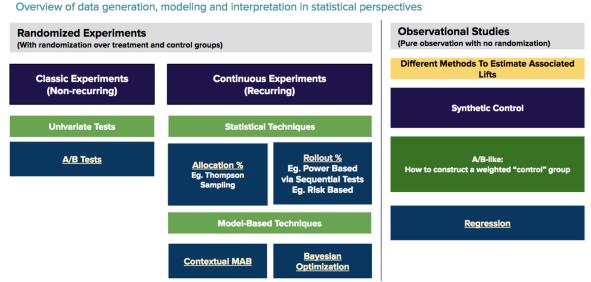
Bayesian A/B Testing

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React Demo: https://palmpalm7.github.io/bayesian ab testing/

1. Introduction

A/B Testing is the application of hypothesis testing in the tech industry. It is the gold standard to monitor growth and make data-driven decisions to improve digital user experience. Many institutions leverage A/B testing along with other online tests to facilitate their decision making process, and a typical online experiment platform could consist of the following framework.



Under the Hood of Uber's Experimentation Platform https://www.uber.com/blog/xp/

As shown on the diagram, traditionally the underlying method for classic experiments leverages the NHST (Null Hypothesis Significance Testing). a typical frequentist approach where a user needs to assume a distribution, calculating the required statistics (e.g. type 1 and 2 error rates, sample sizes, minimum required changing and applying the corresponding of the where hundreds and thousands of experiments are run concurrently at different product levels. However, the frequentist structure usually comes along with a few pitfalls, namely in multivariate tests, sequentiality and multiple comparisons, and statistical power in large-scale tests. In addition, it also creates unnecessary complexity when explaining p-value to non-tech stakeholders.

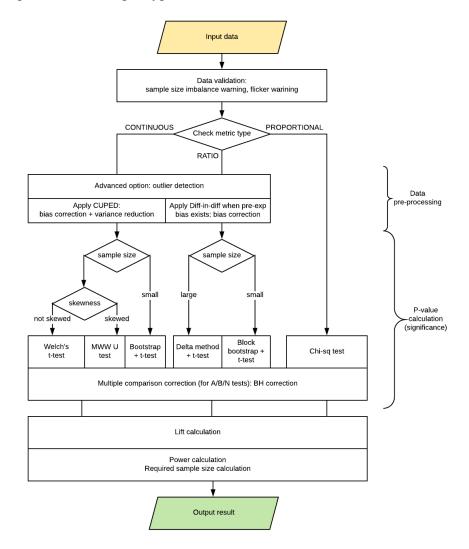
Therefore, we aim to address these challenges in our project and demonstrate the superiority of the Bayesian framework by comparing the frequentist approach and the Bayesian approach in a marketing A/B <u>dataset from kaggle</u>.

2. Background

To understand the Bayesian approach, we need to examine the fundamentals of both the frequentist's NHST the Bayesian hypothesis testing framework.

Frequentist Framework

The frequentist approach leverages this set of decision-making flowchart, where we perform numerous steps before making a hypothesis test.



Under the Hood of Uber's Experimentation Platform

https://www.uber.com/blog/xp/

Notably, we need to perform:

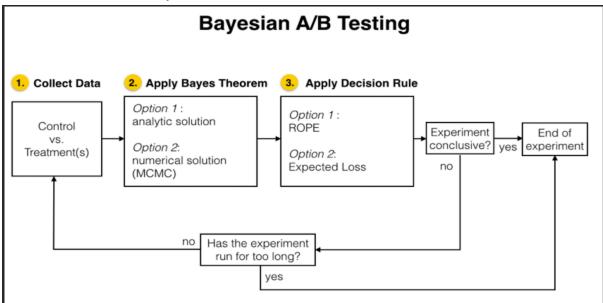
- 1. Data validation
- 2. Metric check
- 3. Outlier check
- 4. Skewness check
- 5. Sample size calculation
- 6. Determining the required distribution and corresponding null-hypothesis test

7. Getting feedbacks

A few more pitfalls could be spotted in this design. First of, we are assuming a distribution that the data should loosely fall into, not addressing any potential data shift. Only by ensuring a rigid framework of assumption then an experiment could be run, thus potentially delaying the experiment. Secondly, we are not taking any prior info. The only possible way to perform a NHST is to have groups of data without statistically significant difference. One could argue this also makes sequential testing worthless, where the different p-value at 25%, 50% and 75% mark of the total sample size is worthless. Along with the few pitfalls introduced in the introduction section, we have identified a few spots for improvements.

