Assignment_3

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Summary

Ans 1:-According to the data in this dataset, there is a 50.88% chance that an injury occurred if an accident has just been reported and no other information is available. This is because data indicates that earlier out of 42,183 cases, 21,462 cases had reported "injury=yes." 20721

Ans 2.1: The following are the precise Bayes conditional probability of an injury (INJURY = Yes) for each of the six possible predictor combinations:

2.2: Using probabilities and a cutoff of 0.5, the 24 accidents were quantitatively classified as follows:

 $\begin{bmatrix} 0.6666667 \ 0.1818182 \ 0.00000000 \ 0.00000000 \ 0.66666667 \ 0.1818182 \ 0.1818182 \ 0.6666667 \\ 0.1818182 \ 0.1818182 \ 0.1818182 \ 0.1818182 \ 0.1818182 \ 0.1818182 \ 0.1818182 \end{bmatrix}$

qualitatively are:

```
["yes" "no" "no" "no" "yes" "no" "no" "no" "no" "no" "yes" "yes" "yes" "yes" "yes" "yes" "no" "no" "no" "no" "yes" "yes" "yes" "yes" "no"]
```

- 2.3: The result of manually computing the naive Bayes conditional probability of an injury given WEATHER_R = 1 and TRAF_CON_R = 1 was "0".
- 2.4: Now that the naive Bayes classifier has been applied to the 24 records and two predictors, along with a check of the model's output to determine the probabilities and classifications for each of the 24 records, it has been discovered that the resultant classifications and ranks are not the same as those produced by the exact Bayes computation.
- Ans 3.1: Using the naive Bayes classifier on the complete training set with the relevant predictors (and INJURY as the response) The Following Confusion Matrix and Statistics are obtained. The accuracy comes out to be 53.3%.

Confusion Matrix and Statistics

Reference

Accuracy : 0.5331

3.2: the overall error of the validation set is "0.4669".

Problem Statement

The file accidentsFull.csv contains information on 42,183 actual automobile accidents in 2001 in the United States that involved one of three levels of injury: NO INJURY, INJURY, or FATALITY. For each accident, additional information is recorded, such as day of week, weather conditions, and road type. A firm might be interested in developing a system for quickly classifying the severity of an accident based on initial reports and associated data in the system (some of which rely on GPS-assisted reporting).

Our goal here is to predict whether an accident just reported will involve an injury (MAX_SEV_IR = 1 or 2) or will not (MAX_SEV_IR = 0). For this purpose, create a dummy variable called INJURY that takes the value "yes" if MAX_SEV_IR = 1 or 2, and otherwise "no."

- 1. Using the information in this dataset, if an accident has just been reported and no further information is available, what should the prediction be? (INJURY = Yes or No?) Why?
- 2. Select the first 24 records in the dataset and look only at the response (INJURY) and the two predictors WEATHER_R and TRAF_CON_R. Create a pivot table that examines INJURY as a function of the two predictors for these 12 records. Use all three variables in the pivot table as rows/columns. 2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors. 2.2:-Classify the 24 accidents using these probabilities and a cutoff of 0.5. 2.3:-Compute manually the naive Bayes conditional probability of an injury given WEATHER_R = 1 and TRAF_CON_R = 1. 2.4:-Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?
- 3. Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%). 3.1:- Run a naive Bayes classifier on the complete training set with the relevant predictors (and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix. 3.2:- What is the overall error of the validation set?

Data Input and Cleaning

Loading the required libraries and reading the input file

library(e1071)
library(caret)

```
## Loading required package: ggplot2
## Loading required package: lattice
library(ggplot2)
```

