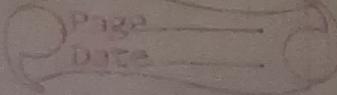


CD



⇒ Higher level language



Pre Processor



Pure higher level lang

Compiler



Assembly lang

Assembler



MC Relocatable

Linker / Loader



MC executable

* Compiler Phase

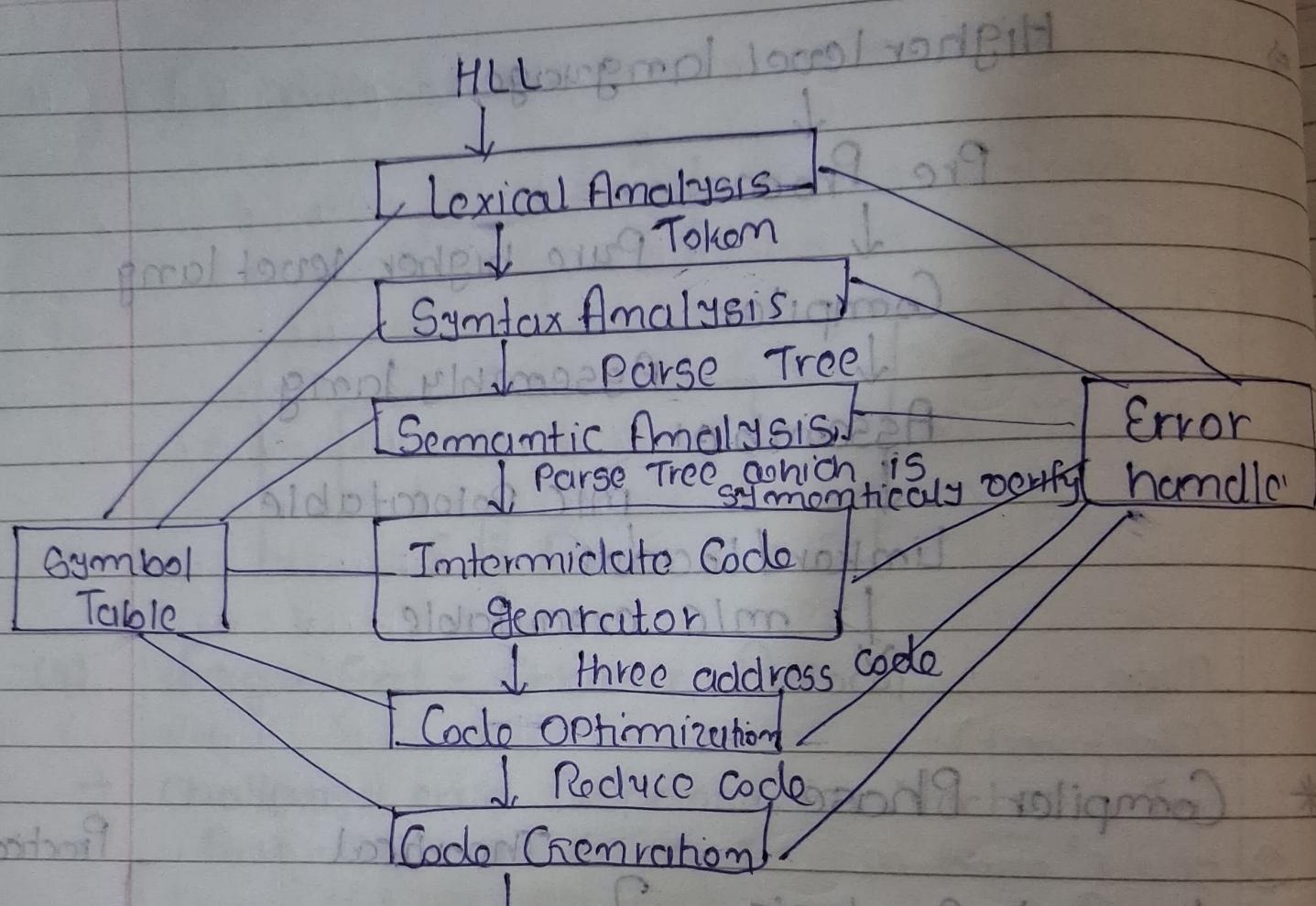
Theoretical

Practical

1	Lexical Analysis	Analysis	Front End
2	Syntax Analysis		
3	Semantic Analysis	Phase	
4	Intermediate Code generation		
5	Code Optimization	Synthesis	
6	Code generation	Phase	Back End

1 Lexical Analysis :

- ↳ Find Tokens
- ↳ Recognize the tokens
- ↳ Remove white Space
- ↳ Remove # Statement



2 Syntax Analysis

Identify proper order

3 Semantic Analysis

Variable Type check

Scop of Variable check

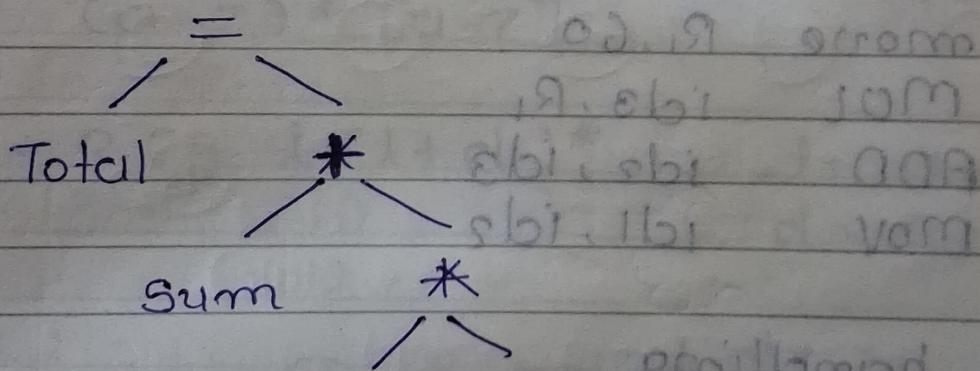
→ Three address code : maximum three
oprnd used

Ex.

Total = Sum + rate * 60;

1 Lexical Token : Tokon atau Identifier
 Total merupakan Identifier
 = Eg. not assign operator
 Sum merupakan Identifier
 + plus operator
 rate merupakan Identifier
 * mul operator
 60 merupakan Constant
 ; Special Symbol

2 Syntax Analysis



3 Semantic Analysis: Type Casting

rate int to Real

4

Intermediate Code Generation

temp1 = int To Real (G0)

temp2 = rate * temp1

temp3 = sum + temp2

total = temp3

5 Code Optimization

temp1 = rate * int To Real (G0)

Total = sum + temp1

→ Unnecessary Symbol reduce into loop.

6 Code Generation

id1 = id2 + id3 * G0

move R1, G0

MUL id3, R1

ADD id2, id3

MOV id1, id2

* Error handling

→ Lexical Analysis: Invalid Variable

Eg: abc, \$j, \$a (Invalid Tokens)

→ Code Optimization: Unreachable Statement

* Type of Compiler

1 OnePass Compiler [Eg: Pascal]

2 MultiPass Compiler [Eg: Java, C (++)]

OnePass

- Faster
- knowledge all phase
- Can't recognize Error easily

Multipass

- Slover
- distribute work
- Find Error Easily

* Cross Compiler: It generate executable file which run in another platform.
Ex: Java (Platform Independent)

x. Write the R.E. that accept the string, which is identifier, the design F.A

$$(a-z)^* [a-z]$$

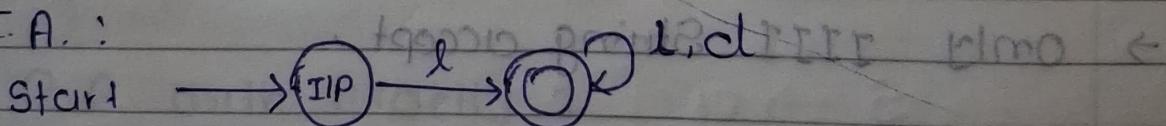
OR

$$R.E. \quad l(l+d)^*$$

$$l = a \dots z$$

$$d = 0 \dots 9$$

F.A. :

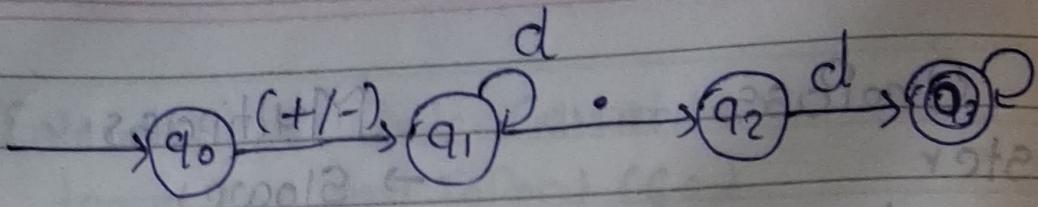


Ex. Write R.E. That accept the string all real numbers and design F.A

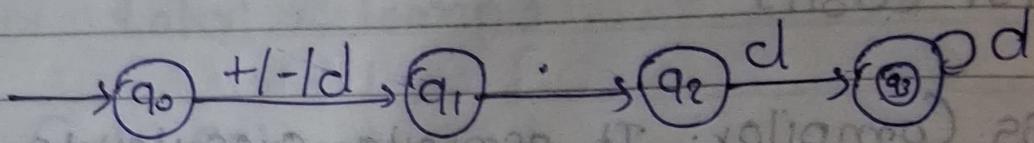
$$r = \{0, 1, \dots m\}^* \text{ or } \{-1, -2, \dots m\}^* \text{ OR } \{0.5, 0.2, \dots\}$$

$$R.E \quad r(r)^*$$

$$(+/-) d^* . d^+$$

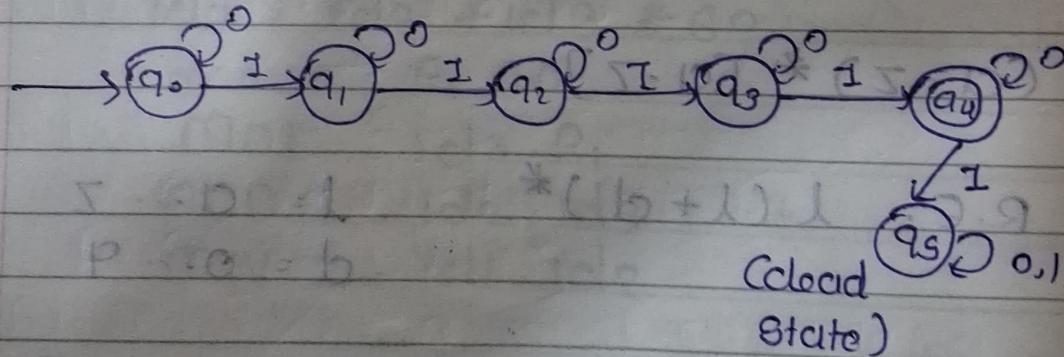


Ex: R.E that accept the string that contain
1111

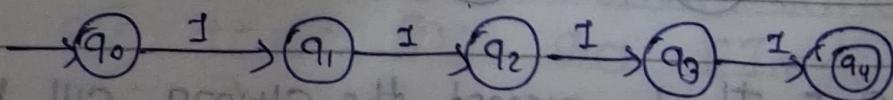


Ex: R.E that accept the string that Contain
1111

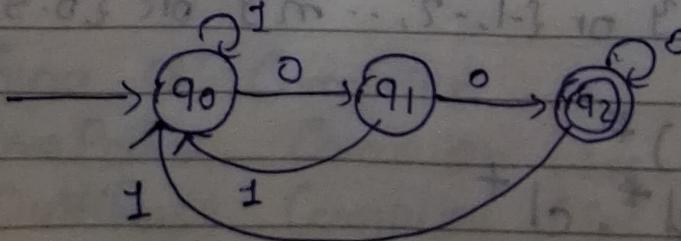
R.E: $(0)^* 1 (0)^* 1 (0)^* 1 (0)^* 1 (0)^*$



→ only 1111 String accept.

