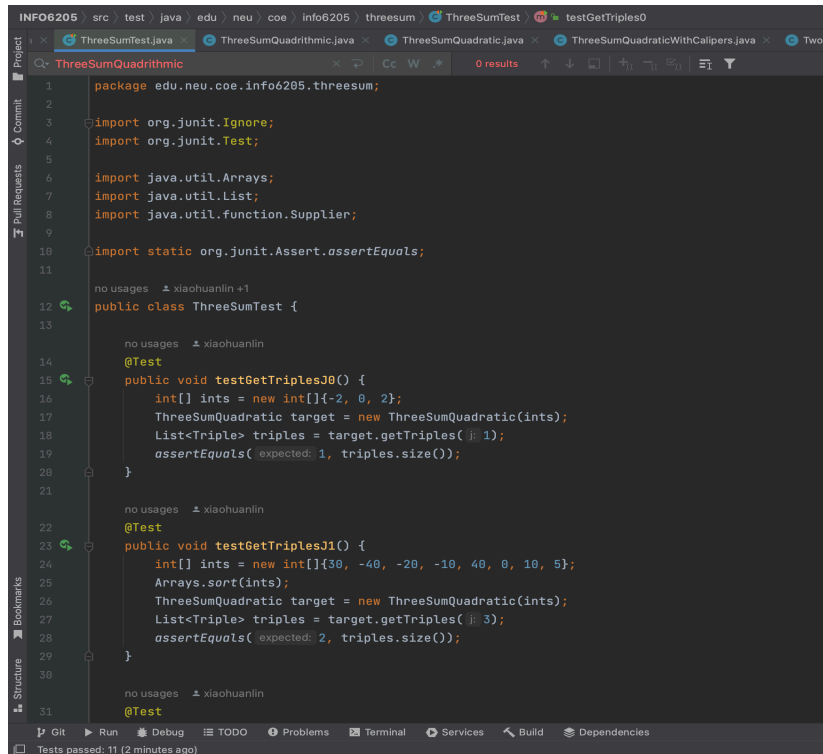


# Assignment 2 (3-SUM)

## 1. Evidence

Screenshots of all running unit tests



```
package edu.neu.coe.info6205.threesum;

import org.junit.Ignore;
import org.junit.Test;

import java.util.Arrays;
import java.util.List;
import java.util.function.Supplier;

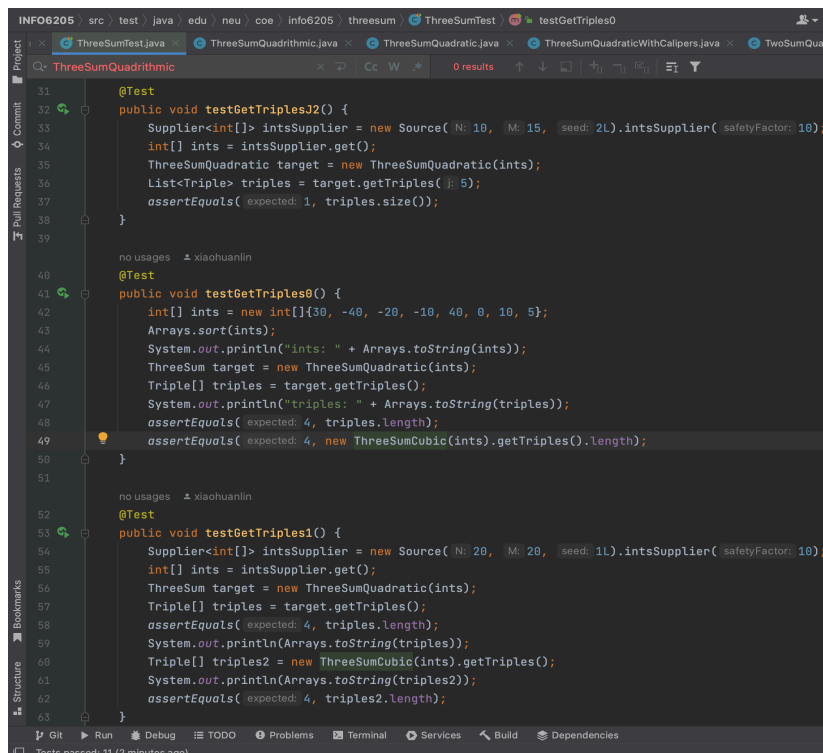
import static org.junit.Assert.assertEquals;

no usages 1 xiaohuanlin +1
public class ThreeSumTest {

    no usages 1 xiaohuanlin
    @Test
    public void testGetTriplesJ0() {
        int[] ints = new int[]{-2, 0, 2};
        ThreeSumQuadratic target = new ThreeSumQuadratic(ints);
        List<Triple> triples = target.getTriples(1);
        assertEquals( expected: 1, triples.size());
    }

    no usages 1 xiaohuanlin
    @Test
    public void testGetTriplesJ1() {
        int[] ints = new int[]{30, -40, -20, -10, 40, 0, 10, 5};
        Arrays.sort(ints);
        ThreeSumQuadratic target = new ThreeSumQuadratic(ints);
        List<Triple> triples = target.getTriples(3);
        assertEquals( expected: 2, triples.size());
    }

    no usages 1 xiaohuanlin
    @Test
```



```
    @Test
    public void testGetTriplesJ2() {
        Supplier<int[]> intsSupplier = new Source( N: 10, M: 15, seed: 2L).intsSupplier( safetyFactor: 10);
        int[] ints = intsSupplier.get();
        ThreeSumQuadratic target = new ThreeSumQuadratic(ints);
        List<Triple> triples = target.getTriples(5);
        assertEquals( expected: 1, triples.size());
    }

    no usages 1 xiaohuanlin
    @Test
    public void testGetTriples0() {
        int[] ints = new int[]{30, -40, -20, -10, 40, 0, 10, 5};
        Arrays.sort(ints);
        System.out.println("ints: " + Arrays.toString(ints));
        ThreeSum target = new ThreeSumQuadratic(ints);
        Triple[] triples = target.getTriples();
        System.out.println("triples: " + Arrays.toString(triples));
        assertEquals( expected: 4, triples.length);
        assertEquals( expected: 4, new ThreeSumCubic(ints).getTriples().length);
    }

    no usages 1 xiaohuanlin
    @Test
    public void testGetTriples1() {
        Supplier<int[]> intsSupplier = new Source( N: 20, M: 20, seed: 1L).intsSupplier( safetyFactor: 10);
        int[] ints = intsSupplier.get();
        ThreeSum target = new ThreeSumQuadratic(ints);
        Triple[] triples = target.getTriples();
        assertEquals( expected: 4, triples.length);
        System.out.println(Arrays.toString(triples));
        Triple[] triples2 = new ThreeSumCubic(ints).getTriples();
        System.out.println(Arrays.toString(triples2));
        assertEquals( expected: 4, triples2.length);
    }
}
```

```
INFO6205 - ThreeSumTest.java
INFO6205 | src | test | java | edu | neu | coe | info6205 | threesum | ThreeSumTest | testGetTriples0