Q1. Using the information in this dataset, if an accident has just been reported and no further information is available, what should the prediction be? (INJURY = Yes or No?) Why?

```
accidents <-
read.csv("C:\\Users\\palla\\OneDrive\\Desktop\\Assignments\\FML\\Assignment
3\\accidentsFull (1).csv")
accidents$INJURY = ifelse(accidents$MAX SEV IR>0,"yes","no")
injury_table <- table(accidents$INJURY)</pre>
injury_table
##
##
      no
            yes
## 20721 21462
head(accidents)
##
     HOUR_I_R ALCHL_I ALIGN_I STRATUM_R WRK_ZONE WKDY_I_R INT_HWY LGTCON_I_R
## 1
                      2
                               2
                                          1
                                                    0
                                                              1
                                                                                   3
## 2
             1
                      2
                               1
                                          0
                                                    0
                                                              1
                                                                       1
                      2
                                                                                   3
## 3
             1
                               1
                                          0
                                                    0
                                                              1
                                                                       0
                                                                                   3
## 4
             1
                      2
                               1
                                          1
                                                    0
                                                              0
                                                                       0
## 5
             1
                      1
                               1
                                          0
                                                    0
                                                              1
                                                                                   3
                                                                       0
                      2
                                          1
                                                              1
                                                                                   3
## 6
             1
                               1
                                                    0
                                                                       0
     MANCOL_I_R PED_ACC_R RELJCT_I_R REL_RWY_R PROFIL_I_R SPD_LIM SUR_COND
##
## 1
               0
                          0
                                       1
                                                  0
                                                              1
                                                                      40
                                                                                 4
## 2
               2
                          0
                                       1
                                                  1
                                                              1
                                                                      70
                                                                                 4
               2
                                                                                 4
                          0
                                       1
                                                  1
                                                              1
                                                                      35
## 3
## 4
               2
                          0
                                       1
                                                  1
                                                              1
                                                                      35
                                                                                 4
               2
                          0
                                       0
                                                              1
                                                                      25
                                                                                 4
## 5
                                                  1
## 6
                          0
                                       1
                                                  0
                                                              1
                                                                      70
                                                                                 4
     TRAF_CON_R TRAF_WAY VEH_INVL WEATHER_R INJURY_CRASH NO_INJ_I
##
PRPTYDMG CRASH
                         3
## 1
                                   1
                                              1
                                                             1
                                                                       1
0
## 2
               0
                         3
                                   2
                                              2
                                                             0
                                                                       0
1
## 3
               1
                         2
                                   2
                                              2
                                                             0
                                                                       0
1
                         2
## 4
               1
                                   2
                                              1
                                                             0
                                                                       0
1
## 5
               0
                         2
                                   3
                                              1
                                                             0
                                                                       0
1
## 6
               0
                         2
                                   1
                                              2
                                                             1
                                                                       1
0
```

```
FATALITIES MAX SEV IR INJURY
## 1
                0
                             1
                                   yes
## 2
                0
                             0
                                     no
## 3
                0
                             0
                                     no
## 4
                0
                             0
                                     no
## 5
                0
                             0
                                     no
                0
## 6
                             1
                                   yes
probability_injury <- (injury_table["yes"] / sum(injury_table))*100</pre>
probability_injury
##
         yes
## 50.87832
#Converting variables to factor
for (i in c(1:dim(accidents)[2])){
  accidents[,i] <- as.factor(accidents[,i])</pre>
}
head(accidents, n=24)
##
       HOUR_I_R ALCHL_I ALIGN_I STRATUM_R WRK_ZONE WKDY_I_R INT_HWY LGTCON_I_R
## 1
               0
                         2
                                  2
                                              1
                                                         0
                                                                    1
                                                                                           3
## 2
               1
                         2
                                  1
                                              0
                                                         0
                                                                                           3
                                                                    1
                                                                             1
## 3
               1
                         2
                                  1
                                              0
                                                         0
                                                                    1
                                                                             0
                                                                                           3
                         2
                                                                                           3
## 4
               1
                                  1
                                              1
                                                         0
                                                                    0
                                                                             0
               1
                                              0
                                                                    1
                                                                             0
                                                                                           3
## 5
                         1
                                  1
                                                         0
## 6
               1
                         2
                                  1
                                              1