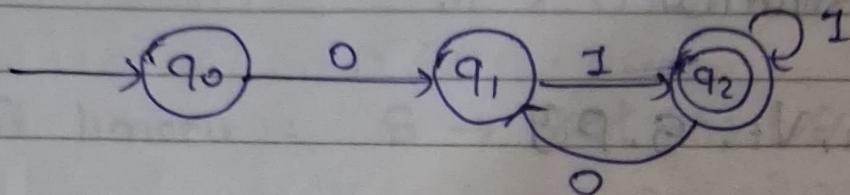


Ex Ending with 00



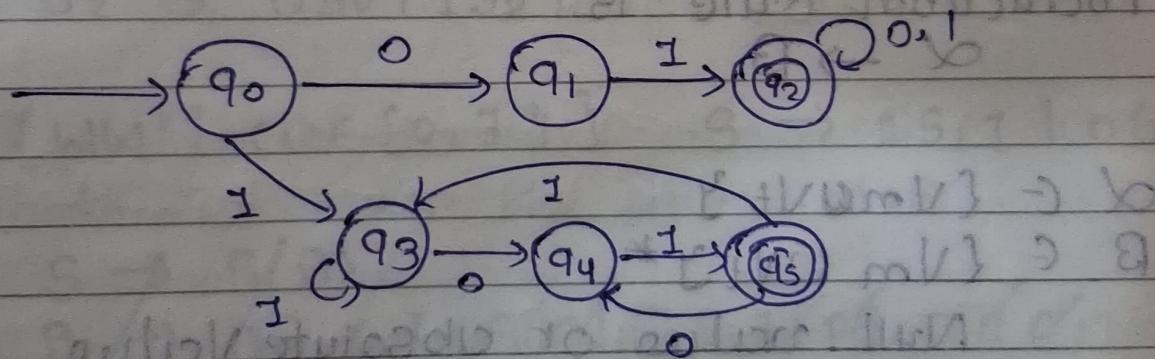
Ex: closig FA and RA the string Start and End with 01

R.E: 01 (0+1)* # or # 01

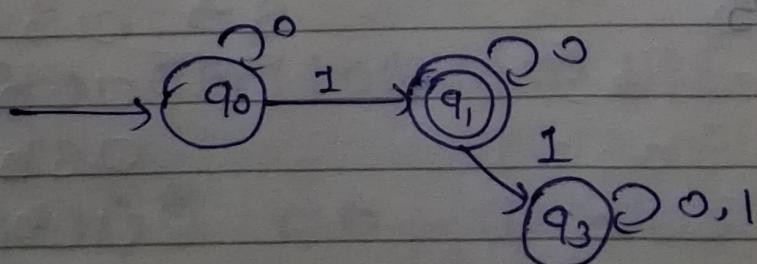


Ex: R.E and F.A that Starting and Ending with 01

R.E: 01 (0+1)* + (0+1)* 01



Ex: R.E with exactly 1 0)* 1 (0)*



Grammar:

It is combination of terminal and non terminal

$$G = \{V_m, V_t, S, P\}$$

V_t : Set of Terminal

V_m : Set of Non terminal

S : String Symbol

P : Production Rule

Production Rule is

$$\alpha \rightarrow \beta$$

$\alpha \in \{V_m\}^*$

$\beta \in \{V_m \cup V_t\}^*$

Null value or absolute Value

$$S \rightarrow a$$

$$S \rightarrow aS \cup \epsilon$$

$$S \rightarrow bS$$

Ex: Make $CFO(0+1)^*$ to nondeterministic

Right linear : $S \rightarrow 0S_1 \leftarrow 2$
 $S_1 \rightarrow 0S_1 \mid \epsilon$

Left linear : $S \rightarrow S_0 S_1 \mid \epsilon \leftarrow S_0 S_1 \mid 0$

Ex: $0^* 1(0+1)^*$

$S \rightarrow S_1 S_2 \leftarrow 0 \rightarrow 01$

$S_1 \rightarrow 0S_1 \mid \epsilon$

$S_2 \rightarrow 0S_2 \mid 1S_2 \mid \epsilon \leftarrow 12$

Ex: $\{WW^r \mid w \in \{0,1\}^*\}$ $S \rightarrow 1S_1 \mid 0S_1 \mid \epsilon$

$S \rightarrow S_1 S_2 \mid$

$S_1 \rightarrow 0S_1 \mid 1S_1 \mid 0101 \mid 10S_1 \mid 0101 \mid \epsilon$

$S_2 \rightarrow$

Ex: Palindrome string

$S \rightarrow S_1 S_2 \mid$

$S_1 \rightarrow 1S_1 \mid 0S_1 \mid 0101 \mid 11\epsilon \mid \epsilon$

$(a+b)^* \quad ab \quad (a+b)^*$

$S \rightarrow S_1 ab S_2$

$S_1 \rightarrow aS_1 bS_2 \mid \epsilon$

Ex: Equal Number of * parenthesis

$$S \rightarrow CSJSI E$$

$$a^m b^m, m > 0, m \geq 0$$

Ex: $a^e b^*$

$$S \rightarrow aJSIS_1 S_2$$
$$S_1 \rightarrow aJSIS_1 E$$
$$S_2 \rightarrow bS_2 | E$$

Ex Equal No of a and b

$$S_1 \rightarrow aS_2 bS_1 bS_2 aS_1 E$$

LM0: Left most Derivative
CStart with left most terminal

RMD: Right most Derivative

String: cibabab

LM0:

$$S \rightarrow aSbS$$

$$\rightarrow aSbSaSbS$$

$$\rightarrow abcaSbSbS$$

$$\rightarrow ababab$$

Prints RMD

$$S \rightarrow aSbS$$

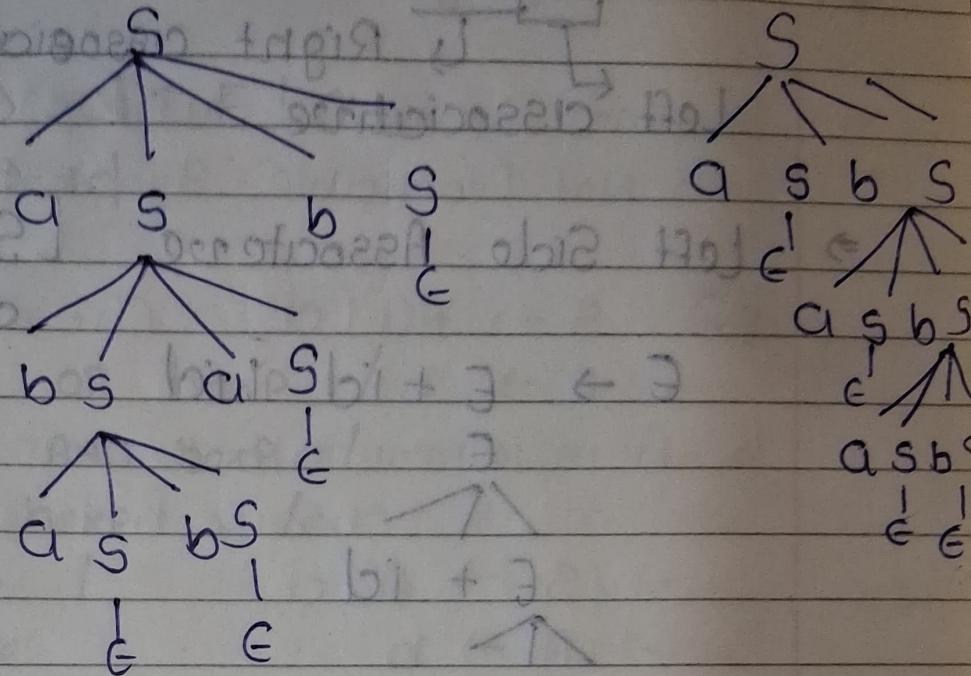
$$aSbcaSb$$

$$asbcaSb$$

$$cisbaSba$$

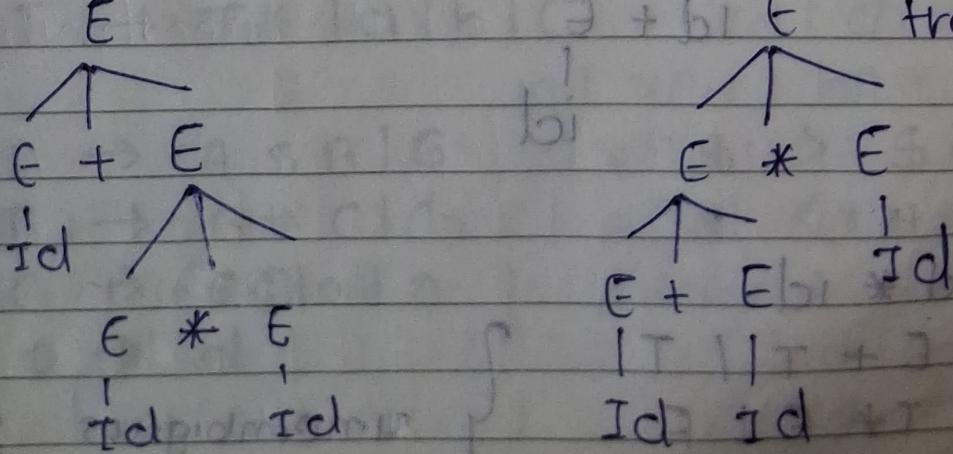
$$ababab$$

Parse Tree



If any grammar contains two parse tree LMDLRMO, It's called Ambiguous Grammar

$E \rightarrow E + E \mid E * E \mid id \mid [higher\ level\ precedence\ is\ lower\ level\ than]$

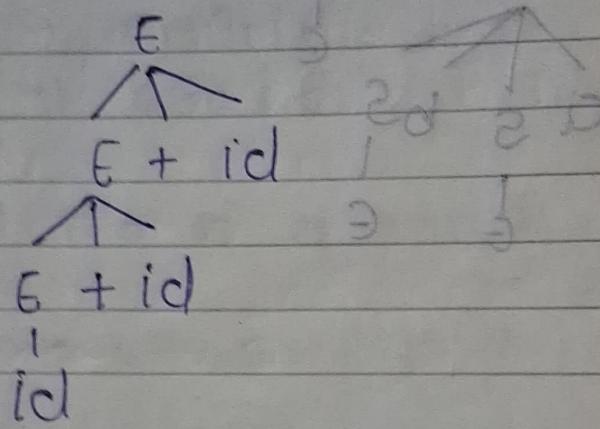


$id + id * id$

Right associative
Left associative

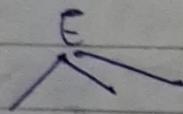
\Rightarrow Left Side Associative [Same precedence tho always used left associative]

$$E \rightarrow E + id$$



\Rightarrow Right Side Associative

$$E \rightarrow id + E id$$



ambiguous local variable + E | E * E | E + E ← E

most common error E → id + E id

ambiguity at point E id + E

E → E + T | T

T → T * F | F

F → id

} unambiguous grammar

2^{3^2} $\rightarrow (2 \uparrow (3 \uparrow 2))$ (Right Associative)

Rule: $E \rightarrow G \uparrow F$
 $G \rightarrow id$

Ex: $bexp \rightarrow bexp \text{ OR } bexp / d \leftarrow A$
 Upper term $bexp \text{ AND } bexp / d \leftarrow A$
 (bexp \times Not bexp) /
 True / $d \leftarrow A$
 False $d \leftarrow A$

 $E \rightarrow E \text{ OR } T / T \leftarrow A$ $T \rightarrow T \text{ AND } F / F$ $F \rightarrow \text{Not } F / \text{true} / \text{false} \leftarrow A$ $R \rightarrow R + R, | R R | R * | a | b | c$ $E \rightarrow E + F / F$ $F \rightarrow F F / T$ $T \rightarrow T * | a | b | c$

\Rightarrow

- A $\rightarrow A \$ B | B$ $\rightarrow \$ > S$ (Left Asso)
- B $\rightarrow B \# C | C$ $\rightarrow \# < H$ (Right Asso)
- C $\rightarrow C @ O | O$
- O $\rightarrow d$

