definitions from: W. Burger, M. J. Burge, "Digital Image Processing", Springer Verlag

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Histograms: A measure used to assess image quality.

Contrasts*)

Contrast is the range between the minimum and maximum grey values in the image. An image with a full contrast range therefore uses the entire range of intensity values (= grey values). To evaluate the contrast, one can form the difference between the maximum and minimum intensity value.

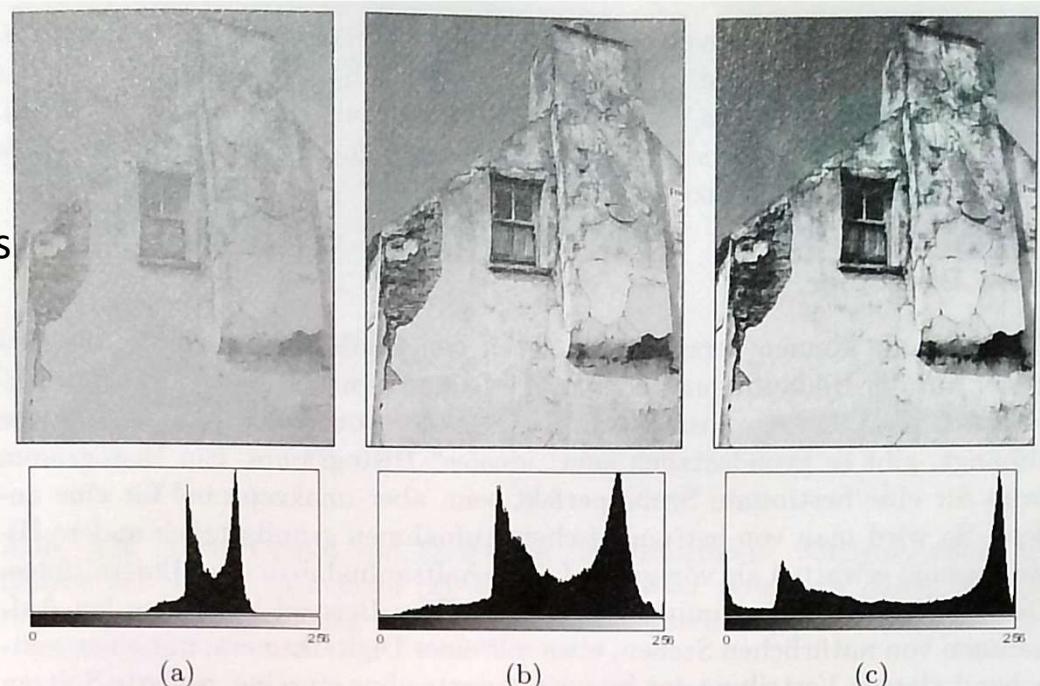


Abb. 4.7. Unterschiedlicher Kontrast und Auswirkungen im Histogramm: niedriger Kontrast (a), normaler Kontrast (b), hoher Kontrast (c).

*) Definitions and images from: W. Burger, M. J. Burge, "Digital Image Processing", Springer Verlag

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Image Editing - Dot Operators

Histograms: A measure used to assess image quality.

Dynamics*)

Dynamic range is the number of different grey values (intensity values) used in an image.

Ideally, every grey value is present in the image.

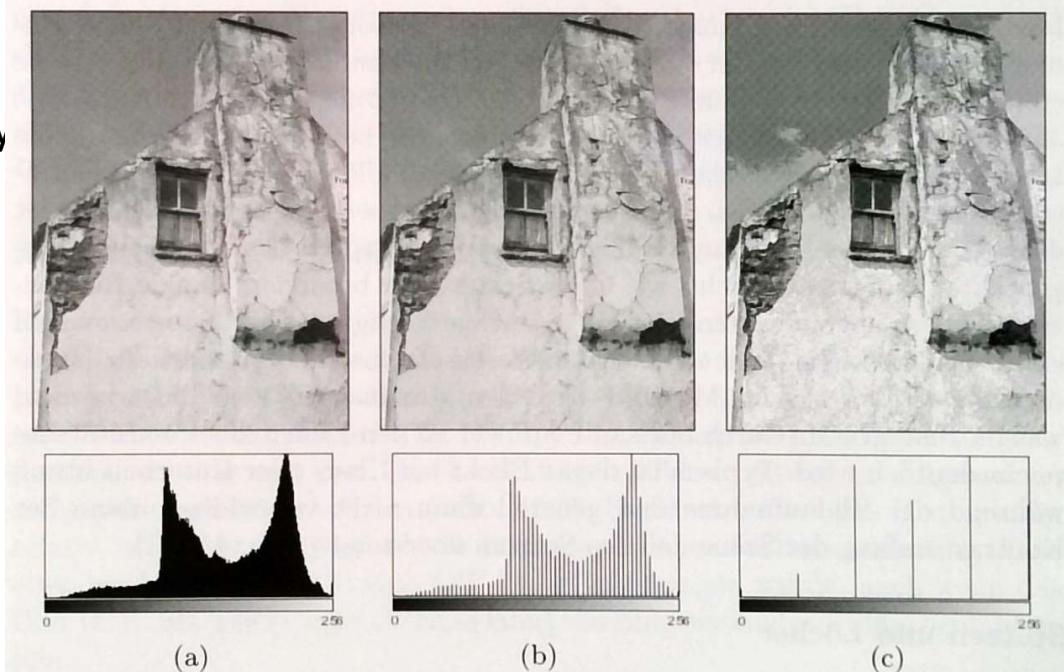


Abb. 4.8. Unterschiedliche Dynamik und Auswirkungen im Histogramm. Hohe Dynamik (a), niedrige Dynamik mit 64 Intensitätswerten (b), extrem niedrige Dynamik mit nur 6 Intensitätswerten (c).

*) Definitions and images from: W. Burger, M. J. Burge, "Digital Image Processing", Springer Verlag

Image Editing - Dot Operators

Histograms: Also a measure for assessing image content?

What does the relative frequency distribution look like in the histograms of the three images?

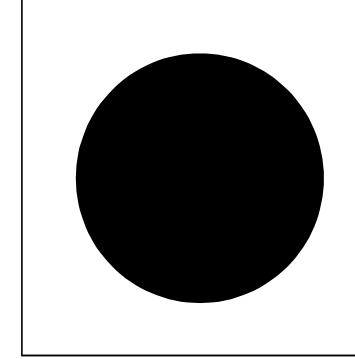
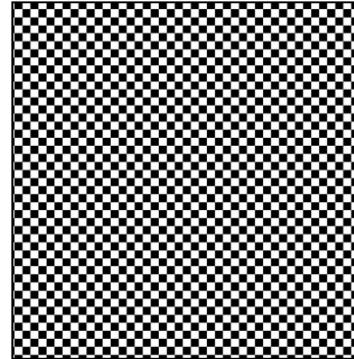
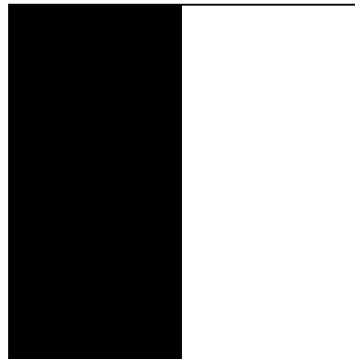
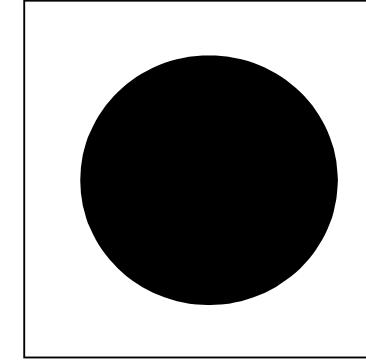
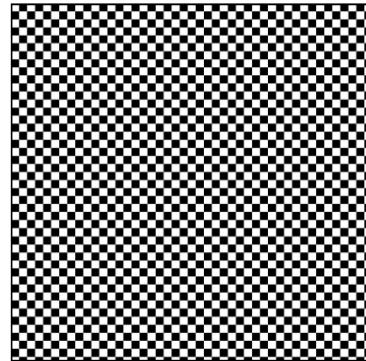
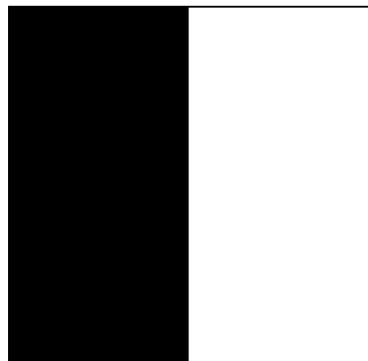


Image Editing - Dot Operators

Histograms: Also a measure for assessing image content?

What does the relative frequency distribution look like in the histograms of the three images?



The histograms of all three images look the same. There are as many black pixels as white pixels.

Image Editing - Dot Operators

Histograms: Not a measure for assessing image content, but image manipulations can be recognised in them.

The effects of JPEG compression can be seen in the histogram.



An image that consists only of black and white pixels.



JPEG compression has added more grey values.

11. digital images

Image Editing - Dot Operators

Histograms: Not a measure for assessing image content, but image manipulations can be recognised in them.

Reducing the contrast range can cause histogram peaks.



Image with full contrast
and dynamic range

Transformation of
the
Grey value range

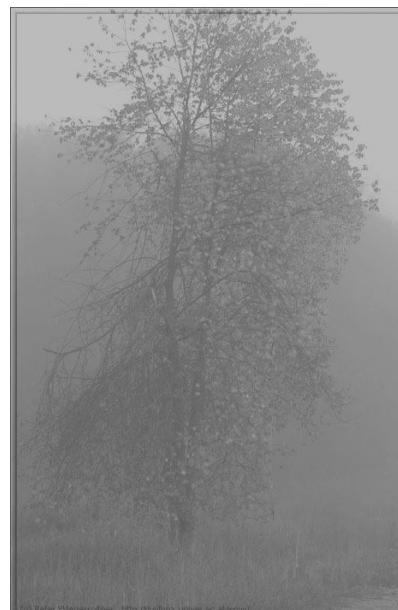
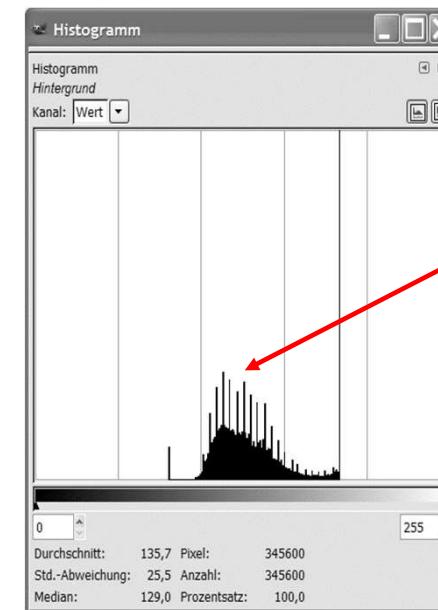


Image with limited
Contrast and dynamic range



Histogram of the image with restricted
Contrast and dynamic range

Histogram
peaks

Image Editing - Dot Operators

Histograms Point operations

- Linear change of the grey values:
 - Changing the picture brightness
 - Invert the image
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- Non-linear change in grey values:
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- Colour Transformations (Color Transformation)

Image Editing - Dot Operators

Point operation:

- denote operations on images that are calculated pixel by pixel
- the grey values of the neighbouring pixels are not used by the operators
- the size and geometry of the image is not changed

Possible point operations are:

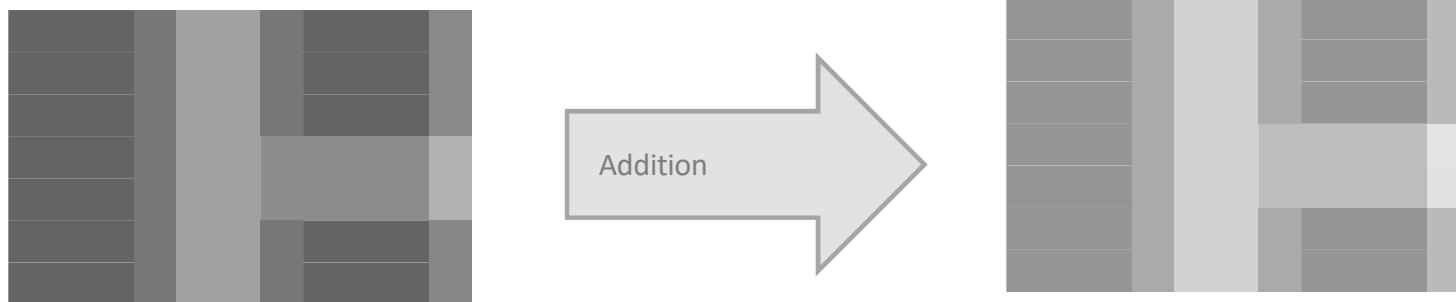
- Changing the picture brightness
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- Changing the contrast
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- Gamma correction
- Colour transformations

11. digital images

Image Editing - Dot Operators

Point operations: Changing the image brightness

Lighten the image by adding a value > 0



$$g(x, y) \leq 205 \text{ then } g'(x, y) = g(x, y) + 50$$

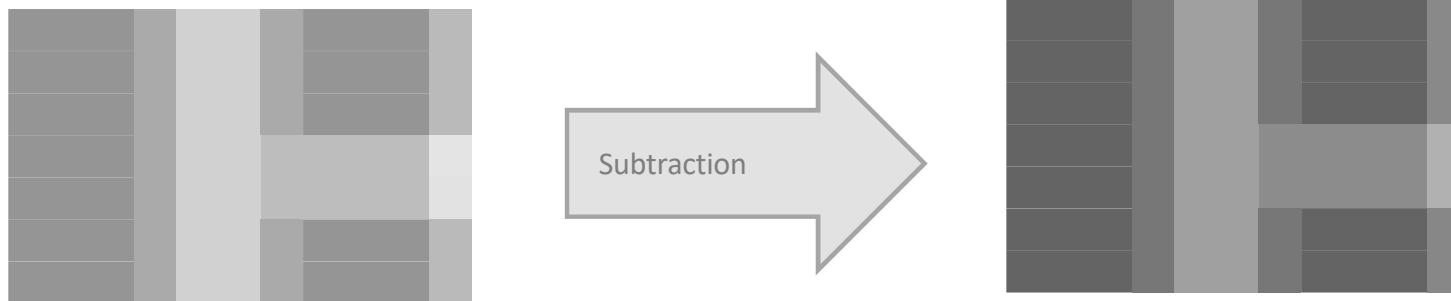
$$g(x, y) > 205 \text{ then } g'(x, y) = 255$$

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Image Editing - Dot Operators

Point operations: Changing the image brightness

Darkening the image by subtracting a value > 0



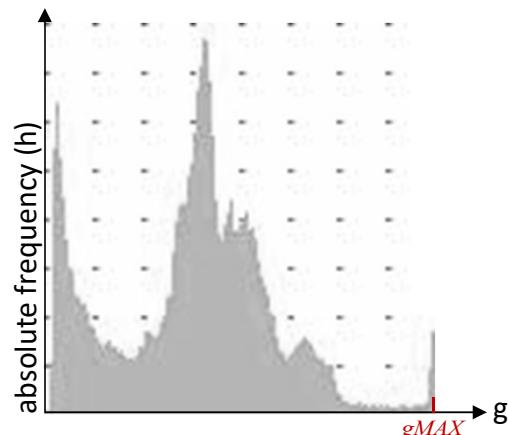
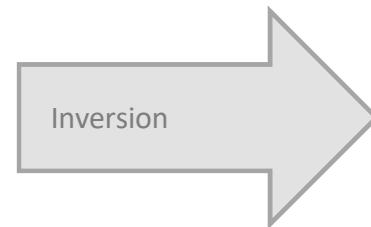
$$g(x, y) \geq 50 \quad \text{then } g'(x, y) = g(x, y) - 50$$

$$g(x, y) < 50 \quad \text{then } g'(x, y) = 0$$

11. digital images

Image Editing - Dot Operators

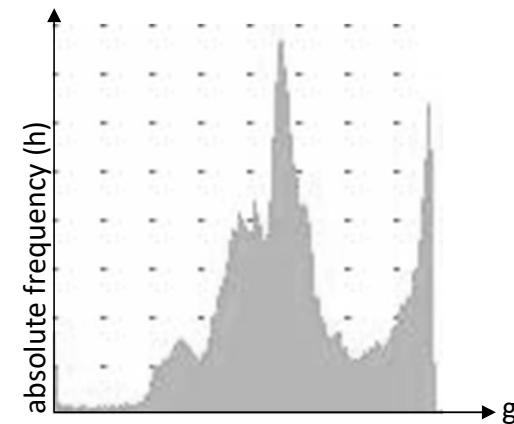
Point operations: Invert the image



$$g'(x, y) = g_{MAX} - g(x, y) \text{ if}$$

follows:

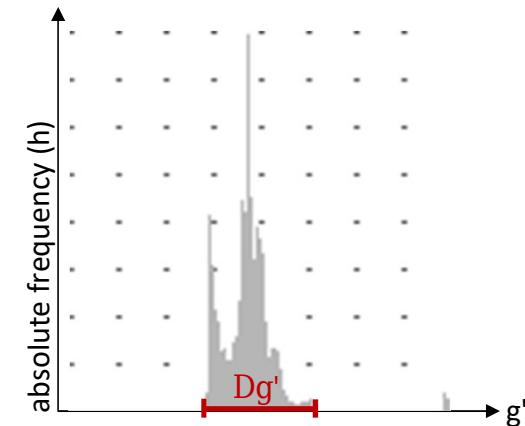
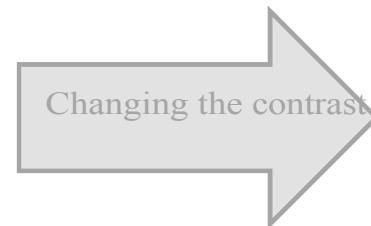
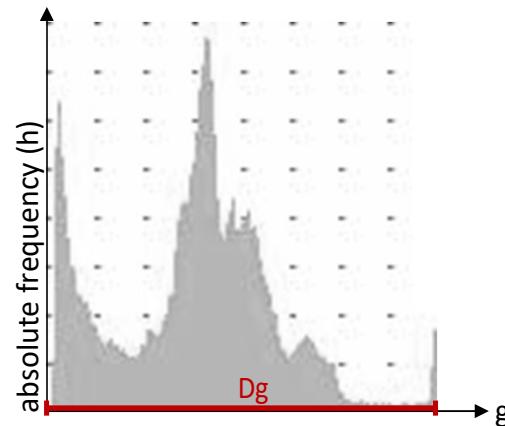
$$h(g'_i) = h(g_{MAX-i})$$



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Image Editing - Dot Operators

Point operations: Changing the contrast



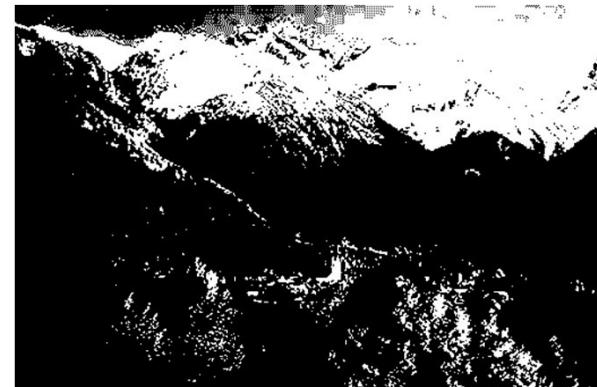
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Image Editing - Dot Operators

Point operations: Binarisation through thresholding



Binarisation with
threshold gS= 127



$$g'(x, y) = 0 \text{ if } g(x, y) < g_s \\ g'(x, y) = 1 \text{ or } 255 \text{ if } g(x, y) \geq g_s$$

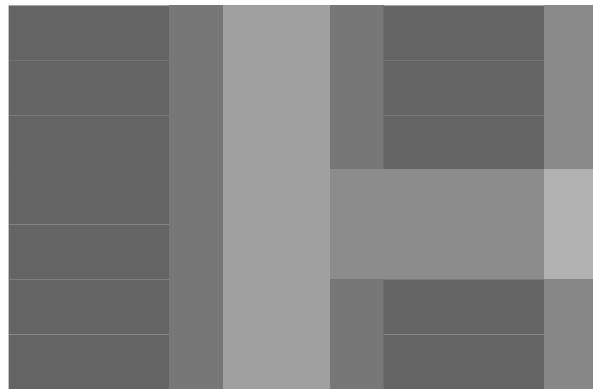
Binarisation with
threshold gS= 180



11. digital images

Image Editing - Dot Operators

Point operations: Binarisation through thresholding



Binarisation with
threshold 112



$$g'(x, y) = 0 \text{ if } g(x, y) < g_s \\ g'(x, y) = 1 \text{ or } 255 \text{ if } g(x, y) \geq g_s$$

Binarisation with
threshold 130



Image Editing - Dot Operators

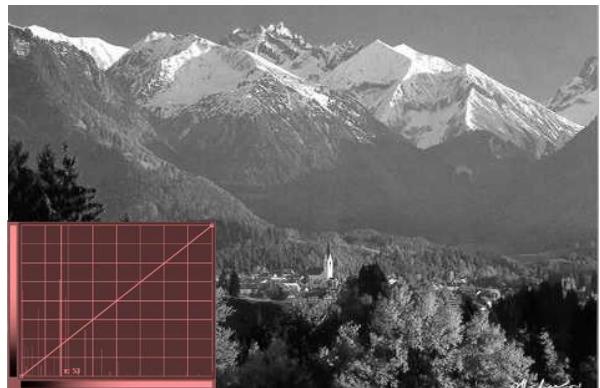
Histograms Point operations

- Linear change of the grey values:
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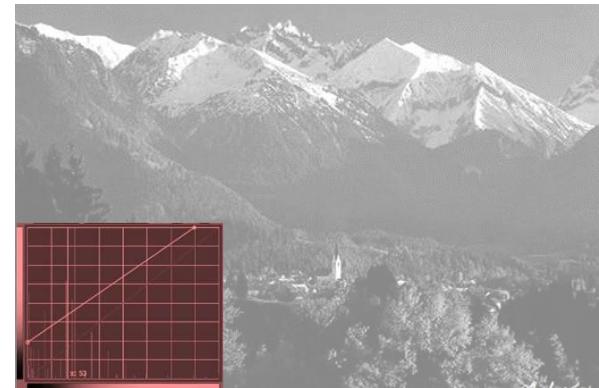
11. digital images

Image Editing - Dot Operators

Point operations: Non-linear change of grey values



Linear change of the
grey values



Non-linear change of the
grey values

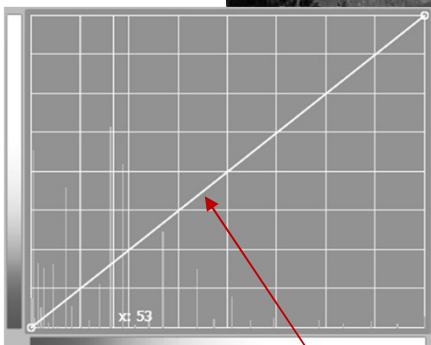


11. digital images

Image Editing - Dot Operators

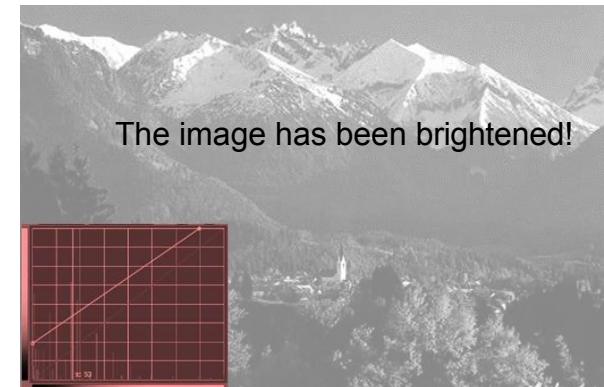
Point operations: Non-linear change of grey values

g' = grey values of
the Output image



Function that maps the input image to the output image.

Linear change of the grey values



The image has been brightened!

Non-linear change of the grey values



The image has been brightened
and the contrast improved!

Image Editing - Dot Operators

Histograms

Point operations **shown in the gg' diagram**

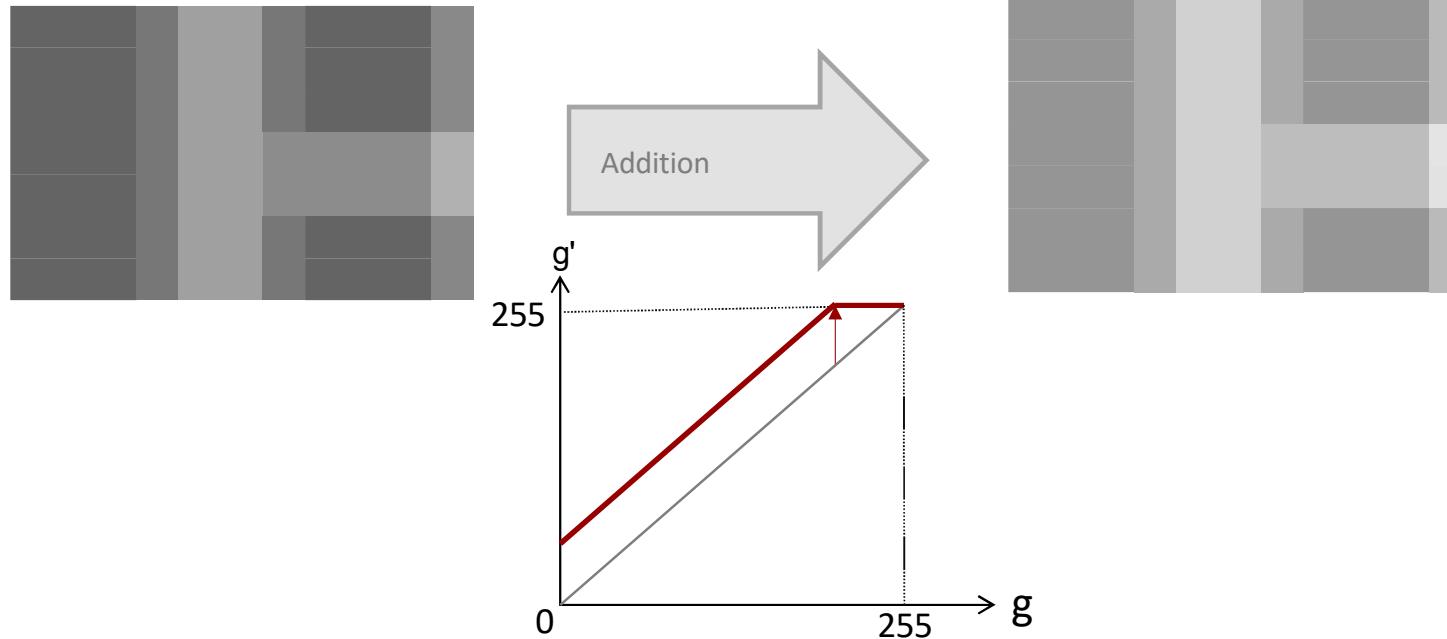
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11. digital images

Image Editing - Dot Operators

Point operations: Changing the image brightness

Lighten the image by adding a value > 0



Note: The image becomes brighter when the angle bisector is the bisector of the angle.

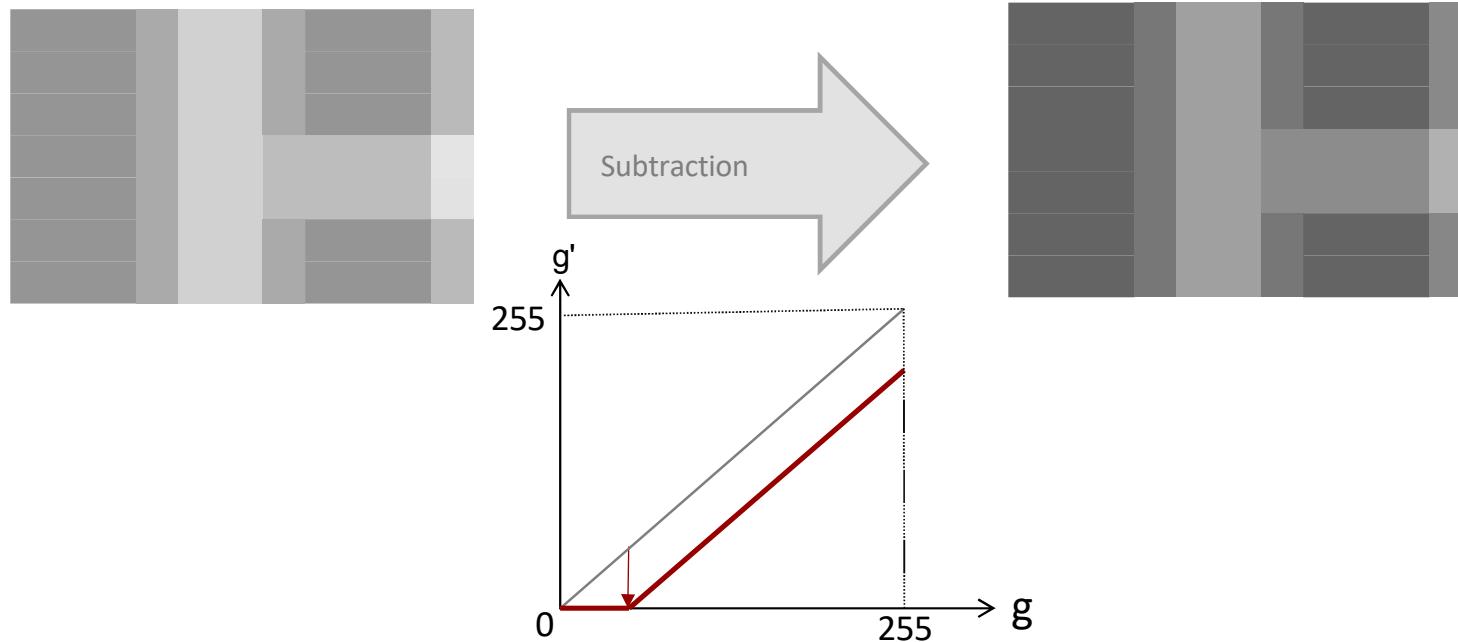
11. digital images

Image Editing - Dot Operators

Point operations: Changing the image brightness

Darkening the image by subtracting a value > 0

Note: The picture becomes darker when the mapping function runs below the angle bisector.

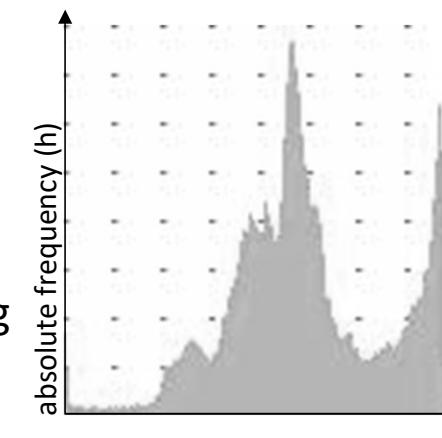
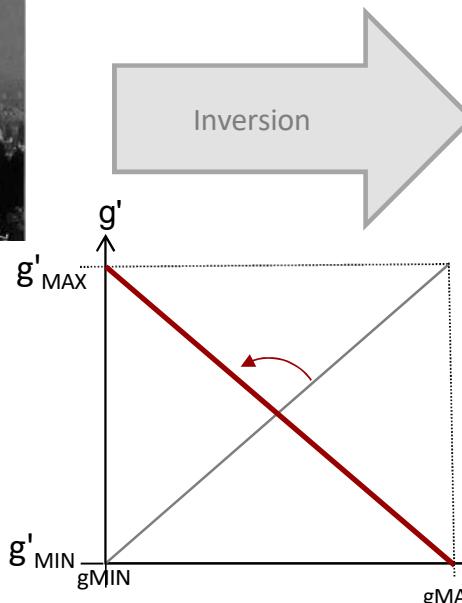
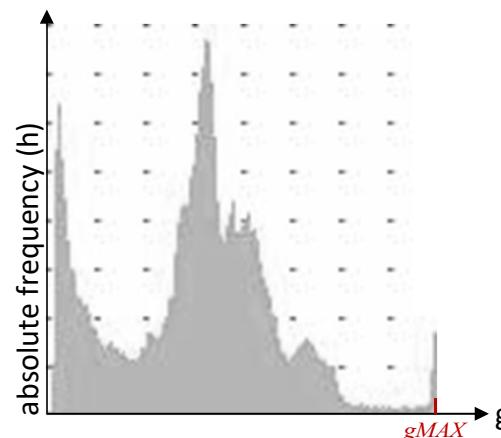


11. digital images

Image Editing - Dot Operators

Point operations: Invert the image

Note: The image is inverted when the slope of the mapping function is negative.