                                                         0
                                                                    1
                                                                             0
                                                                                          3
                         2
                                                                                          3
## 7
               1
                                  1
                                              0
                                                         0
                                                                    1
                                                                             1
## 8
               1
                         2
                                  1
                                              1
                                                         0
                                                                    1
                                                                             0
                                                                                           3
                         2
                                                                                          3
## 9
               1
                                  1
                                              1
                                                         0
                                                                    1
                                                                             0
                         2
                                                                                          3
## 10
               0
                                  1
                                              0
                                                         0
                                                                    0
                                                                             0
               1
                         2
                                              0
                                                                    1
                                                                             0
                                                                                           3
## 11
                                  1
                                                         0
                         2
## 12
               1
                                  1
                                              1
                                                         0
                                                                    1
                                                                             0
                                                                                           3
                         2
                                  1
                                                                    1
                                                                                          3
## 13
               1
                                              1
                                                         0
                                                                             0
## 14
               1
                         2
                                  2
                                              0
                                                         0
                                                                    1
                                                                             0
                                                                                          3
## 15
               1
                         2
                                  2
                                              1
                                                         0
                                                                    1
                                                                             0
                                                                                          3
                         2
                                  2
                                                                                          3
## 16
               1
                                              1
                                                         0
                                                                    1
                                                                             0
## 17
               1
                         2
                                  1
                                              1
                                                         0
                                                                    1
                                                                             0
                                                                                          3
                         2
                                                                                           3
               1
                                  1
                                                         0
                                                                    0
                                                                             0
## 18
                                              1
               1
                         2
                                  1
                                                                    1
                                                                             0
                                                                                          3
## 19
                                              1
                                                         0
                         2
## 20
               1
                                  1
                                              0
                                                         0
                                                                    1
                                                                             0
                                                                                           3
                         2
## 21
               1
                                  1
                                              1
                                                         0
                                                                    1
                                                                             0
                                                                                           3
               1
                         2
                                  2
                                              0
                                                         0
                                                                    1
                                                                             0
                                                                                          3
## 22
## 23
               1
                         2
                                  1
                                              0
                                                         0
                                                                    1
                                                                             0
                                                                                          3
## 24
                         2
                                  1
                                              1
                                                                    1
                                                                             9
       MANCOL_I_R PED_ACC_R RELJCT_I_R REL_RWY_R PROFIL_I_R SPD_LIM SUR_COND
##
                 0
## 1
                             0
                                           1
                                                                    1
                                                                            40
                  2
## 2
                             0
                                                                    1
                                                                            70
                                           1
                                                       1
                                                                                        4
                  2
                             0
                                           1
                                                       1
                                                                    1
                                                                            35
                                                                                        4
## 3
## 4
                 2
                             0
                                           1
                                                       1
                                                                    1
                                                                            35
                                                                                        4
                  2
                             0
                                           0
                                                                    1
                                                                            25
## 5
                                                       1
                                                                                        4
```