Bayesian Framework

Whereas in the Bayesian framework we leverage Bayesian Hypothesis Testing, especially the action function and the bayesian factor.



The decision framework consists of three steps:

- 1. Leveraging the Posterior Distribution in Bayesian Hypothesis Testing
- 2. Applying the Decision Rule via a loss function.
- 3. Making the decision by interpreting results
- 4. Analyzing the Bayes Factor for further explanation

Leveraging Posterior Distribution

In Bayesian hypothesis testing, the goal is to evaluate competing hypotheses using **posterior distributions**. Suppose we have two hypotheses:

- **H0**: The null hypothesis, typically representing the control group (A).
- H1: The alternative hypothesis, typically representing the treatment group (B).

$$\pi(heta \mid x) = rac{\mathcal{L}(x \mid heta)\pi(heta)}{\int \mathcal{L}(x \mid heta')\pi(heta')d heta'}$$

 $L(x|\theta)$ is the likelihood function $\pi(\theta)$ is the prior distribution $\pi(\theta|x)$ is the posterior distribution

The posterior distributions describe the updated belief about the parameters of interest after observing the data. These posterior distributions are calculated using Bayes' theorem, combining prior knowledge (the prior distribution) with the observed data (the likelihood). The resulting posterior distributions allow us to make decisions about whether to accept or reject the null hypothesis.

Applying Decision Rule

To take action based on the posterior distributions, we define a **loss function** that quantifies the cost of incorrect decisions. In hypothesis testing, there are two types of errors to consider:

- 1. **Type I error**: Rejecting the null hypothesis when it is true.
- 2. **Type II error**: Accepting the null hypothesis when the alternative hypothesis is true.

We also define two possible actions:

- **a0**: Accept the null hypothesis (H0).
- **a1**: Accept the alternative hypothesis (H1).

For a 0-1 loss function:

$$L(heta,a_i) = egin{cases} 0, & ext{if } heta \in \Theta_i, \ 1, & ext{if } heta \in \Theta_j, \, j
eq i. \end{cases}$$

The **expected loss** under each hypothesis is then calculated using the posterior distribution:

$$E^{\pi(heta \mid x)}[L(heta, a_i)] = \int L(heta, a_i) \pi(heta \mid x) d heta.$$

The loss function assigns a cost to each decision depending on whether it is correct or incorrect. For example:

- There is no loss if the correct hypothesis is accepted.
- There is a loss (or penalty) if the wrong hypothesis is accepted.

The next step is to calculate the **expected loss** for each action. This involves taking into account the posterior probabilities of the hypotheses. The expected loss tells us the potential cost of making a wrong decision for each action.

We then **choose the action with the smallest expected loss**. This ensures that the decision minimizes the overall risk based on the posterior probabilities.

Making Decision

The decision-making process can be summarized as follows:

- 1. **Define a loss function**: A simple loss function assigns no loss to correct decisions and a penalty to incorrect decisions.
- 2. **Compute the expected loss**: The expected loss for each action is calculated based on the posterior probabilities of the hypotheses.
- 3. **Compare the expected losses**: We choose the action (accept H0 or H1) that minimizes the expected loss.
- 4. **Compare posterior probabilities**: Minimizing expected loss is equivalent to comparing the posterior probabilities of the two hypotheses. The hypothesis with the higher posterior probability is accepted.

In simple terms, we make the decision by asking:

• Is the posterior probability of H0 greater than that of H1? If yes, we accept H0; otherwise, we accept H1.

