```
In [1]:
             from sklearn.datasets import load boston
             boston = load boston()
          2
          3
             import matplotlib.pyplot as plt
In [2]:
         1
            print(boston.data.shape)
        (506, 13)
In [3]:
             print(boston.feature_names)
        ['CRIM' 'ZN' 'INDUS' 'CHAS' 'NOX' 'RM' 'AGE' 'DIS' 'RAD' 'TAX' 'PTRATIO'
         'B' 'LSTAT']
In [4]:
             print(boston.target)
              21.6 34.7 33.4 36.2 28.7 22.9 27.1 16.5 18.9 15.
         18.2 19.9 23.1 17.5 20.2 18.2 13.6 19.6 15.2 14.5 15.6 13.9 16.6 14.8
         18.4 21. 12.7 14.5 13.2 13.1 13.5 18.9 20. 21. 24.7 30.8 34.9 26.6
         25.3 24.7 21.2 19.3 20. 16.6 14.4 19.4 19.7 20.5 25.
                                                               23.4 18.9 35.4
         24.7 31.6 23.3 19.6 18.7 16. 22.2 25.
                                                33. 23.5 19.4 22.
                                                                    17.4 20.9
         24.2 21.7 22.8 23.4 24.1 21.4 20.
                                           20.8 21.2 20.3 28.
                                                                23.9 24.8 22.9
         23.9 26.6 22.5 22.2 23.6 28.7 22.6 22. 22.9 25.
                                                           20.6 28.4 21.4 38.7
         43.8 33.2 27.5 26.5 18.6 19.3 20.1 19.5 19.5 20.4 19.8 19.4 21.7 22.8
         18.8 18.7 18.5 18.3 21.2 19.2 20.4 19.3 22. 20.3 20.5 17.3 18.8 21.4
         15.7 16.2 18.
                        14.3 19.2 19.6 23.
                                           18.4 15.6 18.1 17.4 17.1 13.3 17.8
         14.
              14.4 13.4 15.6 11.8 13.8 15.6 14.6 17.8 15.4 21.5 19.6 15.3 19.4
              15.6 13.1 41.3 24.3 23.3 27. 50. 50.
                                                      50.
                                                           22.7 25.
                                                                    50.
         23.8 22.3 17.4 19.1 23.1 23.6 22.6 29.4 23.2 24.6 29.9 37.2 39.8 36.2
         37.9 32.5 26.4 29.6 50.
                                  32.
                                       29.8 34.9 37.
                                                      30.5 36.4 31.1 29.1 50.
         33.3 30.3 34.6 34.9 32.9 24.1 42.3 48.5 50.
                                                      22.6 24.4 22.5 24.4 20.
         21.7 19.3 22.4 28.1 23.7 25.
                                       23.3 28.7 21.5 23.
                                                           26.7 21.7 27.5 30.1
         44.8 50. 37.6 31.6 46.7 31.5 24.3 31.7 41.7 48.3 29.
                                                               24.
                                                                    25.1 31.5
                       20.1 22.2 23.7 17.6 18.5 24.3 20.5 24.5 26.2 24.4 24.8
         23.7 23.3 22.
         29.6 42.8 21.9 20.9 44.
                                  50.
                                       36.
                                            30.1 33.8 43.1 48.8 31.
                                                                     36.5 22.8
         30.7 50. 43.5 20.7 21.1 25.2 24.4 35.2 32.4 32.
                                                           33.2 33.1 29.1 35.1
                             32.2 22.
                                       20.1 23.2 22.3 24.8 28.5 37.3 27.9 23.9
         45.4 35.4 46.
                        50.
         21.7 28.6 27.1 20.3 22.5 29. 24.8 22. 26.4 33.1 36.1 28.4 33.4 28.2
         22.8 20.3 16.1 22.1 19.4 21.6 23.8 16.2 17.8 19.8 23.1 21. 23.8 23.1
                        24.6 23. 22.2 19.3 22.6 19.8 17.1 19.4 22.2 20.7 21.1
         20.4 18.5 25.
         19.5 18.5 20.6 19. 18.7 32.7 16.5 23.9 31.2 17.5 17.2 23.1 24.5 26.6
         22.9 24.1 18.6 30.1 18.2 20.6 17.8 21.7 22.7 22.6 25.
                                                                19.9 20.8 16.8
         21.9 27.5 21.9 23.1 50.
                                  50.
                                       50.
                                            50.
                                                 50. 13.8 13.8 15.
         13.1 10.2 10.4 10.9 11.3 12.3 8.8
                                            7.2 10.5
                                                      7.4 10.2 11.5 15.1 23.2
          9.7 13.8 12.7 13.1 12.5 8.5
                                             6.3 5.6
                                                      7.2 12.1
                                                                8.3
                                                                      8.5
                                       5.
         11.9 27.9 17.2 27.5 15.
                                  17.2 17.9 16.3 7.
                                                       7.2 7.5 10.4
                                                                     8.8
         16.7 14.2 20.8 13.4 11.7 8.3 10.2 10.9 11.
                                                       9.5 14.5 14.1 16.1 14.3
         11.7 13.4 9.6 8.7 8.4 12.8 10.5 17.1 18.4 15.4 10.8 11.8 14.9 12.6
         14.1 13. 13.4 15.2 16.1 17.8 14.9 14.1 12.7 13.5 14.9 20.
                                                                    16.4 17.7
         19.5 20.2 21.4 19.9 19. 19.1 19.1 20.1 19.9 19.6 23.2 29.8 13.8 13.3
         16.7 12. 14.6 21.4 23. 23.7 25. 21.8 20.6 21.2 19.1 20.6 15.2 7.
          8.1 13.6 20.1 21.8 24.5 23.1 19.7 18.3 21.2 17.5 16.8 22.4 20.6 23.9
         22.
              11.9]
```