* Restriction on CFG (↑ E ↑ ?) ← ↗

⇒ Remove unnecessary (useless) Symbol
 ↳ Not Reachable Symbol remove

Ex: $S \rightarrow A B | C a$ (B - non generating)

$A \rightarrow b$

↳ B is eliminate because it's not useful
 (because B has not expanded)

$S \rightarrow A a | C a$

$A \rightarrow b$

↳ A is non reachable. So,

$S \rightarrow a$

Ex: $S \rightarrow A B c | d$

$B \rightarrow bC$

↓

Remove useless symbol

$S \rightarrow d$

Ex $S \rightarrow aB | bX$

$A \rightarrow BAd | bSx | a$

$B \rightarrow aSB | bBx |$

$X \rightarrow SBD | aBx | ad$

1. B is Non-generating

$S \rightarrow bX$

$A \rightarrow bSx | a$

$X \rightarrow ad$

2. A is not reachable

$S \rightarrow bX$

$X \rightarrow ad$

Ex: $A \rightarrow xyz \mid xyzz$ $x \rightarrow xz \mid xyz$ $y \rightarrow yyz \mid xz$
 $z \rightarrow zy \mid z$

→ Non-Generating $(x, y) \in A$

$A \rightarrow xyz \mid xyzz$
 $x \rightarrow$
 $z \rightarrow zy \mid z$

→ Not Reachable (z)

$A \rightarrow xyz$

Ex: $B \rightarrow aC \mid SB \leftarrow \exists$
 $A \rightarrow bSCa \leftarrow \exists$
 $B \rightarrow aSB \mid bBC \exists$
 $C \rightarrow aBC \mid ad$

Non-generating

$S \rightarrow aC$

$C \rightarrow ad$

$A \rightarrow bSCa$

Not Reachable: CA

$S \rightarrow aC$

$C \rightarrow ad$

⇒ Unit Production
 non terminal → one non terminal
 $A \rightarrow B$ unique production)

Ex: $A \rightarrow B$

$B \rightarrow \alpha$

↓

$A \rightarrow \alpha$

Ex: $S \rightarrow A$

$A \rightarrow a$

↳ $S \rightarrow a$

c: $S \rightarrow AB$

$A \rightarrow a$

$B \rightarrow C1b$

$C \rightarrow D$

$D \rightarrow E$

$E \rightarrow a$

Ex: $I \rightarrow a1b | Ta | Tb | T0 | T1$

$F \rightarrow T | (E)$

$T \rightarrow F | T * F$

$E \rightarrow T | I | E + T$

$F \rightarrow I$

$T \rightarrow F$

$E \rightarrow T$

$S \rightarrow AB$

$A \rightarrow a$

$B \rightarrow a1b$

~~$S \rightarrow AB$~~

~~$I \rightarrow a1b | Ta | Tb | T0 | T1$~~

~~$F \rightarrow T | (E)$~~

~~$T \rightarrow F | T * F$~~

~~$E \rightarrow T | I | E + T$~~

(T01 બધી value એવી)

$I \rightarrow aIbI IaI IbI IoI I_1$

$F \rightarrow aIbI IaI IbI IoI I_1 | CE)$

$T \rightarrow aIbI IaI IbI IoI I_1 | CE) | T * F$

$E \rightarrow aIbI IaI IbI IoI I_1 | CE) | T * F | E + T$

\Rightarrow Eliminate Null Value

Ex: $S \rightarrow aA \rightarrow aAa \leftarrow A$
 $A \rightarrow bI\epsilon \quad A \rightarrow b$

Ex: $S \rightarrow AaB \rightarrow AaB * B \leftarrow A$
 $A \rightarrow aI\epsilon \quad B \rightarrow bI\epsilon$

$S \rightarrow AaB | AaI aB | aB a \leftarrow A$

$A \rightarrow a \quad B \rightarrow b$

Ex: $S \rightarrow ABAC$

$A \rightarrow aAIE \quad B \rightarrow bBIE$

$C \rightarrow c$

$S \rightarrow ABC | BAC | BCI | C | AAC | AC | ABAC$

$A \rightarrow aAIE$

$B \rightarrow bBIE$

$C \rightarrow c$

* Issue in CFG

i. Ambiguity

3 Indirect Left Recursion

2 Left Recursion ↗ Left Factoring

$A \rightarrow A\alpha_1 B$ (Accept string like $B\alpha^*$)

$A \rightarrow \alpha A / B$ (Right Recursion)

↳ Accept like $\alpha^* B$

↳ Problem In Left Recursion

$A(\)$

{ ↗ It's going to infinite loop.

$A(\)/\alpha;$ ↗ It's going to infinite loop.

y

↳ Right Recursion

$A(\)$

{ ↗ Here problem of infinite loop not occurred.

$A(\)$

y

↳ Solution: Remove Left Recursion

$A \rightarrow BA'$

$A' \rightarrow \alpha A' / \epsilon$

Ex: $A \rightarrow A \alpha B$
 $E \rightarrow E + T \mid T$

$E \rightarrow TE'$
 $E' \rightarrow E \mid + TE'$

Ex: $A \rightarrow A\alpha_1 \mid A\alpha_2 \mid A\alpha_3 \mid B_1 \mid B_2 \mid B_3$

$A \rightarrow B_1 A' \mid B_2 A' \mid B_3 A'$
 $A' \rightarrow C \mid A' \alpha_1 \mid A' \alpha_2 \mid A' \alpha_3$
 $A' \rightarrow C \mid A' \alpha_1 \mid A' \alpha_2 \mid A' \alpha_3$

Ex: $T \rightarrow T + F \mid F$
 $F \rightarrow F \times G \mid G$
 $G \rightarrow id$

Correct $T \rightarrow FT'$

$T' \rightarrow G \mid + FT'$
 $F \rightarrow FG'$
 $F' \rightarrow E \mid T \cdot G F'$
 $G \rightarrow id$

Ex: $S \rightarrow x \mid x_0 \mid \gamma a$
 $x \rightarrow x\alpha \mid c \mid b$
 $\gamma \rightarrow \alpha \mid a$

$S \rightarrow x \mid x_0 \mid \gamma a$
 $x \rightarrow \alpha x' \mid b x'$
 $x' \rightarrow e \mid \alpha x'$
 $\gamma \rightarrow \alpha \mid a$

$A \rightarrow A \mid Ab \mid b$

$T \mid T+3 \leftarrow \emptyset$

$A \rightarrow A \mid bA'$

$A' \rightarrow \epsilon \mid bA'$

$S \rightarrow A$

$A \rightarrow Ad \mid Ae \mid ab \mid ac$

$B \rightarrow bBc \mid f$

$C \rightarrow g$

$S \rightarrow A$

$A \rightarrow aba' \mid aca'$

$A' \rightarrow da' \mid ca' \mid e$

$B \rightarrow bBc \mid f$

$C \rightarrow g$

$S \rightarrow Bblc$

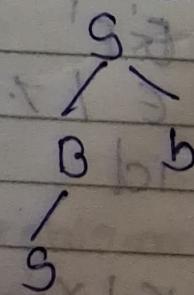
$B \rightarrow Bc \mid Sd \mid e$

(3rd Issue)
(Indirect Left Recursion)

$S \rightarrow Bblc$

$B \rightarrow Sd \mid B' \mid eB'$

$B' \rightarrow CB' \mid E$



$S \rightarrow Bblc$

$B \rightarrow Bc \mid Bbd \mid cdd \mid e$

\Downarrow

$S \rightarrow Bblc$

$B \rightarrow cdB' \mid cbB'$

$B' \rightarrow CB' \mid bdB' \mid G$

Ex: $\mathcal{Q} \rightarrow \mathcal{Q}ED1q$
 $E \rightarrow e$
 $D \rightarrow \text{NFA1d}$
 $N \rightarrow \text{DFA1m}$
 $F \rightarrow f$
 $A \rightarrow a$

$\mathcal{Q} \rightarrow \mathcal{Q}ED1q$

$E \rightarrow e$

$D \rightarrow \text{NFA1d}$

$N \rightarrow \text{NFAFA1dFA1m}$

$F \rightarrow f$

$A \rightarrow a$

$\mathcal{Q} \rightarrow q\mathcal{Q}'$

$\mathcal{Q}' \rightarrow ED\mathcal{Q}'1e$

$E \rightarrow e$

$D \rightarrow \text{NFA1d}$

$N \rightarrow \text{DFAN'1mN'}$

$N' \rightarrow e \mid \text{FAFAN'}$

$F \rightarrow f$

$A \rightarrow a$

Ex: $A \rightarrow B1a1cBD$

$B \rightarrow C1b1b$

$C \rightarrow A1z$

$D \rightarrow d$

$A \rightarrow 0|a|1 ABDI zBD$ $\leftarrow \theta$
 $B \rightarrow C|b$ $\leftarrow \theta$
 $C \rightarrow A|z$ $\leftarrow \theta$
 $D \rightarrow d$ $\leftarrow \theta$

~~$A \rightarrow BA|1|c|A'1|z|BD|A^*$~~
~~$A' \rightarrow BDA'|1|c$~~
~~$B \rightarrow C|b$~~

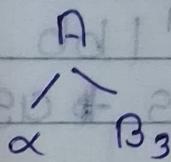
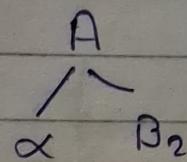
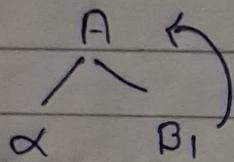
$A \rightarrow C|b|1 ABDI zBD|1|d$ $\leftarrow \theta$
 \downarrow
 $A \rightarrow A|z|1 b|ABD|z|BD|1|a$ $\leftarrow \theta$
 $B \rightarrow C|b$ \rightarrow $\leftarrow \theta$
 $C \rightarrow A|z$ $\leftarrow \theta$
 $D \rightarrow d$ $\leftarrow \theta$

$A \rightarrow zA'|1|bA'|1|z|BD|A'|1|a|A'$ $\leftarrow \theta$
 $A' \rightarrow BDA'|1|c$ $\leftarrow \theta$
 $B \rightarrow C|b$ $\leftarrow \theta$
 $C \rightarrow A|z$ $\leftarrow \theta$
 $D \rightarrow d$ $\leftarrow \theta$

- Deterministic: Only one path for output
- Non-Deterministic: Multiple paths for output

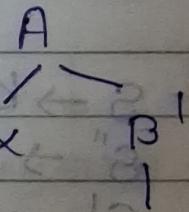
Grammar

$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \alpha\beta_3$ (Left factoring)



No of backtracking occurred (First Value same, so multiple option, backtracking occurred)