In this case: $g_{MAX} = g'_{MAX}$
 $g_{MIN} = g'_{MIN}$

11. digital images

Image Editing - Dot Operators

Point operations: Changing the contrast

Note: The image becomes less contrasty,

mapping the full range of the

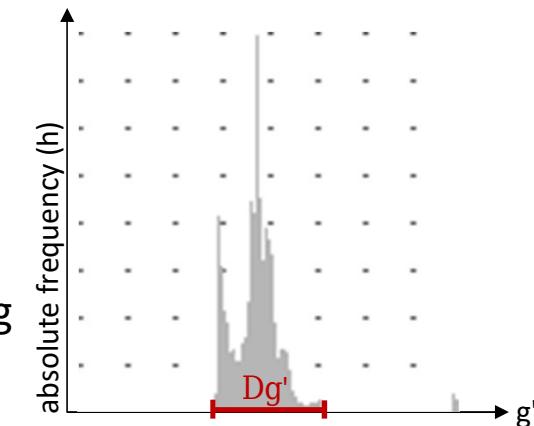
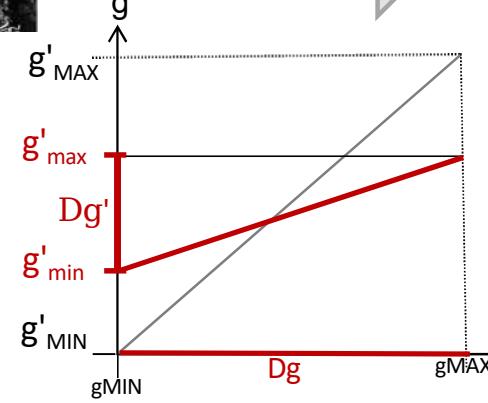
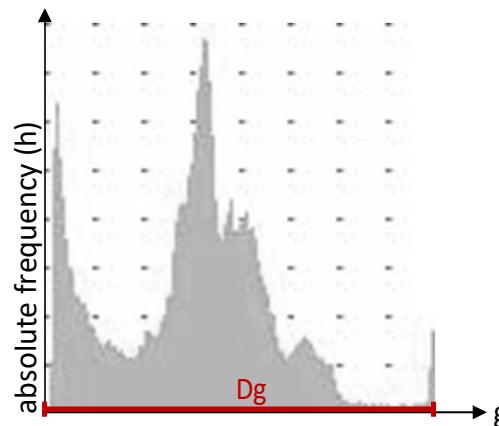


high-contrast

Contrast reduction



low contrast



11. digital images

Image Editing - Dot Operators

Point operations: Changing the contrast

Note: The image becomes richer in contrast,
while the shape of the

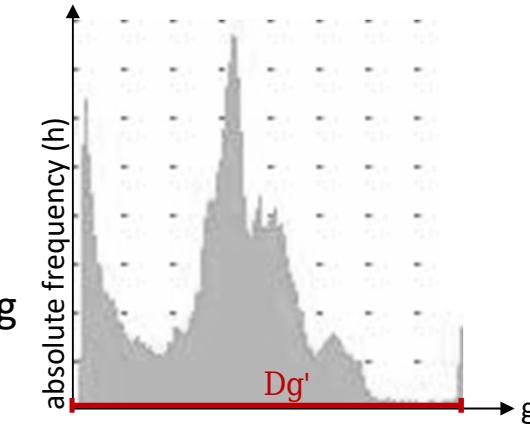
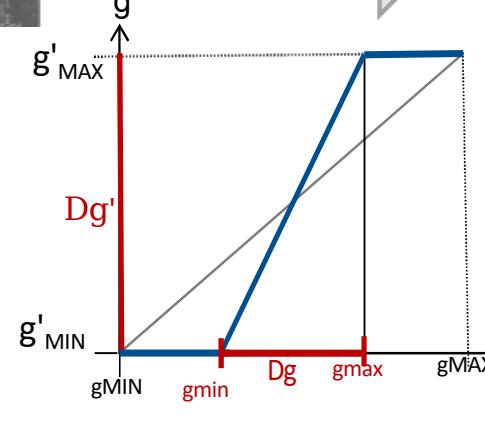
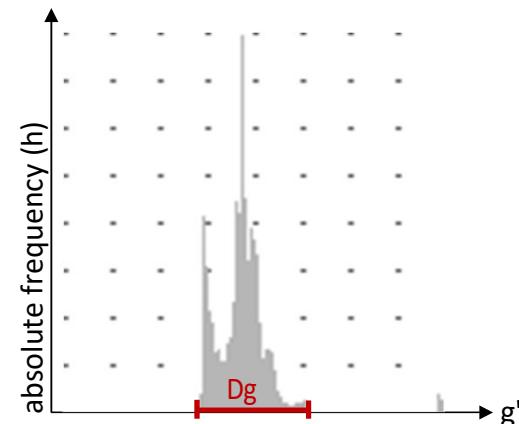


low contrast

Improving the contrast



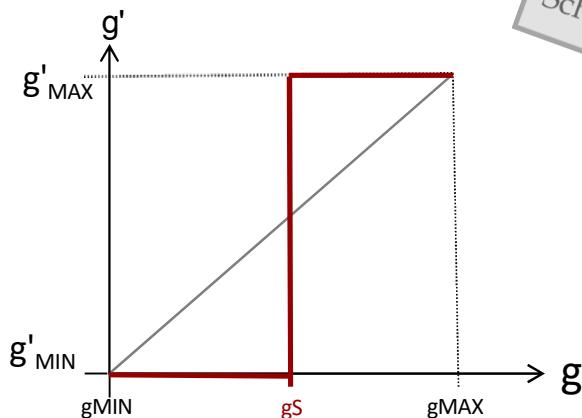
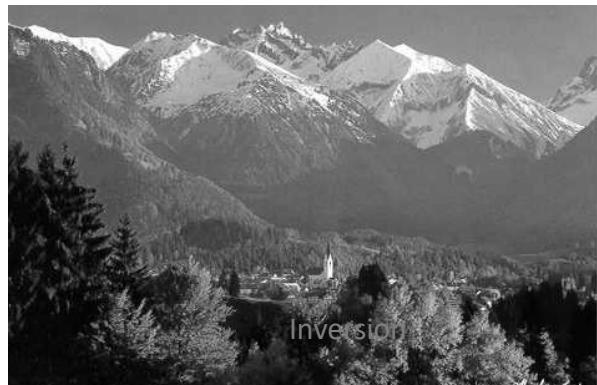
high-contrast



11. digital images

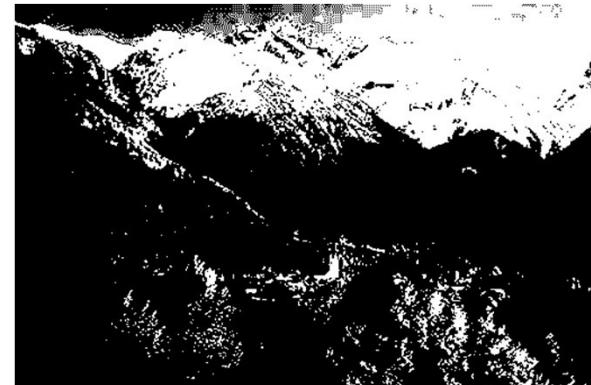
Image Editing - Dot Operators

Point operations: Binarisation through thresholding



Binarisation with threshold
 $g_S = 127$

Binarisierung mit
Schwellwert $g_S = 180$

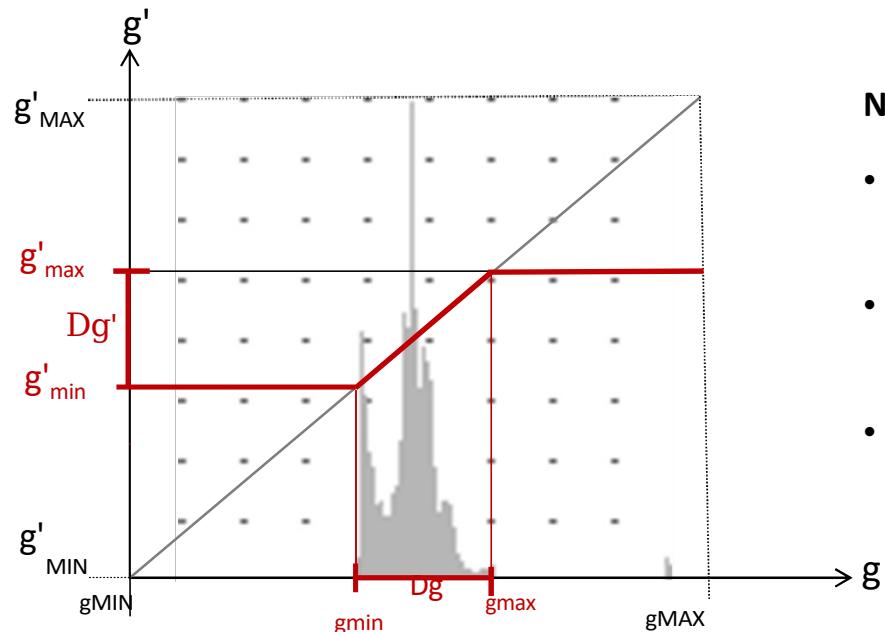


Note: Binarisation can be used to split an image into the foreground (white by default) and the background (black).

11. digital images

Image Editing - Dot Operators

gg' diagram: An effective form of representation for the point operators is the gg' diagram, which maps the grey values of the input image to the grey values of the output image.
Often the gg'-graph is linked to the histogram of the input image.



Notice:

- g_{min} and g_{max} are the minimum and maximum grey values present in the input image.
- g_{MIN} and g_{MAX} are the minimum and maximum grey values available to display the input image.
- g'_{min} and g'_{max} as well as g'_{MIN} and g'_{MAX} characterise the output image equivalently .

11. digital images

Image Editing - Dot Operators

An example from practice:

First the motivation: What can you do with satellite images?



Link:

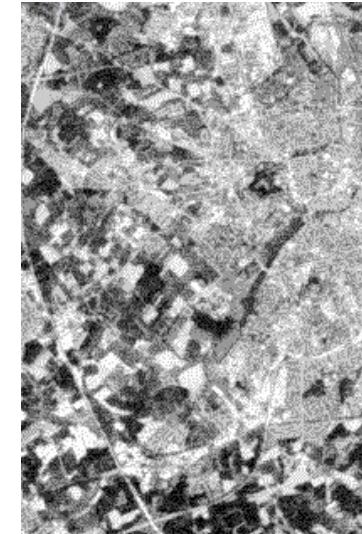
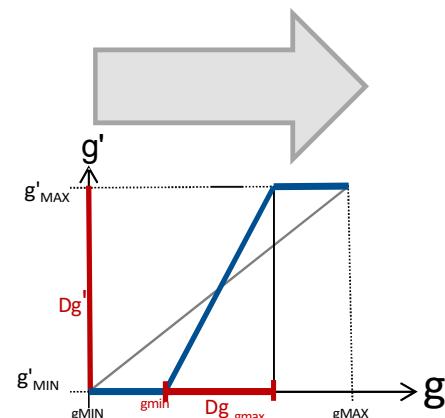
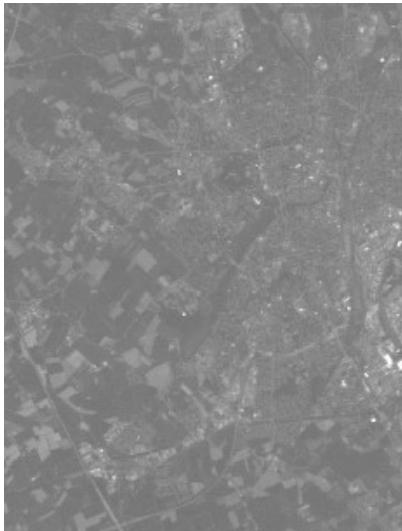
<https://www.youtube.com/watch?v=lrZ-vWzv0as>

11. digital images

Image Editing - Dot Operators

An example from practice:

A first step is often to prepare the images in such a way that the maximum available colour space is used, if possible without distorting the image data. The data is distorted when image information (grey values) is added or deleted.



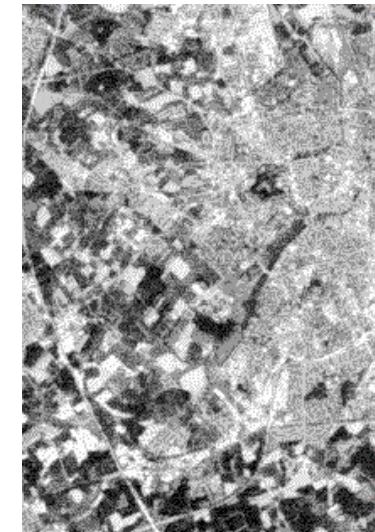
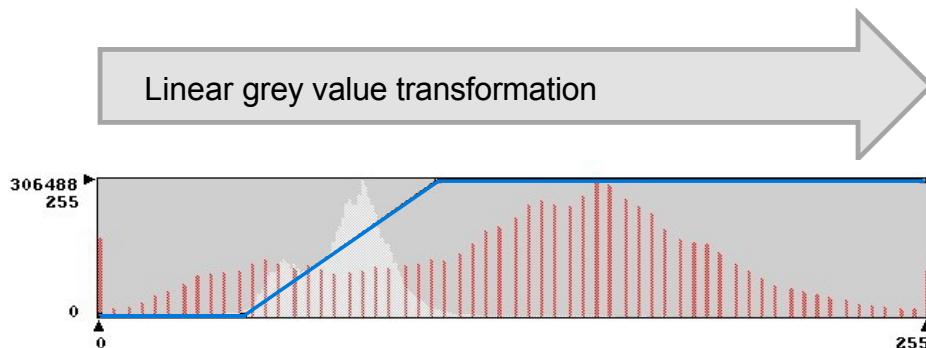
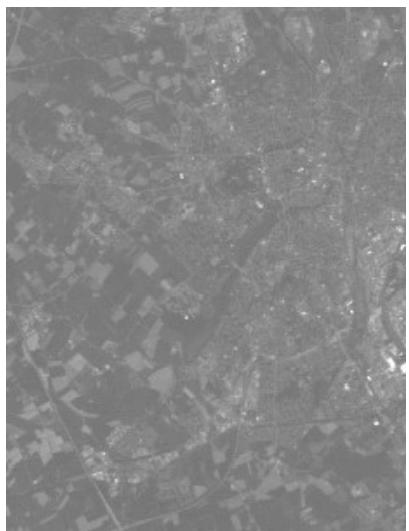
Images from: http://ivvgeo.uni-muenster.de/Vorlesung/FE_Script/kapitel3/main3-2.html (page no longer exists)

11. digital images

Image Editing - Dot Operators

An example from practice:

A first step is often to prepare the images in such a way that the maximum available colour space is used, if possible without distorting the image data. The data is distorted when image information (grey values) is added or deleted.