##	_	•	_	•		-	=-	_
	6	0	0	1	0	1	70	4
##	7	0	0	0	0	1	70	4
##	8	0	0	0	0	1	35	4
##		0	0	1	0	1	30	4
##						1		
		0	0	1	0		25	4
##		0	0	0	0	1	55	4
##	12	2	0	0	1	1	40	4
##	13	1	0	0	1	1	40	4
	14	0	0	Ø	0	1	25	4
##		0	0	0	0	1	35	4
##	16	0	0	0	0	1	45	4
##	17	0	0	0	0	1	20	4
	18	0	0	0	0	1	50	4
##		0	0	0	0	1	55	4
##	20	0	0	1	1	1	55	4
##	21	0	0	1	0	0	45	4
##		0	0	1	0	0	65	4
##		0	0	0	0	0	65	4
##	24	2	0	1	1	0	55	4
##	TRAF CON	R TRAF W	AY VEH IN	/L WEATHER	_R INJURY_CRA	SH NO INJ	I	
	PTYDMG_CRASH		_	-	_	_	_	
		0	2	1	1	1	1	
##	1	0	3	1	1	1	1	
0								
##	2	0	3	2	2	0	0	
1								
	2	1	2	2	2	0	0	
##	3	1	2	2	2	0	0	
1								
##	4	1	2	2	1	0	0	
1								
##	Е		_	2				
	7	Ω			1	0	Ω	
1	3	0	2	3	1	0	0	
		0	2	3	1	0	0	
##		0	2	1	2	0	0 1	
0	6	0	2	1	2	1	1	
0 ##	6							
0 ## 1	6 7	0	2	1	2	1	1	
0 ##	6 7	0	2	1	2	1	1	
0 ## 1 ##	6 7	0	2	1	2	1	1	
0 ## 1 ## 0	6 7 8	0 0 0	2 2 1	1 1 1	2 2 1	1 0 1	1 0 1	
0 ## 1 ## 0 ##	6 7 8 9	0	2	1	2	1	1	
0 ## 1 ## 0 ##	6 7 8 9	0000	2 2 1	1 1 1	212	1 0 1 0	1 0 1 0	
0 ## 1 ## 0 ##	6 7 8 9	0 0 0	2 2 1	1 1 1	2 2 1	1 0 1	1 0 1	
0 ## 1 ## 0 ## 1	6 7 8 9	0000	2 2 1	1 1 1	212	1 0 1 0	1 0 1 0	
0 ## 1 ## 0 ## 1 ##	6 7 8 9 10	000000	2 2 1 1	1 1 1 1	2 2 1 2 2	1 0 1 0	1 0 1 0	
0 ## 1 ## 0 ## 1 ##	6 7 8 9	0000	2 2 1	1 1 1	212	1 0 1 0	1 0 1 0	
0 ## 1 ## 0 ## 1 ## 1	6 7 8 9 10 11	0000000	2 2 1 1 1	1 1 1 1 1	212222	1 0 1 0 0	1 0 1 0 0	
0 ## 1 ## 0 ## 1 ## 1	6 7 8 9 10	000000	2 2 1 1	1 1 1 1	2 2 1 2 2	1 0 1 0	1 0 1 0	
0 ## 1 ## 0 ## 1 ## 1 ##	6 7 8 9 10 11	0000000	2 2 1 1 1	1 1 1 1 1	212222	1 0 1 0 0	1 0 1 0 0	
0 ## 1 ## 0 ## 1 ## 1 ## 1	6 7 8 9 10 11 12	0000002	2 2 1 1 1 1	1 1 1 1 1 1 2	 2 1 2 2 1 	1 0 1 0 0 0	1 0 1 0 0	
0 ## 1 ## 0 ## 1 ## 1 ## 1 ##	6 7 8 9 10 11	0000000	2 2 1 1 1	1 1 1 1 1	212222	1 0 1 0 0	1 0 1 0 0	
0 ## 1 ## 1 ## 1 ## 1 ## 1 ##	6 7 8 9 10 11 12 13	00000020	2 2 1 1 1 1 1	1 1 1 1 1 2	2 2 1 2 2 2 1	1 0 1 0 0 0	1 0 1 0 0 0 0	
0 ## 1 ## 1 ## 1 ## 1 ## 1 ##	6 7 8 9 10 11 12	0000002	2 2 1 1 1 1	1 1 1 1 1 1 2	 2 1 2 2 1 	1 0 1 0 0 0	1 0 1 0 0	
0 ## 1 ## 1 ## 1 ## 1 ## 1 ##	6 7 8 9 10 11 12 13	00000020	2 2 1 1 1 1 1	1 1 1 1 1 2	2 2 1 2 2 2 1	1 0 1 0 0 0	1 0 1 0 0 0 0	
0 ## 1 ## 0 ## 1 ## 1 ## 1 ## 1 ##	6 7 8 9 10 11 12 13	00000020	2 2 1 1 1 1 1	1 1 1 1 1 2	2 2 1 2 2 2 1	1 0 1 0 0 0	1 0 1 0 0 0 0	

