The importance of sample size & good study design

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The most important aspect of a statistical analysis is not what you do with the data, it's what data you use

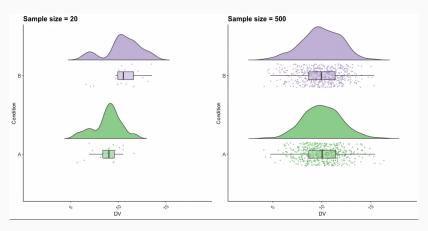
The importance of sample size

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The importance of sample size

- · Many studies have too low sample sizes.
- Low sample sizes miss subtle effects, but also **prone to bias**.

Low sample sizes very sensitive to random noise



https://twitter.com/ajstewart_lang/status/1020038488278945797

Low sample sizes may bias inferences about population



http://statisticalgate.com/regression-simulation/

Low sample sizes may bias inferences

See The evolution of correlations

Stopping rules

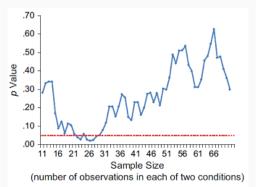


Fig. 2. Illustrative simulation of p values obtained by a researcher who continuously adds an observation to each of two conditions, conducting a t test after each addition. The dotted line highlights the conventional significance criterion of $p \le .05$.

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- · Plan to have at least 10-30 observations per predictor.
- Complex models (w/ many predictors, interactions etc) require high sample sizes.

Calculating sample size for Gaussian (Normal) response model:

- · expected mean: 30
- expected sd: 10
- 10 parameters (predictors)
- · expected R-squared: 0.2

```
library(pmsampsize)
pmsampsize(type = "c", parameters = 10, intercept = 30, sd = 10, rsquared = 0.2)
```

NB: Assuming 0.05 acceptable difference in apparent & adjusted R-squared
NB: Assuming MMOE <= 1.1 in estimation of intercept & residual standard deviation
SPP - Subjects per Predictor Parameter

```
Samp size Shrinkage Parameter Rsq SPP
Criteria 1
             313
                    0.900
                             10 0.2 31.3
Criteria 2
          161
                   0.827 10 0.2 16.1
Criteria 3 244 0.876 10 0.2 24.4
         313 0.900
                             10 0.2 31.3
Criteria 4*
Final
                   0.900
                             10 0.2 31.3
            313
```

Minimum sample size required for new model development based on user inputs = 313

```
* 95% CI for intercept = (29.69, 30.31), for sample size n = 313
```

Calculating sample size for binary response model:

- · expected prevalence: 0.1
- 20 parameters (predictors)
- · expected R-squared: 0.2

```
library(pmsampsize)
pmsampsize(type = "b", parameters = 20, prevalence = 0.1, rsquared = 0.2)
NB: Assuming 0.05 acceptable difference in apparent & adjusted R-squared
NB: Assuming 0.05 margin of error in estimation of intercept
NB: Events per Predictor Parameter (EPP) assumes prevalence = 0.1
          Samp size Shrinkage Parameter Rsg Max Rsg EPP
Criteria 1
               796
                       0.900
                                   20 0.2 0.48 3.98
                    0.893 20 0.2 0.48 3.69
Criteria 2
               738
Criteria 3
               139 0.900 20 0.2 0.48 0.70
Final
               796 0.900
                                 20 0.2 0.48 3.98
```

Minimum sample size required for new model development based on user inputs = 796, with 80 events (assuming an outcome prevalence = 0.1) and an EPP = 3.98