Using the expected losses, the decision-making process boils down to comparing **posterior odds**:

$$P(H_1 \mid x)$$
 vs. $P(H_0 \mid x)$.

We accept the hypothesis with the higher posterior probability. This can be expressed as:

$$E^{\pi(heta \mid x)}[L(heta, a_0)] < E^{\pi(heta \mid x)}[L(heta, a_1)] \iff P(H_1 \mid x) < P(H_0 \mid x).$$

Analyzing Bayes Factor

To measure the strength of evidence in favor of one hypothesis over the other, we use a quantity called the **Bayes Factor**. The Bayes Factor compares how well each hypothesis explains the observed data, defined as:

$$BF = rac{\mathcal{L}(x \mid H_1)}{\mathcal{L}(x \mid H_0)}.$$

• If the Bayes Factor is greater than 1, it means the observed data provides stronger evidence for the alternative hypothesis (H1).

• If the Bayes Factor is less than 1, it means the observed data supports the null hypothesis (H0).

The Bayes Factor also plays a role in updating our beliefs. The **posterior odds** (our updated belief) are calculated by multiplying the **prior odds** (our initial belief) by the Bayes Factor.

 $Posterior\ Odds = Prior\ Odds \times BF$

Summary

- 1. Use the **posterior distributions** to compute expected losses.
- 2. Define the **loss function** to quantify the cost of errors.
- 3. Choose the action aia iai that minimizes the expected loss.
- 4. Use the **Bayes Factor** to quantify evidence for the hypotheses and update posterior odds.

The methodology ensures that decisions are made systematically using probabilistic reasoning, balancing prior beliefs with observed data. This framework provides a robust alternative to frequentist hypothesis testing.

3. Related Work

Here's a list of related work on A/B Testing, Online Experiment and Bayesian A/B Testing we looked into.

Overlapping Experiment Infrastructure: More, Better, Faster Experimentation

Overlapping Experiment Infrastructure: More, Better, Faster Experimentation

This paper describes Google's infrastructure for running overlapping experiments, facilitating increased testing capacity and efficiency. It is viewed as the foundation of A/B Testing platforms.

Trustworthy Online Controlled Experiments

Trustworthy Online Controlled Experiments

This book offers a comprehensive guide to designing and interpreting online experiments. We view it as the encyclopedia toolbook for A/B Testing.

Under the Hood of Uber's Experimentation Platform

Under the Hood of Uber's Experimentation Platform | Uber Blog

This article provides insights into Uber's experimentation platform, detailing the use of various statistical methodologies. It not only focuses on the classic NHST experiment, but also covers the whole online experiment platform ecosystem.

Driving Performance at Microsoft Bing

Driving Performance at Microsoft Bing | Engineering Blog

A recent outlining Bing's experimentation framework, emphasizing the role of data-driven decision-making and the scale of its operation.

Rapid and Scalable Bayesian AB Testing

[2307.14628] Rapid and Scalable Bayesian AB Testing

This paper introduces a hierarchical Bayesian approach to enhance statistical power in multivariate A/B tests, enabling sequential testing and early stopping without increasing false positives.

Talking Bayes to Business: A/B Testing Use Case | Shopify

■ Talking Bayes to Business: A/B Testing Use Case | Shopify

This video discusses the application of Bayesian methods in A/B testing within a business context, highlighting practical advantages over traditional approaches.

Bayesian A/B Testing at VWO

Bayesian A/B Testing at VWO

This whitepaper details VWO's implementation of Bayesian statistics in their A/B testing platform, offering intuitive answers to common testing questions and mitigating common methodological errors.

Continuous Monitoring of A/B Tests without Pain: Optional Stopping in Bayesian Testing

Continuous monitoring of A/B tests without pain: Optional stopping in Bayesian testing This paper proves the validity of Bayesian testing with continuous monitoring, allowing for real-time decision-making without compromising statistical integrity.

