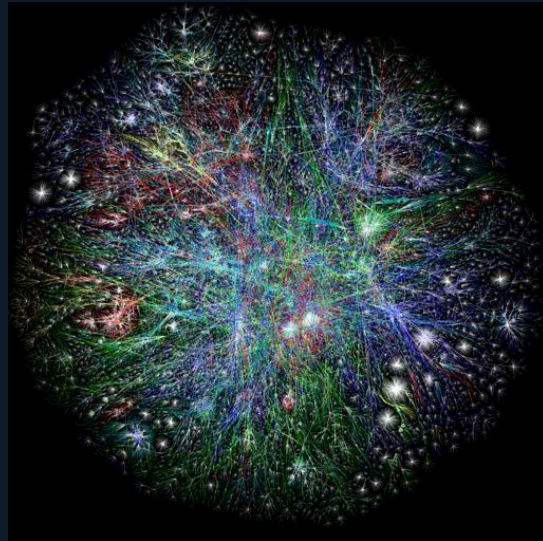


Graphs Traversal



Lecture Contents

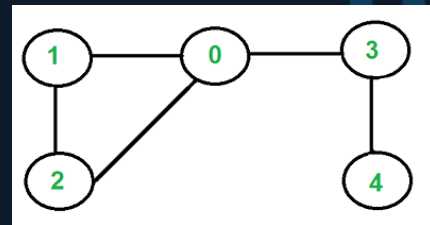
- Traversing a Graph
- Depth First Search
- Breadth First Search
- Minimum Spanning Trees

Traversing a graph

- There's no point in storing information in a graph unless you want to explore the relationships between nodes.
- We calculate this information by traversing the graph.
- We can find out all sorts of things by traversing a graph:
 - How to get from one node to another, when they aren't directly connected
 - How far away one node is from another
 - How many once removed connections (friends of friends), thrice removed connections, etc, two nodes share.
 - Check if a graph is connected or unconnected.

Traversing a graph

- Traversing a graph is just, when starting at a given node, jumping along edge to edge touching every connected node in the graph, performing some processing at each node.
- Because a node in a graph can have more than one incoming edge, traversing a graph has some problems not found in traversing lists or trees.
- We can come to a node from multiple directions as we traverse the graph. In cyclic or non-directed graphs, this could lead to an infinite loop.
- Specifically we want to make sure we only touch each node once.



Traversing a graph

- The typical solution to this is quite simple.
- Just use a bool as a visited flag inside each node.
- Before traversing the graph, loop through every node, setting their visited flags to false.
- Then, when traversing, as we reach each node, set its visited flag to true.

Traversing a graph

- There are two common algorithms for traversing a graph:
 - Depth First Search (DFS)
 - Breadth First Search (BFS)

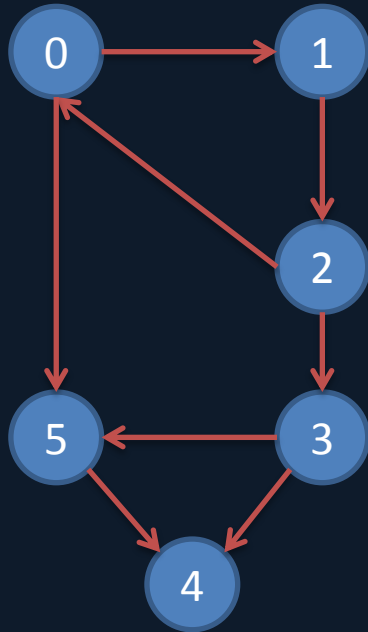
Depth First Search

- Depth first search involves searching as far down a path as possible before backtracking.
- Can be done recursively, or by using a stack.

