



Design for CKMR



Mark Bravington, CSIRO: Aug 2022

O&A www.csiro.au











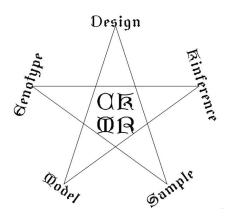


Design in CKMR

If You...

- do not collect enough samples, or
- do not collect the right types of sample, or
- do not measure their stuff adequately

... then CKMR will fail



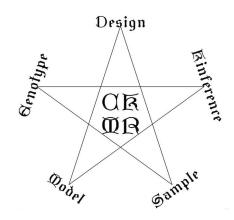


Design in CKMR

If You...

- do not collect *enough* samples, or
- do not collect the right types of sample, or
- do not measure their stuff adequately

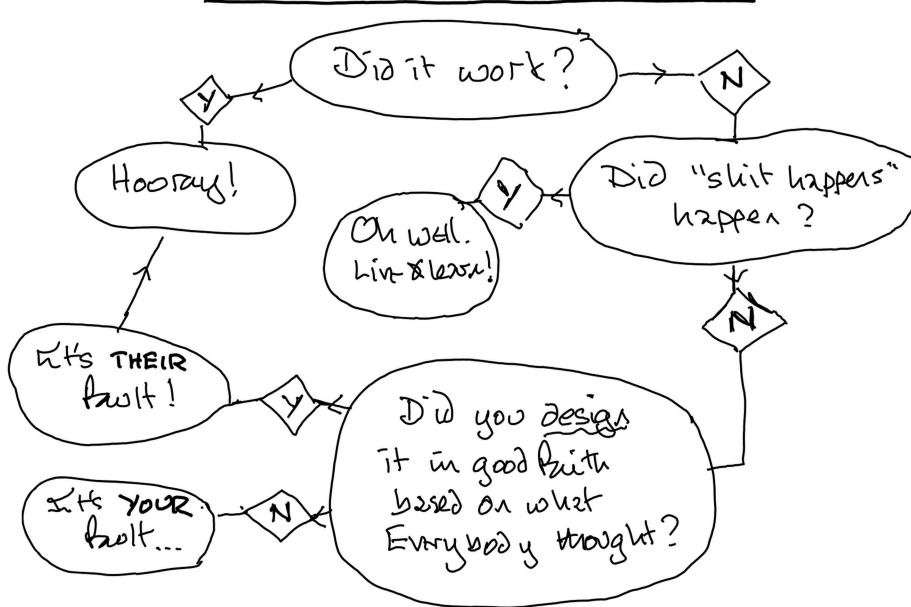
... then CKMR will fail



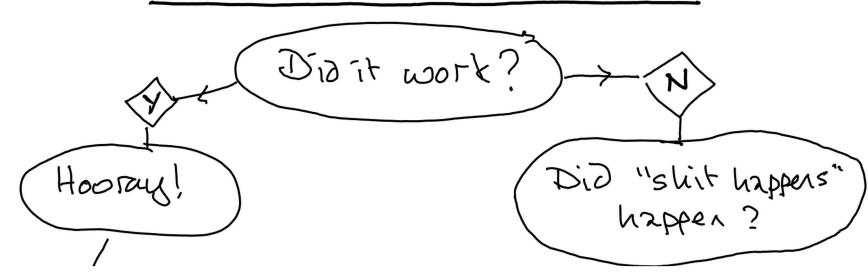
"enough samples" really means "enough kin-pairs" ...