Solution: $A \rightarrow \alpha\beta'$



Ex: $S \rightarrow iEtS \mid iEtScs \mid a$

$S \rightarrow S' \mid s' \mid a$

$S' \rightarrow iEtS$

$S \rightarrow iEtSS' \mid a$

$S' \rightarrow \epsilon \mid cs$

Ex: $A \rightarrow \alpha\beta\gamma A \mid \alpha\beta\gamma A\gamma A \mid a$

$\beta \rightarrow b$

$A \rightarrow \alpha\beta\gamma A\gamma' \mid a$

$A' \rightarrow zA \mid \epsilon$

$B \rightarrow b$

Ex: $S \rightarrow aSSbS \mid aSaSb \mid abb \mid b$

$S \rightarrow aSS' \mid abb \mid b$

$S' \rightarrow SbS \mid aSb$

$S \rightarrow aS'' \mid b$

$S'' \rightarrow SS' \mid bb$

$S' \rightarrow SbS \mid aSb$

Ex: $S \rightarrow bSSaS \mid bSSaSb \mid bsb \mid a$

$S \rightarrow bSSaS' \mid bSb \mid a$

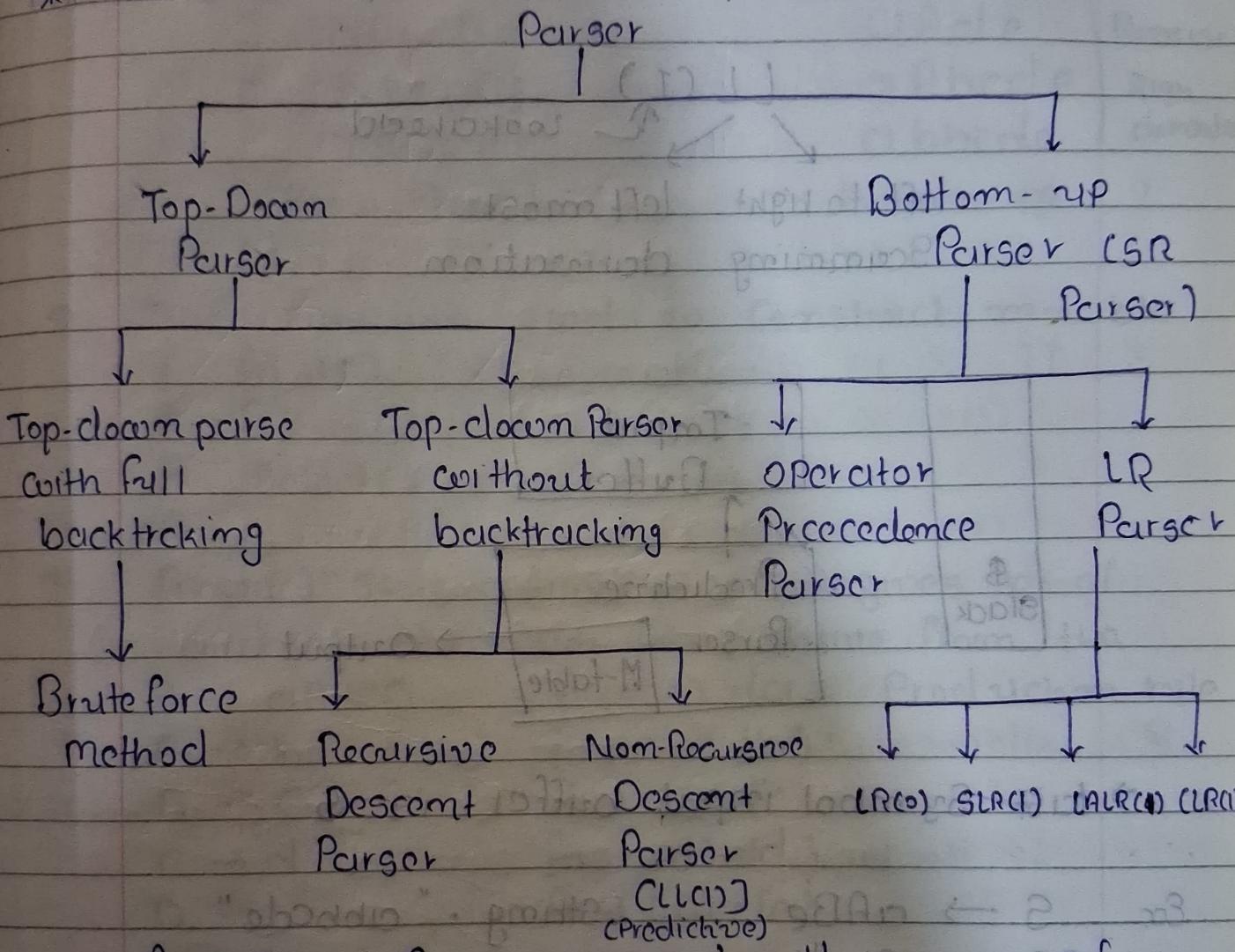
$S' \rightarrow aS \mid sb$

$S \rightarrow bSS'' \mid a$

$S'' \rightarrow Sas' \mid b$

$S' \rightarrow aS \mid sb$

* Parser : A program which converts input string into output string *



- Ambiguous Grammar not allowed by any of Parser.
- Operator Precedence parser only allows ambiguous grammar.
- LR: Left to Right Reduce-Right most derivation
- Top down: Starting Symbol to given string
Bottom up: given string to Starting Symbol

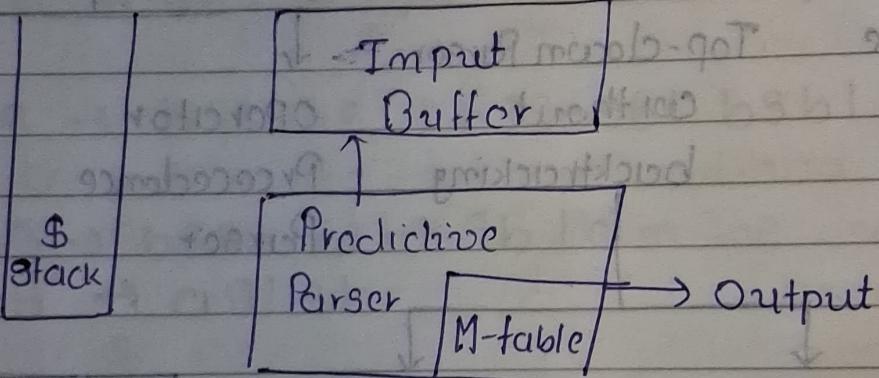
Top-down \rightarrow when to use
 bottom-up \rightarrow What to use

Page _____
 Date _____

* Predictive Parser (LL(1)) (Top-down Method)

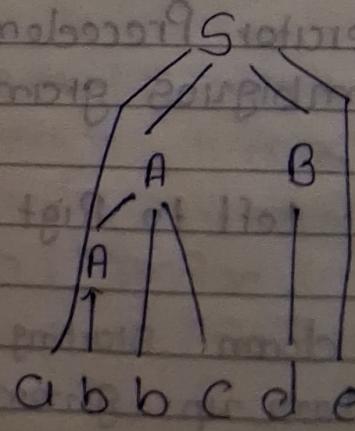
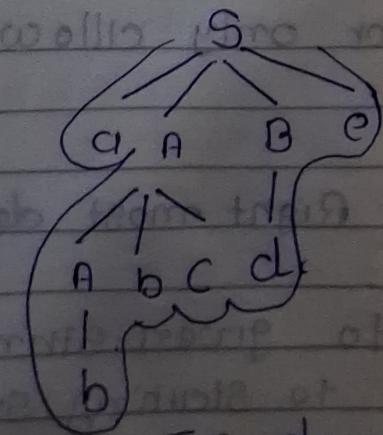
$LL(1)$ |
 ↘ lookahead

left to right left most
 Scanning derivation



\rightarrow last symbol in input buffer is \$

Ex $S \rightarrow aABe$ string : "abbcde"
 $A \rightarrow Abcb$
 $B \rightarrow d$



↳ Top-down approach follows left-most derivation.
 ↳ Bottom-up approach follows right-most derivation in reverse order.

$$S \rightarrow eABe$$

$$eABe$$

$$eAbcBe$$

$$eAbcBe$$

$$eAbcBe$$

Top - down

$$S \rightarrow aABe$$

$$aABe$$

$$aAde$$

$$aAde$$

$$aAbcde$$

$$aAbcde$$

bottom-up

Reverse
Right
derivation

→ Three functions used to construct m-table

1. first()

2. follow()

3. Select()

1. First(): It is a function which gives set of terminals that begin string derive from the

Ex:	$S \rightarrow aABCD$	$\text{first}(S) = \{a\}$	Production rule
	$A \rightarrow b$	$\text{first}(A) = \{b\}$	
	$B \rightarrow C$	$\text{first}(B) = \{C\}$	
	$C \rightarrow d$	$\text{first}(C) = \{d\}$	
	$D \rightarrow e$	$\text{first}(D) = \{e\}$	

Ex:	$S \rightarrow AB$	$\text{first}(S) = \{b\}$	
	$A \rightarrow b$	$\text{first}(A) = \{b\}$	
	$B \rightarrow C$	$\text{first}(B) = \{C\}$	

Ex:	$S \rightarrow AB$	$\text{first}(S) = \{b, C\}$	
	$A \rightarrow bCE$	$\text{first}(A) = \{b, E\}$	
	$B \rightarrow C$	$\text{first}(B) = \{C\}$	

↳ Starting Symbol (S) follow(S) always contain $\{\$\}$.

⇒ Algorithm: First()

1 If x is terminal, First(x) is $\{x\}$

2 If $x \rightarrow e$ is production, then add e to set of first(x).

3 If x is non-terminal,
(a) $x \rightarrow y$, first(y) is an element of the set of first(x).
(b) If first(y) has ϵ as an element and $x \rightarrow yz$ then
 $\text{First}(x) = \text{first}(y) - \{\epsilon\} \cup \text{First}(z)$

2 Follow(): It is function which gives set of terminal that can be appended immediately to the right of given symbol.

Ex: $S \rightarrow ABCD$

$A \rightarrow b | c$ $\text{follow}(A) = \text{First}(BCD)$

$B \rightarrow C$ $= \{c\}$

$C \rightarrow D$ $\text{follow}(B) = \{cd\}$

$D \rightarrow e$ $\text{follow}(C) = \{e\}$

$\text{follow}(CD) = \text{follow}(S)$

$\text{follow}(S) = \{\$\}$

Ex: $S \rightarrow AB$ $\text{follow}(S) = \{\$, y\}$
 $A \rightarrow a|c|e$ $\text{follow}(A) = \{a, b, \$\}$
 $B \rightarrow b|c|e$ $\text{follow}(B) = \$$

⇒ Algorithm: Follow(S)

1. $\$$ is an element of $\text{follow}(S)$, where S is starting symbol and $\$$ indicate the end of Input.
2. if $A \rightarrow \alpha x \gamma$ is a production, the set $\text{First}(\gamma)$ is in set $\text{follow}(x)$, excluding ϵ .
3. If $A \rightarrow \alpha x$ or $A \rightarrow \alpha x \gamma$ are production, the $\text{First}(\gamma)$ has an element ϵ , the set $\text{follow}(x)$ is in set $\text{follow}(A)$.

Ex: I $E \rightarrow TA$ $\text{First}(E) = \{C, id\}$
 $A \rightarrow +TA|\epsilon$ $\text{First}(A) = \{+, \epsilon\}$
 $T \rightarrow FB$ $\text{First}(T) = \{C, id\}$
 $B \rightarrow *FB|\epsilon$ $\text{first}(B) = \{*, \epsilon\}$
 $F \rightarrow (ED)id$ $\text{First}(F) = \{C, id\}$

 $\text{Follow}(E) = \{\$, y\}$ $\text{follow}(F) = \{*, +, D, B\}$
 $\text{Follow}(A) = \{\$, y\}$
 $\text{Follow}(T) = \{+, \$\}$
 $\text{Follow}(B) = \{+, \$\}$

Ex: $S \rightarrow AaAbcdBbBa$
 $A \rightarrow e$
 $B \rightarrow e$

first(S) = {a, b}

first(A) = {e}

first(B) = {e}

Follow(S) = {e, \$}

Follow(A) = {a, b}

Follow(B) = {a, b}

Ex: 2 $S \rightarrow aBDh$

B $\rightarrow cc$

C $\rightarrow bc$

D $\rightarrow EF$

E $\rightarrow gIE$

F $\rightarrow fIE$

First(S) = {c, g}

First(B) = {c}

First(C) = {b, c}

First(D) = {g, f, e}

First(E) = {g, f}

First(F) = {f, e}

Follow(S) = {g, y}

Follow(B) = {g, f, h}

Follow(C) = {g, f, h}

Follow(D) = {h}

Follow(E) = {f, h}

Follow(F) = {h}

Ex: $S \rightarrow ABBB$

$A \rightarrow a1e$

$B \rightarrow b1e$

$$\text{First}(S) = \{a, b, \epsilon\}$$

$$\text{follow}(S) = \{\$ \}$$

$$\text{First}(A) = \{a, \epsilon\}$$

$$\text{follow}(A) = \{b, a, \$\}$$

$$\text{First}(B) = \{b, \epsilon\}$$

$$\text{follow}(B) = \{a, b, \$\}$$

Ex

$S \rightarrow aSe1B$

$B \rightarrow bBe1C$

$C \rightarrow cCe1d$

$$\text{first}(S) = \{a, b, c, d\}$$

$$\text{follow}(S) = \{\$, c\}$$

$$\text{first}(B) = \{b, c, d\}$$

$$\text{follow}(B) = \{\$, c\}$$

$$\text{first}(C) = \{c, d\}$$

$$\text{follow}(C) = \{\$, c\}$$

3 Select(\cdot):

$A \rightarrow \omega$

$$\text{Select}(A \rightarrow \omega) = \text{First}(\text{first}(\omega) \cdot \text{follow}(A))$$