0								
##	16	0	1	1	1	1	1	
0	10	Ü	-	_	-	-	_	
##	17	0	1	1	2	0	0	
1			_	_	_		•	
##	18	0	1	1	2	0	0	
1								
##	19	0	1	1	2	0	0	
1								
##	20	0	1	1	2	0	0	
1								
##	21	0	3	1	1	1	1	
0			_	_	_			
##	22	0	3	1	1	0	0	
1	22	2	2	1	2	1	2	
## 0	23	2	2	1	2	1	2	
##	2/	0	2	2	2	1	1	
0	24	0	2	۷	2	Δ.	1	
##		FATAL TTTES	MAX_SEV_IR	TNJURY				
##	1	0	1	yes				
##		0	0	no				
##		0	0	no				
##		0	0	no				
##	5	0	0	no				
##		0	1	yes				
##		0	0	no				
##		0	1	yes				
##		0	0	no				
##		0	0	no				
##		0	0	no				
	12	0	0	no				
##		0	1	yes				
	14 15	0 0	0 1	no				
##		0	1	yes				
##		0	0	yes no				
##		0	0	no				
##		0	0	no				
	20	0	0	no				
##		0	1	yes				
##		0	0	no				
##	23	0	1	yes				
	24	0	1	yes				

Q2. Select the first 24 records in the dataset and look only at the response (INJURY) and the two predictors WEATHER_R and TRAF_CON_R. Create a pivot table that examines INJURY as a function of the two predictors for these 12 records. Use all three variables in the pivot table as rows/columns. 2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors. 2.2:-Classify the 24

accidents using these probabilities and a cutoff of 0.5. 2.3:=Compute manually the naive Bayes conditional probability of an injury given WEATHER_R = 1 and TRAF_CON_R = 1. 2.4:-Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

```
accidents24 <- accidents[1:24,c("INJURY","WEATHER_R","TRAF_CON_R")]</pre>
head(accidents24)
##
     INJURY WEATHER R TRAF CON R
## 1
        yes
                     1
## 2
                     2
                                0
         no
## 3
         no
                     2
                                1
                     1
                                1
## 4
         no
## 5
                     1
                                0
         no
## 6
                     2
                                0
        yes
Pt1 <- ftable(accidents24)
Pt2 <- ftable(accidents24[,-1]) # print table only for conditions
Pt1
##
                     TRAF_CON_R 0 1 2
## INJURY WEATHER R
## no
          1
                                3 1 1
          2
                                9 1 0
##
## yes
          1
                                6 0 0
          2
                                2 0 1
##
Pt2
             TRAF_CON_R
## WEATHER R
## 1
                             1 1
                          9
## 2
                         11 1 1
```

2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors.

```
#Injury = yes

p1 = Pt1[3,1] / Pt2[1,1] # Injury, Weather=1 and Traf=0

p2 = Pt1[4,1] / Pt2[2,1] # Injury, Weather=2, Traf=0

p3 = Pt1[3,2] / Pt2[1,2] # Injury, W=1, T=1

p4 = Pt1[4,2] / Pt2[2,2] # I, W=2,T=1

p5 = Pt1[3,3] / Pt2[1,3] # I, W=1,T=2

p6 = Pt1[4,3] / Pt2[2,3] #I,W=2,T=2

# Injury = no

n1 = Pt1[1,1] / Pt2[1,1] # Weather=1 and Traf=0

n2 = Pt1[2,1] / Pt2[2,1] # Weather=2, Traf=0

n3 = Pt1[1,2] / Pt2[1,2] # W=1, T=1
```

```
n4 = Pt1[2,2] / Pt2[2,2] # W=2,T=1
n5 = Pt1[1,3] / Pt2[1,3] # W=1,T=2
n6 = Pt1[2,3] / Pt2[2,3] # W=2,T=2
print(c(p1,p2,p3,p4,p5,p6))

## [1] 0.6666667 0.1818182 0.0000000 0.0000000 1.0000000
print(c(n1,n2,n3,n4,n5,n6))

## [1] 0.3333333 0.8181818 1.0000000 1.0000000 0.0000000
```

