Estimation theory & hypothesis testing

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[5]: #Q1)
      import scipy.stats as stats
      mean_pop=60
      std_dev=66
      n = 40
      sample_mean=58
      error = std_dev/(n**0.5)
      z=(sample_mean-mean_pop)/error
      probability = stats_norm_cdf(z)
      print(f"Required Probability: {probability}")
     Required Probability: 0.4240069369665028
 [8]: #Q2)
      import scipy.stats as stats
      avg=310
      n = 40
      std_dev=89
      z_{critical} = 1.96
      error=std_dev/(n**0.5)
      error_margin = z_critical * error
      lower_bound=avg-error_margin
      upper_bound=avg+error_margin
      print(f"Lower bound: {lower_bound}")
      print(f"Upper bound: {upper_bound}")
     Lower bound: 282.4186142480114
     Upper bound: 337.5813857519886
[10]: #O3)
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# Null Hypothesis: The mean waiting time has not changed from 4.5 minutes (H0:
       \hookrightarrow mu = 4.5 \text{ minutes}).
      # Alternate Hypothesis: The mean waiting time has changes from 4.5 minutes (h1:
       \hookrightarrow mu != 4.5 minutes).
      # In this case it will be a two-tailed test.
[11]: #Q4)
      import scipy.stats as stats
      z_stat = 2.00
      p_value = 2 * (1-stats_norm_cdf(z_stat)) #Multiplying by two because it is a_
        ⇔two tailed test
      print(f"p-value: {p_value}")
     p-value: 0.04550026389635842
[12]: #Q5)
      import scipy.stats as stats
      sample_mean = 30000
      hypothesized_mean = 29000
      std_dev = 8000
      n = 400
      error = std_dev / (n ** 0.5)
      z_stat = (sample_mean - hypothesized_mean) / error
      p_value = 1 - stats_norm_cdf(z_stat)
```

[12]: (2.5, 0.006209665325776159)

z_stat, p_value