Ex: Example 1 in follow

$$\text{Select}(C \rightarrow TA) = \text{First}(\text{first}(TA) \cdot \text{follow}(C))$$

$$= \text{First}(\{c, idy\} \times \{\$, c\})$$

$$= \{c, idy\}$$

$$\text{Select } CA \rightarrow +TA = \text{First}(\text{First}(+TA) \times \text{Follow}(CA))$$

$$= \text{First}(\{+\} \times \{\$\}, \$)$$

$$\text{Select } CA \rightarrow C = \text{First}(\{C\} \times \text{Follow}(CA))$$

$$= \text{First}(\{C\} \times \{\$\}, \$)$$

$$\text{Select } CT \rightarrow FB = \text{first}(\text{first}(FB) \cdot \text{Follow}(CT))$$

$$= \text{first}(\{C, id\} \cdot \{+, \$, \}\})$$

$$\text{Select } (B \rightarrow *FB) = \text{first}(\{* \} \cdot \{+, \$, \}\})$$

$$= \{*\}$$

$$\text{Select } (B \rightarrow C) = \text{first}(\{C\} \cdot \{+, \$, \}\})$$

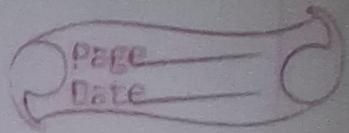
$$= \{+, \$, \}\})$$

$$\text{Select } (F \rightarrow (C)) = \text{first}(\{C\} \cdot \{+, *,), \$\}\})$$

$$= \{C\}$$

$$\text{Select } (F \rightarrow id) = \text{first}(\{id\} \cdot \{+, *,), \$\}\})$$

$$= \{id\}$$



→ Construct m-table

	$b_1 \cdot b_1$	$b_1 \cdot b_1$	$b_1 b_1 \cdot$
+	*	()
E	$a \cdot b_1$	$E \rightarrow TA$	$E \rightarrow TA$
T	$b \cdot a$	$T \rightarrow FB$	$T \rightarrow FB$
A	$A \rightarrow +TA$	$A \rightarrow E$	$A \rightarrow E$
F		$F \rightarrow (E)$	$F \rightarrow id$
B	$B \rightarrow C$	$B \rightarrow *FB$	$B \rightarrow C$
			$B \rightarrow E$

→ If any cell contain multiple production than it is not LL(1) grammar.

→ id + id * id accept or not

Stack	IIP String	Production Rule
\$	id + id * id \$	
ES	id + id * id \$	
TA\$	id + id * id \$	$E \rightarrow TA$
FBAS	id + id * id \$	$T \rightarrow FB$
idBA\$	id + id * id \$	$F \rightarrow id$
BA\$	+ id * id \$	
A\$	+ id * id \$	$B \rightarrow C$
+ TA\$	+ id * id \$	$A \rightarrow +TA$
TA\$	id * id \$	
FBAS	id * id \$	$T \rightarrow FB$
idBAS	id * id \$	$F \rightarrow id$
BA\$	* id \$	
* FBAS	* id \$	$B \rightarrow *FB$

FBAS	id \$	
idBAS	id \$	$F \rightarrow id$
BAS	\$	
AS	\$	$B \rightarrow E$
S	\$	$A \rightarrow E$

string is accepted.

Ex: 2 Construct m-table. check "C1bbgfh"
String accept or not.

→ Select $C \rightarrow C1B0h$ = first(first(C1B0h)) · follow(S)

→ Select $(B \rightarrow cC) = \text{first(first}(cc) \cdot \text{follow}(B))$

→ Select $(C \rightarrow bC) = \text{first(first}(bc) \cdot \text{follow}(C))$

→ Select $(CC \rightarrow E) = \text{first(first}(E) \cdot \text{follow}(C))$

→ Select $(D \rightarrow EF) = \text{first(first}(EF) \cdot \text{follow}(D))$

FBAG	id \$	
idBAG	id \$	$F \rightarrow id$
BAG	\$	
AG	\$	$B \rightarrow E$
G	\$	$A \rightarrow G$

string is accepted.

Ex:2 Construct m table. check "CICbbgfh"
String accept or not.

→ Select $C \rightarrow ABGh$ = first(first(CABGh)) · follow(S)

$$= \{A\}$$

→ Select $(B \rightarrow CC) = first(first(CC) \cdot follow(B))$

$$= \{C\}$$

→ Select $(C \rightarrow bC) = first(first(bC) \cdot follow(c))$

$$= \{fb\}$$

→ Select $(CC \rightarrow EF) = first(first(EF) \cdot follow(C))$

$$= \{g, f, h\}$$

→ Select $(D \rightarrow EF) = first(first(EF) \cdot follow(D))$

$$= \{g, f, h\}$$

→ Select ($E \rightarrow g$) = {g}

Select ($CE \rightarrow C$) = {f, h}

Select ($F \rightarrow f$) = {f}

Select ($F \rightarrow E$) = {h}

a	b	c	f	g	h	s
S	ABOh					

B	CC	D	C	E	A	E	I	J	K	L	M
C	BC	E		E	A	E	I	J	K	L	M
D		EF		EF		EF					
E		G		G		G					
F		F		F		F					

Stack

\$

Input String	Production
aboh	ϵ
abohs	$S \rightarrow aboh$
bhgs	$B \rightarrow bh$
ccdhgs	$C \rightarrow cc$
cdhgs	$C \rightarrow cd$
bcdhgs	$C \rightarrow bc$
cdhs	$C \rightarrow cd$
bcdhs	$C \rightarrow bc$
cddhs	$C \rightarrow cd$
dhs	$C \rightarrow \epsilon$

FFhs
gFns
Fhs
fhg
hg
s

gfhs
gfhs
fhs
fhg
hg
s

D → EF
E → g
F → f

→ String is accepted.

Ex: 3 $S \rightarrow (L) | a$

$L \rightarrow LS | S$

Construct an table and check following string is accepted? (a, (a, a))

1. Remove Left Recursion

$S \rightarrow CL | a$

$L \rightarrow SL'$

$L' \rightarrow , SL' | E$

First(S) = {c, a}

first(L) = {c, a}

First(L') = {, c}

follow(S) = {g, , C}

follow(L) = {j}

follow(L') = {C}

Select ($S \rightarrow CL$) = First(First(CL)) · Follow(S)

$$= \{C\}$$

Select ($S \rightarrow a$) = {a}

Select ($L \rightarrow SL'$) = First(First(SL')) · Follow(L)

$$= \{C, a\}$$

Select ($L' \rightarrow , SL'$) = First(First(, SL')) · Follow(L')

$$= \{\}\$$

Select ($L' \rightarrow C$) = {}

(a)	,	\$
S (L)	a			
L SL'	SL'	C		
L'		SL'		

Stack

TIP String

Production

SS

(a, (a, a)) \$

(L) \$

(a, (a, a)) \$

$S \rightarrow CL$

L) \$

(a, (a, a)) \$

CL) \$

(a, (a, a)) \$

$S \rightarrow a$

L) \$

(a, (a, a)) \$

, SL') \$

(a, (a, a)) \$

$L' \rightarrow SL'$

SL') \$

(a, (a, a)) \$

Top-down: Expand the non-terminal to terminal
Bottom-up: Reduce the terminal to non-terminal upto starting symbol

Page
Date

(L) L' \$	(a,a) \$	S → L
L L' \$	(a,a) \$	L → SL
SL L' \$	(a,a) \$	S → a
aL L' \$	(a,a) \$	
L' L' \$	(a,a) \$	
SL' L' \$	(a,a) \$	L' → SL
SL' L' \$	(a,a) \$	
aL' L' \$	(a,a) \$	S → a
L' L' \$	(a,a) \$	
SL' L' \$	(a,a) \$	
L' L' \$	(a,a) \$	
L' \$	(a,a) \$	L' → E
L \$	(a,a) \$	L' → E
\$	(a,a) \$	

String accepted.

⇒ Note:

1. Check first grammar is left Recursion then remove left recursion
 2. Check grammar is left factoring, then remove it
- [Non-deterministic grammar is left factored to Convert deterministic first remove left factoring]

* Bottom-up Parser

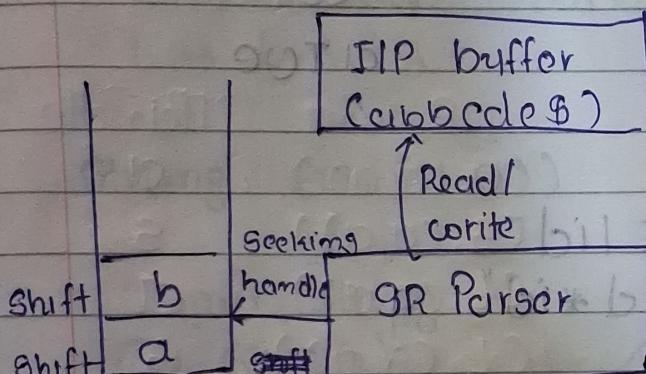
SR Parser

1. Shift : Push
2. Reduce : Pop

3. Accept : String accept

4. Error : Error in parsing

(4-operation / function)



S → aTc
T → Tbclb
c → d

Handle: Handle is substring that matches right hand side production rule in grammar and whose reduction to the non-terminal of left hand side of that grammar rule is at step alone reverse of right most derivation.

Ex: $S \rightarrow a T b c e$
 $T \rightarrow Tbclb$
 $U \rightarrow d$

find handle

IP string: cibbcode

Input string

cibbcode

aTbcde

aTde

aTbe

S

handle

b

TbC

d

rolled structure

(cibbcode)

Ex: $E \rightarrow E + E | E * E$ (id)

String: "id + id * id"

handle

id

id

E + E

id

E * E

id + id * id

id + id * E

id + E

E + E

E

id + id *

E

E + E

E

E

E + G

E + G

E + E

E + id

E + id

Input String

id + id * id

E + id * id

E + E * id

E + E * E

E + E

E

Handle

id

id

id

~~id E * E~~

E * E

Ex: S → (L) 1 a (W, D, P)

L → L, S | S

String: (a, (a, a))

Input String

(a, (a, a))

(S, (a, a))

(S, (S, a))

(S, (S, S))

(L, (S, S))

(L, (L, S))

(L, (L))

(L, S)

(L)