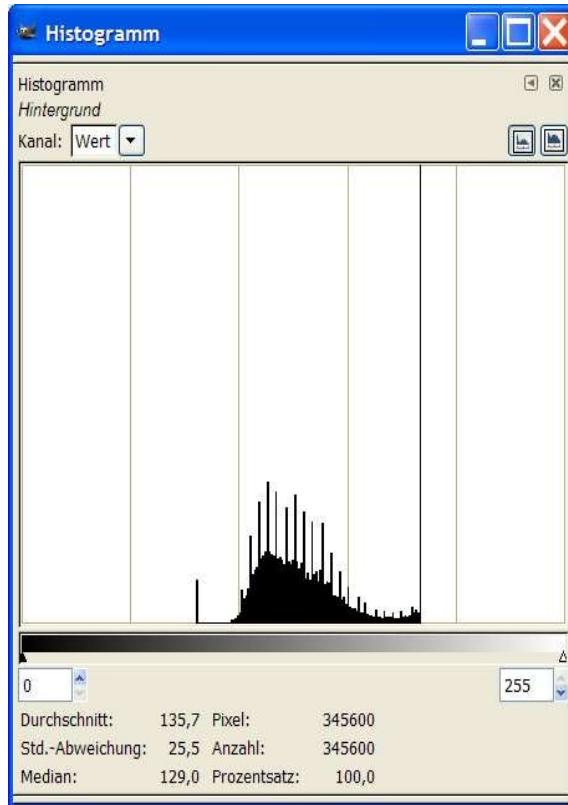
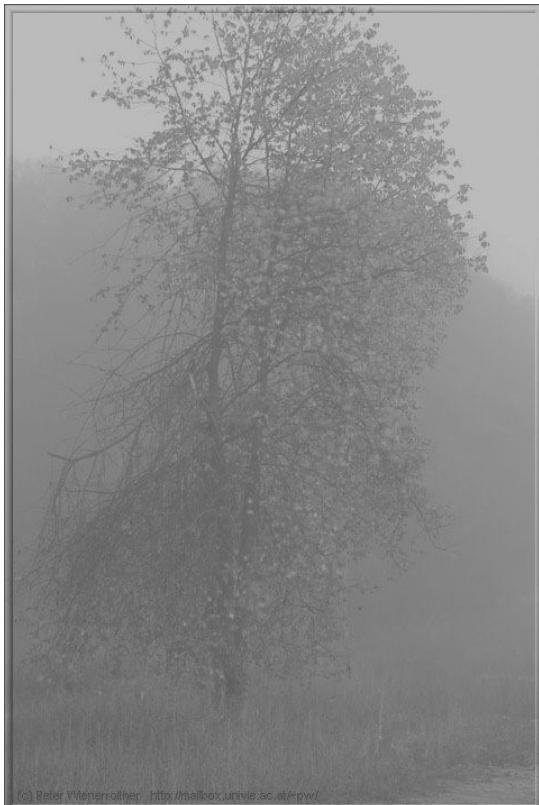


Images from: http://ivvgeo.uni-muenster.de/Vorlesung/FE_Script/kapitel3/main3-2.html (page no longer exists)

11. digital images

Image Editing - Dot Operators

Another example:



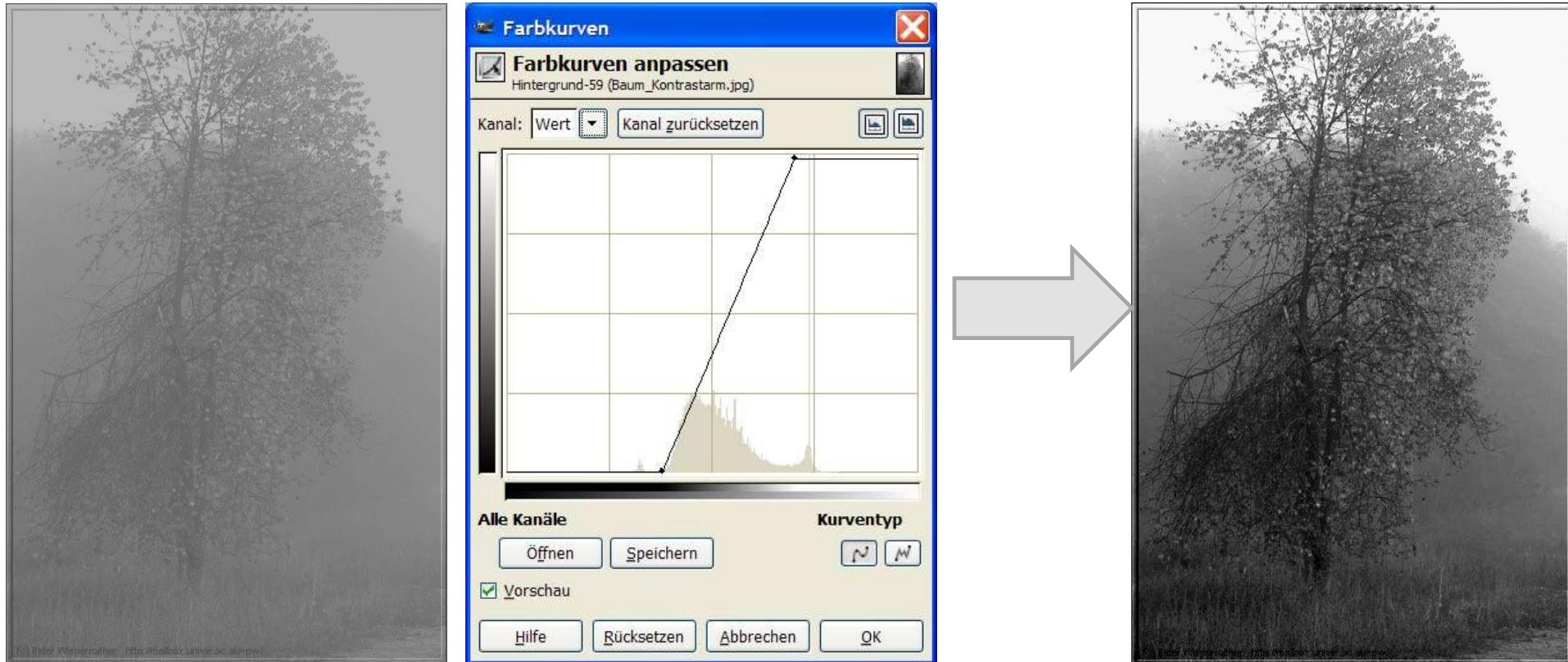
Initial situation:

A low-contrast image whose grey values are all in the middle range.

11. digital images

Image Editing - Dot Operators

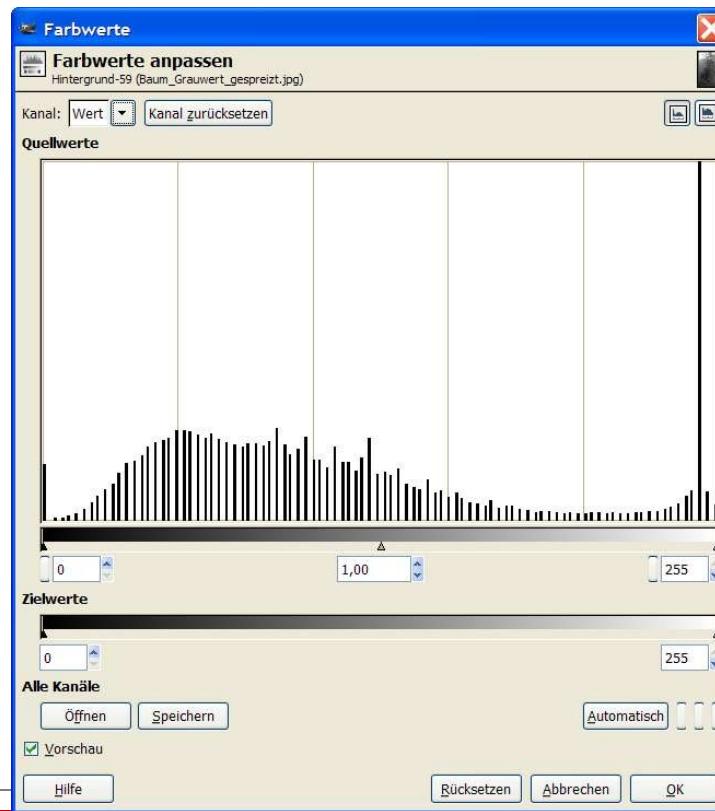
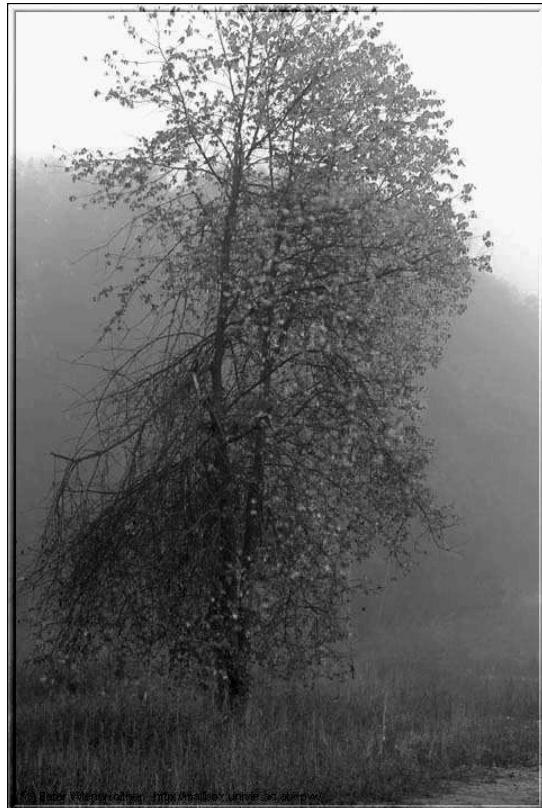
Another example:



11. digital images

Image Editing - Dot Operators

Another example:



Conclusion:

- The grey values of the low-contrast image were evenly distributed over the available grey value interval.
- Each pixel of the input image was assigned a new grey value g' by the linear grey value transformation, based on the grey value g .
- **Thus, the image information does not seem to have been distorted.**
- **We can only check whether this is really the case if we know how the calculation of the linear grey value transformation is carried out.**

Image Editing - Dot Operators

Calculation of the linear grey value transformation for contrast spreading:

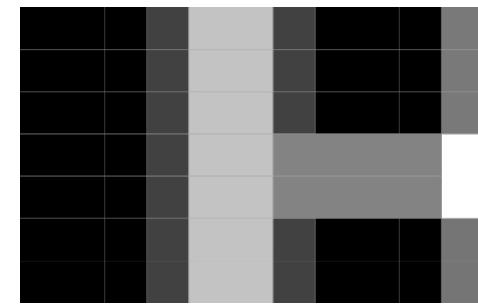
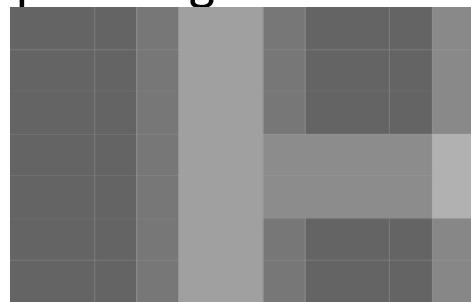
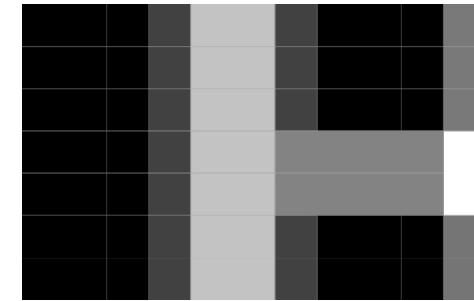
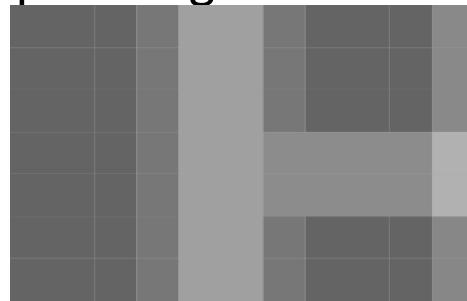
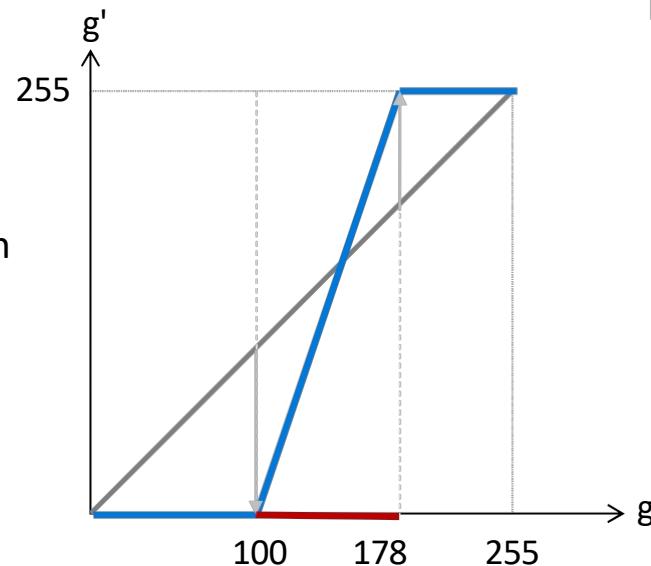


Image Editing - Dot Operators

Calculation of the linear grey value transformation for contrast spreading:



The linear grey value transformation is described by a straight line equation: $g' = f(g) = m \cdot g + b$



Step 1:
The slope m is calculated: $g' = m \cdot g$

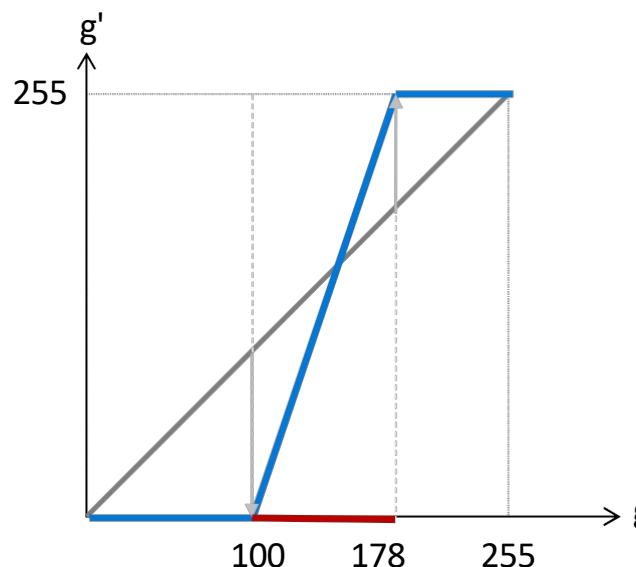
Generally speaking:

$$g'_m(i, j) = g(i, j) \cdot \frac{g'_{\text{MAX}} - g'_{\text{MIN}}}{g_{\text{max}} - g_{\text{min}}}$$

In the example: $g'_{\text{MAX}}=255$, $g'_{\text{MIN}}=0$, $g_{\text{max}}=178$, $g_{\text{min}}=100$

Image Editing - Dot Operators

Calculation of the linear grey value transformation for contrast spreading:



Step 1:
The slope m is calculated: $g' = m \cdot g$

Generally speaking:

$$g'_m(i, j) = g(i, j) \cdot \frac{g'_{\text{MAX}} - g'_{\text{MIN}}}{g_{\text{max}} - g_{\text{min}}}$$

In the example: $g'_{\text{MAX}}=255$, $g'_{\text{MIN}}=0$, $g_{\text{max}}=178$, $g_{\text{min}}=100$

11. digital images

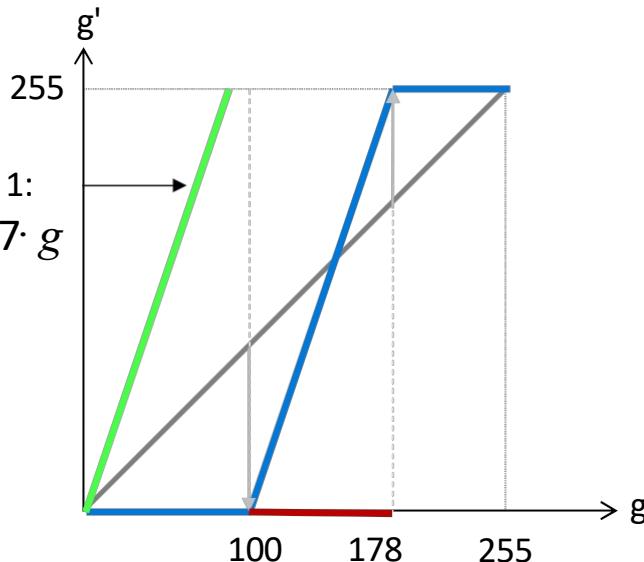
Image Editing - Dot Operators

Calculation of the linear grey value transformation ...

:

Linear grey value transformation after step 1:

$$g' = 3.27 \cdot g$$



1. Step:

The slope m is calculated: $g' = m \cdot g$

Generally speaking:

$$g'_m(i,j) = g(i,j) \cdot \frac{g'_{MAX} - g'_{MIN}}{g_{max} - g_{min}}$$

In the example: $g'_{MAX}=255$, $g'_{MIN}=0$, $g_{max}=178$, $g_{min}=100$

The slope m of the linear grey value transformation $g' = m \cdot g$ is therefore:
 $m = (255-0) / (178-100) = \underline{3.27}$

11. digital images

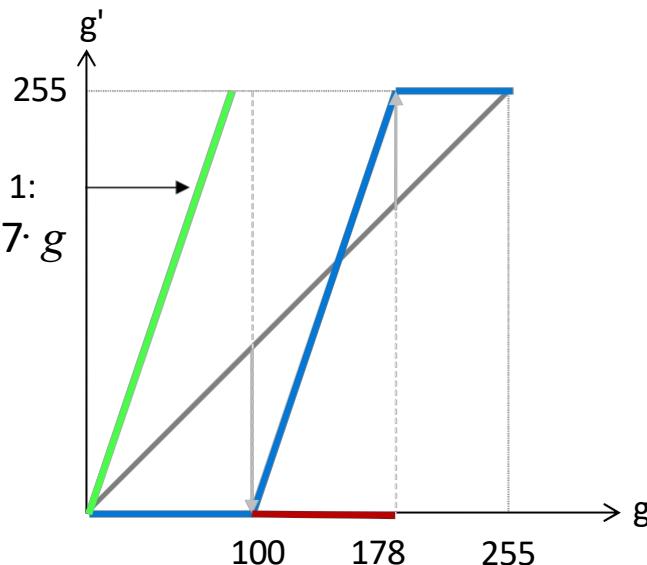
Image Editing - Dot Operators

Calculation of the linear grey value transformation ...