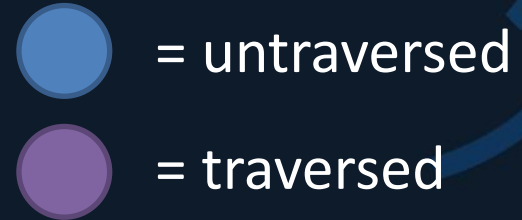
Depth First Search

- The algorithm is:
 - Push first node on stack
 - While stack not empty
 - Get the top off the stack and remove it
 - Process it.
 - Mark it as traversed
 - Loop through its edges
 - If end node of edge not traversed or on the stack
 - » Push end node onto the stack

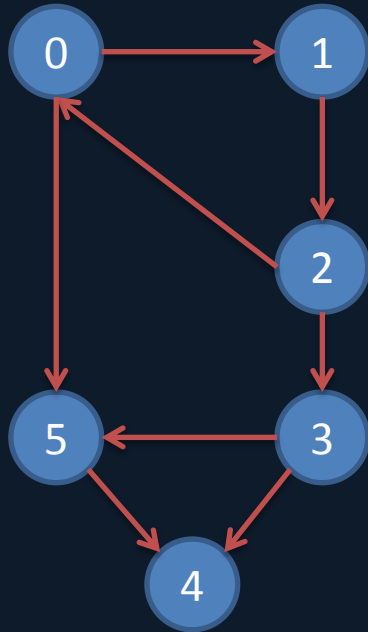
Depth First Search





Stack:



Depth First Search

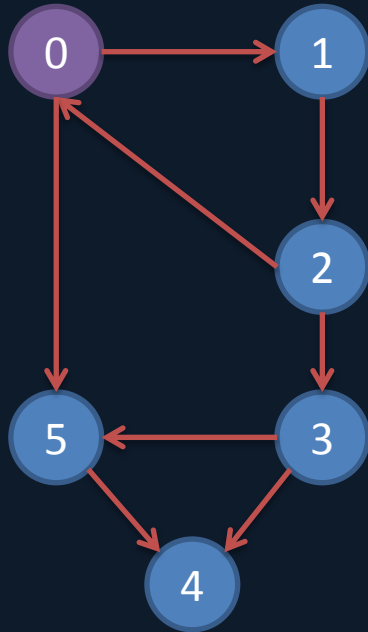


 = untraversed
 = traversed



Stack:

0

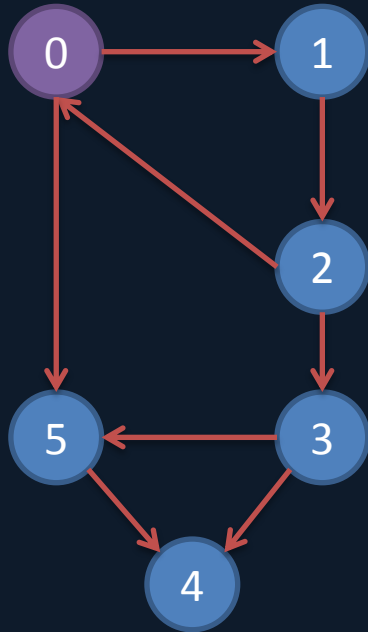
Depth First Search





Stack:

 = untraversed
 = traversed

Depth First Search

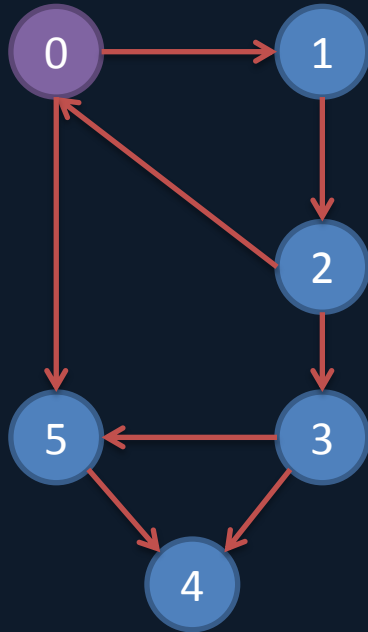




 = untraversed
 = traversed

Stack:

1

Depth First Search

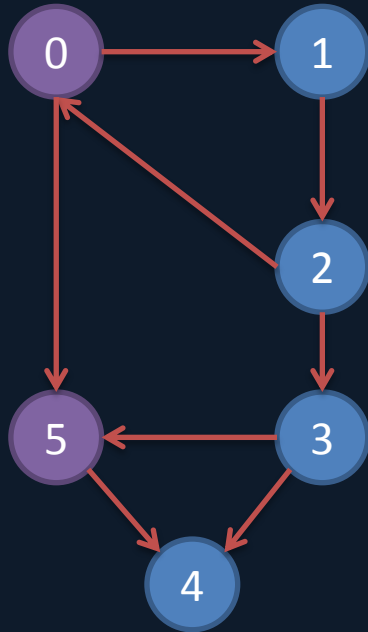




 = untraversed
 = traversed

Stack:

5
1

Depth First Search

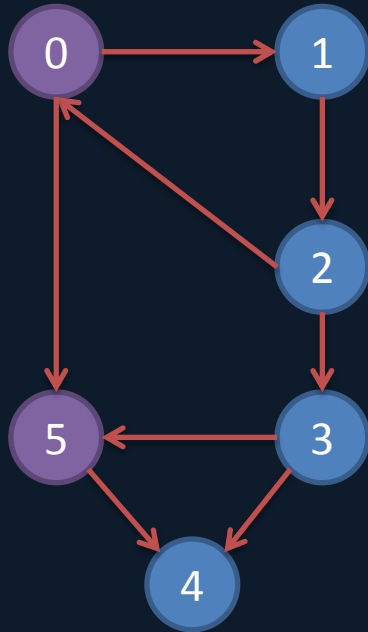




 = untraversed
 = traversed

Stack:

1

Depth First Search

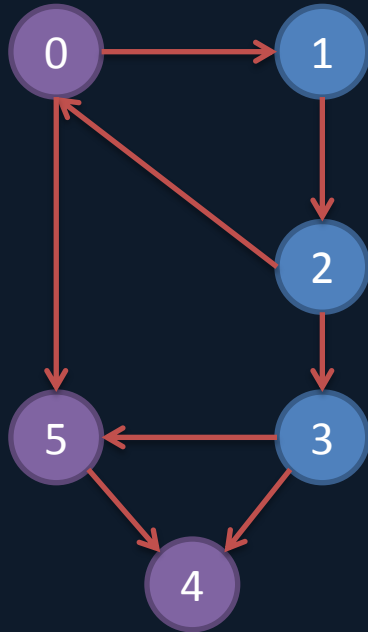


 = untraversed
 = traversed

Stack:

4
1

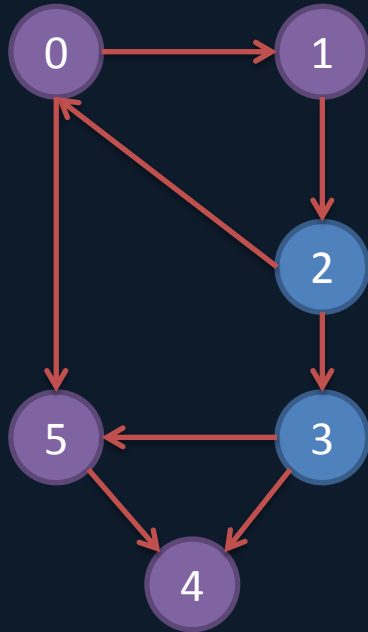
Depth First Search



Stack: 1

● = untraversed
● = traversed

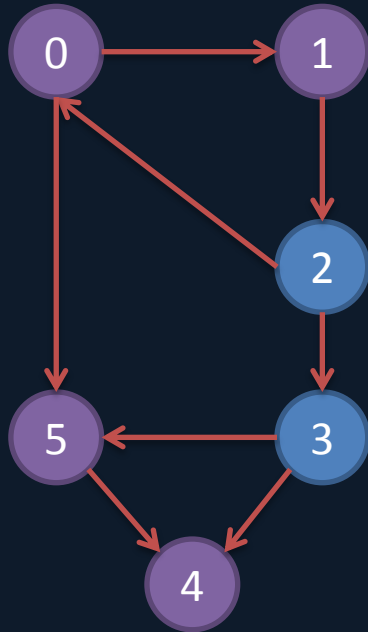
Depth First Search



● = untraversed
● = traversed

Stack:

