

Quantitative Management Modelling
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Assignment 4 – LP Model (R Program)

Question 2:

Let X = Large, Y = Medium and Z= small

2A. Decision Variables:

Let X_1, Y_1, Z_1 be the quantities produced in L, M & S for plant 1

Let X_2, Y_2, Z_2 be the quantities produced in L, M & S for plant 2 Let

X_3, Y_3, Z_3 be the quantities produced in L, M & S for plant 3

2B. Formulating LP model:

Let the objective function be Z which represents the maximum profit =

$$Z = 420 (X_1 + X_2 + X_3) + 360 (Y_1 + Y_2 + Y_3) + 300 (Z_1 + Z_2 + Z_3)$$

Capacity Constraints:

$X_1 + Y_1 + Z_1 \leq 750$ (Excess production of 750 units of plant 1 every day)

$X_2 + Y_2 + Z_2 \leq 900$ (excess production of 900 units of plant 2 every day)

$X_3 + Y_3 + Z_3 \leq 450$ (excess production of 450 units of plant 3 every day) Storage

constraint:

$20X_1 + 15Y_1 + 12Z_1 \leq 13000$ (storage capacity of plant 1 13000 sq.ft)

$20X_2 + 15Y_2 + 12Z_2 \leq 12000$ (storage capacity of plant 2 12000 sq.ft)

$20X_3 + 15Y_3 + 12Z_3 \leq 5000$ (storage capacity of plant 3 5000 units sq.ft) Sales

constraints:

$L = X_1 + X_2 + X_3 \leq 900$ (900 Units needs to be sold plant 1 every day)

$M = Y_1 + Y_2 + Y_3 \leq 1200$ (1200 Units needs to be sold plant 2 every day)

$S = Z_1 + Z_2 + Z_3 \leq 750$ (750 Units needs to be sold plant 3 every day)

$X_x, Y_x, Z_x \geq 0$

Percentage Constraints:

As said that plant always consumes same % of their excess capacity to produce the new product, below are the equations:

$$(X1+Y1+Z1)/750=(X2+Y2+Z2)/900=(X3+Y3+Z3)/S450$$

It can be written as:

$$900(X1+Y1+Z1) = 750 (X2+Y2+Z2)$$

$$450 (X2+Y2+Z2) = 900 (X3+Y3+Z3)$$

$$450 (X1+Y1+Z1) = 750(X3+Y3+Z3) \text{ Non-}$$

Negative zero:

$$X1,Y1,Z1, X2,Y2,Z2,X3,Y3, Z3 \geq 0$$

QMM_Assignment 4

"Pallavi"

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#calling the "lpSolve" library and declaring the objective function as "f.obj" #library
#objective function

```
library(lpSolve)
f.obj<-c(420,420,420,360,360,360,300,300,300)
f.con<-matrix(c(1,0,0,1,0,0,1,0,0,
               0,1,0,0,1,0,0,1,0,
               0,0,1,0,0,1,0,0,1,
               20,0,0,15,0,0,12,0,0,
               0,20,0,0,15,0,0,12,0,
               0,0,20,0,0,15,0,0,12,
               1,1,1,0,0,0,0,0,0,
               0,0,0,1,1,1,0,0,0,
               0,0,0,0,0,0,1,1,1,
               900,-750,0,900,-750,0,900,-750,0,
               0,450,-900,0,450,-900,0,450,-900,
               450,0,-750,450,0,-750,450,0,-750),ncol=9, byrow=TRUE)

f.con
```

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9]
## [1,]    1    0    0    1    0    0    1    0    0
## [2,]    0    1    0    0    1    0    0    1    0
## [3,]    0    0    1    0    0    1    0    0    1
## [4,]   20    0    0   15    0    0   12    0    0
## [5,]    0   20    0    0   15    0    0   12    0
## [6,]    0    0   20    0    0   15    0    0   12
## [7,]    1    1    1    0    0    0    0    0    0
## [8,]    0    0    0    1    1    1    0    0    0
## [9,]    0    0    0    0    0    0    1    1    1
## [10,]  900 -750    0  900 -750    0  900 -750    0
## [11,]    0  450 -900    0  450 -900    0  450 -900
## [12,]  450    0 -750  450    0 -750  450    0 -750
```

#Declaring the direction as "f.dir"

```
f.dir<-c("<=", "<=", "<=", "<=", "<=", "<=", "<=", "<=", "<=", "=", "=", "=")
```

#Declaring the right hand side constants as "f.rhs"

```
f.rhs<-c(750,900,450,13000,12000,5000,900,1200,750,0,0,0)
```

#Calling the LP function to solve the problem based on objective function to maximize the profit using "int. vec" to get exact values

```
f.sol<- lp("max",f.obj,f.con,f.dir,f.rhs,int.vec = 1:9)
```

```
f.sol$solution
```

```
## [1] 530    0    1 160 688    8    0 140 405  
f.sol  
## Success: the objective function is 694680
```