LinearRegression In [5]: print(boston.DESCR) Boston House Prices dataset Notes _ _ _ _ _ _ Data Set Characteristics: :Number of Instances: 506 :Number of Attributes: 13 numeric/categorical predictive :Median Value (attribute 14) is usually the target :Attribute Information (in order): - CRIM per capita crime rate by town - ZN proportion of residential land zoned for lots over 25,000 s q.ft. - INDUS proportion of non-retail business acres per town - CHAS Charles River dummy variable (= 1 if tract bounds river; 0 o therwise) - NOX nitric oxides concentration (parts per 10 million) average number of rooms per dwelling - RM proportion of owner-occupied units built prior to 1940 AGE weighted distances to five Boston employment centres - DIS - RAD index of accessibility to radial highways - TAX full-value property-tax rate per \$10,000 - PTRATIO pupil-teacher ratio by town 1000(Bk - 0.63)^2 where Bk is the proportion of blacks by to - B wn - LSTAT % lower status of the population MEDV Median value of owner-occupied homes in \$1000's

:Missing Attribute Values: None

:Creator: Harrison, D. and Rubinfeld, D.L.

This is a copy of UCI ML housing dataset.

http://archive.ics.uci.edu/ml/datasets/Housing (http://archive.ics.uci.edu/ml/d atasets/Housing)

This dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.

The Boston house-price data of Harrison, D. and Rubinfeld, D.L. 'Hedonic prices and the demand for clean air', J. Environ. Economics & Management, Used in Belsley, Kuh & Welsch, 'Regression diagnostics vol.5, 81-102, 1978. N.B. Various transformations are used in the table on ...', Wiley, 1980. pages 244-261 of the latter.

The Boston house-price data has been used in many machine learning papers that address regression problems.

^{**}References**

10/27/2018 LinearRegression

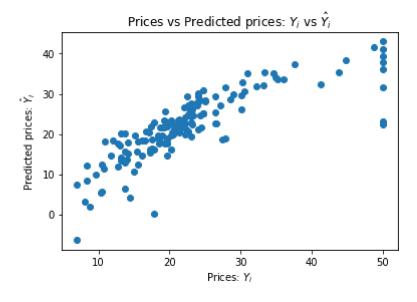
- Belsley, Kuh & Welsch, 'Regression diagnostics: Identifying Influential Da ta and Sources of Collinearity', Wiley, 1980. 244-261.

- Quinlan, R. (1993). Combining Instance-Based and Model-Based Learning. In Proceedings on the Tenth International Conference of Machine Learning, 236-243, University of Massachusetts, Amherst. Morgan Kaufmann.
- many more! (see http://archive.ics.uci.edu/ml/datasets/Housing) (http://ar chive.ics.uci.edu/ml/datasets/Housing))

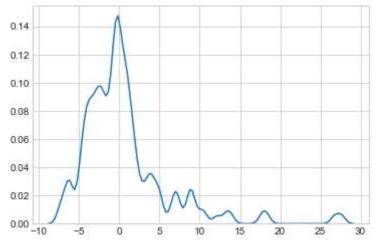
```
In [6]:
         1
             import pandas as pd
             bos = pd.DataFrame(boston.data)
             print(bos.head())
                      1
                            2
                                 3
                                               5
                                                     6
                                                             7
                                                                              10
                                                                  8
                                                  65.2 4.0900
                                                                      296.0
        0 0.00632
                    18.0
                          2.31
                                0.0
                                     0.538
                                           6.575
                                                                1.0
                                                                            15.3
        1 0.02731
                                    0.469 6.421
                                                  78.9 4.9671
                                                                2.0
                                                                     242.0
                     0.0
                         7.07
                                0.0
                                                                            17.8
        2 0.02729
                          7.07
                                    0.469 7.185
                                                  61.1 4.9671
                                                                2.0
                                                                     242.0
                                                                            17.8
                     0.0
                                0.0
        3 0.03237
                               0.0 0.458 6.998
                                                  45.8 6.0622 3.0
                     0.0
                         2.18
                                                                     222.0 18.7
        4 0.06905
                     0.0
                         2.18
                               0.0 0.458 7.147
                                                  54.2 6.0622 3.0
                                                                     222.0 18.7
               11
                     12
        0
          396.90 4.98
          396.90 9.14
        1
        2
          392.83 4.03
        3
           394.63 2.94
          396.90 5.33
In [7]:
             bos['PRICE'] = boston.target
         1
          2
            X = bos.drop('PRICE', axis = 1)
             Y = bos['PRICE']
In [ ]:
         1
In [8]:
            from sklearn.model selection import train test split
         1
         2
            X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size = 0.3, re
          3
            print(X train.shape)
            print(X_test.shape)
         5
            print(Y_train.shape)
            print(Y_test.shape)
        (354, 13)
        (152, 13)
        (354,)
        (152,)
In [9]:
         1
             # Standardizing the data
         2
          3
            from sklearn.preprocessing import StandardScaler
            scaler = StandardScaler()
         5
          6
            X train = scaler.fit transform(X train)
             X_test = scaler.transform(X_test)
```

