

HW3

1. $A = [6, 8, 6, 10, 12, 9, 15, 13, 14, 19, 18, 17, 16]$

2. a. $A = [10, 3, 9, 4, 8, 5, 7, 6]$, $p = 1$, $r = 8$, $k = 2$
 $A = [3, 4, 5, 6, 9, 8, 7, 10]$, $p = 1$, $r = 8$, $k = 2$
 $A = [3, 4, 5, 6, 8, 9, 7, 10]$, $p = 1$, $r = 8$, $k = 2$
 $A = [3, 4, 5, 6, 8, 9, 7, 10]$

- b. 1. The first base occurs when the starting and ending indexes are equal.
Executed steps: step 1 (passes).
 $T(\text{first base case}) = 7$

2. The second base case occurs when k th smallest number is equal to the pivotDistance, so then the number at the pivot index is returned, $A[q]$.
Executed steps: step 1 (fails), step 2, step 3, step 4 (passes), step 5.
 $T(\text{second base case}) = 20n + 17$

3. Executed steps: step 1 (fails), step 2, step 3, step 4 (fails), step 6, step 7 (executed if step 6 passes), step 8 (executed if step 6 fails).
Worst case: $T(n) = (T(n-1) (20n + 16 + T(n-1))) + 7$
Best case (one element): $T(n) = 7$
Best case (sorted array): $T(n) = 20n + 7$

3. A = [19, 6, 10, 7, 16, 17, 13, 14, 12, 9]

C =

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	0	0	0	0	1	1	0	1	1	0	1	1	1	0	1	1	0	1

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0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	0	0	0	0	1	2	2	3	4	4	5	6	7	7	8	9	9	10

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0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	0	0	0	0	0	1	2	2	3	4	4	5	6	7	7	8	9	9

B = [6, 7, 9, 10, 12, 13, 14, 16, 17, 19]

4. 1. [3210, 4321, 2345, 4567, 5678]
2. [3210, 4321, 2345, 4567, 5678]
3. [3210, 4321, 2345, 4567, 5678]
4. [2345, 3210, 4321, 4567, 5678]

5. If $\text{length}(A)=15$
Bucket0: $0..1/15$
Bucket1: $1/15..2/15$
Bucket2: $2/15..3/15$
Bucket3: $3/15..4/15$
Bucket4: $4/15..5/15$
Bucket5: $5/15..6/15$
Bucket6: $6/15..7/15$
Bucket7: $7/15..8/15$
Bucket8: $8/15..9/15$
Bucket9: $9/15..10/15$
Bucket10: $10/15..11/15$
Bucket11: $11/15..12/15$
Bucket12: $12/15..13/15$
Bucket13: $13/15..14/15$
Bucket14: $14/15..15/15$

If $\text{length}(A)=n$
Bucket0: $0..1/n$
Bucket1: $1..2/n$
Bucket(n-2): $n-2/n..n-1/n$
Bucket(n-1): $n-1/n..n/n$

6. a.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	1	14	3	3	3	1	1	8	3	3	3	3	1	14	18	16	19	20	1

b.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
-3	1	14	3	3	3	1	1	8	3	3	3	3	1	14	1	16	16	16	16

c.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
3	1	-20	3	3	3	1	1	8	3	3	3	3	3	14	3	16	16	16	16

d.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	1	14	3	3	3	1	1	8	3	3	3	3	1	14	1	1	1	1	1

7.

