

1. Let G be the group with presentation $G = \langle a, b, c \mid a^3 = b, ac = ca \rangle$.

(a) Simplify the word $a^4 c^2 a^2 b^{-3} cb$.

(b) Show that $a^{-1}c^{-1} = c^{-1}a^{-1}$

(c) Simplify the word $a^{-9}c^{-1}b^2c^2a$.

(d) Prove that the group is abelian. [Hint: It suffices to argue that $ab = ba$ and $bc = cb$.]

2. Let X be the set $X = \{1, 2, 3\}$.

(a) Give an example of two different functions from X to X .

(b) How many functions are there from X to X ?

(c) How many one-to-one correspondences are there from X to X ?

3. As before, let $X = \{1, 2, 3\}$. Let $f, g : X \rightarrow X$ where $f(1) = 2, f(2) = 3, f(3) = 1$ and $g(1) = 3, g(2) = 2$ and $g(3) = 1$.

(a) Find $(f \circ g)(i)$ for $i = 1, 2, 3$

(b) Find $(g \circ f)(i)$ for $i = 1, 2, 3$

(c) What is f^{-1} ? Describe as above.

(d) What is g^{-1} ? Describe as above.

(e) What is $f \circ f \circ f$?