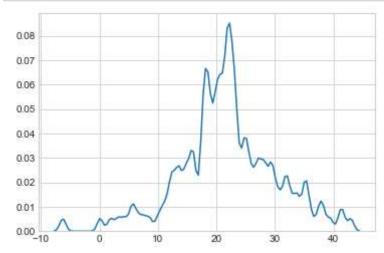
```
In [ ]: 1
```

```
In [10]:
              # code source:https://medium.com/@haydar_ai/learning-data-science-day-9-lined
              from sklearn.linear model import LinearRegression
           2
           3
           4
              lm = LinearRegression()
           5
              lm.fit(X_train, Y_train)
           7
              Y_pred = lm.predict(X_test)
           8
              plt.scatter(Y_test, Y_pred)
           9
          10
              plt.xlabel("Prices: $Y_i$")
              plt.ylabel("Predicted prices: $\hat{Y}_i$")
          11
              plt.title("Prices vs Predicted prices: $Y_i$ vs $\hat{Y}_i$")
          12
              plt.show()
          13
```



ROOT Mean Squared Error of linear regression 5.541049738742553





Defining the SGD Linear Algorithm

```
In [15]: 1 X.shape
Out[15]: (506, 13)
In [40]: 1 X_train.shape
Out[40]: (354, 13)
```

```
In [57]:
              def dL dW(X,e,N):
           1
           2
                  x11= (-2/N)*(X.T @ (e))
           3
                  # for derivative functn w.r.t to 'w' we are taking the dot product (using
           4
                  return x11
           5
              def dL db(e,N):
           6
                  return (-2/N)*np.sum(e)
           7
                  # for derivative functn w.r.t to 'b' we are takinh summation of error e
           8
              def gradient_descent(learning_rate ,ierations):
           9
                  We are defining the SGD fucto here for each of the training data in X.
          10
                  the error is calculated and funtn is is updated in order to reduce the er
          11
                  This process is repeated for a fixed number of iterations, the learning r
          12
          13
                  N = len(X train)
          14
                  w1 = np.random.rand(1,(X_train.shape[1]))
          15
          16
                  b1 = np.random.rand()
          17
                  optimal w = []
          18
                  optimal_b = []
          19
                  for j in range (ierations):
          20
                      # getting the error e , which returns me a vector of (354,1)
                      e = (Y_train[:,np.newaxis] - (X_train @ w1.T) - b1)
          21
                      # getting the w1 , which returns me a vector of (1,13)
          22
                      w1 = (w1) - (learning rate*(dL dW(X train,e,N))).T
          23
                      b1 = (b1) - (learning rate*dL db(e,N))
          24
          25
                  return w1,b1
              w,b = gradient_descent(learning_rate = 0.1,ierations =10000)
In [81]:
           1
           2
              w,b
Out[81]: (array([[-1.26415881, 0.94329906, -0.16687636,
                                                           0.18653568, -1.49252028,
                   2.79557313, -0.29648219, -2.72594888, 2.76899352, -2.1378414,
                  -2.09193889, 1.16450017, -3.29650834]]), 22.556214689265538)
In [70]:
              o= w.T
           2
              o.shape
Out[70]: (13, 1)
```

```
In [37]:
          1
              from sklearn.metrics import mean squared error
           2
           3
             Y_pred_sgd = (X_test @ (o))+(b)
             mse = (mean_squared_error(Y_test, Y_pred_sgd))
           4
             print('ROOT Mean Squared Error',np.sqrt(mse))
           5
             plt.scatter(Y_test, Y_pred_sgd)
              plt.xlabel("Prices: $Y i$")
           7
             plt.ylabel("Predicted prices: $\hat{Y}_i$")
              plt.title("Prices vs Predicted prices: $Y_i$ vs $\hat{Y}_i$")
             plt.show()
          10
```

ROOT Mean Squared Error 5.541049688511123



```
In [84]:
              from prettytable import PrettyTable
           1
           2
              x = PrettyTable()
           3
           4
           5
              x.field_names = ["Method", "Metric to compare"]
           6
              x.add_row(["Linaer Regrssion Function", 'ROOT Mean Squared Error is 5.5410497
           7
              x.add_row(["SGD Function", 'ROOT Mean Squared Error is 5.541049688511123'])
           8
           9
              print(x)
          10
```

```
| Method | Metric to compare | Herric to compa
```

```
In [ ]: 1
```