

# EE23010 Assignment

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Question 12.13.3.103

If  $A$ ,  $B$  and  $C$  are three independent events such that

$\Pr(A) = \Pr(B) = \Pr(C) = p$ , then

$P(\text{At least two of } A, B, C \text{ occur}) = 3p^2 - 2p^3$

**Solution:**

RV	Value	Description
X	0	none of the events occur
	1	only one of the events occur
	2	any two of the events occur
	3	all the three events occur

TABLE 0

RANDOM VARIABLE DECLARATION

$$\Pr(X = 0) = \Pr(A'B'C') \quad (1)$$

$$= \Pr(A')\Pr(B')\Pr(C') \quad (2)$$

$$= (1 - p)^3 \quad (3)$$

$$\Pr(X = 1) = \Pr(AB'C') + \Pr(BC'A') + \Pr(CA'B') \quad (4)$$

$$= \Pr(A)\Pr(B')\Pr(C') + \Pr(B)\Pr(C')\Pr(A')$$

$$+ \Pr(C)\Pr(A')\Pr(B') \quad (5)$$

$$= 3p(1 - p)^2 \quad (6)$$

$$\Pr(X = 2) = \Pr(ABC') + \Pr(BCA') + \Pr(CAB') \quad (7)$$

$$= \Pr(A)\Pr(B)\Pr(C') + \Pr(B)\Pr(C)\Pr(A')$$

$$+ \Pr(C)\Pr(A)\Pr(B') \quad (8)$$

$$= 3p^2(1 - p) \quad (9)$$

$$\Pr(X = 3) = \Pr(ABC) \quad (10)$$

$$= \Pr(A)\Pr(B)\Pr(C) \quad (11)$$

$$= p^3 \quad (12)$$

$$\Pr(X \geq 2) = \Pr(X = 2) + \Pr(X = 3) \quad (13)$$

$$= 3p^2(1 - p) + p^3 \quad (14)$$

$$= 3p^2 - 2p^3 \quad (15)$$