ThreeSumTest.java | ThreeSumQuadrithmic.java | ThreeSumQuadratic.java | ThreeSumQuadraticWithCalipers.java | TwoSumQuadratic.java
ThreeSumQuadrithmic
no usages | xiaohuanlin
@Test
public void testGetTriples1() {
    Supplier<int[]> intsSupplier = new Source( N: 20, M: 20, seed: 1L).intsSupplier( safetyFactor: 10);
    int[] ints = intsSupplier.get();
    ThreeSum target = new ThreeSumQuadratic(ints);
    Triple[] triples = target.getTriples();
    assertEquals( expected: 4, triples.length);
    System.out.println(Arrays.toString(triples));
    Triple[] triples2 = new ThreeSumCubic(ints).getTriples();
    System.out.println(Arrays.toString(triples2));
    assertEquals( expected: 4, triples2.length);
}

@Test
public void testGetTriples2() {
    Supplier<int[]> intsSupplier = new Source( N: 10, M: 15, seed: 3L).intsSupplier( safetyFactor: 10);
    int[] ints = intsSupplier.get();
    ThreeSum target = new ThreeSumQuadratic(ints);
    System.out.println(Arrays.toString(ints));
    Triple[] triples = target.getTriples();
    System.out.println(Arrays.toString(triples));
    assertEquals( expected: 1, triples.length);
    assertEquals( expected: 1, new ThreeSumCubic(ints).getTriples().length);
}

no usages | xiaohuanlin
Git | Run | Debug | TODO | Problems | Terminal | Services | Build | Dependencies
Tests passed: 11 (3 minutes ago)
```

```
INFO6205 - ThreeSumTest.java
INFO6205 | src | test | java | edu | neu | coe | info6205 | threesum | ThreeSumTest | testGetTriples2
ThreeSumTest.java | ThreeSumQuadrithmic.java | ThreeSumQuadratic.java | ThreeSumQuadraticWithCalipers.java | TwoSumQuadratic.java
ThreeSumQuadrithmic
no usages | xiaohuanlin
@Test
public void testGetTriplesC0() {
    int[] ints = new int[]{30, -40, -20, -10, 40, 0, 10, 5};
    Arrays.sort(ints);
    System.out.println("ints: " + Arrays.toString(ints));
    ThreeSum target = new ThreeSumQuadratic(ints);
    Triple[] triples = target.getTriples();
    System.out.println("triples: " + Arrays.toString(triples));
    assertEquals( expected: 4, triples.length);
    assertEquals( expected: 4, new ThreeSumCubic(ints).getTriples().length);
}

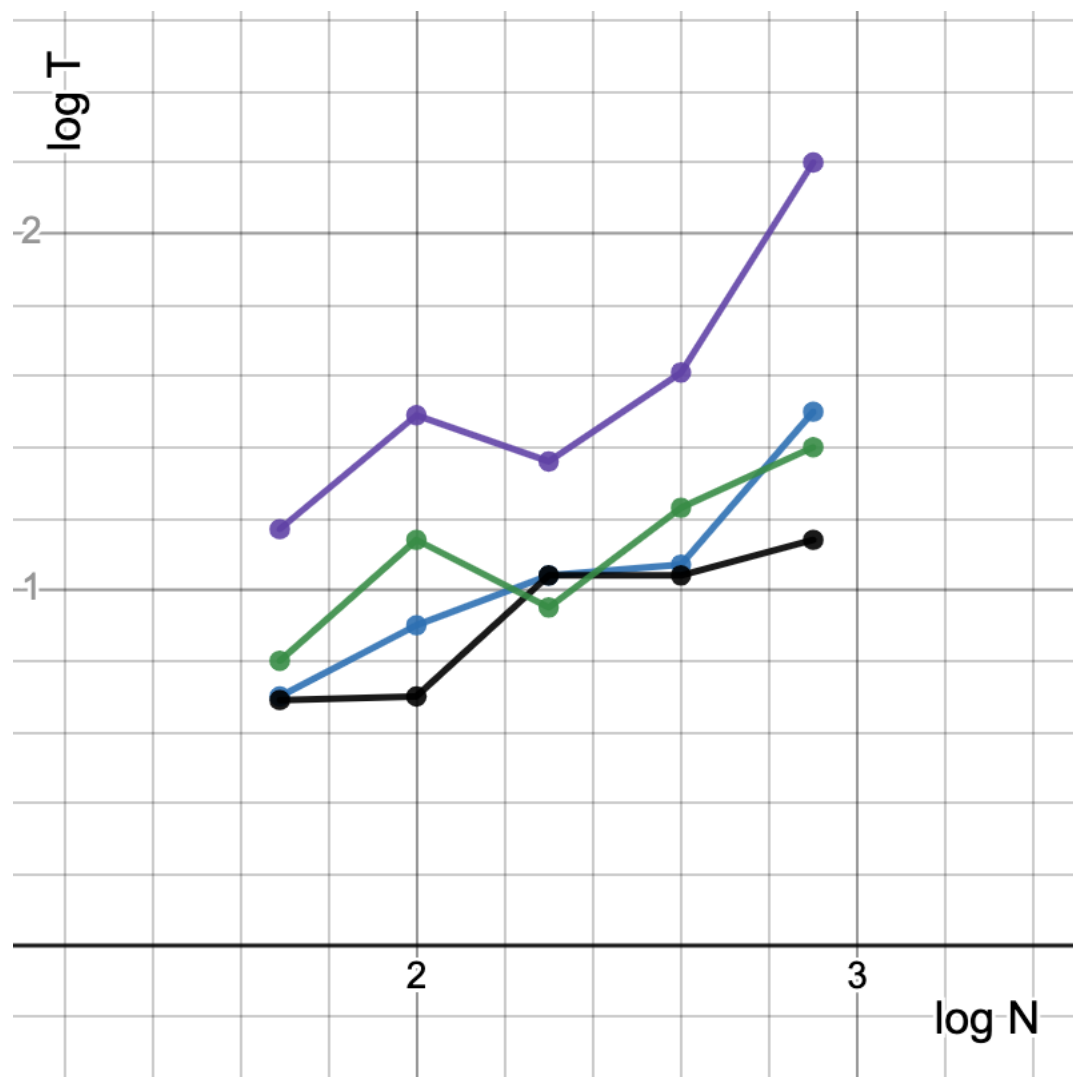
@Test
public void testGetTriplesC1() {
    Supplier<int[]> intsSupplier = new Source( N: 20, M: 20, seed: 1L).intsSupplier( safetyFactor: 10);
    int[] ints = intsSupplier.get();
    ThreeSum target = new ThreeSumQuadraticWithCalipers(ints);
    Triple[] triples = target.getTriples();
    assertEquals( expected: 4, triples.length);
    System.out.println(Arrays.toString(triples));
    Triple[] triples2 = new ThreeSumCubic(ints).getTriples();
    System.out.println(Arrays.toString(triples2));
    assertEquals( expected: 4, triples2.length);
}

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Git | Run | Debug | TODO | Problems | Terminal | Services | Build | Dependencies
Tests passed: 11 (4 minutes ago)
```