:

Linear grey value transformation after step 1:

$$g' = 3.27 \cdot g$$



1. Step:

The slope m is calculated: $g' = m \cdot g$

Generally speaking:

$$g_m'(i, j) = g(i, j) \cdot \frac{g'^{\text{MAX}} - g'^{\text{MIN}}}{g_{\text{max}} - g_{\text{min}}}$$

2. Step:

Y-axis intersection point b is calculated:

11. digital images

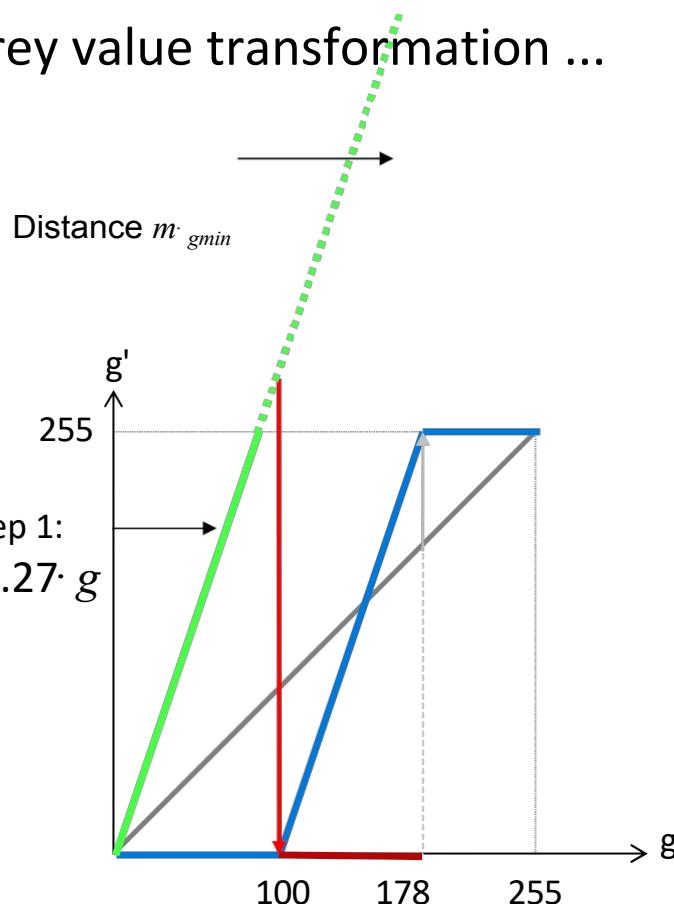
Image Editing - Dot Operators

Calculation of the linear grey value transformation ...

:

Linear grey value transformation after step 1:

$$g' = 3.27 \cdot g$$



1. Step:

The slope m is calculated: $g' = m \cdot g$

Generally speaking:

$$g'_m(i, j) = g(i, j) \cdot \frac{g'_{MAX} - g'_{MIN}}{g_{max} - g_{min}}$$

2. Step:

Y-axis intersection point b is calculated:

Conclusion: The Y-axis intersection point b is calculated by subtracting the distance $m \cdot g_{min}$ from the straight line $g' = m \cdot g$.

$$b = -g_{min} \cdot \frac{g'_{MAX} - g'_{MIN}}{g_{max} - g_{min}}$$

$$\text{In our case: } g' = m \cdot g - (100 \cdot m)$$

11. digital images

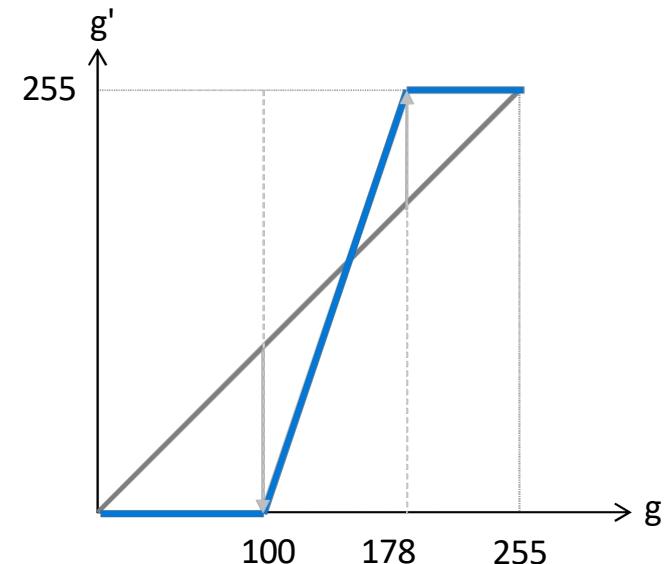
Image Editing - Dot Operators

Calculation of the linear grey value transformation for contrast spreading :

General wording:

$$g'(i, j) = g(i, j) \left[\frac{g'_{MAX} - g'_{MIN}}{g_{MAX} - g_{MIN}} \right] + \left[\frac{g'_{MAX} - g'_{MIN}}{g_{MAX} - g_{MIN}} \right]$$

Slope Y-axis intersection



associated linear grey value transformation:

$$g' = 3.27 \cdot g - (327)$$

with $g' = 0$ for $g < 100$ and $g' = 255$ for $g > 178$

11. digital images

Image Editing - Dot Operators

Calculation of the linear grey value transformation for contrast spreading :

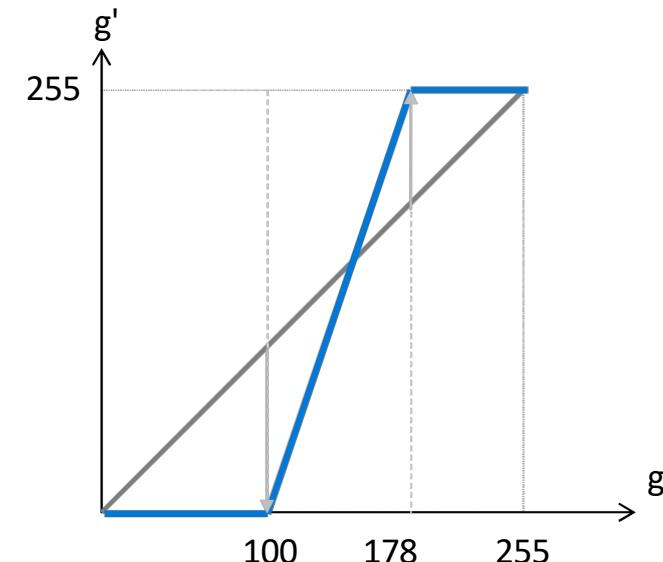
General wording:

$$g'(i, j) = g(i, j) \left[\frac{g'_{MAX} - g'_{MIN}}{g_{MAX} - g_{MIN}} \right] + \left[\frac{g'_{MAX} - g'_{MIN}}{g_{MAX} - g_{MIN}} \right]$$

mult *add*

$$g'(i, j) = g(i, j) \cdot mult + add$$

$$\begin{aligned} mult &= \frac{g'_{MAX} - g'_{MIN}}{g_{MAX} - g_{MIN}} \\ \text{mit } &\boxed{} \\ add &= \boxed{-g_{MIN}} \cdot mult \end{aligned}$$



associated linear grey value transformation:

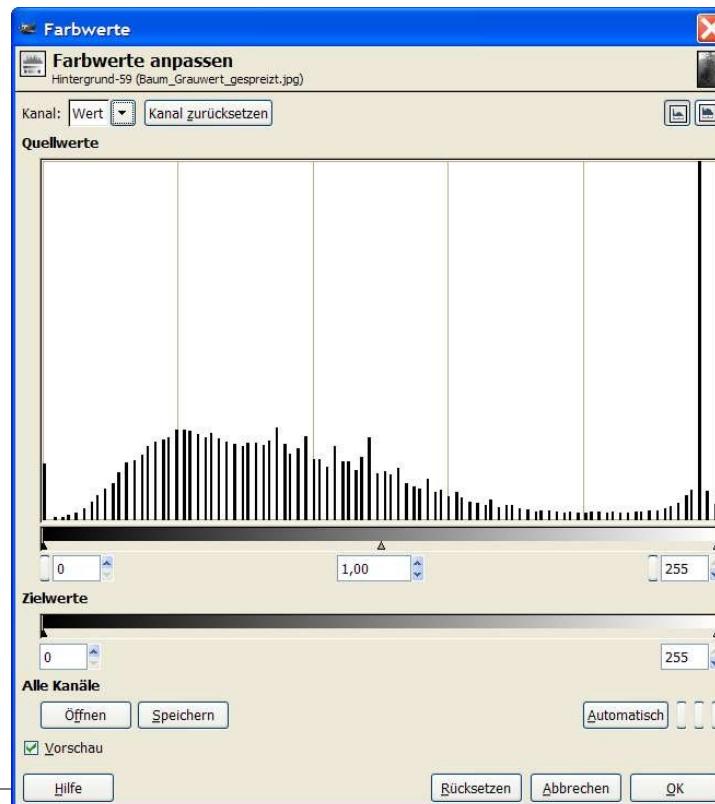
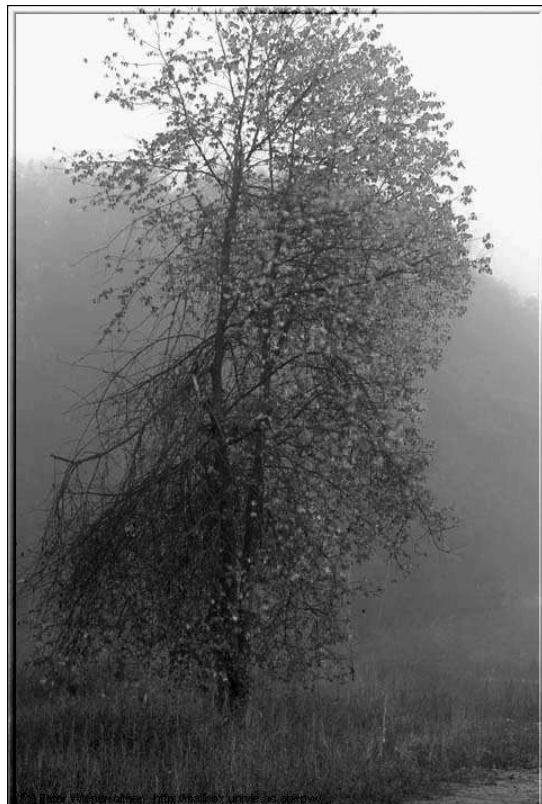
$$g' = 3.27 \cdot g - (327)$$

with $g' = 0$ for $g < 100$ and $g' = 255$ for $g > 178$

11. digital images

Image Editing - Dot Operators

One question is still open: Does the linear grey value transformation distort image information?



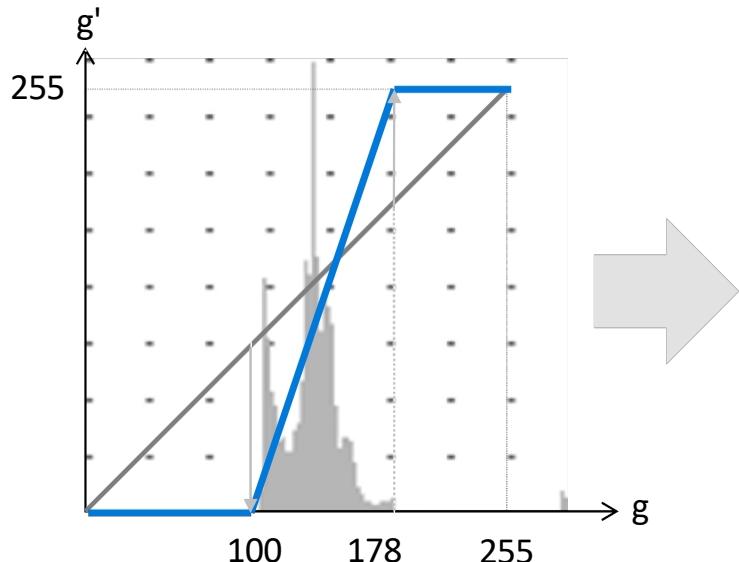
Conclusion:

- The grey values of the low-contrast image were evenly distributed over the available grey value interval.
- Each pixel of the input image was assigned a new grey value g' by the linear grey value transformation based on the grey value g .
- Thus, the image information does not seem to have been distorted.
- We can only check whether this is really the case if we know how the calculation of the linear grey value transformation is carried out.

11. digital images

Image Editing - Dot Operators

Is image information distorted by the linear grey value transformation?



Linear grey value transformation:

$$g' = 3.27 \cdot g - 327$$

with $g' = 0$ for $g < 100$ and

$$g' = 255 \text{ for } g > 178$$

g	g'	Displayable grey value
100	0	0
101	3,27	3
102	6,54	6
...
139	127,53	128
...
176	248,52	249
177	251,79	252
178	255,06	255

Calculate the linear grey value transformation for the grey values of the input image that lie between g_{\min} and g_{\max} .

Objective: check whether two grey values are mapped onto one grey value

- If two grey values are mapped onto one grey value, image information is lost that can no longer be reconstructed.
- with our contrast spreading, image distortion can be excluded, as no two grey values are mapped onto one grey value
- This is not generally valid proof, but it is a strong indication that contrast enhancement does not distort image content and can therefore also be used for sensitive data (medical images, satellite images).

Image Editing - Dot Operators

Histograms Point operations

- Linear change of the grey values:
 - Changing the picture brightness
 - Invert the image
 - Changing the contrast
 - Binarisation through thresholding
- Non-linear change in grey values:
 - Gamma correction
- Colour Transformations (Color Transformation)

11. digital images

Image Editing - Dot Operators

Non-linear change of grey values: Gamma correction

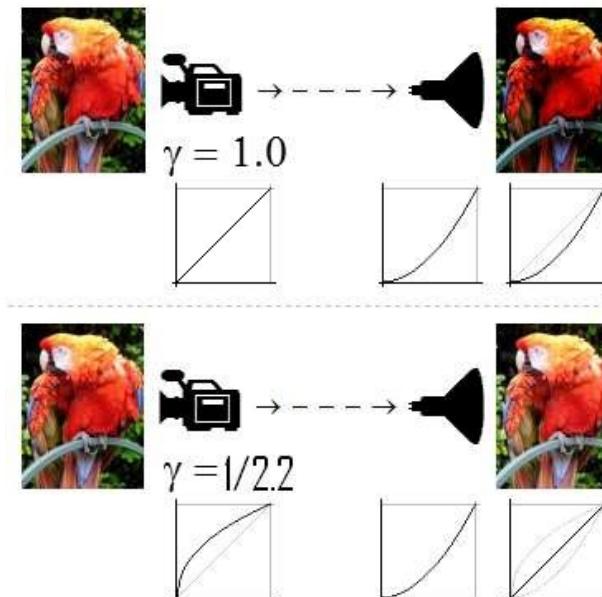
Assumptions so far:

- When taking pictures and videos, the grey values change linearly with our perception.
- When representing the grey value on displays, the screen pixels change linearly to our perception

It is not so.

Gamma correction is used to correct the non-linear behaviour when taking and reproducing pictures.

