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EE23010 Assignment

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Question 12.13.3.11

Prove that

- (i) Pr(A) = Pr(AB) + Pr(AB')
- (ii) Pr(A + B) = Pr(AB) + Pr(AB') + Pr(A'B)

Solution:

(i) consider RHS:

$$A = A(B + B')$$

$$Pr(A) = Pr(A(B + B'))$$

$$= Pr(AB + AB')$$
(1)
(2)

$$= \Pr(AB) + \Pr(AB') - \Pr((AB)(AB'))$$

$$= \Pr(AB) + \Pr(AB') - \Pr(ABB')$$
 (5)

$$= \Pr(AB) + \Pr(AB') \tag{6}$$

(ii) consider RHS:

$$A + B = A(B + B') + B(A + A') \tag{7}$$

$$Pr(A + B) = Pr(A(B + B') + B(A + A'))$$
(8)
= Pr(AB + AB + AB' + BA') (9)
= Pr(AB + AB' + BA') (10)

But,

$$AB(AB') = 0 (11)$$

$$AB(A'B) = 0 (12)$$

$$AB'(A'B) = 0 (13)$$

AB, AB' and A'B are mutually exclusive as their pairwise product is zero.

$$= \Pr(AB) + \Pr(AB') + \Pr(A'B) - \Pr(AB(AB')) - \Pr(AB'(A'B)) - \Pr(A'B(AB)) + \Pr((AB)(AB')(A'B))$$

$$(14)$$

$$= \Pr(AB) + \Pr(AB') + \Pr(A'B) - 0 - 0 - 0 + 0$$

$$(15)$$

$$= \Pr(AB) + \Pr(AB') + \Pr(A'B) \tag{16}$$