

# Computing the controller $H_r(s)$ using the logarithmic diagrams

## Compute and declare my transfer function

The transfer function has the following form:

$$H_f(s) = \frac{K_f}{s(T_f s + 1)}$$

Knowing that my values are  $K_f = 4$  and  $T_f = 8$ , the function becomes:

$$H_f(s) = \frac{4}{s(8s + 1)}$$

I declare my transfer function in code:

```
Hf = tf(4,[8 1 0])
```

```
Hf =
```

$$\frac{4}{8s^2 + s}$$

```
Continuous-time transfer function.
```

The controllers that will be computed need to satisfy the following specifications:

$$\varepsilon_{\text{stp}} = 0$$

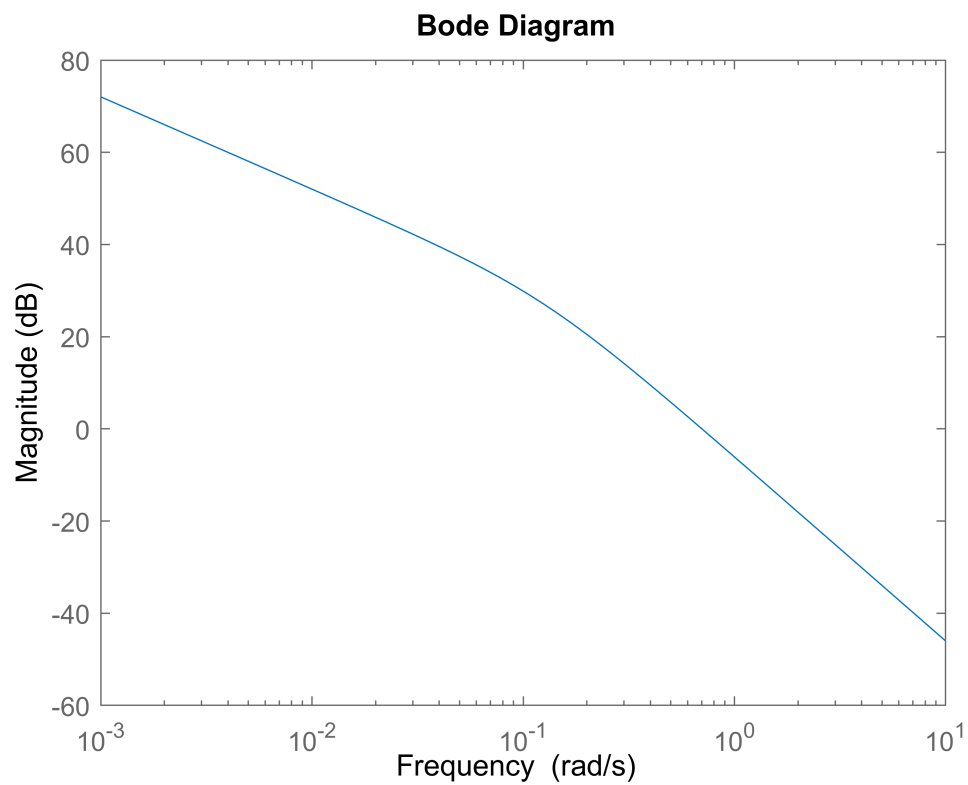
$$t_r^* \leq 5 \text{ sec}$$

$$\sigma^* \leq 10\%$$

$$c_v \geq 3$$

$$\Delta w_b^* \leq 15 \frac{\text{rad}}{\text{sec}}$$

```
bodemag(Hf)
```

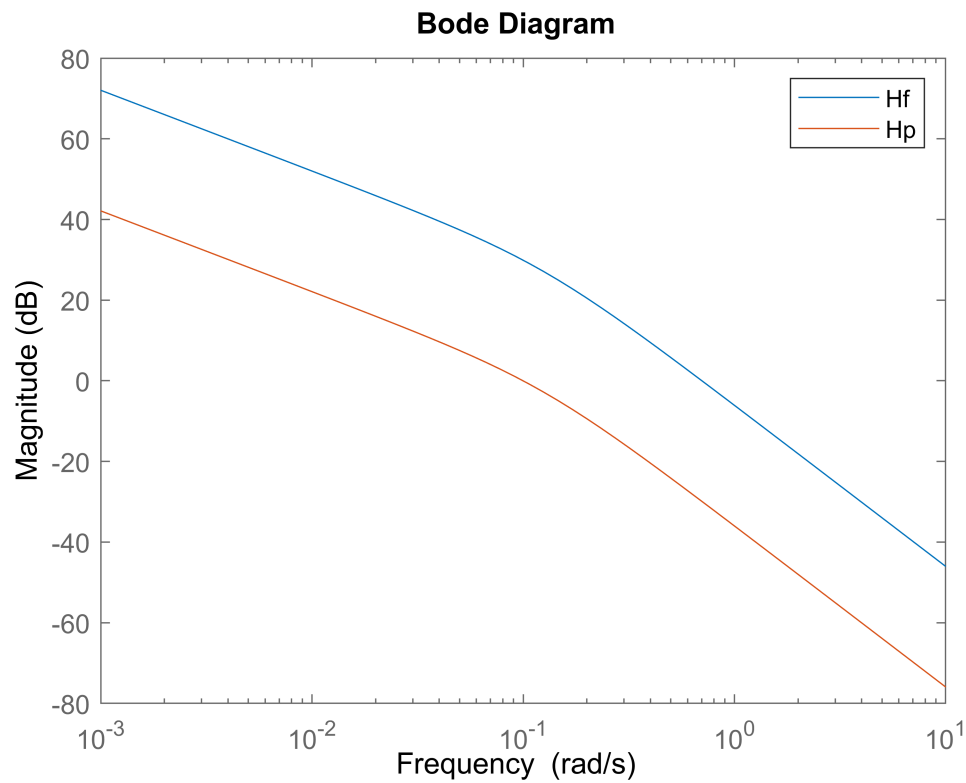


## Computing the P controller

```

Wco = 0.7; % cut-off frequency
Wc = 1/8; % corner frequency
o = 0.1; % overshoot