Image from: [Gamma correction - Wikipedia](#)



Above: linear image sensor without gamma correction ($\gamma=1$) captures a high-contrast but unnatural image

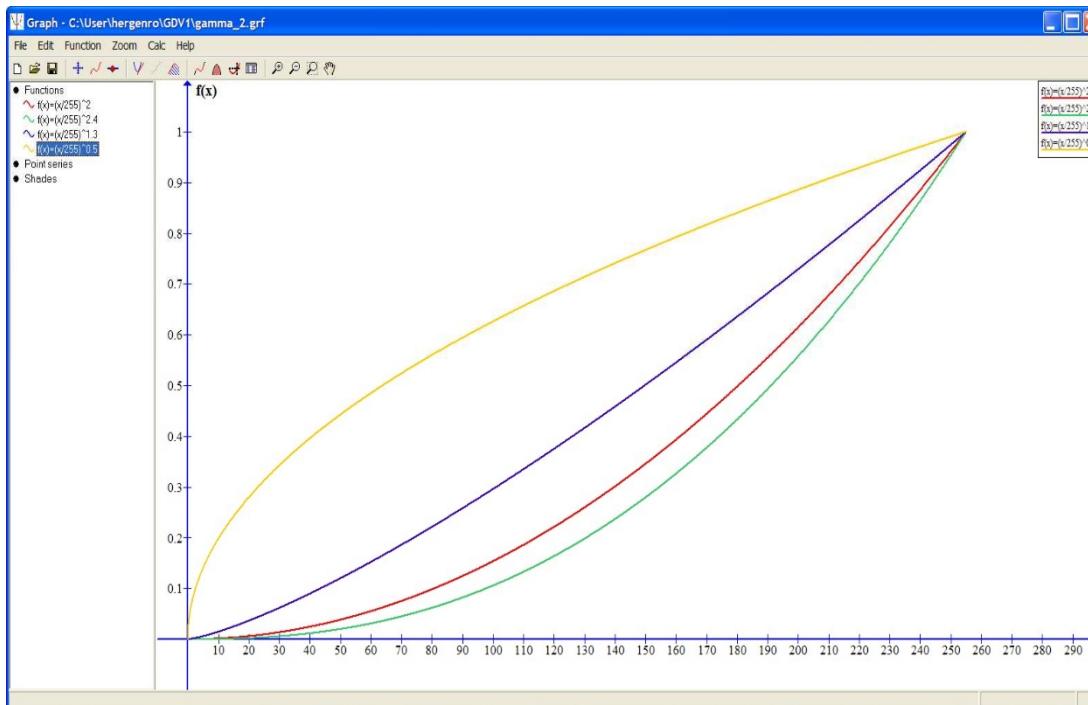
below: Image sensor with gamma correction captures a faithfully perceptible image

11. digital images

Image Editing - Dot Operators

Non-linear change of grey values: Gamma correction

Exemplary representation of the course of the gamma function



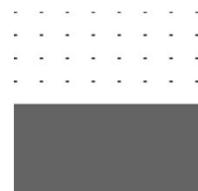
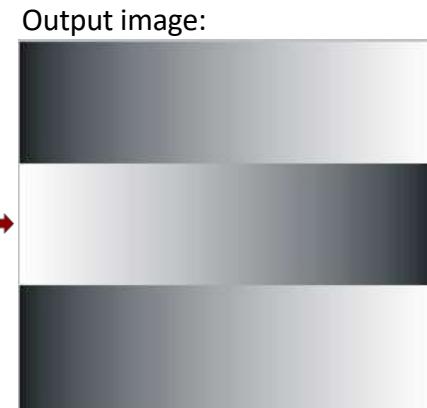
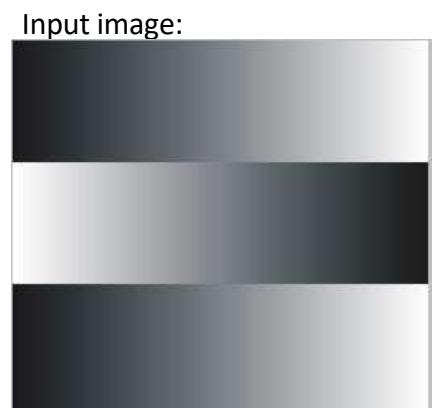
11. digital images

Image Editing - Dot Operators

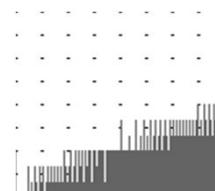
Non-linear change of grey values: Gamma correction

Non-linear brightening of the image content

Gamma function that transforms the input image into the output image.

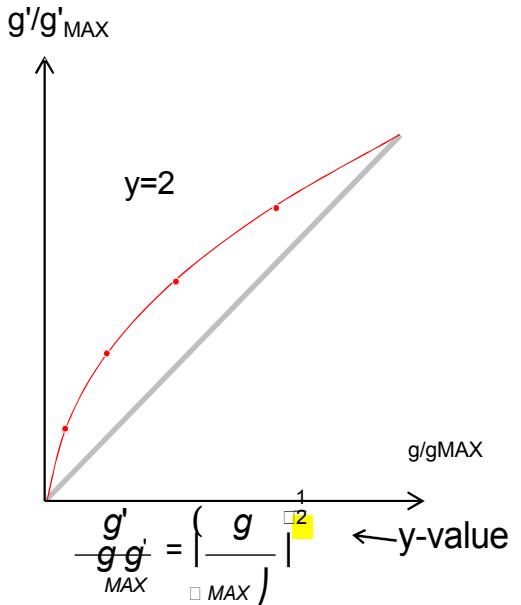


Histogram of the input image



Histogram of the output image

transformed:



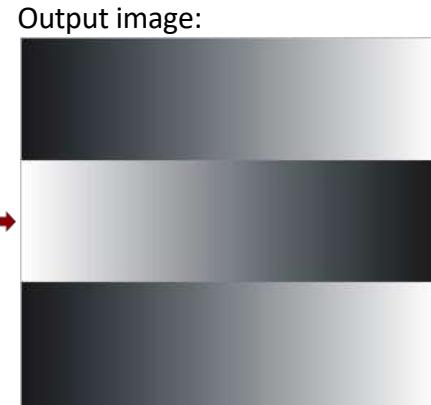
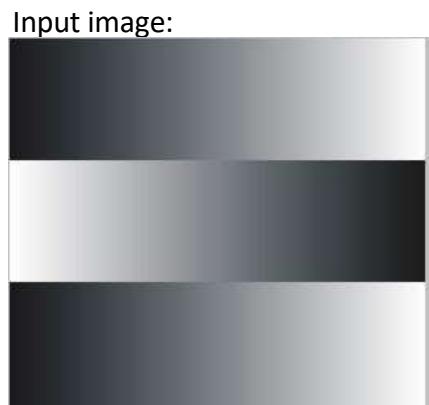
11. digital images

Image Editing - Dot Operators

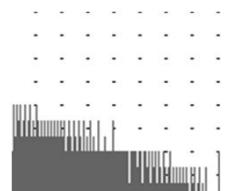
Non-linear change of grey values: Gamma correction

Non-linear darkening of the image content

Gamma function that transforms the input image into the output image.

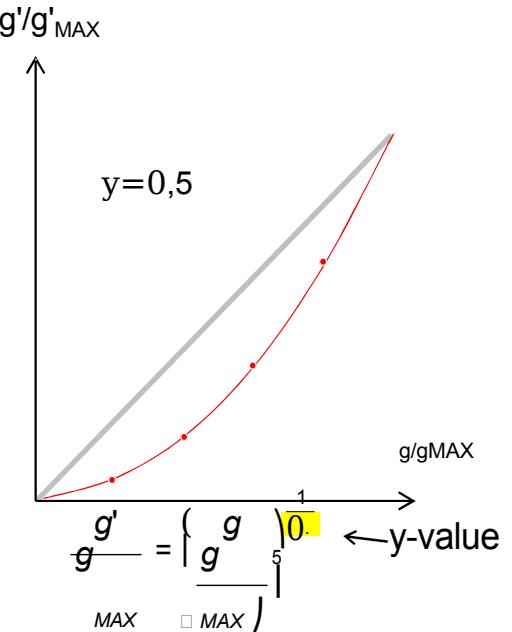


Histogram of the input image



Histogram of the output image

transformed:



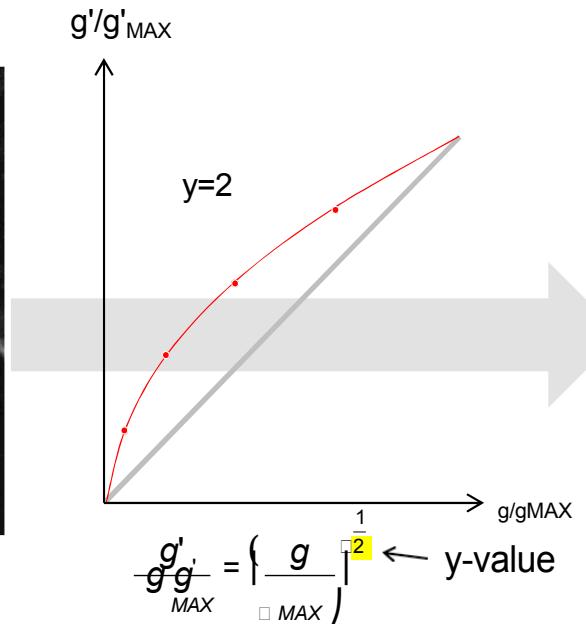
11. digital images

Image Editing - Dot Operators

Non-linear change of grey values: Gamma correction

Has the contrast in the bright areas been increased?

How can you tell where the contrast has been increased or reduced?



11. digital images

Image Editing - Dot Operators

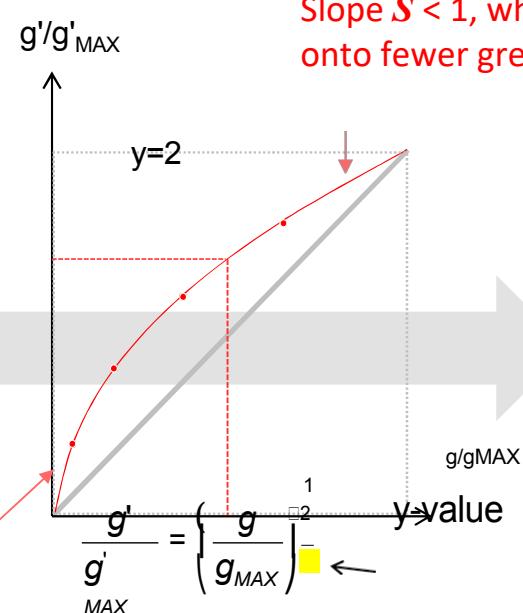
Non-linear change of grey values: Gamma correction

Has the contrast in the bright areas been increased?

How can you tell where the contrast has been increased or reduced?



Slope $S > 1$, which means: half of the grey values g are mapped onto considerably more grey values g' .



Slope $S < 1$, which means: half of the grey values g are mapped onto fewer grey values g' , image information is lost



11. digital images

Image Editing - Dot Operators



Combined gamma correction in all rgb channels the same

Gamma correction $y < 1$
the same in all rgb channels

Gamma correction $y > 1$
the same in all rgb channels

- Up to now, gamma correction has only been applied to greyscale images.
- In the examples on the left, the same gamma corrections were applied to all three colour channels. In the three cases shown, the corrections were successful. However, this is not always the case.
- Better transfer the images to HSV, YCbCr or a similar colour system and then correct the intensity channel.
- Remember:** Gamma correction alters image information. For this reason, it should not be used in sensitive application areas.

Image Editing - Dot Operators

Histograms Point operations

- Linear change of the grey values:
 - Changing the picture brightness
 - Invert the image
 - Changing the contrast
 - Binarisation through thresholding
- Non-linear change in grey values:
 - Gamma correction
- Colour Transformations (Color Transformation)

11. digital images

Image Editing - Dot Operators

Colour Transformations (Color Transformation)

- To perform image transformations, you have to set a lot of parameters.
- However, this only works well if you have knowledge about how the parameters work.



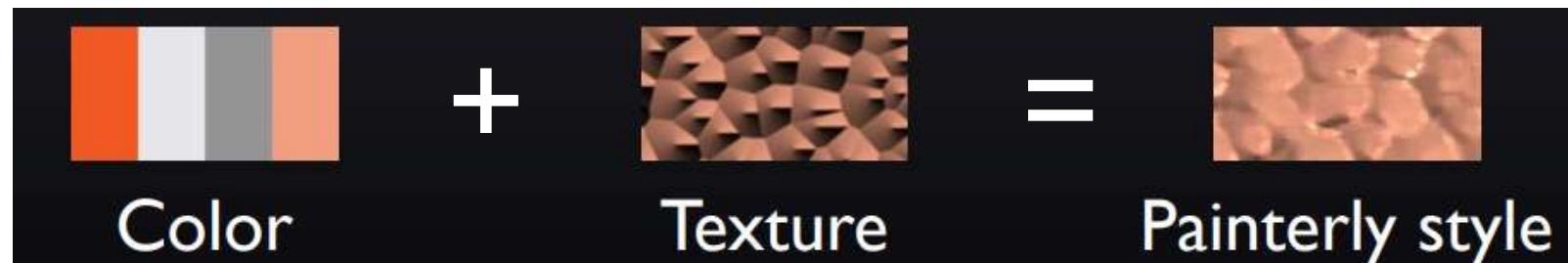
From: T. Pouli, E. Reinhard: "Example-based colour image manipulation and enhancement", SIGGRAPH 2012 Courses, [Example-based colour image manipulation and enhancement | ACM SIGGRAPH 2012 Courses](#)

11. Digital images

Image Editing - Dot Operators

Colour Transformations (Color Transformation)

- It would be more intuitive if you could transfer the properties of one image to another.
- This is exactly what we are dealing with in the field of colour transformations.



From: T. Pouli, E. Reinhard: "Example-based colour image manipulation and enhancement", SIGGRAPH 2012 Courses, [Example-based colour image manipulation and enhancement | ACM SIGGRAPH 2012 Courses](#)

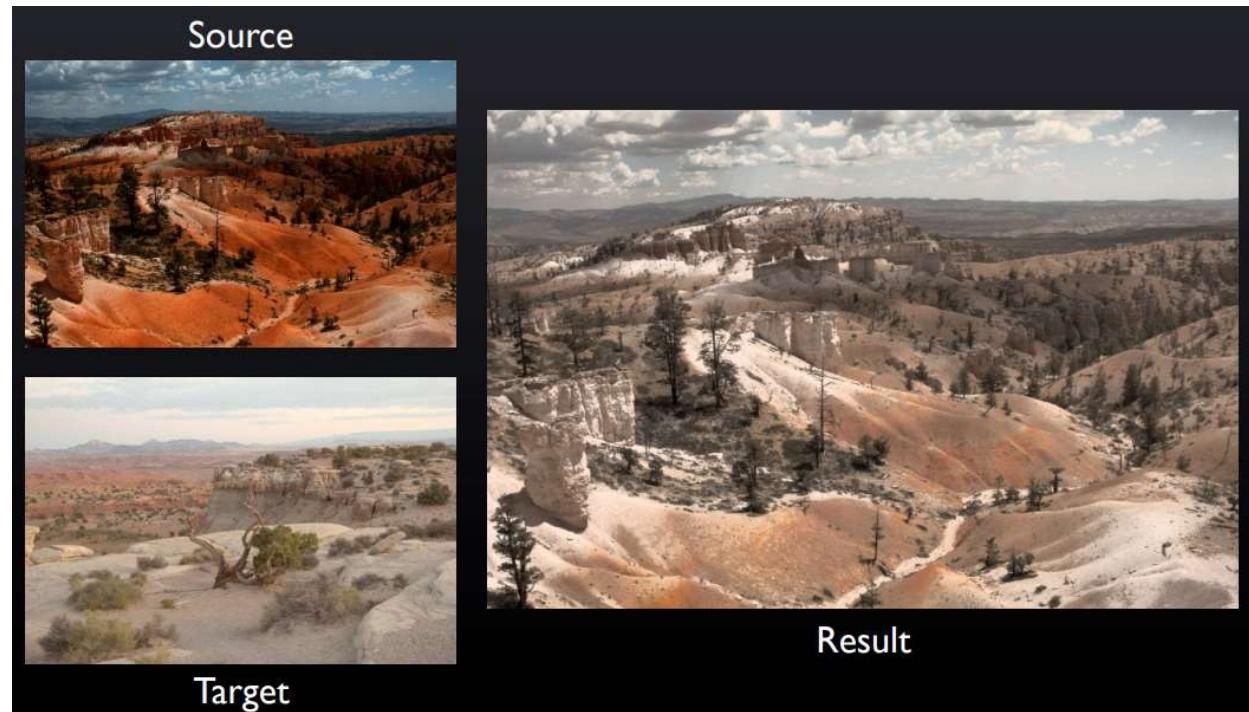
11. Digital images

Image Editing - Dot Operators

Colour Transformations (Color Transformation)

The goal is:

- Transfer the colour composition of the target image to the input image (Source).
- A method must be developed with which the colour design of the target image can be captured and transferred to the input image (source). The image content of the source should be preserved as much as possible in the result image.