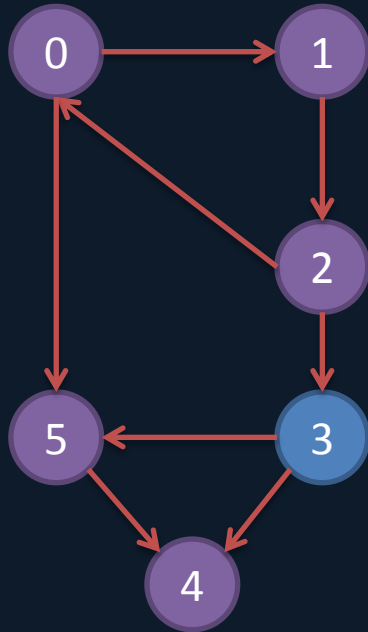
Depth First Search





Stack: 2

● = untraversed
● = traversed

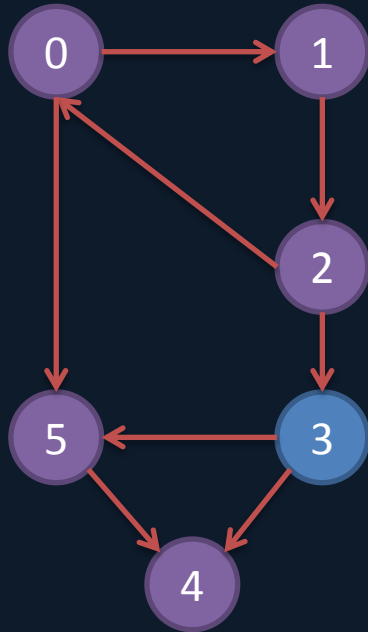
Depth First Search





 = untraversed
 = traversed

Stack:

Depth First Search

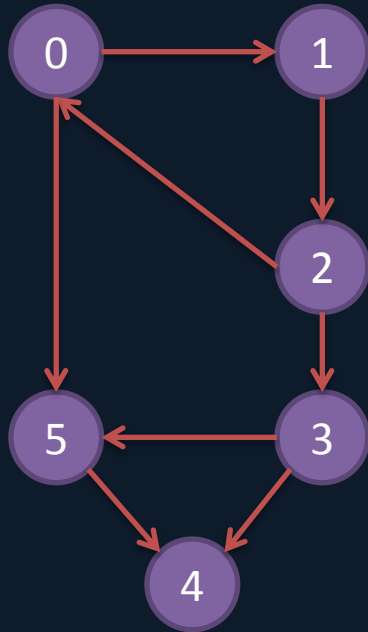


 = untraversed
 = traversed

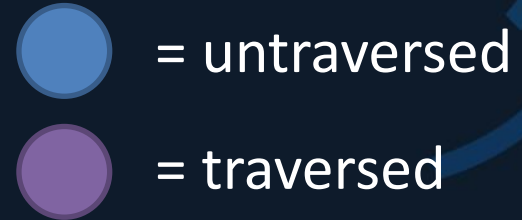
Stack:

3

Depth First Search



Stack:



Breadth First Search

- Breadth-First Search involves processing all of the neighbours of each node before processing their neighbours and so on.
- You can think of it as fanning out from the starting node, evenly in all directions.
- It is typically implemented with a queue

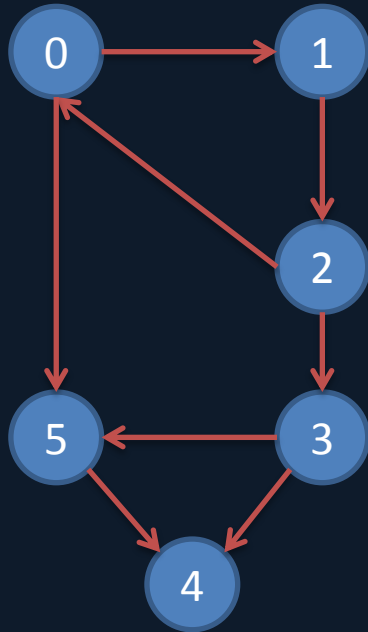
Breadth First Search

- The algorithm is:
 - Push first node onto queue
 - While queue not empty
 - Get the end off the queue and remove it
 - Process it.
 - Mark it as traversed
 - Loop through its edges
 - If end node of edge not traversed or in the queue
 - » Push end node onto the queue

