

## \* Probability \*

- It is the measure of the likelihood of an event.

E.g. Tossing a coin.  
 $S = \{H, T\}$

Probability =  $\frac{\text{No. of ways an event can occur}}{\text{No. of possible outcomes}}$

$$Pr(H) = 1/2$$

E.g. Rolling a Dice  
 $S = \{1, 2, 3, 4, 5, 6\}$

$$Pr(1) = 1/6$$

$$Pr(2) = 1/6$$

⋮

$$Pr(6) = 1/6$$

Venn diagram

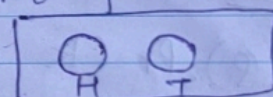
### \* Mutual Exclusive Event :-

E.g. Tossing a coin

possible  $\Rightarrow$   $\boxed{H \text{ or } T}$  ✓

$\boxed{H \& T}$  ✗

↓  
Is mutual exclusive



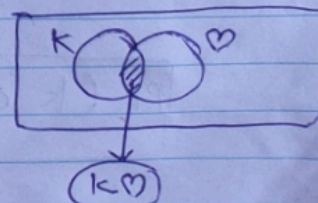
### \* Not Mutual Exclusive Event :-

E.g. Taking out a card from deck of cards

possible:  $\boxed{\text{King} \& \heartsuit}$  ✓

↓  
Is non mutual exclusive

Venn Diagram





E.g.: Tossing a coin

$$Q). \Pr(H \text{ or } T) ? = \Pr(H) + \Pr(T)$$

$$\Downarrow$$

Mutual exclusive

$$= \frac{1}{2} + \frac{1}{2}$$
$$= \underline{\underline{\frac{1}{1}}}$$

E.g.: Rolling a dice

$$Q). \Pr(1 \text{ or } 2 \text{ or } 3) = \Pr(1) + \Pr(2) + \Pr(3)$$

$$\Downarrow$$

Mutual exclusive

$$= \frac{1}{6} + \frac{1}{6} + \frac{1}{6}$$
$$= \underline{\underline{0.5}}$$

This technique is called for Additive Rule (ME)  
Let's, ~~find~~ check formula for non mutual exclusive

e.g.: Taking out a card from the deck

$$Q). \Pr(K \text{ or } \heartsuit) = \cancel{\Pr(K)} \text{ (and)} \cancel{\Pr(\heartsuit)}$$

$$\Rightarrow \neq \cancel{\frac{4}{52}} \text{ (and)} \cancel{\frac{13}{52}}$$

$$\Pr(K) = \frac{4}{52}$$

$$\Pr(\heartsuit) = \frac{13}{52}$$

$$\Pr(K \text{ and } \heartsuit) = \frac{1}{52}$$

$$\Pr(K \text{ or } \heartsuit) = \Pr(K) + \Pr(\heartsuit) - \Pr(K \cap \heartsuit)$$
$$= \frac{4}{52} + \frac{13}{52} - \frac{1}{52}$$

$$\boxed{\Pr(K \text{ or } \heartsuit) = \underline{\underline{\frac{16}{52}}}}$$



Formula's we have seen for mutual & non mutual exclusive event - Additive rule.

\* Additive Rule :-

ME	$Pr(A \text{ or } B) = Pr(A) + Pr(B)$
NME	$Pr(A \text{ or } B) = Pr(A) + Pr(B) - Pr(A \cap B)$

\* Multiplicative Rule :-

Independent Event	Dependent Event
e.g: Tossing a coin H T H $\{1, 2, 3\}$	e.g: Taking a card from a deck
1 <sup>st</sup> Experiment $\Rightarrow Pr(H) = \frac{1}{2}$	1 <sup>st</sup> Experiment $\Rightarrow Pr(K) = \frac{1}{52}$
2 <sup>nd</sup> Experiment $\Rightarrow Pr(T) = \frac{1}{2}$	2 <sup>nd</sup> Experiment $\Rightarrow Pr(Q) = \frac{1}{51}$
3 <sup>rd</sup> Experiment $\Rightarrow Pr(H) = \frac{1}{2}$	3 <sup>rd</sup> Experiment $\Rightarrow Pr(J) = \frac{1}{50}$
- No. of total outcome will not reduce	- No. of total outcome will reduce



① Independent Event

e.g.: Rolling a dice

Q) Pr(1 and 3) ?

$$\boxed{\text{Pr}(A \text{ and } B) = \text{Pr}(A) * \text{Pr}(B)} \leftarrow \text{formula}$$

$$\text{Pr}(1 \text{ and } 3) = \text{Pr}(1) * \text{Pr}(3)$$

$$= \frac{1}{6} * \frac{1}{6}$$

$$= \frac{1}{36} //$$

② Dependent Event

e.g.: Removing / Taking out a card from deck.

Q) Pr(K and Q) ?

$$\boxed{\text{Pr}(A \text{ and } B) = \text{Pr}(A) * \text{Pr}(B/A)} \leftarrow \text{formula}$$

$$\text{Pr}(K \text{ and } Q) = \text{Pr}(K) * \text{Pr}(Q/K)$$

$$= \frac{1}{52} * \frac{1}{51}$$

$$= \frac{1}{2652}$$

\* Multiplicative Rule Formula :-

Independent  $\text{Pr}(A \text{ and } B) = \text{Pr}(A) * \text{Pr}(B)$

Dependent  $\text{Pr}(A \text{ and } B) = \text{Pr}(A) * \text{Pr}(B/A) \rightarrow \text{conditional event}$