S

Handle

a

a

a

a

a

a

a

a

a

a

a

$S \rightarrow (L)$

~~(L, S)~~

~~(L, (L))~~

~~(L, (L, S))~~

~~(L, (S, S))~~

~~(S, (S, a))~~

~~(S, (a, a))~~

~~(a, (a, u))~~

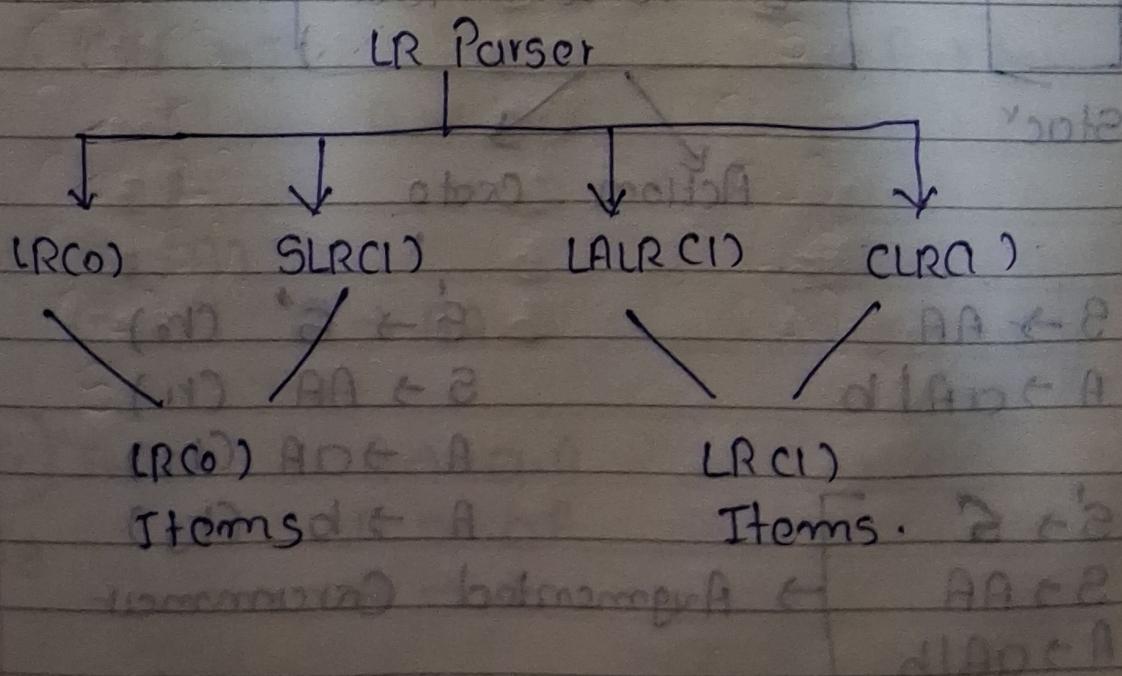
$S \rightarrow (L)$	IIP string	Handle
(L, S)	(ca, ca, a))	b
(L, (L))	(S, (a, a))	S
(L, (L, S))	(L, (a, a))	a
(L, (L, a))	(L, (S, a))	S
(L, (S, a))	(L, (L, a))	S
(L, (a, a))	(L, (L, S))	L, S
(S, (a, a))	(L, (L))	(L)
(a, (a, u))	(L, S)	(L, S)
	(L)	(L),
	S	

Ex: $E \rightarrow E + E \mid E * E \mid (E) \mid id$

String: id * (id+id) \$ Accept or not

Stack	Input String	Action
\$	id * (id + id) \$	Shift id
\$ id	* (id + id) \$	Reduce E → id
\$ E	* (id + id) \$	Shift *
\$ E *	(id + id) \$	Shift C
\$ E * C	id + id) \$	Shift id
\$ E * C id	+ id) \$	Reduce E → id
\$ E * C E	+ id) \$	Shift +
\$ E * C E +	id) \$	Shift id
\$ E * C E + id) \$	Reduce E → id
\$ E * C E + E) \$	Reduce E → E + E
\$ E * C E) \$	Shift)
\$ E * C E)	\$	Reduce E → C E)
\$ E * E	\$	Reduce E → E * E
\$ E	\$	Accept

* LR Parser



If we put "•" in production, it's called items.

$$S \rightarrow \cdot X Y Z \text{ (Items)}$$

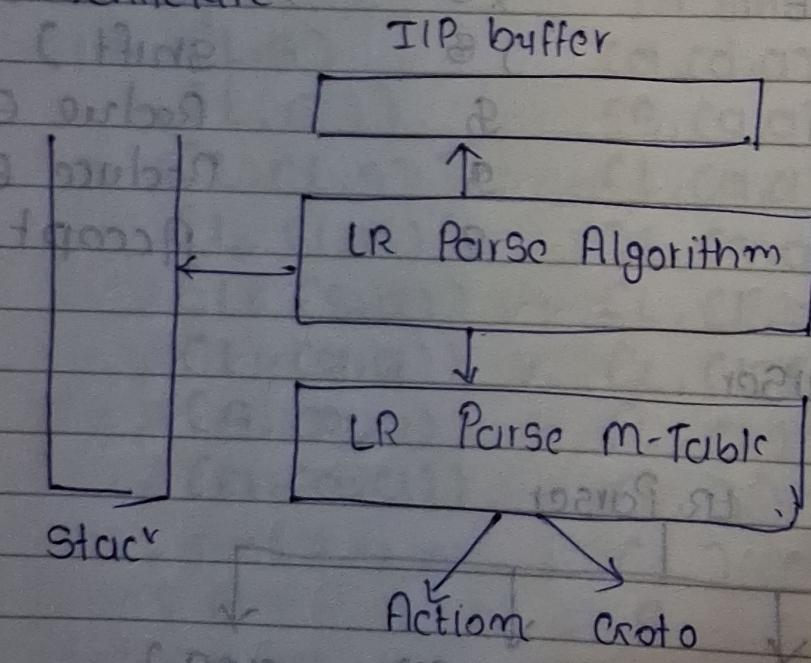
$$\cdot X Y Z$$

$$X Y \cdot Z$$

$$X Y Z \cdot$$

Entire seen production rule than we perform Reduce operation

Architecture:



Eg:

$$S \rightarrow AA$$

$$A \rightarrow a A b$$

$$S' \rightarrow S$$

$$S \rightarrow AA$$

$$A \rightarrow a A b$$

$$S \rightarrow S^* (r_0)$$

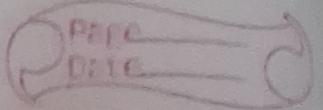
$$S \rightarrow AA (r_1)$$

$$A \rightarrow a A (r_2)$$

$$A \rightarrow b (r_3)$$

Augmented Grammar

- $I_0 : S' \rightarrow \cdot S$ → $(I_6 : (I_2, b))$
 $S \rightarrow \cdot AA$
 $A \rightarrow \cdot aA$
 $A \rightarrow \cdot b$
- $I_1 : (I_0, S)$ → $I_6 : (I_3, A)$
 $S' \rightarrow S.$ $A \rightarrow aA.$
- $I_2 : (I_0, A)$
 $S \rightarrow A \cdot A \rightarrow (I_7 : (I_3, a))$
 $A \rightarrow \cdot aA$
 $A \rightarrow \cdot b$ $A \rightarrow a \cdot A$
 $A \rightarrow \cdot aA$
- $I_3 : (I_0, a)$ $A \rightarrow \cdot b$
 $A \rightarrow a \cdot A$
 $A \rightarrow \cdot aA$
 $A \rightarrow \cdot b$ → $(I_8 : (I_3, b))$
- ↓
→ $I_4 : (I_0, b)$ $I_4 : A \rightarrow b.$
 $A \rightarrow b.$
- $I_5 : (I_2, A)$ $S \rightarrow AA.$
- $(I_6 : (I_2, a)) : I_3$ $A \rightarrow a \cdot A$
 $A \rightarrow \cdot aA$
 $A \rightarrow \cdot b$



→ m-table :

	Action			Grto
	a	b	\$	d, 3
I ₀	s ₃	s ₄	s ₅	1
I ₁				2
I ₂	s ₃	s ₄		5
I ₃	s ₃	s ₄		6
I ₄	r ₃	r ₃	r ₃	
I ₅	r ₁	r ₁	r ₁	A, d ← a
I ₆	r ₂	r ₂	r ₂	A, d ← A

String ← aabbbs

Stack	Input buffer	Action
\$	aabbbs	s ₃
\$, a ₃	abbbs	s ₃
\$, a ₃ , a ₃	bbbs	s ₄
\$, a ₃ , a ₃ , b ₄	bs	r ₃
\$, a ₃ , a ₃ , A ₅	b\$	r ₂
\$, a ₃ , A ₅	b\$	(d, r ₂)
\$, A ₂	b\$	s ₄
\$, A ₂ , b ₄	\$	r ₃
\$, A ₂ , A ₅	\$	(A, r ₁)
\$, S ₁	\$, AA ← a	Accept

Ex: $S \rightarrow dA|cB$ (SIT)
 $A \rightarrow bA|c$ (SF)
 $B \rightarrow bB|c$

$S' \rightarrow S$
 $S \rightarrow dA|cB$
 $A \rightarrow bA|c$
 $B \rightarrow bB|c$

$r_0 S' \rightarrow S$
 $r_1 S \rightarrow dA$
 $r_2 S \rightarrow cB$
 $r_3 A \rightarrow bA$
 $r_4 A \rightarrow c$
 $r_5 B \rightarrow bB$
 $r_6 B \rightarrow c$

$I_0: S' \rightarrow \cdot S$
 $S \rightarrow \cdot dA$
 $S \rightarrow \cdot cB$

$I_4: (I_2, A)$

$I_5: (I_2, b)$

$I_1: (I_0, S)$
 $S' \rightarrow S.$

$A \rightarrow b \cdot A$
 $A \rightarrow \cdot bA$
 $A \rightarrow \cdot c$

$I_2: (I_0, d)$

$S \rightarrow d \cdot A$
 $A \rightarrow \cdot bA$
 $A \rightarrow \cdot c$

$I_6: (I_2, C)$
 $A \rightarrow c \cdot A$

$I_3: (I_0, a)$
 $S \rightarrow a \cdot B$
 $B \rightarrow \cdot bB$
 $B \rightarrow \cdot c$

$I_7: (I_3, B)$
 $S \rightarrow aB \cdot$

$I_8: (I_3, b)$
 $B \rightarrow b \cdot B$
 $B \rightarrow \cdot bB$
 $B \rightarrow \cdot c$

I₉: (I₃, C)

$$\begin{array}{l} \text{ABC} \leftarrow \text{A} \\ \text{B} \rightarrow \text{C.B} \leftarrow \text{B} \\ \text{A} \leftarrow \text{A} \end{array}$$

I₁₀: (I₅, A)

$$\begin{array}{l} \text{ABC} \leftarrow \text{A} \\ \text{B} \leftarrow \text{B} \\ \text{A} \rightarrow \text{BA} \leftarrow \text{B} \end{array}$$

(I₁₂): (I₈, C)

$$\begin{array}{l} \text{I}_8 \\ \text{B} \rightarrow \text{C.B} \leftarrow \text{B} \end{array}$$

(I₁₁): (I₅, b)

$$\begin{array}{l} f_5 \text{A} \rightarrow \text{b.A} \\ \text{A} \rightarrow \text{.bA} \leftarrow \text{a} \\ \text{A} \rightarrow \text{.C} \end{array}$$

(I₁₁): (I₅, c)

$$\begin{array}{l} f_5 \text{A} \leftarrow \text{A} \\ I_6 \text{A} \rightarrow \text{C.A} \end{array}$$

I₁₁: (I₈, B)

$$\text{B} \rightarrow \text{b.B} \leftarrow \text{A}$$

(I₁₂): (I₈, b)

$$\begin{array}{l} I_8 \\ \text{B} \rightarrow \text{b.B} \\ \text{B} \rightarrow \text{b.B} \leftarrow \text{B} \\ \text{B} \rightarrow \text{.CD} \leftarrow \text{B} \\ \text{B} \leftarrow \text{D} \end{array}$$

LR(0) we can't check follow, it possible
to take unnecessary step

⇒ m-table:

	Action					Context	S	A	B
	d	a	b	c	\$				
I ₀	s ₂	s ₃					1		
I ₁						Accept			
I ₂			s ₅	s ₆				4	
I ₃			s ₈	s ₉					7
I ₄	r ₁	r ₁	r ₁	r ₁					
I ₅			s ₅	s ₆				10	
I ₆	r _u	r _u	r _u	r _u					
I ₇	r ₂	r ₂	r ₂	r ₂					
I ₈			s ₈	s ₉				11	
I ₉	r ₆	r ₆	r ₆	r ₆					
I ₁₀	r ₃	r ₃	r ₃	r ₃					
I ₁₁	r ₅	r ₅	r ₅	r ₅					

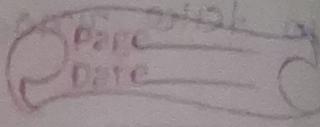
"d b b b a"

Stack	TIP buffer	Action
s ₀	dbbba\$	s ₂
s ₀ s ₂	bbbba\$	d s ₅
s ₀ s ₂ b ₅	bbba\$	s ₅
s ₀ s ₂ b ₅ b ₈	bbas\$	s ₅
s ₀ s ₂ b ₅ b ₈ b ₁₈	bas\$	s ₅
s ₀ s ₂ b ₅ b ₈ b ₁₈ b ₈	a\$	Error

"dbbbc"

multiple entry in table than not LR.

