# 0904 Class Activity

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## 1. $K_{m,n}$ 의 edge의 개수는?

Proof) The number of edges in  $K_{m,n}$  is mn. We want to use the handshaking lemma to prove this. First, let V, E be the vertex set and the edge set of the  $K_{m,n}$ . By definition of the  $K_{m,n}$ , we can partition V into two disjoint vertex sets  $V_1, V_2$ ;  $|V_1| = m, |V_2| = n$ . Since each vertex in  $V_1$  is connected to all of the vertices in  $V_2, v \in V_1$  has degree n. Similarly,  $v \in V_2$  has degree m. Hence,  $\sum_{v \in V} deg(v) = \sum_{v \in V_1} deg(v) + \sum_{v \in V_2} deg(v) = \sum_{v \in V_1} n + \sum_{v \in V_2} m = mn + nm = 2mn = 2|E|$ . Therefore, |E| = mn.

## 2. $K_{m,n}$ 이 regular graph가 되기 위한 필요충분조건은?

All vertices in a regular graph have the same degree. Let  $V = V_1 \cup V_2$ ;  $V_1 \cap V_2 \neq \emptyset$ . As I wrote above,  $v \in V_1$  has degree n and  $v \in V_2$  has degree m. So, m = n has to be satisfied to  $K_{m,n}$  be a regular graph, and vice versa.