4. Methodology

The goal of the following analyses is to evaluate the effectiveness of A/B testing in marketing settings. We employ both frequentist and Bayesian approaches to highlight the differences in their interpretations and outputs. Under the frequentist framework, chi-square tests analyze differences in observed frequencies between the two test groups for categorical distributions. Additionally, t-tests compare mean conversion rates between the two groups and calculate the t-statistic and p-value to determine whether the difference in conversion rates is statistically significant. Both frequentist approaches provide p-values to detect statistically significant differences; however, they lack the considerations of prior knowledge or uncertainty beyond the observed data.

Therefore, we adopt a Bayesian approach to address these limitations. This method incorporates prior beliefs and creates posterior distributions to quantify uncertainty and

provide more interpretable results. It also enables posterior predictive checks, confidence intervals, and model selection where necessary.

In the live demo (https://palmpalm7.github.io/bayesian_ab_testing/), we could view how Bayesian helps with the decision making by offering a solid decision that holds true no matter how many comparison groups we are leveraging or sequential tests we are performing. Furthermore, we mitigates the p-value NHST framework by not requiring a sample size requirement and ensure the results still hold true even when new data comes in a sequential manner. It does not nullifies the previous results (p-values).

4.1 Frequentist Approch

4.1.1 Dataset Overview

The dataset used for our analysis is the "Marketing A/B Testing" dataset, available on Kaggle, which provides insights into a marketing campaign aimed at increasing conversions through A/B testing. Marketing companies often seek to determine whether their campaigns will be successful and, more importantly, how much of that success can be attributed to the advertisements themselves. In this case, the campaign was designed with a randomized control trial, dividing participants into two groups: the experimental group, which was exposed to advertisements, and the control group, which was either exposed to a public service announcement (PSA) or no ads at all. The analysis aims to identify factors that influence conversion rates, such as test group assignment and the timing of ads, to understand what drives success in the campaign.

The dataset includes key variables such as whether a user converted (i.e., bought the product), which we used as the target variable for our analysis. Additionally, it provides a user id for unique identification, the test group variable indicating whether a user saw the ad ("ad") or the PSA ("psa"), and information on the total ads seen by each user, as well as the most ads day and most ads hour, which indicate the day and hour during which the user encountered the most ads. By exploring these factors, we can gain insights into how ad timing and group assignment contribute to conversion outcomes.

4.1.2 Chi-Squure Test

A Chi-Square test is an appropriate statistical method for analyzing the relationship between categorical variables, as it assesses whether observed frequencies significantly differ from what we would expect under the null hypothesis. In our project, the test helps determine whether factors such as test group assignment (e.g., A (ad) vs. B (psa)), the most active day for ads (most ads day), or the most active hour for ads (most ads hour) are significantly associated with conversion rates. By evaluating these categorical variables against the "converted" outcome, the Chi-Square test enables us to identify whether variations in conversion rates across these categories are due to random chance or suggest underlying patterns. Specifically, our null hypothesis assumes no significant difference in conversion rates across groups. Rejecting this hypothesis indicates that the test group, day, or hour has a significant effect on conversion behavior.

To conduct this analysis, we used Python's *scipy.stats.chi2_contingency* function to perform the Chi-Square test for independence on each categorical variable. For each variable, we created a contingency table to capture the frequency distribution of its categories relative to the "Converted" outcome, which allowed us to calculate the Chi-Square test statistic and the p-value. Using a significance level of alpha = 0.05, we found that all three tests—test group assignment, most active ad day, and most active ad hour—produced extremely small p-values, well below the threshold. As a result, we rejected the null hypothesis for all variables, concluding that the observed differences in conversion rates are statistically significant and unlikely to be due to random variability. The results are as follows:

Statistical Significance: All three tests show statistically significant results, with p-values well below the significance threshold of 0.05, indicating that the differences in conversion rates are not due to random variability.

Key Findings: The analysis suggests that conversion rates are significantly influenced by test group assignment, the day with the most ads shown, and the hour with the most ads shown. These results indicate that both time-related factors and group assignment play a significant role in conversion outcomes.