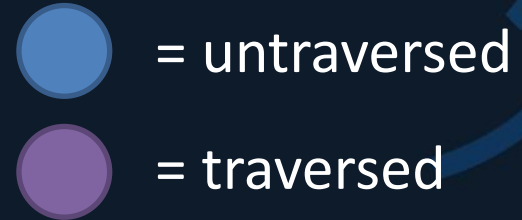
Breadth First Search

- You'll notice this algorithm is *very* similar to the DFS search.
- The only difference is we are using a queue instead of a stack to pick the next node to traverse.

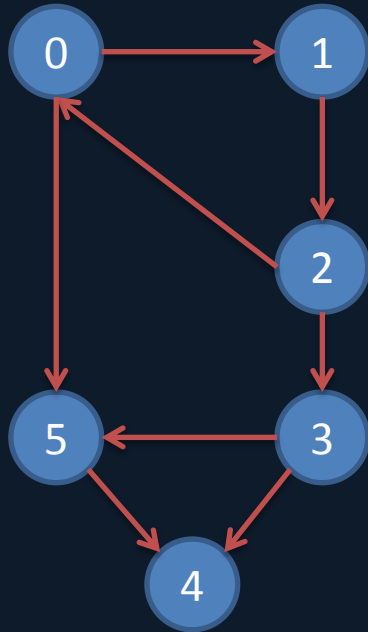
Breadth First Search





Queue:



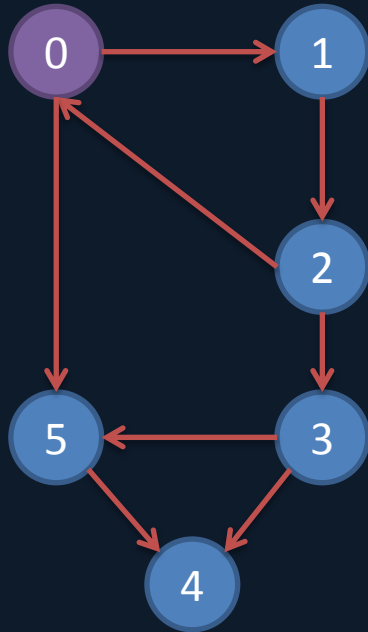
Breadth First Search



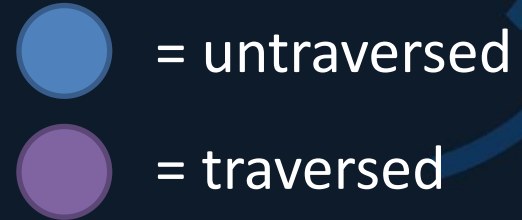
Queue: 0

 = untraversed
 = traversed

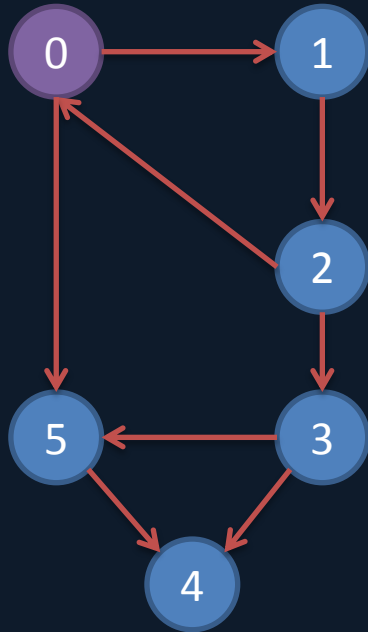
Breadth First Search





Queue:



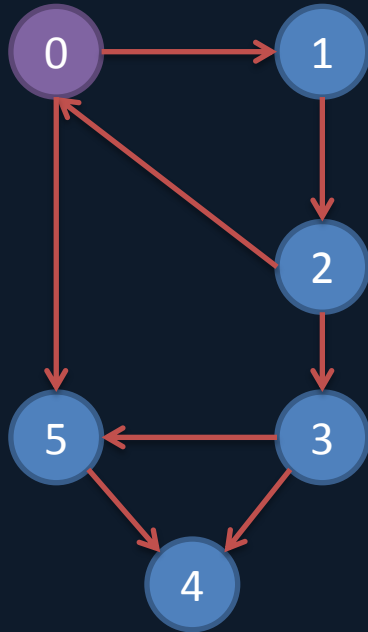
Breadth First Search



Queue: 1



 = untraversed
 = traversed

Breadth First Search

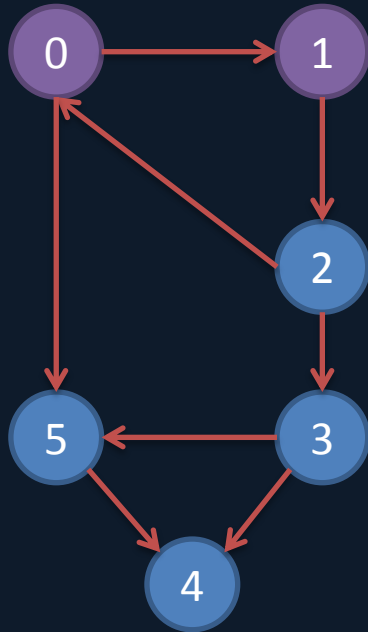


Queue:

1
5

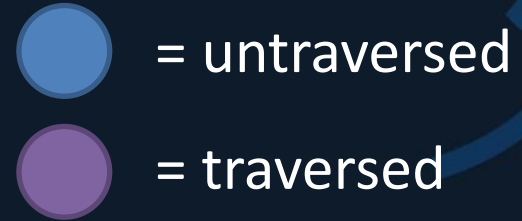
 = untraversed
 = traversed

Breadth First Search

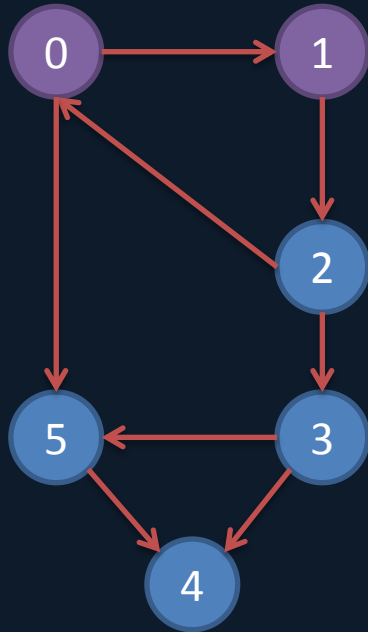


Queue:

5





Breadth First Search

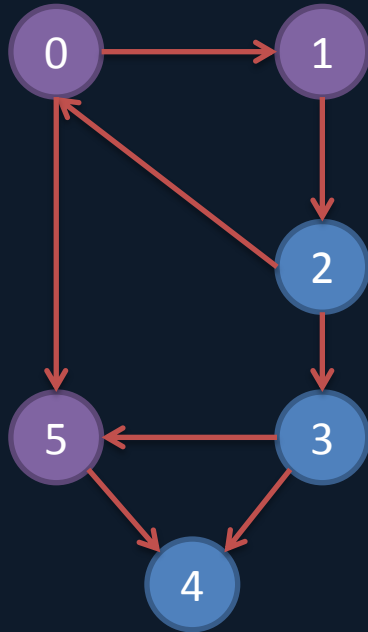


Queue:



5
2

 = untraversed
 = traversed

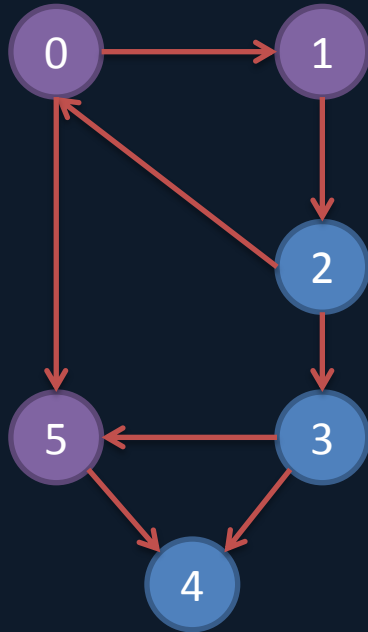
Breadth First Search



Queue: 2



 = untraversed
 = traversed

Breadth First Search

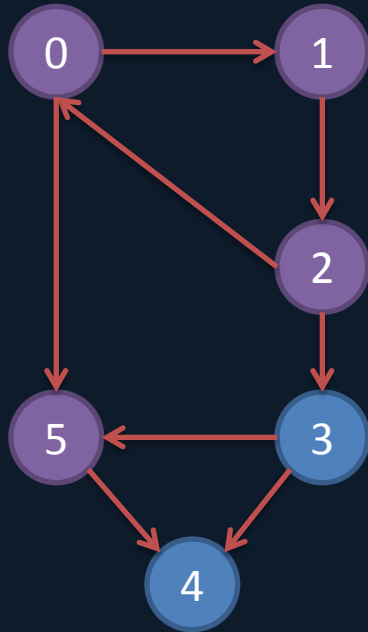


Queue:



2
4

 = untraversed
 = traversed

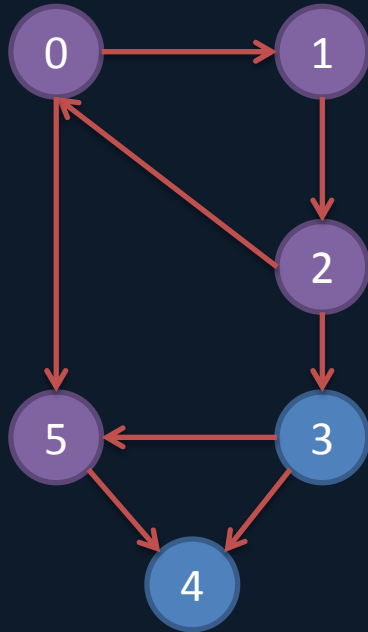
Breadth First Search



Queue: 4



 = untraversed
 = traversed

Breadth First Search

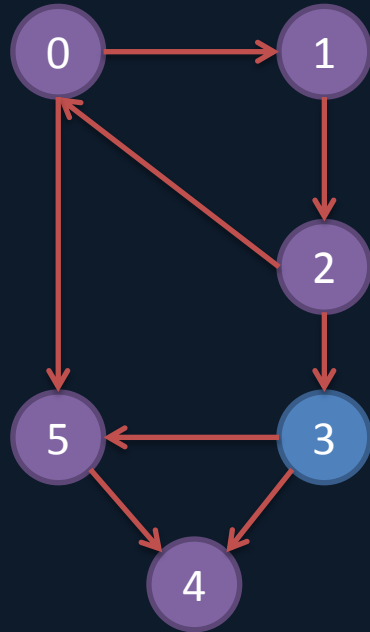


Queue:



4
3

 = untraversed
 = traversed

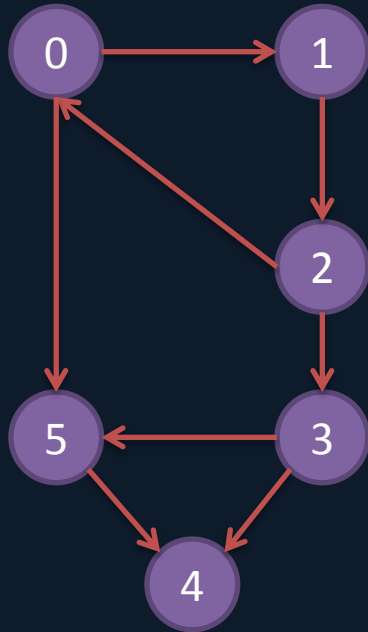
Breadth First Search



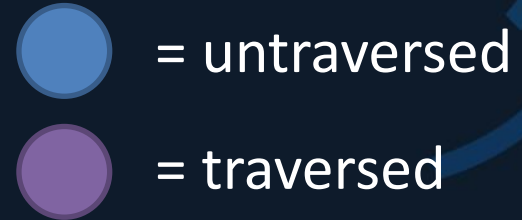
Queue: 3

 = untraversed
 = traversed

Breadth First Search



Queue:



Questions?