If SIR both together than not LR



Stack	TIP buffer	Action
\$0	bb	82b
\$0d2	bbC	82 S5
\$0d2bs	bC	S5
\$0d2bsbs	BC	85
\$0d2bsbsbs	C	86
\$0d2bsbsbsCs		r4
\$0d2bsbsbsA10		r3
\$0d2bsbsA10		r3
\$0d2bsA10		r3
\$0d2A4		r1
\$0S1		21 Accept
*		
SLR(1):		

Eoc: $S \rightarrow AA$

follow(A) = { \$, a, b }

$A \rightarrow aAb$

follow(S) = { \$ }

main A

rolled TIP

input

action

\$0d2bs

goto

2

C 22 b

\$ 21 d2d

3

Abs

I0 S3 22 S4

21 d2d

1

I1 22

accept

21 d

22 d2d2d2

I2 S3 S4

21 d

22 d2d2d2

I3 S3 S4

21

5bot

I4 r3 r3 r3

r1

6

I5 r2 r2 r2

r1

"2dddb"

Ex: $E \rightarrow T + E \mid T$
 $T \rightarrow i$

$S' \rightarrow E \stackrel{r_0}{\mid} r_1$
 $E \rightarrow T + E \mid T$
 $T \rightarrow i$

$I_0: S' \rightarrow \cdot E$
 $E \rightarrow \cdot T + E$
 $T \rightarrow \cdot i$
 $E \rightarrow \cdot T$

$I_1: (I_0, E)$

$S' \rightarrow E \cdot$

$I_2: (I_0, T)$

$E \rightarrow T \cdot + E$
 $E \rightarrow T \cdot$

$I_3: (I_0, i)$

$\overline{T} \rightarrow i \cdot$

$I_4: (I_2, +)$

$E \rightarrow T + \cdot E$

$E \rightarrow \cdot T + E$

$E \rightarrow \cdot T$
 $T \rightarrow \cdot i$

$I_5: (I_4, E)$

$(I_G): (I_4, T)$

$I_2 \quad E \rightarrow T \cdot + E +$
 $E \rightarrow T \cdot$

$(I_G): (I_4, i)$

$I_3 \quad T \rightarrow i \cdot$

Action

	+	i	\$
I ₀		S ₃	

I₁ Accept

I₂ S_{4/r₂} r₂ r₂

I₃ r₃ r₃ r₃

I₄ S₃ T

I₅ r₁ r₁ r₁

[Conflict no, not parsing LR(0)]

\Rightarrow SLR(1) \leftarrow follow(E) = { \$ }
 follow(CT) = { +, \$ }

Action

	+	i	\$
I ₀		S ₃	

Accept

I₂ S₄ r₂

I₃ r₃ r₃

I₄ S₃ T

I₅ r₁

GoTo

E	T
1	2

(T, o₁) : o₁

3 + T \leftarrow 3

5 T \leftarrow 2

(I₅, T) : T

... j \leftarrow T

(+ s₁) : u₁

3 + T \leftarrow 3

3 + T \leftarrow 3

Bottom-up not required to remove
left Recursion



Ex:

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

~~$$E' \rightarrow E \mid E + T \mid T$$~~

$$E \rightarrow E + T \quad r_1$$

$$E \rightarrow T \quad r_2$$

$$T \rightarrow T * F \quad r_3$$

~~$$T \rightarrow F \quad r_4$$~~

~~$$F \rightarrow (E) \quad r_5$$~~

~~$$F \rightarrow id \quad r_6$$~~

~~$$E' \rightarrow E$$~~

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

~~$$F \rightarrow (E) \mid id$$~~

$$I_0: \quad E' \rightarrow .E$$

$$E \rightarrow .E + T$$

$$E \rightarrow .T$$

$$T \rightarrow .T * F$$

$$T \rightarrow .F$$

$$F \rightarrow .(E)$$

$$F \rightarrow .id$$

$$I_u: (I_0, F)$$

~~$$F \rightarrow .(E)$$~~

~~$$E \rightarrow .E + T$$~~

~~$$E \rightarrow .T$$~~

~~$$T \rightarrow .T * F$$~~

~~$$T \rightarrow .F$$~~

~~$$F \rightarrow .(E)$$~~

~~$$F \rightarrow .id$$~~

$$I_1: (I_0, E)$$

$$E' \rightarrow E.$$

$$I_4.$$

~~$$I_4. \quad (I_0, C)$$~~

$$I_2: (I_0, E)$$

$$E \rightarrow E. + T$$

~~$$E \rightarrow x.$$~~

$$F \rightarrow (.E)$$

$$E \rightarrow .E + T$$

$$E \rightarrow .T$$

$$T \rightarrow .T * F$$

~~$$T \rightarrow .F$$~~

~~$$F \rightarrow .(E)$$~~

~~$$F \rightarrow .id$$~~

$$I_3: (I_0, T)$$

$$T \rightarrow T. * F$$

$$E \rightarrow T.$$

~~$$T \rightarrow (.F)$$~~

~~$$F \rightarrow .(E)$$~~

~~$$F \rightarrow .id$$~~

$$I_3: (I_0, F) : T \rightarrow F.$$

Diagram of bottom up parsing
Method [1] - [2]

I₅

P₅: (I₀, id)

F → id

I₆

P₆: (I₂, +)

E → E + T

T → . T * F

T → . F

E → . (E)

F → . id

I₇

P₇: (I₂, *)

T → T * . F

F → . (E)

F → . id

I₈ I₄

P₈: (I₈, E)

F → (E.)

I₉: (I₆, T)

E → E + T.

I₁₀ I₇

P₉: (I₆, F)

(E) . T

T → T * F.

T I T + 3 ← 3

I₁₁ I₁₃ I₈ T ← T

P₁₀: (Z₉,)

F → (E).

T I T + 3 ← 3

I₁₁ I₁₃ * T ← T

Follow(E) = {+,), \$}

follow(T) = {* , +,), \$}

T + 3, ← 3

Follow(F) = {* , +,), \$}

T + 3, ← 3

(E). (E) ← 3

b. ← 3

(E, .) ← 3

3 ← 3

(E, .) ← 3

3 ← 3

(E, .) ← 3

3 ← 3

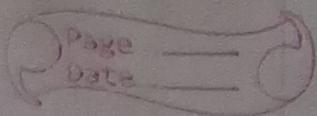
(T, .) ← 3

3 * T ← T

3 ← 3

SR - Conflict (Shift-Reduce)

RR - Conflict (Reduce-Reduce)



⇒ LR(0)

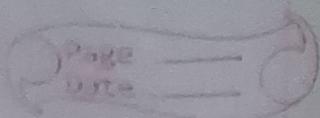
	Action				Cronto				
	+	*	C)	id	\$	E	T	F
I ₀			S ₄		S ₅		I		
I ₁	S ₆					Accept			
I ₂	r ₂	S ₇ /r ₂	r ₂	r ₂	r ₂	r ₂			
I ₃	r ₄	r ₄	r ₄	r ₄	r ₄	r ₄			
I ₄			S ₄		S ₅		8	2	3
I ₅	r ₆	r ₆	r ₆	r ₆	r ₆	r ₆			
I ₆			S ₄		S ₅			9	3
I ₇			S ₄		S ₅				10
I ₈				S ₁₁					
I ₉	r ₁	r ₁	r ₁	r ₁	r ₁	r ₁			
I ₁₀	r ₃	r ₃	r ₃	r ₃	r ₃	r ₃			
I ₁₁	r ₅	r ₅	r ₅	r ₅	r ₅	r ₅			

⇒ SLR(1)

	+	*	C)	id	\$	E	T	F
I ₀			S ₄		S ₅		I	2	3
I ₁	S ₆					Accept			
I ₂	r ₂	S ₇ /	-	r ₂	-	r ₂			
I ₃	r ₄	r ₄	r ₄	r ₄		r ₄			
I ₄			S ₄		S ₅		8	2	3
I ₅	r ₆	r ₆	r ₆			r ₆			
I ₆			S ₄		S ₅			9	3
I ₇			S ₄		S ₅				10
I ₈				S ₁₁					
I ₉	r ₁		r ₁		r ₁				
I ₁₀	r ₂		r ₂		r ₂				

SR-Conflict (Shift-Reduce)

RR-Conflict (Reduce-Reduce)



⇒ LRCO?

	Action						Goto		
	+	*	()	id	\$	E	T	F
I ₀			S ₄		S ₅		I		
I ₁	S ₆					Accept			
I ₂	r ₂	S ₇ /r ₂	r ₂	r ₂	r ₂	r ₂			
I ₃	r ₄	r ₄	r ₄	r ₄	r ₄	r ₄			
I ₄			S ₄		S ₅		8	2	3
I ₅	r ₆	r ₆	r ₆	r ₆	r ₆	r ₆			
I ₆			S ₄		S ₅			9	3
I ₇			S ₄		S ₅				10
I ₈				S ₁₁					
I ₉	r ₁	r ₁	r ₁	r ₁	r ₁	r ₁			
I ₁₀	r ₃	r ₃	r ₃	r ₃	r ₃	r ₃			
I ₁₁	r ₅	r ₅	r ₅	r ₅	r ₅	r ₅			

⇒ SLR(1)

	+	*	()	id	\$	E	T	F
I ₀			S ₄		S ₅		I	2	3
I ₁	S ₆					Accept			
I ₂	r ₂	S ₇ /	-	r ₂	-	r ₂			
I ₃	r ₄	r ₄	r ₄	r ₄	r ₄	r ₄			
I ₄			S ₄		S ₅		8	2	3
I ₅	r ₆	r ₆	r ₆	r ₆	r ₆	r ₆			
I ₆			S ₄		S ₅			9	3
I ₇			S ₄		S ₅				10
I ₈				S ₁₁					
I ₉	r ₁		r ₁		r ₁				
I ₁₀	r ₃	r ₃	r ₃	r ₃	r ₃	r ₃			

$S \rightarrow AaAb \mid BaBb$
 $A \rightarrow E$
 $B \rightarrow G$

$S' \rightarrow S \quad r_0$
 $S \rightarrow AaAb \mid BaBb \quad r_2$
 $A \rightarrow E \quad r_3$
 $B \rightarrow G \quad r_4$

$I_0: \quad S' \rightarrow .S$
 $S \rightarrow .AaAb$
 $S \rightarrow .BaBb$
 $A \rightarrow .$
 $B \rightarrow .$

$I_5: (I_3, A)$
 $S \rightarrow Ba.Bb$
 $B \rightarrow .$
 $I_6: (I_4, A)$

$I_1: (I_0, S)$
 $S' \rightarrow S.$

$S \rightarrow AaA.b$
 $|$
 $I_7: (I_5, B)$

$I_2: (I_0, A)$
 $S \rightarrow A.cABb$

$S \rightarrow BaB.b$

$I_3: (I_0, B)$
 $S \rightarrow B.cABb$

$I_8: (I_6, b)$

$I_4: (I_2, a)$
 $S \rightarrow Aa.Ab$
 $A \rightarrow .$

$S \rightarrow AaAb.$
 $I_9: (I_7, b)$
 $S \rightarrow BaB.b.$

LR(0)

