Note from Henrik:

Newton-Cotes methods are easy to program, so I recommend that you implement your own program from scratch.

Task for lecture 8

• Consider the following integrals.

$$\int_0^1 \cos(x^2)e^{-x}dx\tag{1}$$

$$\int_0^1 \sqrt{x} \cos(x^2) e^{-x} dx \tag{2}$$

$$\int_0^1 \frac{1}{\sqrt{x}} \cos(x^2) e^{-x} dx \tag{3}$$

$$\int_0^1 1000 \cdot e^{\left(\frac{-1}{x}\right)} \cdot e^{\left(\frac{-1}{1-x}\right)} dx \tag{4}$$

- Approximate eq. 1 using the the midpoint(Rectangle) method, the trapezoidal method and the Simpson's method.
- Approximate eq. 2 using the the Simpson's method.
- Approximate eq. 3 using the the midpoint(Rectangle) method
- Approximate eq. 4 using the the trapezoidal method.
- For each solution, apply *Richardson Extrapolation* to evaluate the order of the method and estimate the error.
- Print the data in tables similar to the one found in todays presentation.