Sample Size: With a sample size of 588,101, the results are highly reliable and have greater statistical power. However, the large sample size could also detect very small, possibly insignificant differences as statistically significant, which may lead to overfitting or misinterpretation of the findings.

The figure below presents the code used for the test along with the corresponding results.

```
alpha = 0.05  # Significance level for the chi-squared test

for variable in df_cat.columns:
    # Skip the target variable 'converted' to avoid self-comparison
    if variable != 'converted':
        # Create a contingency table (cross-tabulation) between the categorical variable and 'converted'
        contingency_table = pd.crosstab(df_cat[variable], df_cat['converted'])

    # Calculate the total sample size from the contingency table
    sample_size = np.sum(contingency_table.values)

# Perform the chi-squared test for independence
    chi2, p, _, _ = chi2_contingency(contingency_table)

# Display the chi-squared test results
    print(f"\nchi-squared test for {variable} vs. converted:")
    print(ffi-fi-squared value: {chi2:.4f}") # Print the test statistic rounded to 4 decimal places
    print(f"p-value: {p:.4e}") # Print the p-value in scientific notation for precision

# Check if the p-value indicates a statistically significant result
    if p < alpha:
        print(f"The difference in conversion rates across {variable} is statistically significant.")
        # Reject the null hypothesis: there is a significant difference in conversion rates across groups
    else:
        print(f"There is no significant difference in conversion rates across {variable}.")
        # Fail to reject the null hypothesis: conversion rates are not significantly different across groups

# Print the total sample size with a preceding blank line for clarity
    print(f"\nSample Size: {sample_size}")</pre>
```

```
Chi-Squared test for test group vs. converted:
Chi-squared value: 54.0058
p-value: 1.9990e-13
The difference in conversion rates across test group is statistically significant.

Chi-Squared test for most ads day vs. converted:
Chi-squared value: 410.0479
p-value: 1.9322e-85
The difference in conversion rates across most ads day is statistically significant.

Chi-Squared test for most ads hour vs. converted:
Chi-squared value: 430.7687
p-value: 8.0276e-77
The difference in conversion rates across most ads hour is statistically significant.

Sample Size: 588101
```

Figure 4.1.2: Code and results of the Chi-Square test for independence, evaluating the relationship between categorical variables and conversion rates.

4.1.3 T-Test

The t-test is used to compare the means of two independent test groups based on continuous data, as it helps to determine whether a statistically significant difference exists between the groups. In this project, we transformed the categorical value "Converted" into the continuous metric "Conversion Rate" by dividing the total conversions by the number of website visitors. The two test groups being analyzed are "ad" and "psa," while other categorical factors "day of the week" and "hour of the day" are used as variables to explore conversion rate differences. By conducting an independent two-sample t-test, we can assess whether the observed differences in conversion rates between the ad and psa groups are statistically significant. Here, the null hypothesis assumes that no significant difference exists between the two groups.

Using the ttest_ind function from the scipy.stats library, we performed the independent t-tests for each day of the week and each hour of the day. For the analysis on "day of the week," the results indicate significant differences in conversion rates on Monday, Tuesday, Wednesday, Friday, and Saturday, which rejects the null hypothesis since the p-value is lower than 0.05. However, Thursday and Sunday show subtle differences with p-values is greater than 0.05, meaning the null hypothesis cannot be rejected. Similarly, for the analysis on "hour of the day," certain timeframes, such as 10 AM to 2 PM, demonstrate significant differences in conversion rates, which leads to rejection of the null hypothesis. On the contrary, other timeframes, such as 3 PM to 4 PM, have no significant variation, and the null hypothesis cannot be rejected.

While the t-test provides valuable insights into statistical differences, it has limitations. The method is ideal for comparing only two groups and relies on key assumptions that the data should follow a normal distribution, the variances between groups should be approximately equal, and the groups must be independent. In this scenario, the conversion rates in the ad group must not influence those in the psa group. More seriously, the t-test focuses solely on rejecting or failing to reject the null hypothesis, without quantifying uncertainty in the results. These limitations emphasize the need for Bayesian approach that can incorporate prior

information and provide a more comprehensive assessment of uncertainty through posterior distributions.