Can't control latter, but can plan former and types, and stuff via... **DESIGN**





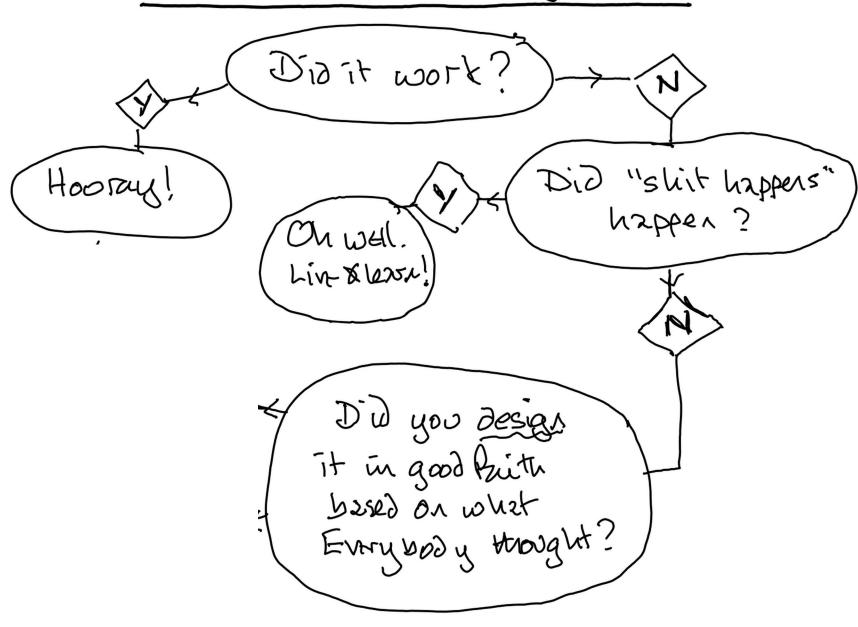
Did it work?

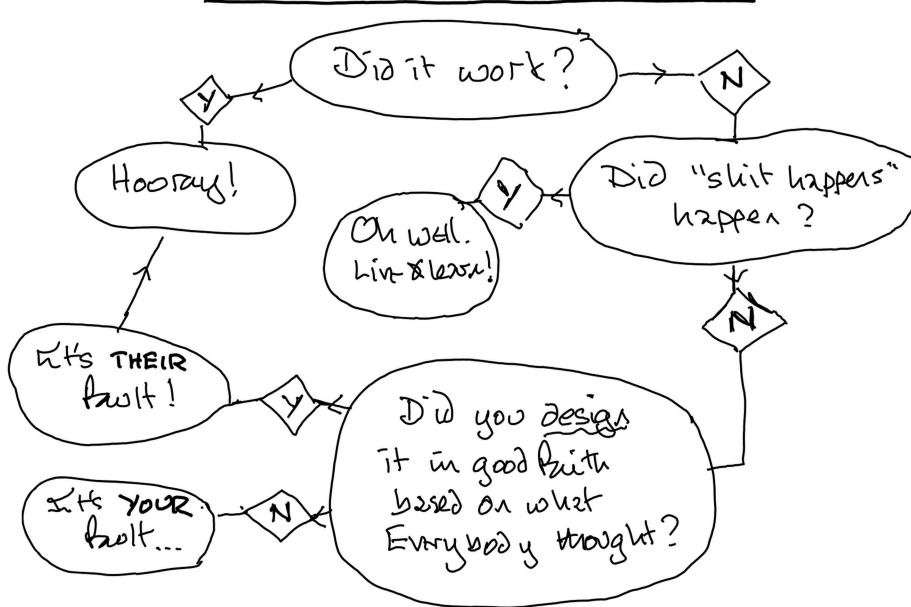


Hoosay!

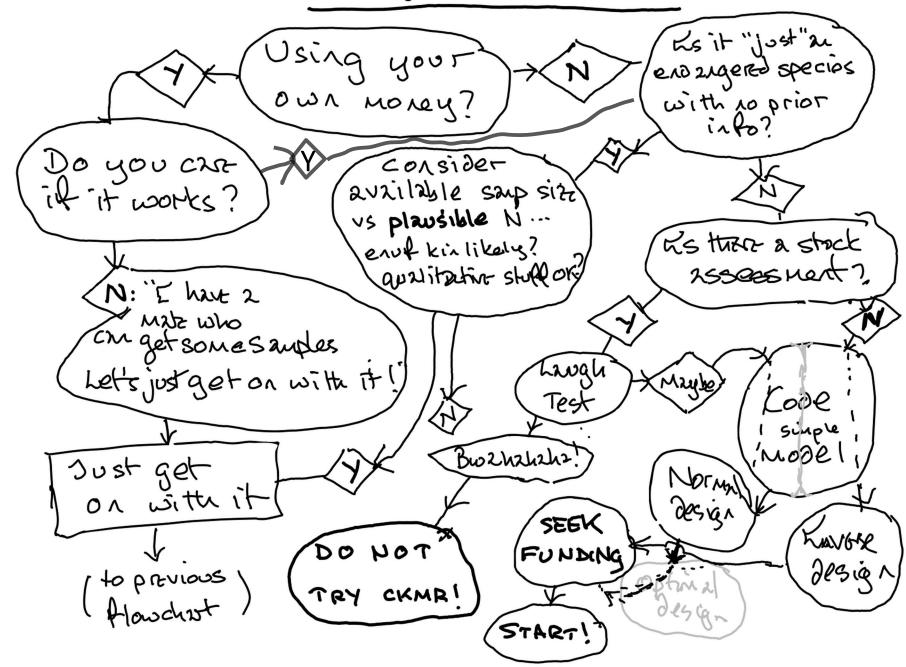
Did it work?