2.2:-Classify the 24 accidents using these probabilities and a cutoff of 0.5.

```
prob.inj \leftarrow rep(0,24)
for (i in 1:24) {
  print(c(accidents24$WEATHER_R[i],accidents24$TRAF_CON_R[i]))
    if (accidents24$WEATHER_R[i] == "1") {
      if (accidents24$TRAF_CON_R[i]=="0"){
        prob.inj[i] = p1
      else if (accidents24$TRAF CON R[i]=="1") {
        prob.inj[i] = p3
      }
      else if (accidents24$TRAF_CON_R[i]=="2") {
        prob.inj[i] = p5
      }
    }
    else {
      if (accidents24$TRAF_CON_R[i]=="0"){
        prob.inj[i] = p2
      else if (accidents24$TRAF_CON_R[i]=="1") {
        prob.inj[i] = p4
      else if (accidents24$TRAF_CON_R[i]=="2") {
        prob.inj[i] = p6
      }
    }
  }
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 1
## Levels: 1 2 0
## [1] 1 1
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
```

```
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 2
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 2
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
accidents24$prob.inj <- prob.inj</pre>
accidents24$prob.inj
## [1] 0.6666667 0.1818182 0.0000000 0.0000000 0.6666667 0.1818182 0.1818182
## [8] 0.6666667 0.1818182 0.1818182 0.1818182 0.0000000 0.6666667 0.6666667
## [15] 0.6666667 0.6666667 0.1818182 0.1818182 0.1818182 0.1818182 0.6666667
## [22] 0.6666667 1.0000000 0.1818182
accidents24$pred.prob <- ifelse(accidents24$prob.inj>0.5, "yes", "no")
accidents24$pred.prob
```

```
## [1] "yes" "no" "no" "no" "yes" "no" "no" "yes" "no" "no" "no" "no" "## [13] "yes" "yes" "yes" "yes" "no" "no" "no" "yes" "y
```

2.3Compute manually the naive Bayes conditional probability of an injury given WEATHER_R = 1 and TRAF_CON_R = 1. Answer:Probability(Injury=Yes/WEATHER_R=1,TRAF_CON_R=1)

```
= [Probability(W=1/Injury=Yes) * Probability(TRAF_CON_R=1/Injury=Yes) * Probability(Injury=Yes) ] / [Probability(W=1/Injury=Yes) * Probability(TRAF_CON_R=1/Injury=Yes) * Probability(Injury=Yes) + Probability(WEATHER_R=1/Injury=No) * Probability(TRAF_CON_R=1/Injury=No) * Probability(Injury=No) ]
```

- = [6/9*0/9*9/24]/[6/9*0/9*9/24+5/15*2/15*15/24] = The result will be "0" since the numerator is equal to zero.
- 2.4:- Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

Let us use Caret

```
library(klaR)

## Loading required package: MASS

#Loading the klaR package for Naive Bayes

# Creating a variable named formula that includes all variables of interest
formula <- INJURY ~ TRAF_CON_R + WEATHER_R

# Training the Naive Bayes model with Laplace</pre>
```

```
accidents24$INJURY <- as.factor(accidents24$INJURY)</pre>
nb2 <- NaiveBayes(formula,data = accidents24)</pre>
# Making predictions with the model
 predict(nb2, newdata = accidents24[, c("INJURY", "WEATHER_R",
"TRAF CON R")])
## $class
##
     1
         2
             3
                 4
                     5
                         6
                             7
                                 8
                                     9
                                        10
                                            11
                                                 12
                                                    13
                                                        14 15
                                                                 16
                                                                     17
                                                                         18
19
   20
## yes
        no