From: T. Pouli, E. Reinhard: "Example-based colour image manipulation and enhancement", SIGGRAPH 2012 Courses, [Example-based colour image manipulation and enhancement | ACM SIGGRAPH 2012 Courses](#)

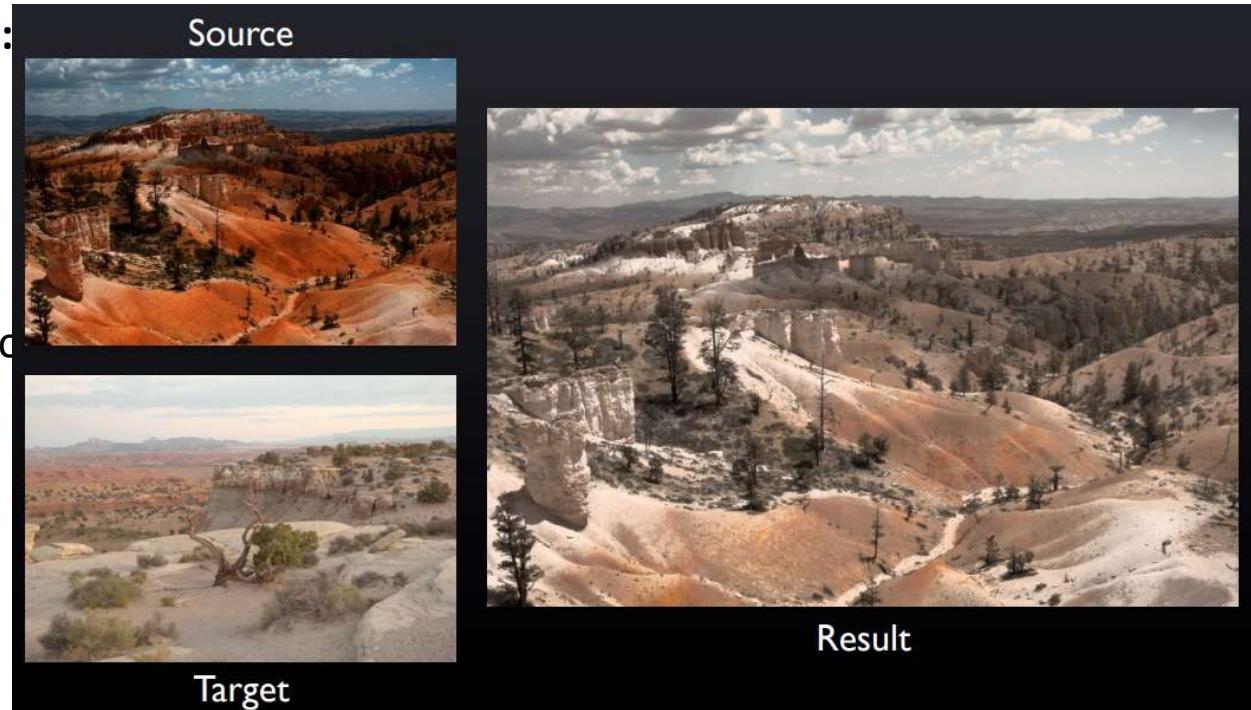
11. digital images

Image Editing - Dot Operators

Colour Transformations (Color Transformation)

The concept for implementing the idea is:

- To capture the colour distribution in source and target, transform both images into the Lab colour system (why will be explained later).
- Per Lab colour channel (l , a , b) one record
 - the average image brightness, corresponds to the average grey value (mean value as floating point number)
 - the dispersion of the grey values around the mean value in the histogram (standard deviation s , floating point number)



From: T. Pouli, E. Reinhard: "Example-based colour image manipulation and enhancement", SIGGRAPH 2012 Courses, [Example-based colour image manipulation and enhancement | ACM SIGGRAPH 2012 Courses](#)

11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

Computer Graphics and Applications 21(5), 2001

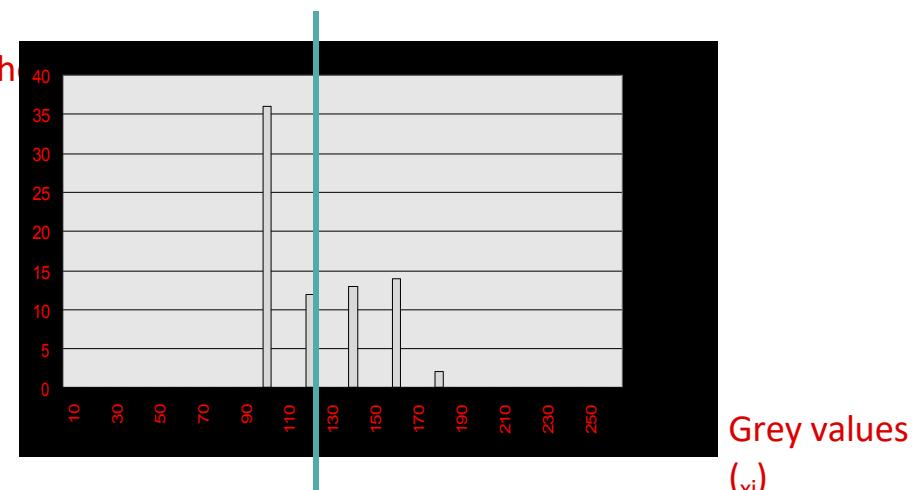
Calculation of the average image brightness by forming the mean value:

The mean value is the average value.

$$\bar{x} = \frac{x_1 + x_2 + x_3 + \dots + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

Mittelwert
Number of grey values
Grey values at the i. position

Frequency of the values



Mean value (=mean image brightness) x_i :
122.857

From DATatab - very informative: <https://datatab.de/tutorial/standardabweichung-varianz-spannweite>

11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

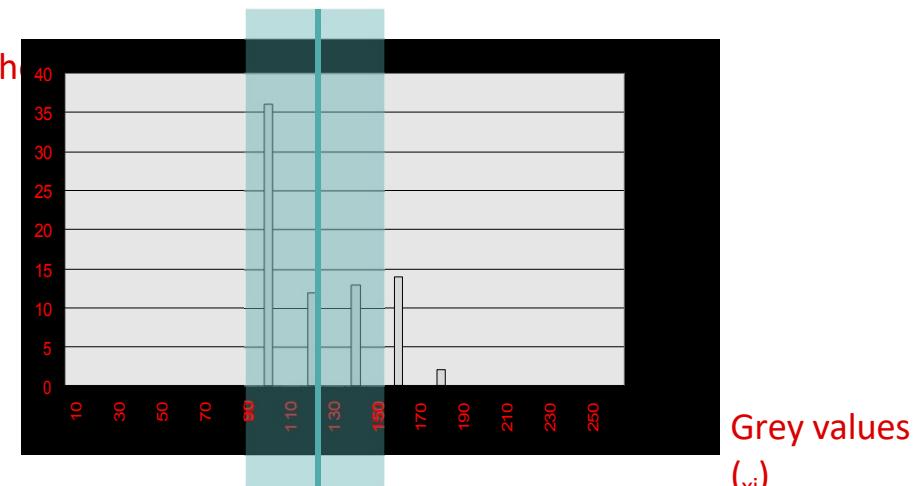
Computer Graphics and Applications 21(5), 2001

Standard deviation depends on the contrast range of the image :

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

Number of grey values
Grey values at the i. Place
Mean image brightness = average value

Frequency of the values



Standard deviation S: approx.
30

From DATAtab - very informative: <https://datatab.de/tutorial/standardabweichung-varianz-spannweite>

11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

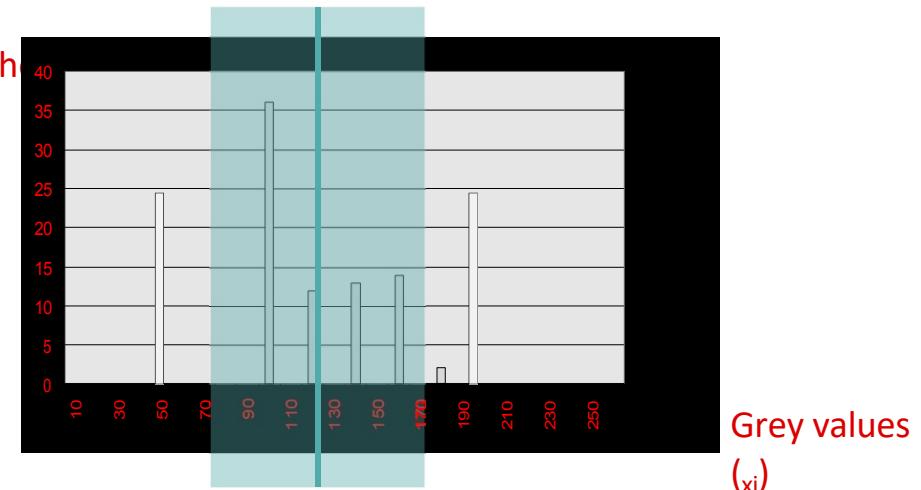
Computer Graphics and Applications 21(5), 2001

Standard deviation depends on the contrast range of the image :

$$\sigma = \sqrt{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$

Number of grey values
Grey values at the i. Place
Mean image brightness = average value

Frequency of the values



Standard deviation S: approx.
50

From DATAtab - very informative: <https://datatab.de/tutorial/standardabweichung-varianz-spannweite>

11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

1. Calculate mean values and standard deviation for the Lab channels of the source and the target:

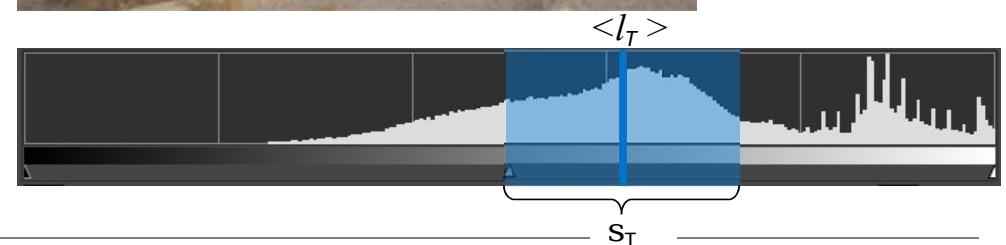
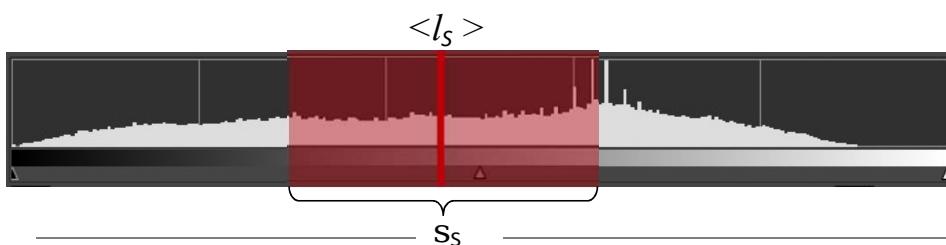
Computer Graphics and Applications 21(5), 2001



Source



Target

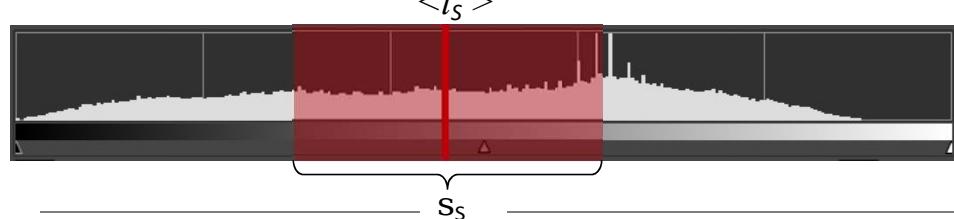


11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE Computer Graphics and Applications 21(5), 2001

2. Subtract the mean values $\langle l_s \rangle$, $\langle a_s \rangle$, $\langle b_s \rangle$ of the source from the values of the corresponding source channels :



$$l_s^* = l_s - \langle l_s \rangle$$

$$a_s^* = a_s - \langle a_s \rangle$$

$$b_s^* = b_s - \langle b_s \rangle$$

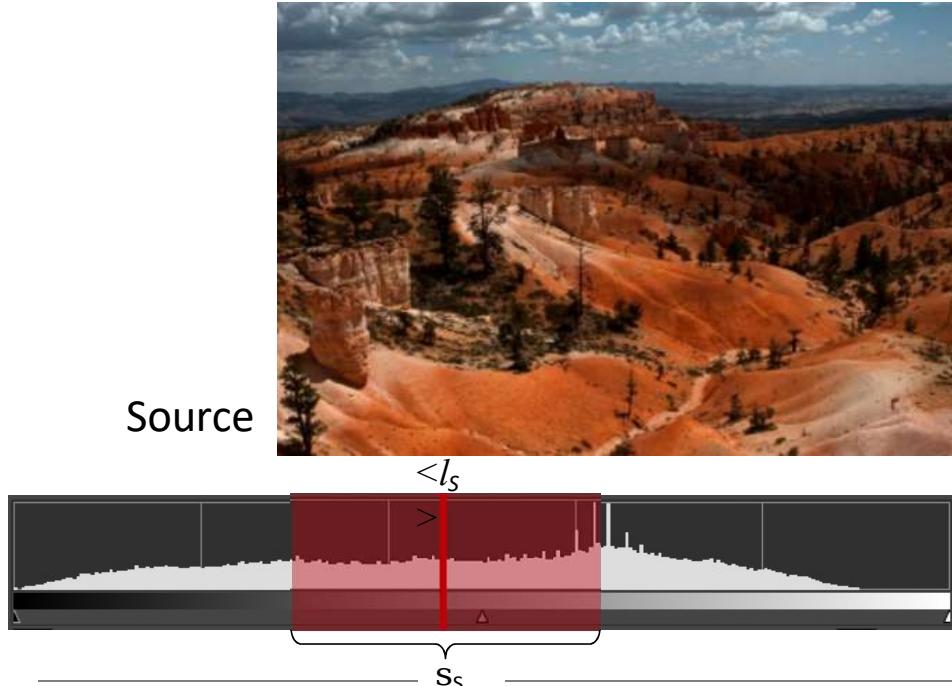
- All Lab colour channels now have the mean value 0.
- The grey values of the channels can also be negative after this subtraction.

11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE Computer Graphics and Applications 21(5), 2001

3. Scale the values of the source transformed by subtraction using the standard deviations (s_T / s_s):



$$l'_s = \frac{s_T^l}{s_s^l} l^*$$

$$a'_s = \frac{s_T^a}{s_s^a} a^*$$

$$b'_s = \frac{s_T^b}{s_s^b} b^*$$

11. digital images

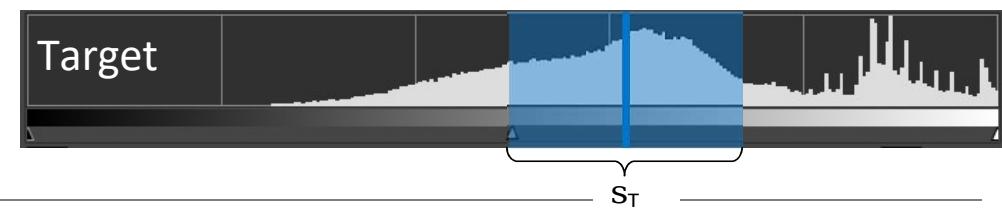
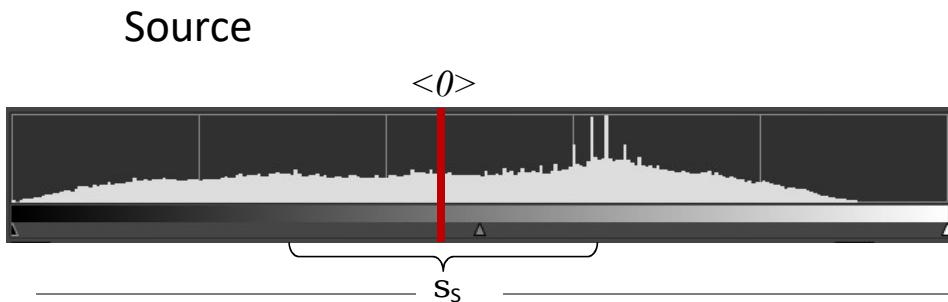
Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE Computer Graphics and Applications 21(5), 2001

Scale the values of the source transformed by subtraction using the standard deviations (s_T / s_s):

Scaling brings the contrast range of the source closer to the target image.

This transformation takes place in all Lab colour channels. The mean values of all colour channels of the source image are still 0.