Did "shit happers"
happer?





DESIGN FLOW CHART



Levels of design

- 0. Qualitative considerations..?
- 1. Aim for at least XXX kin-pairs
 - by calculating E[total POPs] & E[total HSPs]
 - (the laugh test)
- 2. Variance straight from model code
- 3. Inverse design
- 4. Optimal design
- 5. "Long CKMR"
- 6. Role of simulation



Design: qualitative sampling needs

What I reckon... for Fish

1. POPs & HSPs

ie ads & "juves" how old can a "juve" be?

- 2. Accurate-enuf juve age
- 3. Ads: age or length both is best and sex, of course
- 4. Full size range of ads
- 5. Reasonable # juve cohorts
- 6. Adequate spatial coverage to allow for checks; a priori important



Design: qualitative sampling needs

What I reckon... for Fish

- 1. POPs & HSPs
 - ie ads & "juves" how old can a "juve" be?
- 2. Accurate-enuf juve age
- 3. Ads: age or length both is best and sex, of course
- 4. Full size range of ads
- 5. Reasonable # juve cohorts
- 6. Adequate spatial coverage to allow for checks; a priori important

What I reckon... for Mammals

- 1. Are you sure?
- 2. Fish version is best
- 3. At a pinch, "juve" HSPs only or even POPs only-- less likely?
- 4. Accurate-enuf juve age
- 5. Plenty of juve cohorts
 NB eg skip-spawning
- 6. Adequate spatial coverage



IJAD

KISS

FFS



IJAD

It's Just A Design...

KISS

FFS



IJAD

It's Just A Design...

KISS

Keep It Simple, Stupid!

FFS



IJAD

It's Just A Design...

KISS

Keep It Simple, Stupid!

FFS

Fast and Fairly Simple



- For a precise estimate*, must find a fair number of kin-pairs
- $\mathbb{P}\left[K_{ij} \neq \mathrm{UP}\right] \sim \bar{N}_{\mathrm{adult}}^{-1}$
- $\hat{\bar{N}}_{\rm adult} \propto (\# {\rm POPs~and/or~HSPs})^{-1}$



- For a precise estimate*, must find a fair number of kin-pairs
- $\mathbb{P}\left[K_{ij} \neq \mathrm{UP}\right] \sim \bar{N}_{\mathrm{adult}}^{-1}$
- $\hat{N}_{\rm adult} \propto (\# {\rm POPs \ and/or \ HSPs})^{-1}$
- #(POPs and/or HSPs) ~ Poisson; so need at least 50 for good CV



- For a precise estimate*, must find a fair number of kin-pairs
- $\mathbb{P}\left[K_{ij} \neq \mathrm{UP}\right] \sim \bar{N}_{\mathrm{adult}}^{-1}$
- $\hat{N}_{\rm adult} \propto (\# {\rm POPs \ and/or \ HSPs})^{-1}$
- #(POPs and/or HSPs) ~ Poisson; so need at least 50 for good CV
- Sample sizes: m_z with covariate z
- Group "alike" comparisons (same z, z')



- For a precise estimate*, must find a fair number of kin-pairs
- $\mathbb{P}\left[K_{ij} \neq \mathrm{UP}\right] \sim \bar{N}_{\mathrm{adult}}^{-1}$
- $\hat{\bar{N}}_{\rm adult} \propto (\# {\rm POPs \ and/or \ HSPs})^{-1}$
- #(POPs and/or HSPs) ~ Poisson; so need at least 50 for good CV



- For a precise estimate*, must find a fair number of kin-pairs
- $\mathbb{P}\left[K_{ij} \neq \mathrm{UP}\right] \sim \bar{N}_{\mathrm{adult}}^{-1}$
- $\hat{N}_{\rm adult} \propto (\# {\rm POPs \ and/or \ HSPs})^{-1}$
- #(POPs and/or HSPs) ~ Poisson; so need at least 50 for good CV

```
• Sample sizes: m_z with covariate z
```