            no
                no yes no no yes no
                                       no no yes yes yes yes yes
                                                                         no
no
   no
##
    21
       22
            23
                24
## yes yes
            no
                no
## Levels: no yes
##
## $posterior
##
                        yes
             no
## 1
      0.4285714 0.571428571
## 2 0.7500000 0.250000000
## 3 0.9977551 0.002244949
## 4 0.9910803 0.008919722
## 5 0.4285714 0.571428571
## 6 0.7500000 0.250000000
## 7 0.7500000 0.250000000
## 8 0.4285714 0.571428571
      0.7500000 0.250000000
## 10 0.7500000 0.250000000
## 11 0.7500000 0.250000000
## 12 0.3333333 0.666666667
## 13 0.4285714 0.571428571
## 14 0.4285714 0.571428571
## 15 0.4285714 0.571428571
## 16 0.4285714 0.571428571
## 17 0.7500000 0.250000000
## 18 0.7500000 0.250000000
## 19 0.7500000 0.250000000
## 20 0.7500000 0.250000000
## 21 0.4285714 0.571428571
## 22 0.4285714 0.571428571
## 23 0.6666667 0.333333333
## 24 0.7500000 0.250000000
predict(nb2, newdata = accidents24[, c("INJURY", "WEATHER_R", "TRAF_CON_R")],
type = "raw")
## $class
##
     1
         2
             3
                 4
                     5
                         6
                             7
                                 8
                                     9
                                        10
                                            11
                                                12
                                                    13
                                                        14
                                                            15
                                                                 16
                                                                     17
                                                                         18
19 20
## yes no
          no no yes no no yes no no no yes yes yes yes no
                                                                        no
```

```
no
no
##
  21
       22
           23
                24
## yes yes no
## Levels: no yes
##
## $posterior
##
             no
                        yes
## 1 0.4285714 0.571428571
## 2 0.7500000 0.250000000
## 3 0.9977551 0.002244949
## 4 0.9910803 0.008919722
## 5 0.4285714 0.571428571
## 6 0.7500000 0.250000000
## 7 0.7500000 0.250000000
## 8 0.4285714 0.571428571
## 9 0.7500000 0.250000000
## 10 0.7500000 0.250000000
## 11 0.7500000 0.250000000
## 12 0.3333333 0.666666667
## 13 0.4285714 0.571428571
## 14 0.4285714 0.571428571
## 15 0.4285714 0.571428571
## 16 0.4285714 0.571428571
## 17 0.7500000 0.250000000
## 18 0.7500000 0.250000000
## 19 0.7500000 0.250000000
## 20 0.7500000 0.250000000
## 21 0.4285714 0.571428571
## 22 0.4285714 0.571428571
## 23 0.6666667 0.333333333
## 24 0.7500000 0.250000000
#predictions
#raw_probabilities
# Comparing the naive Bayes model and exact Bayes classification
classification_match <- all(accidents24$nbpred.prob == accidents24$prob.inj)</pre>
probability_match <- all.equal(accidents24$nbpred.prob, accidents24$prob.inj)</pre>
# Checking if classifications and rankings are equivalent
if (classification match && is.na(probability match)) {
  cat("The resulting classifications and rankings are equivalent.\n")
} else {
  cat("The resulting classifications and rankings are not equivalent.\n")
}
## The resulting classifications and rankings are not equivalent.
```