dr = abs(log(o))/sqrt(log(o)^2+pi^2); % damping ratio
A = 1/4/dr^2;
N = 20*log10(A);
F = 27;
Vr = 10^((N-F)/20);
figure;
hold on;
bodemag(Hf)
bodemag(Vr*Hf)
hold off;
legend("Hf", "Hp");

```



```
Wco = 0.1;
Wn = 2*dr*Wco;
tr = 4/dr/Wn % settling time
```

```
tr = 57.2305
```

$t_r \leq 5$  "False"

```
Cv = -36 % the velocity coefficient read at w=1
```

```
Cv = -36
```

$c_v \geq 3$  "False"

```
deltaWb = Wco % the bandwidth
```

```
deltaWb = 0.1000
```

$\Delta w_b \leq 15$  "True"

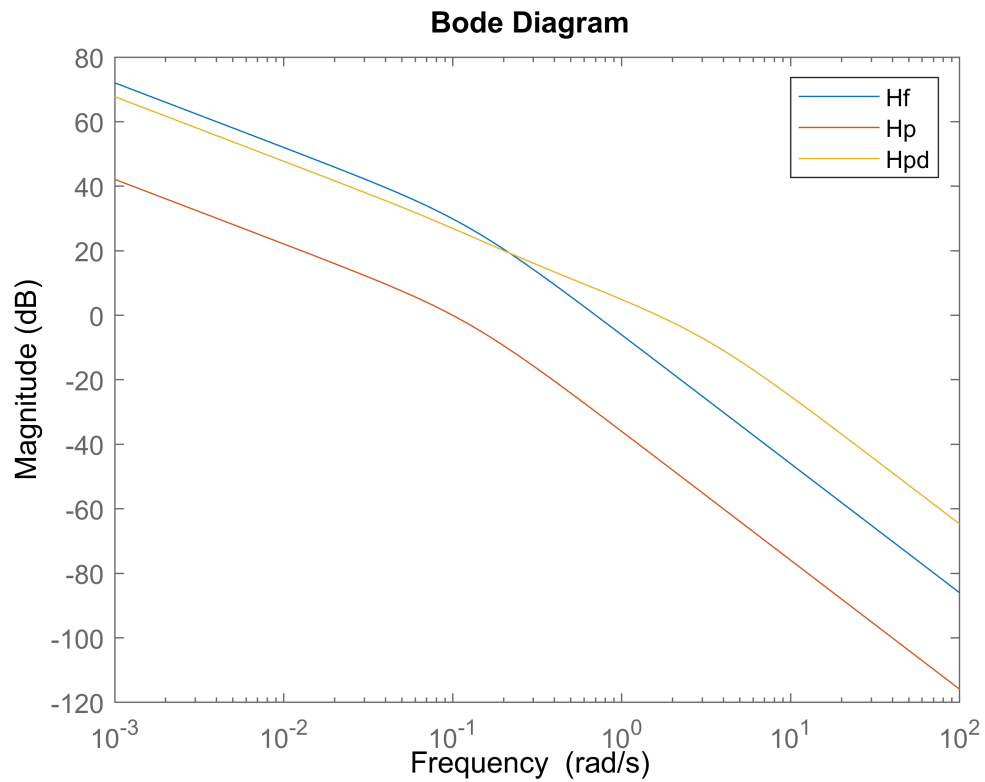
## Computing the PD controller

```
trstar = 3;
Wco2 = 2/dr^2/trstar;
Wco = 2/dr^2/tr;
Vr2 = Vr*Wco2/Wco;
td = 6;
```

```

Tn = td*trstar/tr;
figure;
hold on;
bodemag(Hf)
bodemag(Vr*Hf)
bodemag(Vr2*Hf*tf([td 1],[Tn 1]))
hold off;
legend("Hf","Hp","Hpd");

```



$c_v = 4.8$  % the velocity coefficient read at  $w=1$

$c_v = 4.8000$

$c_v \geq 3$  "True"

```

figure;
% step(feedback(Vr2*Hf*tf([td 1],[Tn 1]),1))

```