Wanna get 50–100

• Group "alike" comparisons (same z, z')

Each comp has prob $^{\circ}O(1/N)$

guess at demographic params

m samples, so $\sim m^2$ comps

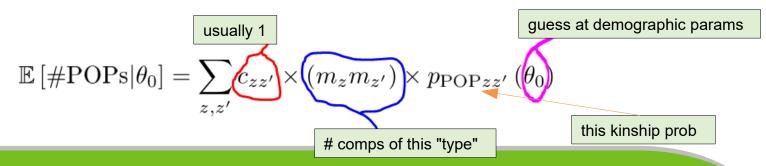
... so
$$m^2$$
 * "const" / $N = 50-100$

this kinship prob

... so m ="const (a different one)" * sqrt(N)



- For a precise estimate*, must find a fair number of kin-pairs
- $\mathbb{P}\left[K_{ij} \neq \mathrm{UP}\right] \sim \bar{N}_{\mathrm{adult}}^{-1}$
- $\hat{N}_{\rm adult} \propto (\# {\rm POPs \ and/or \ HSPs})^{-1}$
- #(POPs and/or HSPs) ~ Poisson; so need at least 50 for good CV
- Sample sizes: m_z with covariate z
- Group "alike" comparisons (same z, z')





"If we sample X of these and Y of those--- will we get enuf kin?"

Software microscoping::ckmr_laugh_test for stock-assessed

It's rough--- but it's ready.



"If we sample X of these and Y of those--- will we get enuf kin?"

Software microscoping::ckmr_laugh_test for stock-assessed

It's rough--- but it's ready.

"PASSING THE LAUGH TEST" IS NOT "DOING A DESIGN"



CKMR design: total Exp[Kin] is not enough

Even if you get lots of kin-pairs, does not guarantee good CV

- depends on covars
- and measuring stuff adequately!



CKMR design: total Exp[Kin] is not enough

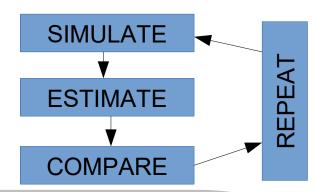
Even if you get lots of kin-pairs, does not guarantee good CV

- depends on covars
- and measuring stuff adequately!

- To properly evaluate a design: choose a goal $g(\theta)$ e.g. trend in biomass
 - check that sample sizes $\{m_{z\in\mathcal{Z}}\}$ will give low enough $\mathbb{V}\left[g(\hat{\theta})\right]$

"Generic" process for evaluation:

That's a **lot** of work !!





- Big populations, sparse sampling: pairwise comps independent
- Each pair comp is Poisson: expected Fisher Info is

$$H(z, z') = 4 \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right] \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right]^{\top}$$

$$H = H_0 + \sum_{z, z'} m_z m_{z'} H(z, z')$$

$$\mathbb{V}\left[g\left(\hat{\theta}\right)\right] \approx \left[\frac{dg}{d\theta} \right]^{\top} H^{-1} \left[\frac{dg}{d\theta} \right]$$

Quadratic dependence on sample size

Numerical derivatives are OK for p and q

NO simulation; NO estimation;

NO repetition!

Other data: priors into H_0 ; pure multinomials (age samples)

What on does all that mean?! pairwise comps independent

• Fach pair comp is Poisson: expected Fisher Info is Well, you just need:

$$H(z, z') = 4 \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right] \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right]^{\top}$$

$$H = H_0 + \sum_{z, z'} m_z m_{z'} H(z, z')$$

$$\mathbb{V}\left[g\left(\hat{\theta}\right)\right] \approx \left[\frac{dg}{d\theta} \right]^{\top} H^{-1} \left[\frac{dg}{d\theta} \right]$$

Quadratic dependence on sample size

Numerical derivatives are OK for p and g

NO simulation; NO estimation; NO repetition!

Other data: priors into H_0 ; pure multinomials (age samples)

What on does all that mean?! pairwise comps independent

• Fach pair comp is Poisson: expected Fisher Info is Well, you just need:

$$H(z, z') = 4 \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right] \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right]^{\top}$$

- to code the lglk you expect to use for real but you can take shortcuts !

on sample size

$$\mathbb{V}\left[g\left(\hat{\theta}\right)\right] \approx \left[\frac{dg}{d\theta}\right]^{\top} H^{-1} \left[\frac{dg}{d\theta}\right]$$

Numerical derivatives are OK for p and g

NO simulation; NO estimation;

NO repetition!

