

ML :-

By Bayes Theorem,

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)}$$

$$\textcircled{1} \quad P(\text{sunny} | \text{a cone of ice cream}) = \frac{P(\text{a cone of ice cream} | \text{sunny}) \cdot P(\text{sunny})}{P(\text{a cone of ice cream})}$$

$$\therefore P(\text{a cone of ice cream} | \text{sunny}) \cdot P(\text{sunny})$$

$$P(\text{a cone of ice cream} | \text{rainy}) \cdot P(\text{rainy})$$

Being Naive :-

$$P(\text{a cone of ice cream}) = P(a) \cdot P(\text{cone}) \cdot P(\text{of}) \cdot P(\text{ice}) \cdot P(\text{cream})$$

As we want to find bigger probability, we can ignore divisor.

$$P(\text{sunny} | \text{a cone of ice cream}) = P(\text{sunny}/a) \cdot P(\text{sunny}/\text{cone}) \cdot P(\text{sunny}/\text{of}) \\ \cdot P(\text{sunny}/\text{ice}) \cdot P(\text{sunny}/\text{cream}) \\ P(\text{sunny})$$

\textcircled{2} \quad P(\text{rainy} | \text{a cup of hot coffee}) = \frac{P(\text{a cup of hot coffee} | \text{rainy}) \cdot P(\text{rainy})}{P(\text{a cup of hot coffee})}

$$\therefore P(\text{a cup of hot coffee} | \text{rainy}) \cdot P(\text{rainy})$$
$$P(\text{a cup of hot coffee} | \text{sunny}) \cdot P(\text{sunny})$$

Being Naive :-

$$P(\text{a cup of hot coffee}) = P(a) \cdot P(\text{cup}) \cdot P(\text{of}) \cdot P(\text{hot}) \cdot P(\text{coffee})$$

As we want to find bigger probability, we can ignore divisor.

$$P(\text{rainy} | \text{a cup of hot coffee}) = P(\text{rainy}/a) \cdot P(\text{rainy}/\text{cup}) \cdot P(\text{rainy}/\text{of}) \\ \cdot P(\text{rainy}/\text{hot}) \cdot P(\text{rainy}/\text{coffee})$$