The figures below illustrates the codes for performing the t-tests and their associated outputs.

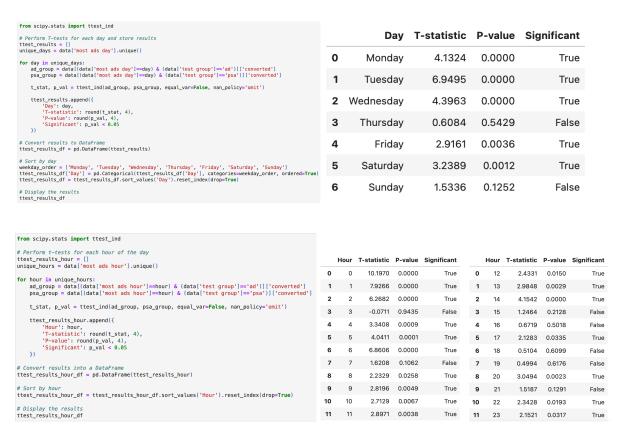


Figure 4.1.3: The codes and outputs associated with t-test that compares the mean conversion rates between the ad and psa groups based on day of the week and hour of the day.

4.2 Bayesian Approach

4.2.1 Misleading: P-values

P-values in frequentist A/B testing can be misleading for several reasons. Firstly, p-values are often misinterpreted as the probability that the null hypothesis is true, when they actually represent the probability of obtaining the results at least as extreme as those observed, assuming the null hypothesis is true. This subtle, but very significant, distinction leads to frequent misunderstanding of the true outcome in test results. P-values also do not provide information about the practical significance or effect size of an observed difference. A low p-value does not necessarily indicate a substantial impact on business metrics, in our case conversion rates, potentially leading to implementation of changes with minimal real-world benefit. The reliance on fixed significance thresholds (p < 0.05) can result in arbitrary decision-making. This can result in a miscommunication with stakeholders. A p value of 0.01 can be interpreted as many different things. This approach also fails to account for the continuous nature of evidence and can lead to an ill-timed conclusion.

4.2.2 Strengths of the Bayesian Approach

The Bayesian approach to A/B testing offers multiple advantages over the traditional frequentist method. One of the key benefits of Bayesian A/B testing is its flexibility and speed. Unlike the frequentist approach, which requires a predetermined sample size, the Bayesian methods allow for continuous updating of probabilities as new information is collected. This enables faster decision-making and more efficient experimentation for businesses to optimize their tests quickly. As mentioned previously, the nature of Bayesian results does not rely on the complex statistical concepts of p-values. The Bayesian approach provides a clear probability that one variant is outperforming another. This simplicity in interpretation is particularly valuable in business settings during the decision-making process.

The ability to incorporate prior knowledge is another strength of the Bayesian approach. By integrating historical/previous experiment results, the testing will exhibit a more well-rounded result and a comprehensive understanding of the probabilities presented. The frequentist way phrases the problem to fit the model. This approach can be quite difficult and only provides you with the point estimate, confidence interval, and p value. However, the Bayesian approach finds a model that fits the problem. This gives you a posterior distribution that allows you to answer a wider range of questions for marketers, data scientists, and stakeholders.

The Bayesian approach can give a more nuanced understanding of experimental results. Bayesian A/B testing is a versatile tool for companies of all sizes and traffic to gather meaningful insights about their business. However, one drawback of the Bayesian approach is time. The Bayesian approach typically requires more computation power, especially for larger and more complex datasets. Inferences involving computing complex integrals over parameter spaces can be computation intensive, so this approach may require more power. Despite the computational challenges, the benefits from the Bayesian approach outweigh the costs.

5. Bayesian A/B Testing Implementation

Bayesian hypothesis testing is also implemented via ReactJS, a Javascript framework to illustrate the easy-to-use Bayesian framework. The following section aims to explain the underlying computation logic beneath the visualization.

