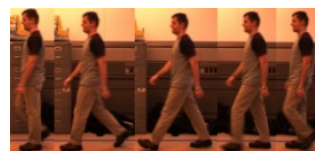
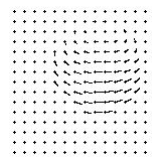


Motion Analysis: Optical Flow

Finally: Motion and tracking

Tracking objects, video
analysis, low level motion



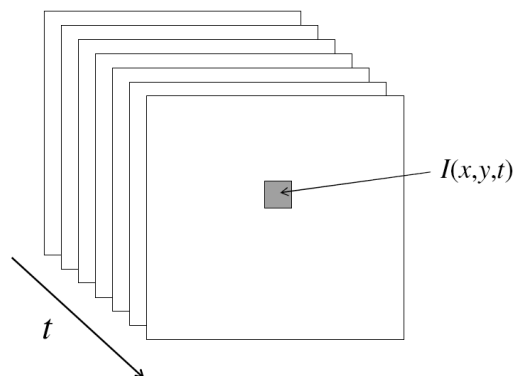
Tomas Izo

Uses of motion

- Estimating 3D structure
- Segmenting objects based on motion cues
- Learning dynamical models
- Recognizing events and activities
- Improving video quality (motion stabilization)

Video

- A video is a sequence of frames captured over time
- Now our image data is a function of space (x, y) and time (t)

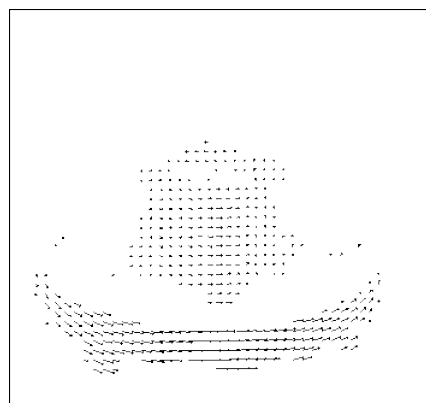
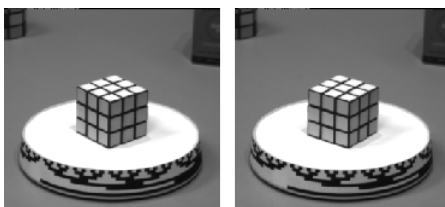


Lecture's goals

- Motion Analysis
 - Optical flow

Motion field

- The motion field is the projection of the 3D scene motion into the image



Motion field + camera motion

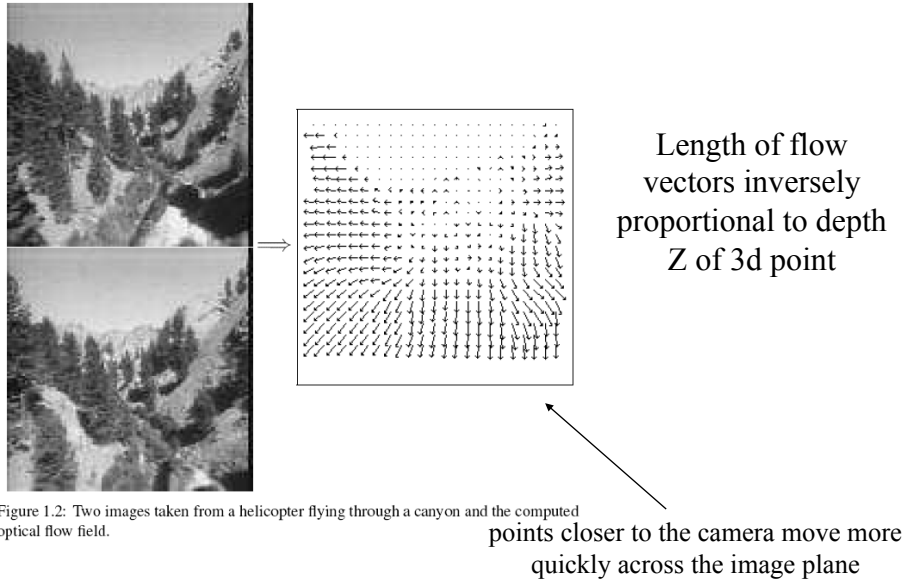


Figure 1.2: Two images taken from a helicopter flying through a canyon and the computed optical flow field.

Figure from Michael Black, Ph.D. Thesis

Optical Flow (Image Flow)

- Estimate velocity based on brightness pattern
- Originates from early psychological work on human vision
 - Cues used by pilots in landing aircraft.
- Local estimates of the velocity of the brightness field
 - Do not require image structure
 - Dense velocity maps

Motion of the Brightness Pattern

- Motion field
 - Velocity vector at each point in the scene
- Optical Flow
 - Apparent motion of the brightness pattern
 - Components u , v at each point on the image
- Mostly they correspond

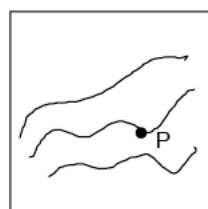


Image at t

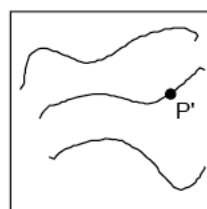


Image at $t + \Delta t$

Correspondence Problem

The Optical Flow Equation

$$I(x, y, t) = I(x + dx, y + dy, t + dt)$$

Image structure doesn't change, just moves

$$I(x + dx, y + dy, t + dt) = I(x, y, t) + \frac{\partial I}{\partial x} dx + \frac{\partial I}{\partial y} dy + \frac{\partial I}{\partial t} dt + (h.o.t)$$