What on does all that mean?! pairwise comps independent

• Fach pair comp is Poisson: expected Fisher Info is Well, you just need:

$$H(z, z') = 4 \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right] \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right]^{\top}$$

- to code the lglk you expect to use for real but you can take shortcuts!
 prior guesstimates of pop dyn stuff eg from stock assessment

$$\mathbb{V}\left[g\left(\hat{\theta}\right)\right] \approx \left[\frac{dg}{d\theta}\right]^{\top} H^{-1} \left[\frac{dg}{d\theta}\right]$$

Numerical derivatives are OK for p and g

NO simulation; NO estimation; NO repetition!

What on does all that mean?! pairwise comps independent

• Fach pair comp is Poisson: expected Fisher Info is Well, you just need:

$$H(z, z') = 4 \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right] \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right]$$

- to code the lglk you expect to use for real but you can take shortcuts!
- prior guesstimates of pop dyn stuff eg from stock assessment ce
- some idea of what you want to find out! dg

Numerical derivatives are OK for p and g

NO simulation; NO estimation; NO repetition!

Other data: priors into H_0 ; pure multinomials (age samples)

What on does all that mean?! pairwise comps independent

• Fach pair comp is Poisson: expected Fisher Info is Well, you just need:

$$H(z, z') = 4 \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right] \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right]^{-1}$$

- to code the Iglk you expect to use for real but you can take shortcuts!
- prior guesstimates of pop dyn stuff eg from stock assessment ce
- some idea of what you want to find out!do
- sample sizes / sampling schemes to try out

Numerical derivatives are OK for p and g

NO simulation; NO estimation; NO repetition!

Other data: $\,\,$ priors into $H_0\,$ $\,$; $\,$ pure multinomials (age samples)

What on does all that mean?! pairwise comps independent

• Fach pair comp is Poisson: expected Fisher Info is Well, you just need:

$$H(z,z')=4\begin{bmatrix}\frac{d\sqrt{p_{zz'}}}{d\theta}&\frac{d\sqrt{p_{zz'}}}{d\theta}\\ -\text{ to code the lglk you expect to use for real}\end{bmatrix} \text{ but you } \mathbf{can} \text{ take shortcuts } !$$

- prior guesstimates of pop dyn stuff eg from stock assessment ce
- some idea of what you want to find out!
- sample sizes / sampling schemes to try out

You **don't** need to *simulate*, nor to actually *fit* your model; there's a generic "glue framework" that does the maths

Other data: $\,$ priors into $H_0\,$ $\,$; $\,$ pure multinomials (age samples)

CKMR design: NAtl makos



CKMR design: NAtl makos etc

Q: But that's just under one scenario about "truth". Shouldn't I explore others?

A: Arguably, that's not really necessary...



CKMR design: Inverse design

What if no prior stock assessment?

eg SAtl makos; Blue-Eye Trevalla



Optimal design

- Everybody knows: "don't trust optimal designs"
- Not always appropriate to try

NEVERTHELESS

- it lets you know when to stop trying
- "CKMR design space" is a big place. Optimal designs are beacons
 - ie several optimal designs for different goals
- You learn a lot about where the "information" comes from



Optimal design for CKMR

$$H(z, z') = 4 \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right] \left[\frac{d\sqrt{p_{zz'}}}{d\theta} \right]^{\top}$$

$$H = H_0 + \sum_{z, z'} m_z m_{z'} H(z, z')$$

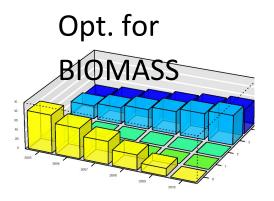
$$\mathbb{V} \left[g\left(\hat{\theta}\right) \right] \approx \left[\frac{dg}{d\theta} \right]^{\top} H^{-1} \left[\frac{dg}{d\theta} \right]$$

$$V\left(m\right) \triangleq \mathbb{V}\left[\hat{g}\left(\theta\right)|m\right]$$

- *H* is sum of outer products: closed form inverse Sherman-Woodbury
- dV/dm, d^2V/dm^2 easily found by Automatic Differentiation
- Cost constraint (or target variance for minimum cost)
- Replace V(m) by 2^{nd} order approx; solve Quadratic Program; repeat
 - reliable and quick
 - NB non-convex QP