Live demo could be found at: https://palmpalm7.github.io/bayesian ab testing/

Code Repository

To reproduce the toolset we used for the demonstration, please go to our repository and refer to this README.md file https://github.com/PalmPalm7/bayesian ab testing for further

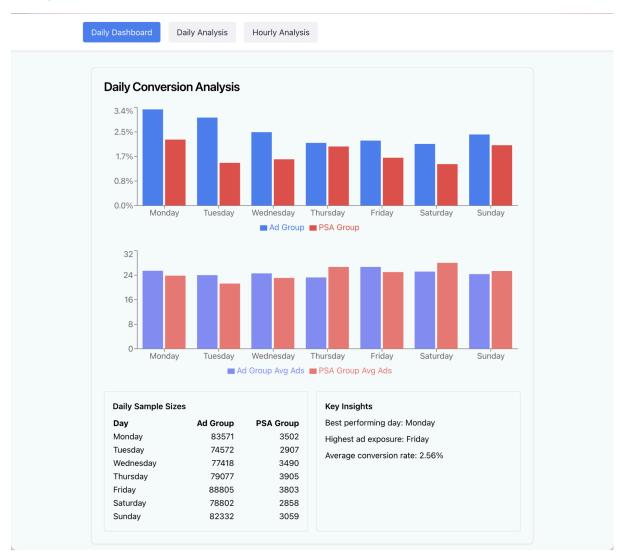
understanding. The current dataset leverages the Kaggle dataset we used, a marketing dataset consists of two groups: PSA (public service announcement) and AD (advertisement).

To run the project, please

- 1. Make sure you have successfully installed NPM. (e.g. via https://nodejs.org/en/download/package-manager)
- 2. Clone the Github repository from the repo. (e.g. *git clone https://github.com/PalmPalm7/bayesian ab testing.git*)
- 3. Install the required npm packages. (e.g. npm install jstat)
- 4. Start running the React App by
 - a. Using npm start or npm restart
 - b. View the application on http://localhost:3000/, or the corresponding port.

To use for Bayesian A/B testing, please refer to the three specific dashboards.

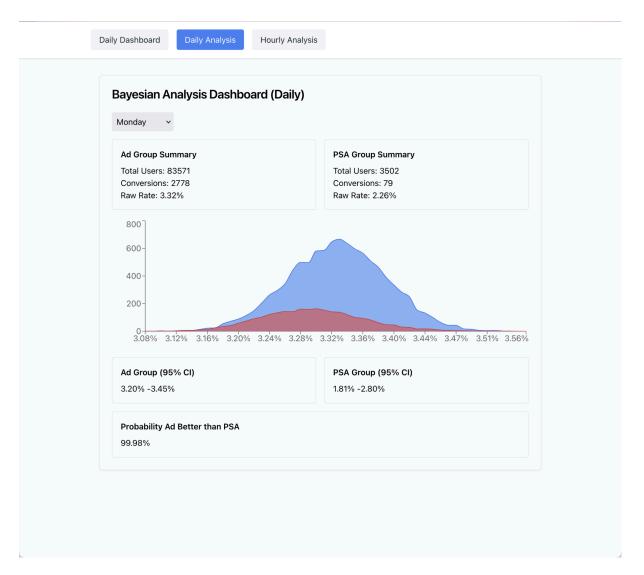
Daily Dashboard



The daily analysis dashboard is a summary of the whole dataset, with a visualization on the conversion rate and count of the advertisement impression per day.

The logic is self explanatory, for further explanation, please refer to: https://github.com/PalmPalm7/bayesian_ab_testing/blob/main/src/components/DailyDashboard.jsx

Daily Analysis Dashboard



This will be the main tool you will use to determine the effectiveness of the two groups.

The "Probability Ad Better than PSA" section calculates the fraction of posterior samples where the Ad group's sampled conversion rate is higher than the PSA group's sampled conversion rate. This fraction represents the Bayesian posterior probability that the Ad variant is better than the PSA variant, given the data and the chosen priors.