Taylor expansion

$$\frac{\partial I}{\partial x} dx + \frac{\partial I}{\partial y} dy + \frac{\partial I}{\partial t} dt = 0$$

$$\frac{\partial I}{\partial x} \frac{dx}{dt} + \frac{\partial I}{\partial y} \frac{dy}{dt} + \frac{\partial I}{\partial t} = 0$$

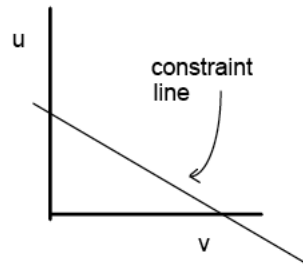
$$\frac{\partial I}{\partial x} u + \frac{\partial I}{\partial y} v + \frac{\partial I}{\partial t} = 0 \quad \text{Optical Flow Equation}$$

Solving Optical Flow

$$\frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v + \frac{\partial I}{\partial t} = 0$$

$\frac{\partial I}{\partial x}$ Image gradient
 $\frac{\partial I}{\partial y}$ Image gradient
 $\frac{\partial I}{\partial t}$ Rate of change of brightness with time

Equation of straight line



No unique solution for u and v

Constrained solution

- Smoothness
 - \blacksquare Should be small $\longrightarrow \left\{ \begin{array}{l} u_x = \frac{\partial u}{\partial x}; \quad u_y = \frac{\partial u}{\partial y} \\ v_x = \frac{\partial v}{\partial x}; \quad v_y = \frac{\partial v}{\partial y} \end{array} \right.$
- Optical Flow constraint $\frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v + \frac{\partial I}{\partial t} = 0$
- Minimise $\longrightarrow \left\{ \begin{array}{l} \sum \sum (u_x^2 + u_y^2) + (v_x^2 + v_y^2) \\ \sum \sum \left(\frac{\partial I}{\partial x}u + \frac{\partial I}{\partial y}v + \frac{\partial I}{\partial t} \right) \end{array} \right.$

Optical Flow Due to Camera Translation

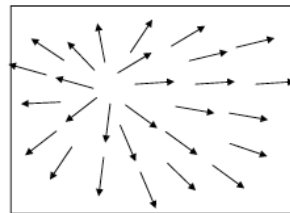


Intervening frames

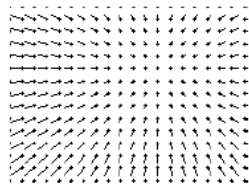


Focus of Expansion

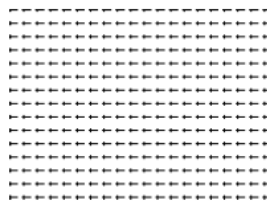
Defines instantaneous direction
of camera motion



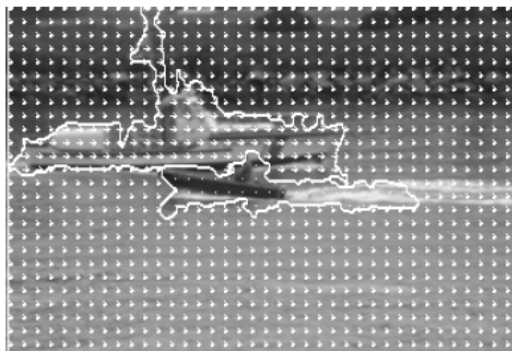
Optical Flow



Focus of contraction



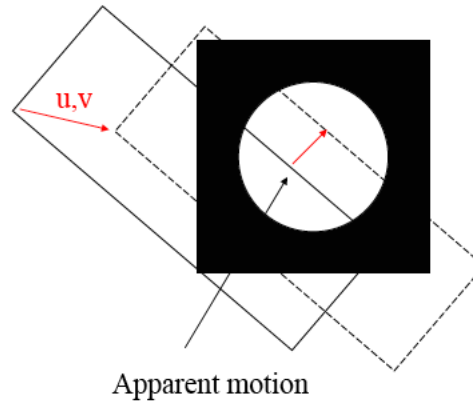
Panning



Motion-based segmentation.
Camera panning left (following smaller boat)
Larger boat moving right.

The Aperture Problem

- Using local information (e.g. derivatives) we can only measure velocity vector *normal to local image gradient*.
- Need to apply further constraints
 - e.g. smoothness
 - Nearby points should have similar velocities



Optical Flow

When/where does this break down?

In what situations does the displacement of pixel patches not represent physical movement of points in space?

A uniform rotating sphere

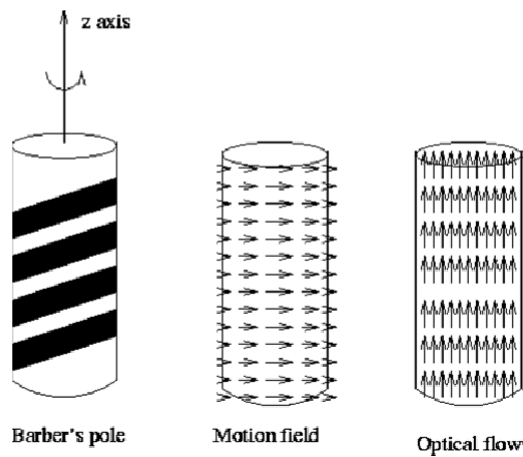
Nothing seems to move, yet it is rotating

Changing directions or intensities of lighting can make things seem to move

For example, if the specular highlight on a rotating sphere moves.

Aperture Problem

Barber pole illusion



Tracking

- Identify significant points
- Track from frame to frame
- Aperture problem avoided if we use identifiable structure.
- Simplest to match structure using cross-correlation
- No epipolar constraint
- May be able to predict motion.