Optimal design: example

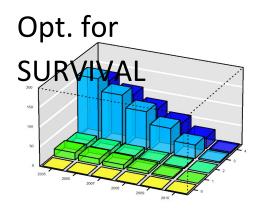
- "Fish-like": age structure, fecundity depends on age, survival depends on year
- Cross-cohort HSPs with 0-year-olds; POPs (all age classes)
- 10-year trend in abundance, 5 ages (5 fixed effects, 10 random effects)



At these two optima:

3X variance (biomass)

2X variance (survival)



- Optimal design does depend on goal
- Runtime: ~ 5 seconds



Summary

- CKMR can handle big problems (big population sizes)
 - but you'll need a lot of samples
- Bare minimum due diligence: will your design give enough kin-pairs?
 - need to compute kinship probs based on a guess at parameters
 - maybe ckmr laugh test will do...
 - or maybe you need to code up your planned lglk. If so, then...
- ... not much extra work to properly evaluate a design
 - just supply a goal function (in R is OK)
- & almost no extra work to consider optimal designs



Design in CKMR: niggling concerns laid to rest

Q: I have 1000 samples but 1000*1000/2 comparisons. Are they *really* all independent? Really?

A: Yeah pretty much, prolly.

At least, if yr popn is Big "sparse sampling"



Design in CKMR: niggling concerns laid to rest

Q: I have 1000 samples but 1000*1000/2 comparisons. Are they *really* all independent? Really?

A: Yeah pretty much, prolly.

At least, if yr popn is Big "sparse sampling"

How to approach the thought-experiment:

- think about Maternal descent Qs ie separately from P descent
- implications & chance of knowing result of "earlier" comp



Design in CKMR: niggling concerns laid to rest

Q: I have 1000 samples but 1000*1000/2 comparisons. Are they *really* all independent? Really?

A: Yeah pretty much, prolly.

At least, if yr popn is Big "sparse sampling"

How to approach the thought-experiment:

- think about Maternal descent Qs ie separately from P descent
- implications & chance of knowing result of "earlier" comp

Post hoc diagnostic: # triads etc.

Larval sampling? different, tricky; not the first resort!



"Long CKMR"

To date, fisheries interest in CKMR has come from The Desperate

- "how on earth can we ground-truth the assessment?"

Then... lots of work to get to that point.

But what happens next?!



"Long CKMR"

To date, fisheries interest in CKMR has come from The Desperate

- "how on earth can we ground-truth the assessment?"

Then... lots of work to get to that point.

But what happens next?!

CKMR is easy once you've gotten your first "N"

?Use in ongoing MPs?

Needs simulation--- can't do via nifty variance calcs



MUCH LESS THAN YOU THINK!

- You don't need simulation for most Designs
 - and you shouldn't do it because it will wa\$te time



MUCH LESS THAN YOU THINK!

- You don't need simulation for most Designs
 - and you shouldn't do it because it will wa\$te time

If you are estimating Something, and you just want to check bias:

- ... even if you do have to Simulate & Repeat
 - ... you don't have to **Estimate** each time

$$\frac{d\Lambda\left(y^{*}\right)}{d\theta}\bigg|_{\hat{\theta^{*}}} = 0$$

$$\hat{\theta}^* - \theta_0 \approx - \left[\frac{d^2 \Lambda (y^*)}{d\theta^2} \Big|_{\theta_0} \right]^{-1} \left[\frac{d \Lambda (y^*)}{d\theta} \Big|_{\theta_0} \right]$$



MUCH LESS THAN YOU THINK!

- You don't need simulation for most Designs
 - and you shouldn't do it because it will wa\$te time



MUCH LESS THAN YOU THINK!

- You don't need simulation for most Designs
 - and you shouldn't do it because it will wa\$te time
- For MSE, can just simulate "from" the CKMR model:

```
dpois() ---> qpois() ed
```

Bozo et al. could have done this (no IBM) to check Pyro Enfum



MUCH LESS THAN YOU THINK!

- You don't need simulation for most Designs
 - and you shouldn't do it because it will wa\$te time
- For MSE, can just simulate "from" the CKMR model:

```
dpois() ---> qpois() ed
```

Bozo et al. could have done this (no IBM) to check Pyro Enfum

- IBM sim is required if you plan to fit a very dicey model...
- CKMR IBMs are somewhat painful
 - tho packages can help: fishSim, kinsimmer, CKMRsim