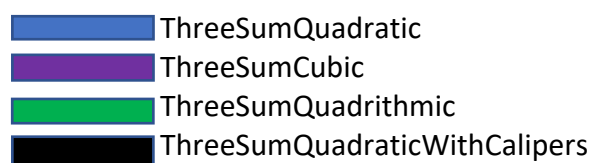
```
INFO6205 src test java edu neu coe info6205 threesum ThreeSumTest testGetTriplesC1
ThreeSumTest.java ThreeSumQuadratic.java ThreeSumQuadraticWithCalipers.java TwoSumQuad
ThreeSumQuadraticWithCalipers.java
0 results
124
125 @Test
126 public void testGetTriplesC2() {
127     Supplier<int[]> intsSupplier = new Source( N: 10, M: 15, seed: 3L).intsSupplier( safetyFactor: 10);
128     int[] ints = intsSupplier.get();
129     ThreeSum target = new ThreeSumQuadraticWithCalipers(ints);
130     System.out.println(Arrays.toString(ints));
131     Triple[] triples = target.getTriples();
132     System.out.println(Arrays.toString(triples));
133     assertEquals( expected: 1, triples.length);
134     assertEquals( expected: 1, new ThreeSumCubic(ints).getTriples().length);
135 }
no usages xiaohuanlin +1
136
137 @Test
138 public void testGetTriplesC3() {
139     Supplier<int[]> intsSupplier = new Source( N: 1000, M: 1000).intsSupplier( safetyFactor: 10);
140     int[] ints = intsSupplier.get();
141     ThreeSum target = new ThreeSumQuadraticWithCalipers(ints);
142     Triple[] triplesQuadratic = target.getTriples();
143     Triple[] triplesCubic = new ThreeSumCubic(ints).getTriples();
144     assertEquals(triplesCubic.length, triplesQuadratic.length);
145 }
no usages xiaohuanlin +1
146
147 @Test
148 public void testGetTriplesC4() {
149     Supplier<int[]> intsSupplier = new Source( N: 1500, M: 1000).intsSupplier( safetyFactor: 10);
150     int[] ints = intsSupplier.get();
151     ThreeSum target = new ThreeSumQuadraticWithCalipers(ints);
152     Triple[] triplesQuadratic = target.getTriples();
153     Triple[] triplesCubic = new ThreeSumCubic(ints).getTriples();
154     assertEquals(triplesCubic.length, triplesQuadratic.length);
155 }
156
Run Debug TODO Problems Terminal Services Build Dependencies
Tests passed: 11 (4 minutes ago)
```