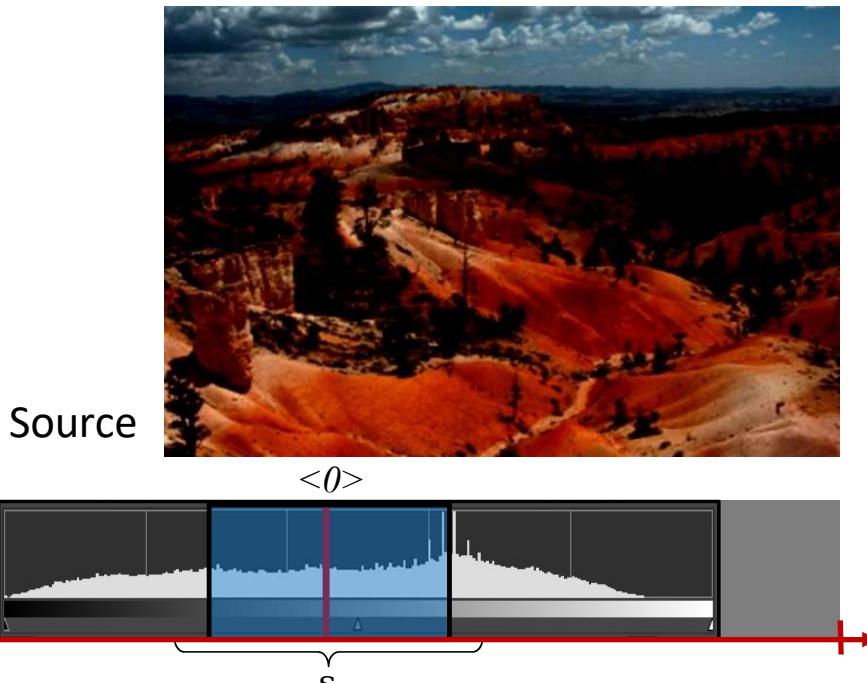
11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

Scale the values of the source transformed by subtraction using the standard deviations (s_T / s_s):

Computer Graphics and Applications 21(5), 2001



Scaling brings the contrast range of the source closer to the target image.

See picture above left, the negative values are shown in black.

This transformation takes place in all Lab colour channels. The mean values of all colour channels of the source image are still 0.

11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

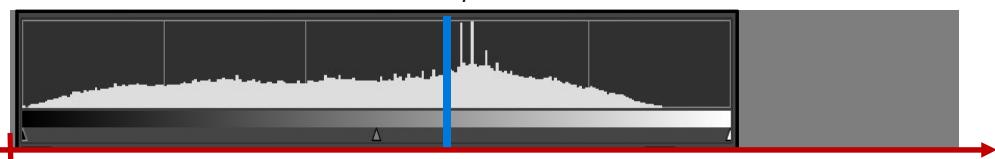
Add the mean values of the respective target channels to the matching transformed source channels (L, a, b):

Computer Graphics and Applications 21(5), 2001



Source

$$\langle l_T \rangle$$



This shifts the values into the positive range and the values become displayable again.

If there are still negative values, they are mapped to the value 0. Values greater than 255 are mapped on 255.

11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

Computer Graphics and Applications 21(5), 2001

$$f(, \begin{array}{c} \text{Source} \\ \text{Target} \end{array}) =$$



Result

From: T. Pouli, E. Reinhard: "Example-based colour image manipulation and enhancement", SIGGRAPH 2012 Courses, [Example-based colour image manipulation and enhancement | ACM SIGGRAPH 2012 Courses](#)

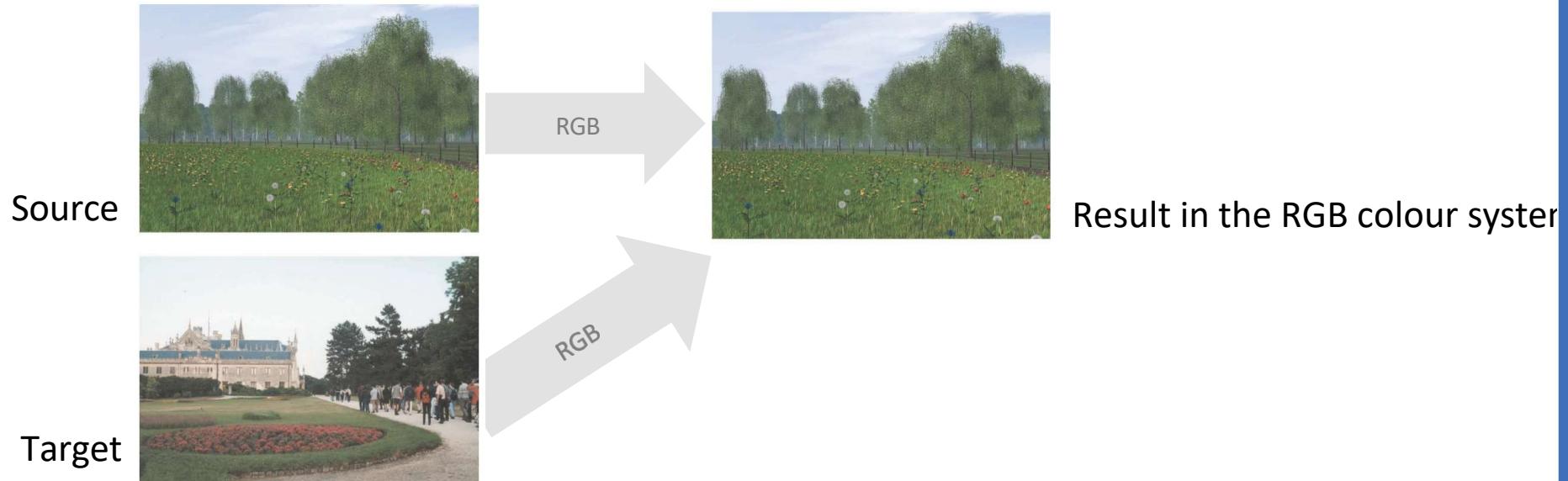
11. digital images

Image Editing - Dot Operators

Colour transformations (Color Transformation): Reinhard et al, 'Color Transfer between Images', IEEE

Computer Graphics and Applications 21(5), 2001

Why does this transformation work in the Lab system but not (in all cases) in the RGB colour system?



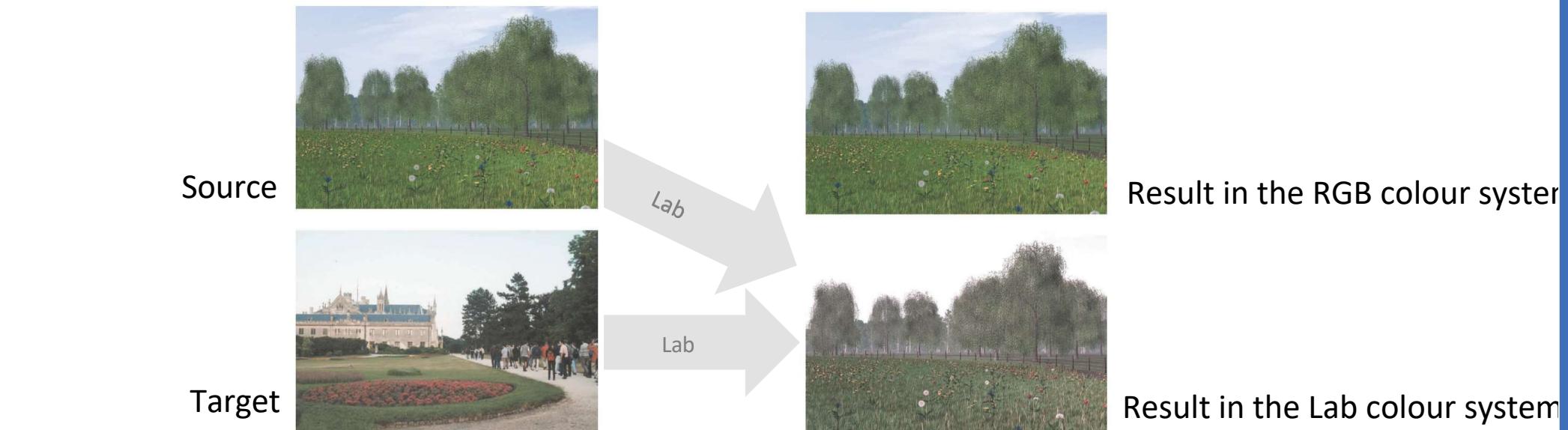
From: T. Pouli, E. Reinhard: "Example-based colour image manipulation and enhancement", SIGGRAPH 2012 Courses, [Example-based colour image manipulation and enhancement | ACM SIGGRAPH 2012 Courses](#)

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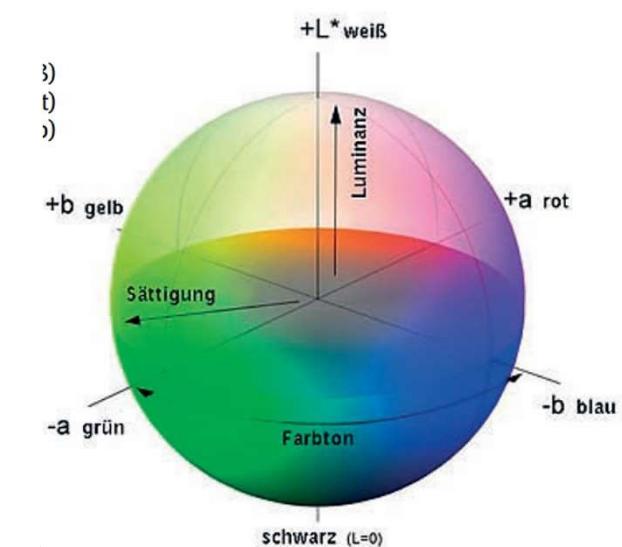
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Why does this transformation work in the Lab system but not (in all cases) in the RGB colour system?

There are two main reasons for this:

1. In the Lab colour space, the length of the distance between two colours is in direct proportion to our ability to distinguish these colours. This is not the case in the RGB colour space.
2. In the RGB colour space, all three colour channels together model a hue. In the Lab system, the hues are modelled by complementary colours and intensity values that have less influence on each other in relation to RGB.



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11. digital images

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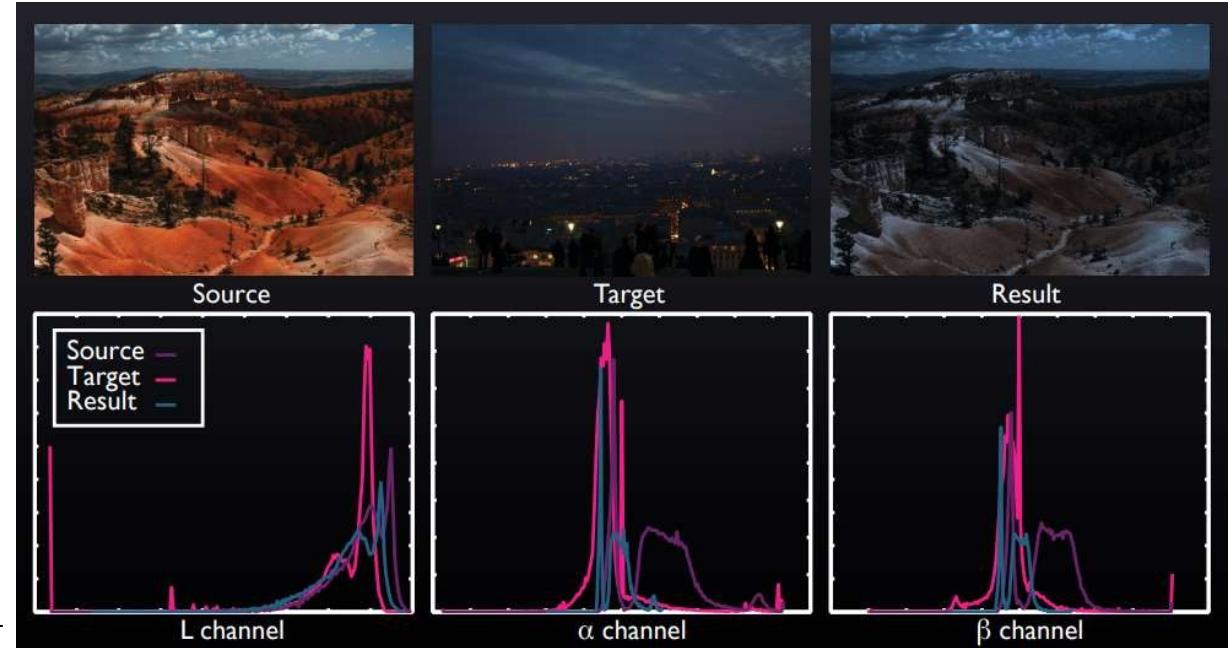
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Why does this transformation work in the Lab system but not (in all cases) in the RGB colour system?

- The aim is to avoid that the target values deviate too much from the source values after the transformation. In this way, the image content is largely preserved.

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IEEE
A result:



4 Using swatches. We applied (a) the atmosphere of Vincent van Gogh's *Cafe Terrace on the Place du Forum, Arles, at Night* (Arles, September 1888, oil on canvas; image from the Vincent van Gogh Gallery, <http://www.vangoghgallery.com>) to (b) a photograph of Lednice Castle near Brno in the Czech Republic. (c) We matched the blues of the sky in both images, the yellows of the cafe and the castle, and the browns of the tables at the cafe and the people at the castle separately.

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Food for thought:

Are the image contents distorted by the colour transfer, so that the colour transfer is not suitable for use on sensitive data, such as in the medical field or for the evaluation of satellite images?



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More result pictures:

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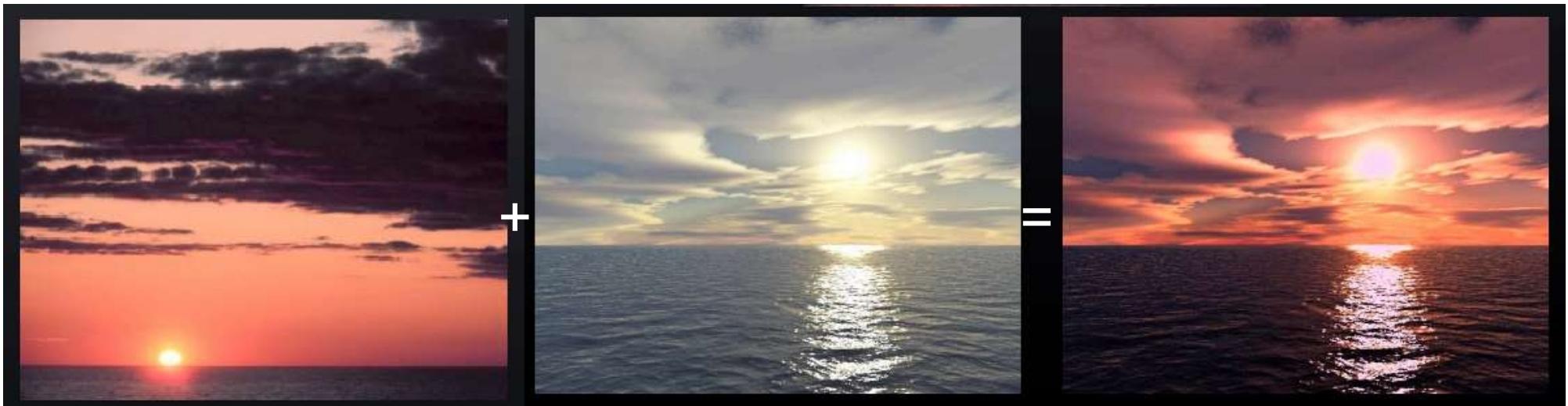
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Concluding remarks:

Implementation and evaluation of the colour transfer of Reinhard et al. take place in the practical course:

Assumptions are that

- ... the process also works well in the HSV colour space
- ... Images that concentrate on one colour tone (e.g. blue) also work in the RGB colour space.

Outlook:

The normalisation of images by means of mean value and standard deviation is also used in other image processing methods. For example, this transformation technique is also used in convolutional neural networks.

Image Editing - Dot Operators

Histograms Point operations

- Linear change of the grey values:
 - Changing the picture brightness
 - Invert the image
 - Changing the contrast
 - Binarisation through thresholding
- Non-linear change in grey values:
 - Gamma correction
- Colour Transformations (Color Transformation)

What happens next?

12. digital images

Image Processing - Local Operators



Left: Poorly contrasted image

Right: Edges highlighted by contrast spreading and edge filters

Pictures from:
<https://invision-news.de/invision/bildverarbeitung/>