Q3, Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%). 3.1, Run a naive Bayes classifier on the complete training set with the

relevant predictors (and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix.

```
set.seed(1)
train.index <- sample(c(1:dim(accidents)[1]), dim(accidents)[1]*0.6)</pre>
train.df <- accidents[train.index,]</pre>
valid.df <- accidents[-train.index,]</pre>
#defining a variable to be used here
vars <- c("INJURY", "HOUR_I_R", "ALIGN_I", "WRK_ZONE", "WKDY_I_R",</pre>
          "INT_HWY", "LGTCON_I_R", "PROFIL_I_R", "SPD_LIM", "SUR_COND",
          "TRAF_CON_R", "TRAF_WAY", "WEATHER_R")
nbTotal <- naiveBayes(INJURY~.,data = train.df[,vars])</pre>
nbTotal
##
## Naive Bayes Classifier for Discrete Predictors
##
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
## A-priori probabilities:
## Y
##
          no
                   yes
## 0.4939745 0.5060255
##
## Conditional probabilities:
##
        HOUR I R
## Y
##
     no 0.5689490 0.4310510
##
     yes 0.5703131 0.4296869
##
##
        ALIGN I
## Y
                 1
                            2
##
     no 0.8712206 0.1287794
##
     yes 0.8652300 0.1347700
##
##
        WRK ZONE
## Y
##
     no 0.97664374 0.02335626
     yes 0.97727805 0.02272195
##
##
##
        WKDY I R
## Y
##
     no 0.2194049 0.7805951
     yes 0.2381510 0.7618490
##
##
##
        INT_HWY
## Y
                     0
##
     no 0.8513837786 0.1481362982 0.0004799232
```

```
##
     ves 0.8593737800 0.1397673147 0.0008589053
##
##
        LGTCON_I_R
## Y
                                      3
##
     no 0.6870101 0.1251000 0.1878899
##
     yes 0.7014914 0.1096275 0.1888811
##
##
        PROFIL I R
## Y
##
     no 0.7531595 0.2468405
##
     yes 0.7633326 0.2366674
##
##
        SPD LIM
## Y
                    5
                                 10
                                              15
                                                            20
                                                                         25
     no 0.0000799872 0.0004799232 0.0043992961 0.0085586306 0.1121420573
##
##
     yes 0.0001561646 0.0003123292 0.0040602795 0.0039041149 0.0906535488
##
        SPD_LIM
## Y
                                 35
                                              40
                                                            45
                   30
                                                                         50
##
     no 0.0860662294 0.1896496561 0.0962246041 0.1553351464 0.0407934730
##
     yes 0.0860466932 0.2123057703 0.1068946670 0.1574139143 0.0394315609
##
        SPD LIM
                   55
## Y
                                 60
                                              65
                                                            70
                                                                         75
     no 0.1590145577 0.0355143177 0.0645496721 0.0409534474 0.0062390018
##
##
     yes 0.1549152807 0.0430233466 0.0621535098 0.0311548372 0.0075739830
##
##
        SUR_COND
                                                                     9
## Y
                                2
                   1
     no 0.774196129 0.176931691 0.016717325 0.028155495 0.003999360
##
     yes 0.815725775 0.151245413 0.010697275 0.016709612 0.005621926
##
##
##
        TRAF_CON_R
## Y
##
     no 0.6566149 0.1902096 0.1531755
##
     yes 0.6213009 0.2191770 0.1595221
##
##
        TRAF WAY
## Y
                              2
##
     no 0.57998720 0.36690130 0.05311150
     yes 0.56063090 0.39743890 0.04193019
##
##
##
        WEATHER R
## Y
##
     no 0.8390657 0.1609343
##
     yes 0.8744437 0.1255563
#generating the confusion matrix using the train.df, the prediction and the
confusionMatrix(train.df$INJURY, predict(nbTotal, train.df[, vars]), positive
= "yes")
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
               no yes
          no 5097 7405
##
          yes 4230 8577
##
##
##
                  Accuracy : 0.5403
##
                    95% CI: (0.5341, 0.5464)
       No Information Rate: 0.6315
##
       P-Value [Acc > NIR] : 1
##
##
##
                     Kappa: 0.0776
##
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.5367
##
               Specificity: 0.5465
            Pos Pred Value: 0.6697
##
##
            Neg Pred Value : 0.4077
##
                Prevalence: 0.6315
            Detection Rate: 0.3389
##
##
      Detection Prevalence: 0.5060
##
         Balanced Accuracy: 0.5416
##
##
          'Positive' Class : yes
##
```

3.2. What is the overall error of the validation set?

```
ConfM= confusionMatrix(valid.df$INJURY, predict(nbTotal, valid.df[, vars]),
positive = "yes")
print(ConfM)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                no yes
##
          no 3203 5016
##
          yes 2862 5793
##
##
                  Accuracy : 0.5331
##
                    95% CI: (0.5256, 0.5407)
##
       No Information Rate: 0.6406
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa: 0.0594
##
##
   Mcnemar's Test P-Value : <2e-16
##
```

```
##
               Sensitivity: 0.5359
               Specificity: 0.5281
##
            Pos Pred Value : 0.6693
##
##
            Neg Pred Value: 0.3897
##
                Prevalence: 0.6406
##
            Detection Rate: 0.3433
##
      Detection Prevalence: 0.5129
##
         Balanced Accuracy: 0.5320
##
##
          'Positive' Class : yes
##
#Calculated overall error
overall_error <- 1 - ConfM$overall["Accuracy"]</pre>
cat("overall error of the validation set:", overall_error, "\n")
## overall error of the validation set: 0.4668721
```

#CONCLUSION

In order to predict injury outcomes in a data set of 24 records, the Naive Bayes classifier was first applied twice, twice with two predictors each.

Our analysis of the first 24 records using the exact Bayes classifier reveals that the most risky combination for drivers is WEATHER_CON=2,TRAF_CON=0 since it has the highest maximum chance for injury, which is "1".

A reasonable level of predictive ability was demonstrated by the model's accuracy on the training set, which was 53.7%, and its validation error, which was 46.3%. However, it makes the assumption that the predictor variables are independent, which may not always be the case in real-world situations and might result in errors. But for classification and ranking, we can utilize the Naive Bayes classifier.