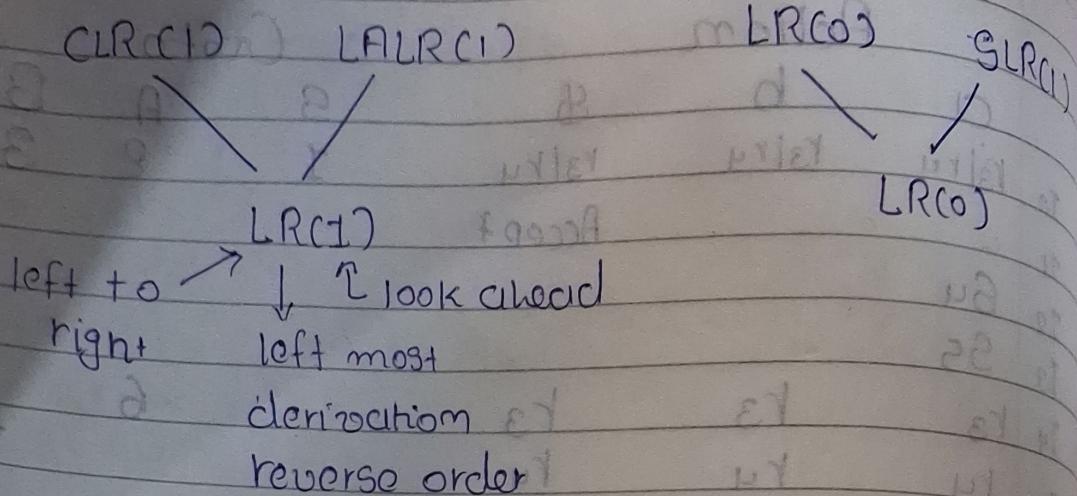
Action

	a	b	\$	Context	Croto
I0	r3 ru	r3 ru	r3 ru	I	S A B
I1			Accept		2 3
I2	S4				
I3	S5				
I4	r3	r3	r3	r3	6
I5	ru	ru	ru	ru	7
I6		S8			
I7		S9			
I8	r1	r1	r1	r1	
I9	r2	r2	r2	r2	B AA. ← B

SLR(1)

Action

	a	b	\$	Context	Croto
I0	r3 r4			I AA. ← A	S A B
I1			Accept		2 3
I2	S4				
I3	S5				
I4	r3	(A. ← A)			
I5	r4	A. A ← A			
I6		S8		d1D. AA. ← A	6
I7		S9		d1D. d. ← A	7
I8			r1		
I9			r2		
I10				d1D. A. A ← A	
I11				d1D. AA. ← A	
I12				d1D. d. ← A	

\Rightarrow 

$$LR(0) + \text{lookahead} = LR(1)$$

$$S \rightarrow \cdot AA, \$$$

\approx look ahead

CLRC10 \rightarrow Reduction only in lookahead part

$$\begin{aligned} S &\rightarrow \cdot AA, r_1 & S' &\rightarrow \cdot S, r_0 \\ A &\rightarrow \cdot aA, r_2 & & \\ A &\rightarrow \cdot b, r_3 & & \end{aligned}$$

$$\begin{aligned} I_0: \quad S' &\rightarrow \cdot S, \$ \\ B &\rightarrow \cdot AA, \$ \\ A A &\rightarrow \cdot aA, a/b \\ F \quad A &\rightarrow \cdot b, a/b \end{aligned}$$

$$\begin{aligned} I_2(I_0, A) \\ B &\rightarrow \cdot A.A, \$ \\ A &\rightarrow \cdot aA, \$ \\ A &\rightarrow \cdot b, \$ \end{aligned}$$

$$I_1: \quad S' \rightarrow \cdot S, \$$$

$$I_3(I_0, A)$$

$$\begin{aligned} A &\rightarrow \cdot a.A, a/b \\ A &\rightarrow \cdot aA, a/b \\ A &\rightarrow \cdot b, a/b \end{aligned}$$

CLR mot any conflict RR and SR

If any conflict than Grammar ambiguous.

I₁: (I₀, b)

A → b., clb

I₈: (I₃, A)

A → cA., clb

I₅: (I₂, A)

A → AA., \$

I₉¹³: (I₃, a)

A → a.A, clb

A → cA, clb

A → .b, clb

I₆: (I₂, a)

A → a.A, \$

I₉¹⁴: (I₃, b)

A → .cA, \$

A → .b, \$

A → b., clb

I₇: (I₂, b)

A → b., \$

I₉: (I₆, A)

A → cA., \$

I₁₀^{I₆}: (I₆, a)

A → a.A, \$

I₁₀^{I₆}: (I₆, b)

A → .cA, \$

A → b., \$

A → .b, \$

Action

cl
I₁₀

b
S₃

\$

S₄

Go To

A

1 (2)

Accept

I₂

S₆

S₇

5

I₃

S₈

S₇

8

I₄

r₃

r₃

2, 3, 4, 5, 6, 7

I₅

r₁

8, 9, 10

I₆

S₆

S₇

2, 3, 4, 5, 6, 7, 8, 9

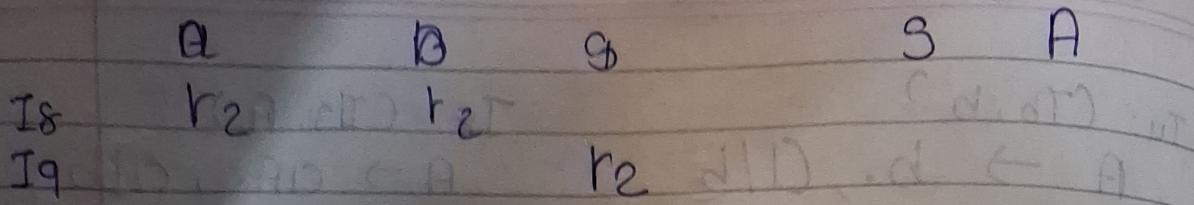
I₇

r₃

10, 11

[CLR > LR(0) = SLR(1) = LALR(1)] It can be seen

↳ CLR more powerful than Parsing



→ LALR(1) is shrinking of CLR(1)

→ Parsing Table for LALR(1)

	Action	Cat 0
I ₀	C ₁ S ₃ PT g	S. A → A
I ₁	S ₃ S ₄	I. d. 2 → A
I ₂	S ₃ S ₄	(d. 5) PT
I ₃	S ₃ S ₄ PT	P. . 89 A
I ₄	r ₃ A. D. r ₃ r ₃	P. A. D. ← A
I ₅		P. A. D. ← A
I ₆	r ₂ r ₂ r ₂	P. A. D. ← A
I ₇		P. A. D. ← A
I ₈		P. d. ← A
I ₉		P. d. ← A
Exc:	$S \rightarrow B a b B c d c b d a$ $B \rightarrow d (c s)$	$S^1 \rightarrow S \quad r_0$

$$I_0 : S^1 \rightarrow .S, g$$

$$S \rightarrow .B a, g$$

$$S \rightarrow .b B c, g$$

$$S \rightarrow .d c, g$$

$$S \rightarrow .b d a, g$$

$$B \rightarrow .d, a$$

I₁: (I₀, S)

S → S., \$

I₂: (I₁, C)

S → dC., \$

I₂: (I₀, B)

S → B.a., \$

I₃: (I₀, C)

S → aBC., B

I₃: (I₀, b)

S → b.BC., \$

I₁₀: (I₉, a)

S → bda., \$

B → .d, C

S → b.da., \$

I₄: (I₀, d)

S → d.c., \$

B → d..a

I₅: (I₂, a)

S → Ba., \$

I₆: (I₃, B)

S → bB.c., \$

I₇: (I₃, d)

B → d., C

S → bd.a., \$

7) I₁: (I₁, C)

	Action					Croto
	a	b	c	d	\$	s B
I ₀			S ₃		S ₄	I 2
I ₁						Accept
I ₂	S ₅					(a, b) . PT
I ₃				S ₇		6
I ₄	r ₅		S ₈			a . b . d ← 2
I ₅					r ₁	
I ₆			S ₉			(a, b) . PT
I ₇	S ₁₀ . nbd		r ₅			a . b . d ← 2
I ₈					r ₃	a . b . d ← 2
I ₉					r ₂	a . b . d ← 2
I ₁₀					r ₄	

Ex: $E \rightarrow E + T \mid T$ $E' \rightarrow E \text{ (cro) } \theta$
 $T \rightarrow T^* F \mid F$
 $F \rightarrow \text{id} \text{ crs)$

I₀: $E' \rightarrow \cdot E, \$.$

$E \rightarrow \cdot E + T, \$ \mid +$

$E \rightarrow \cdot T, \$ \mid +$

$T \rightarrow \cdot T^* F, \$ \mid + \mid *$

$T \rightarrow \cdot F, \$ \mid + \mid *$

$F \rightarrow \cdot \text{id}, \$ \mid + \mid *$

I₁ ($\hookrightarrow I_0, E$)

$E' \rightarrow E, \$$

$E' \rightarrow E, \$$

$E \rightarrow E + T, \$ \mid +$

I₂: (I₀, T)

(b₁, a₁) (T)

E → T₀, \$ | +

T → T₀ * F, \$ | + | *

I₃: (I₀, F)

(T, a₁) (F)

T → F₀, \$ | + | * | a₁ . . . T ← T

I₄: (I₀, id)

(b₁, a₁) (id)

F → id., \$ | + | * | a₁ . . . b₁ ← ?

I₅: (I₁, +)

(*, a₁) (P)

E → E + . T, \$ | +

T → . T * E, \$ | + | *

T → . F + , \$ | + | *

F → . id , \$ | + | *

I₆: (I₂, *)

(a₁, b₁) A

T → T * . F, \$ | + | *

F → . id , \$ | + | *

I₇: (I₅, T)

E → E + T, \$ | +

T → T * F, \$ | + | *

I₈: (I₅, F)

T → F, \$ | + | *

I₈: (I_S, id)

I_u

F → id., \$ | + | *

I₈: (I_G, F)

T → T * F., \$ | + | *

I₉: (I_C, id)

I_u

F → id., \$ | + | *

I₉: (I_T, *)

I_C

E → E T → T * . F, \$ | + | * ← T

F → . id | \$ | + | * ← T

I₉

Action

(Root) : T

+ * id | \$ | + | * ← E T C F

I₀

S₄ I b i 2 3

I₁ S₅

Accept

I₂ r₂ S₆

r₂

I₃ r₄ r₄

r₄

I₄ r₅ r₅

r₅

I₅

S₄

7 3

I₆

S₄

8

I₇ r₁

r₁

I₈ r₃ r₃

r₃

* Chomsky Hierarchy:

⇒ 4 type of Grammar

1 type-0: Unrestricted Grammar

2 type-1: Context Sensitive Grammar

3 type-2: Context Free Grammar

4 type-3: Regular Grammar

1. Type 0

$$\alpha \rightarrow \beta$$

$$\alpha \in (V_n \cup V_t)^+$$

$$\beta \in (V_n \cup V_t)^*$$

e.g. $AabB \rightarrow cdF$

Type 1

$$C_m = \{V_n, V_t, S, P\}$$

$$\alpha \rightarrow \beta,$$

where $|\alpha| \leq |\beta|$

and $\beta \neq \text{Null}$

ex: $S \rightarrow abc$ (Type 0 and Type 1)

$S \rightarrow \epsilon$ (Type 0 only)

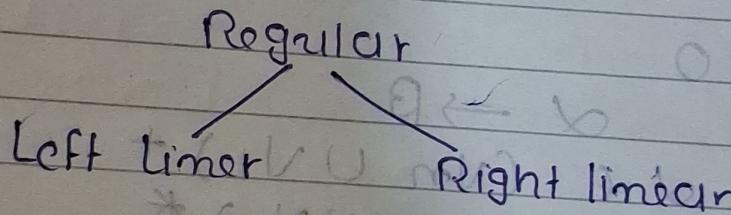
3 Context Free Grammar

$$\alpha \rightarrow \beta \quad \alpha \in V_n$$

$$\beta \in (V_n \cup V_f)^*$$

Left side only 1 non terminal

4 Regular Grammar



$$A \rightarrow WB \quad (\text{left most position contains non terminal})$$

$$A \rightarrow BW \quad (\text{right most position contains non terminal})$$

Ex.

$$S_1 \rightarrow S_1 a \quad (\text{left linear})$$

$$S \rightarrow a S \quad (\text{right linear})$$

Ex. $O \{ O | I \}^*$ write left linear and Right linear grammar

$$S \rightarrow O A$$

$$A \rightarrow O A | I A | E$$

(Right linear?)

$$S \rightarrow S O | S I | O$$

Intermediate
Code Optimization
Error detection
Symbol Table