The posterior distribution is obtained by using a Beta distribution to model the conversion rate. Given some data (number of conversions and trials in each group), we update the prior Beta distributions for both groups to get posterior distributions. These posterior distributions reflect our updated beliefs about the true conversion rates after seeing the data.

For each group (Ad and PSA), the posterior is a Beta distribution determined by:

```
Posterior(p)=Beta(p; \alpha + successes, \beta + failures)
```

where α and β typically start at 1 and 1 (a uniform prior), and "successes" and "failures" are derived from the observed conversion data.

```
In the Javascript code, it is implemented this way:

const ad_alpha_post = 1 + adSuccesses;

const ad_beta_post = 1 + (adTrials - adSuccesses);

const psa_alpha_post = 1 + (psaTrials - psaSuccesses);

const psa_beta_post = 1 + (psaTrials - psaSuccesses);
```

Then we draw SAMPLE_SIZE = 10,000 random samples from each posterior distribution where each sample represents a plausible "true" conversion rate scenario based on the observed data and the prior.

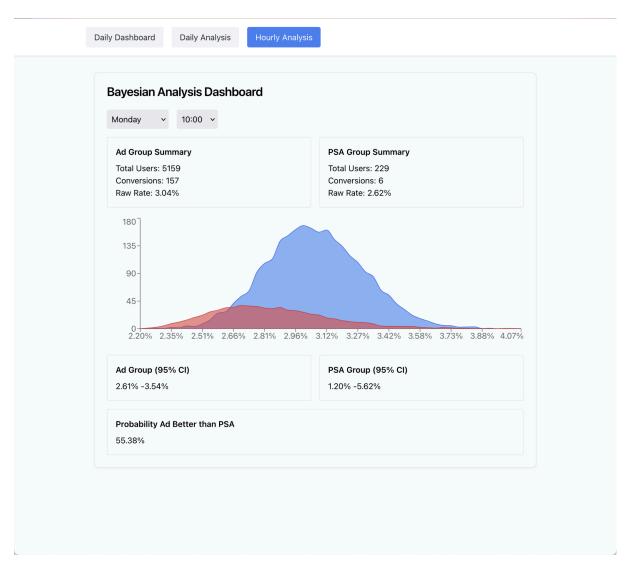
```
const adPosterior = Array.from({length: SAMPLE_SIZE}, () =>
jStat.beta.sample(ad_alpha_post, ad_beta_post));
const psaPosterior = Array.from({length: SAMPLE_SIZE}, () =>
jStat.beta.sample(psa_alpha_post, psa_beta_post));
```

In the end, the posterior comparison is done by estimating the probability that one group is better than the other, once we have arrays of samples from the Ad group's posterior and the PSA group's posterior.

```
let countAdBetter = 0;
for (let i = 0; i < SAMPLE_SIZE; i++) {
  if (adPosterior[i] > psaPosterior[i]) countAdBetter++;
}
const probAdBetter = countAdBetter / SAMPLE_SIZE;
```

In other words, for each pair of samples (adPosterior[i], psaPosterior[i]), it checks if adPosterior[i] > psaPosterior[i]. If this happens most of the time, it means that the Ad variant likely has a higher true conversion rate than the PSA variant, given the data and priors.

Hourly Analysis Dashboard



At last, there is a hourly analysis dashboard that utilizes the logic similar to the daily analysis dashboard.

6. Conclusion

In conclusion, our exploration highlights the advantages of the Bayesian framework over traditional frequentist A/B testing. By incorporating prior knowledge, seamlessly handling multiple comparisons, and updating results continuously as new data emerges, Bayesian methods provide more intuitive and flexible inferences that resonate well with both technical and non-technical stakeholders. This approach overcomes many frequentist limitations such as rigid assumptions, difficulty in interpretation, and the complexity of scaling to large, iterative experiments. As demonstrated through our comparison with the frequentist chi-square and t-tests, Bayesian testing not only simplifies decision-making but also facilitates ongoing experimentation. Ultimately, Bayesian A/B testing emerges as a more

adaptive, transparent, and robust method for informed decision-making in real-world, data-driven marketing and product optimization scenarios.