## 2. Timing Observations

Algorithm	N	Time (ms)	log N	log T
ThreeSumCubic	50	15	1.69	1.17
ThreeSumCubic	100	31	2	1.49
ThreeSumCubic	200	23	2.3	1.36
ThreeSumCubic	400	41	2.6	1.61
ThreeSumCubic	800	164	2.9	2.2
ThreeSumQuadratic	50	6	1.69	0.7
ThreeSumQuadratic	100	9	2	0.9
ThreeSumQuadratic	200	11	2.3	1.04
ThreeSumQuadratic	400	12	2.6	1.07
ThreeSumQuadratic	800	34	2.9	1.5
ThreeSumQuadraticWithCalipers	50	5	1.69	0.69
ThreeSumQuadraticWithCalipers	100	6	2	0.7
ThreeSumQuadraticWithCalipers	200	11	2.3	1.04
ThreeSumQuadraticWithCalipers	400	11	2.6	1.04
ThreeSumQuadraticWithCalipers	800	14	2.9	1.14
ThreeSumQuadrithmic	50	7	1.69	0.8
ThreeSumQuadrithmic	100	14	2	1.14
ThreeSumQuadrithmic	200	9	2.3	0.95
ThreeSumQuadrithmic	400	17	2.6	1.23
ThreeSumQuadrithmic	800	31	2.9	1.4



Graph based on experimental values



### 3. Quadratic Method

Sorting the array takes  $O(n \log n)$ , so overall complexity is  $O(n \log n + n^2)$  equivalent to  $O(n^2)$ . We have used loops couple of times first we are iterating each element of array which makes complexity  $n$  times & in second loop, we are checking if index of left value is greater than 0 & index of right value is less than the length of array which again makes complexity  $n$  times. Hence, total time complexity  $O(n \cdot n) = O(n^2)$ . Quadratic method is time efficient and it has better performance.